

PHYS 225

Fundamentals of Physics: Mechanics

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Lecture 13: Force and motion-I

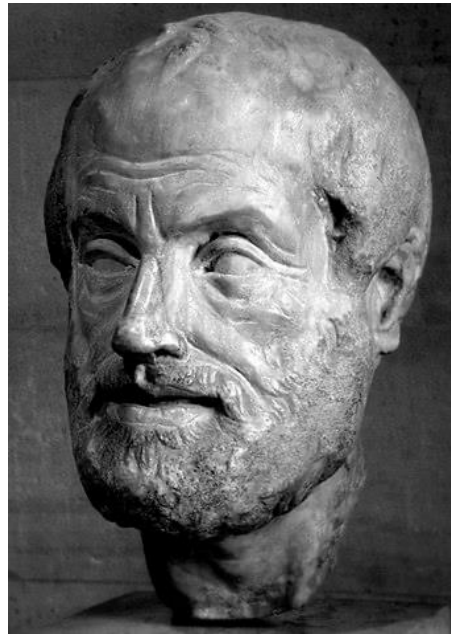
Chapter 5

- Learning objectives
 - Newton's three laws
 - Some particular forces: Gravitational force, normal force, friction, tension, etc.
 - Practice: Free body diagram, Atwood's machine, inclines, etc.

Learning goals for today

- Force and motion
 - Newton's three laws

A little history of forces



Force is needed to change motion rather than to sustain it!

Aristotle: “everything moving must be moved by something” (384–322 BC)



Force

[Article](#) [Talk](#)

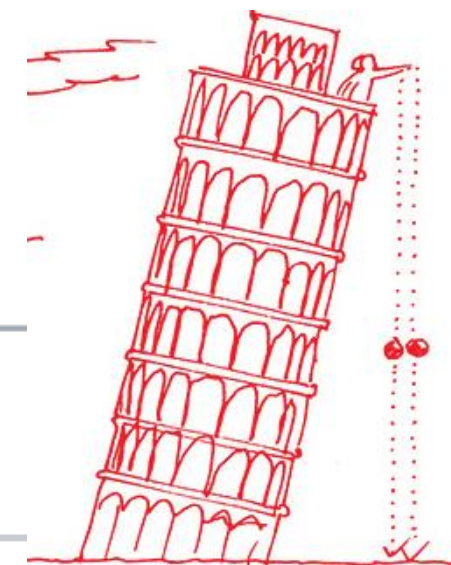
From Wikipedia, the free encyclopedia

For other uses, see [Force \(disambiguation\)](#). "Physical force" redirects here. For other uses, see [P](#).

In **physics**, a **force** is an influence that can cause an **object** to change its **velocity**, i.e., to **accelerate**, meaning a change in speed or direction, unless counterbalanced by other forces. The concept of force



Galileo: (17th century)



Newton: Newton's three laws (17th century)

Demo

\vec{F} changes the motion,
not to sustain it.

Clicker question 1

- Which of the following is true about force?

A

Everything moving must be moved by the force.

B

Force is needed to change motion rather than to sustain it!

C

Force causes an object to accelerate.

D

Both B and C.

\vec{a} : rate of change of \vec{v}

Force

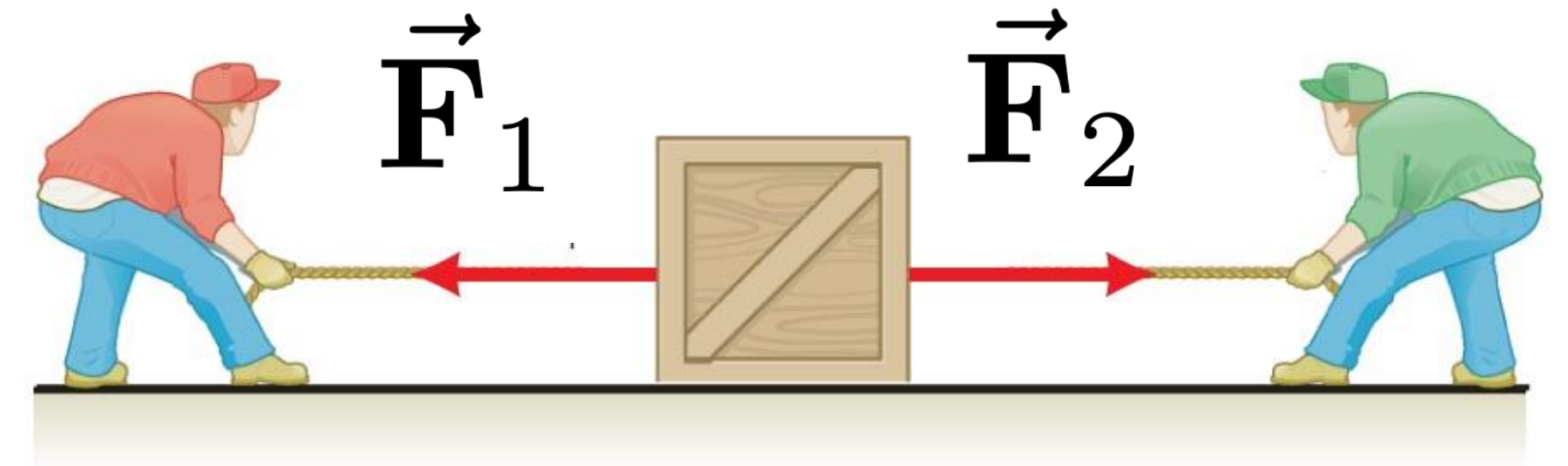
- **Force** is something that causes acceleration.

- ▶ Contact forces: push/pull

- ▶ Non-contact forces: e.g. gravity, electrostatic, etc.

- **Force is a vector**

- **Force unit: N (or kg * m * s⁻²)** $N \sim kg \cdot m \cdot s^{-2}$

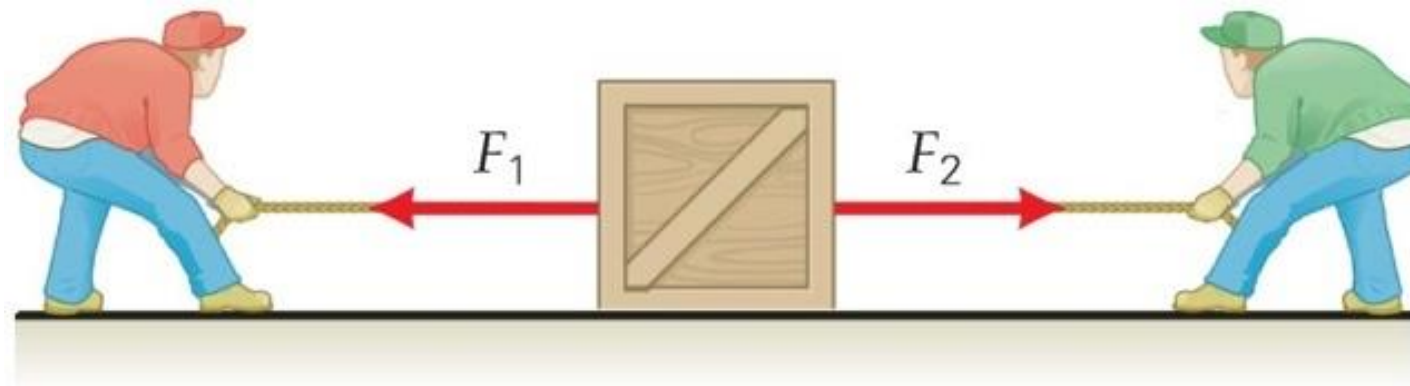


(a)

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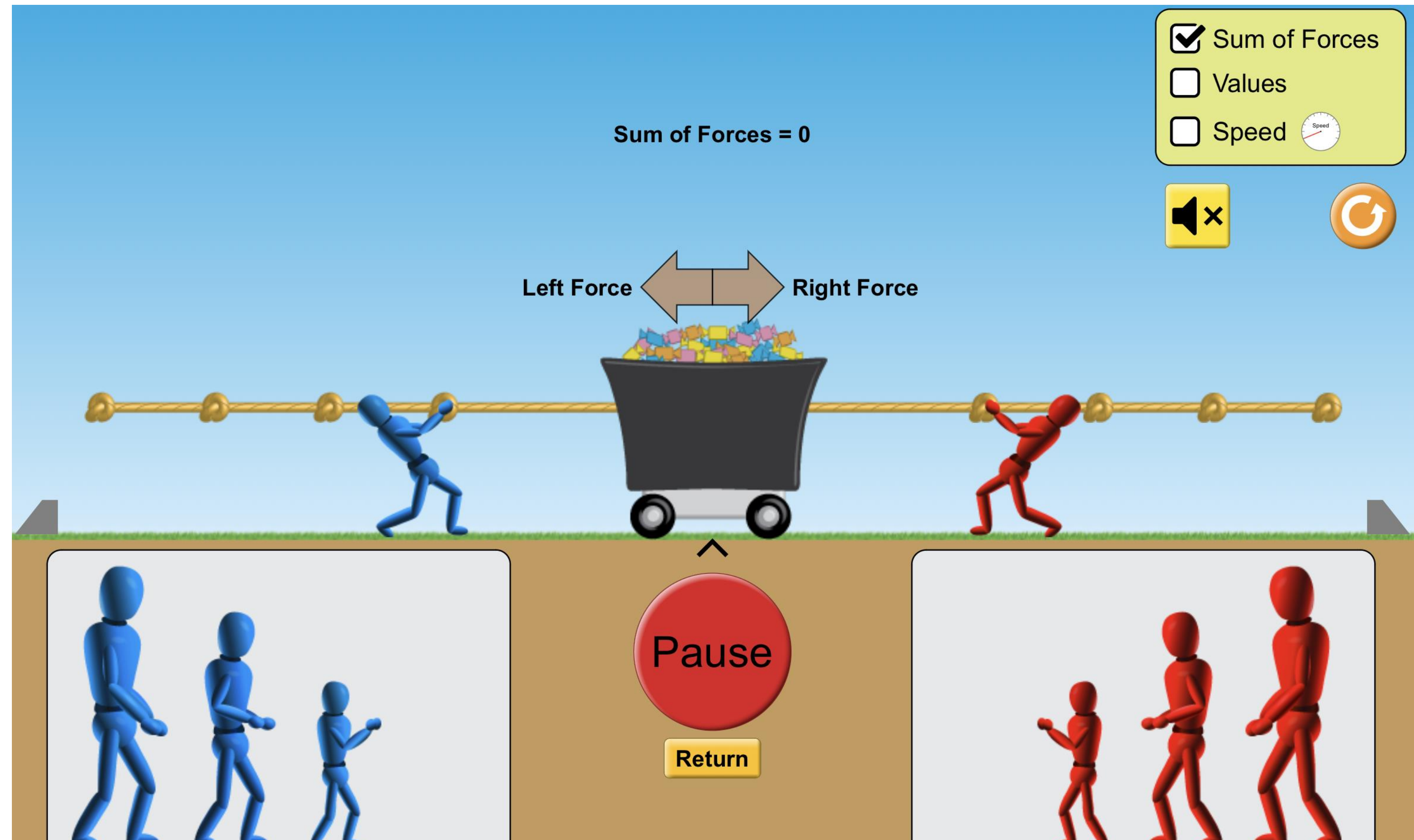
Net force

- **Net force:** Vector addition of all forces acting on the same object: $\vec{F}_{\text{net}} \equiv \sum \vec{F}_i$ Sum



$$\vec{F}_{\text{net}} = \sum \vec{F}_i = \vec{F}_1 + \vec{F}_2 + \dots$$

Simulation demo



https://phet.colorado.edu/sims/html/forces-and-motion-basics/latest/forces-and-motion-basics_all.html

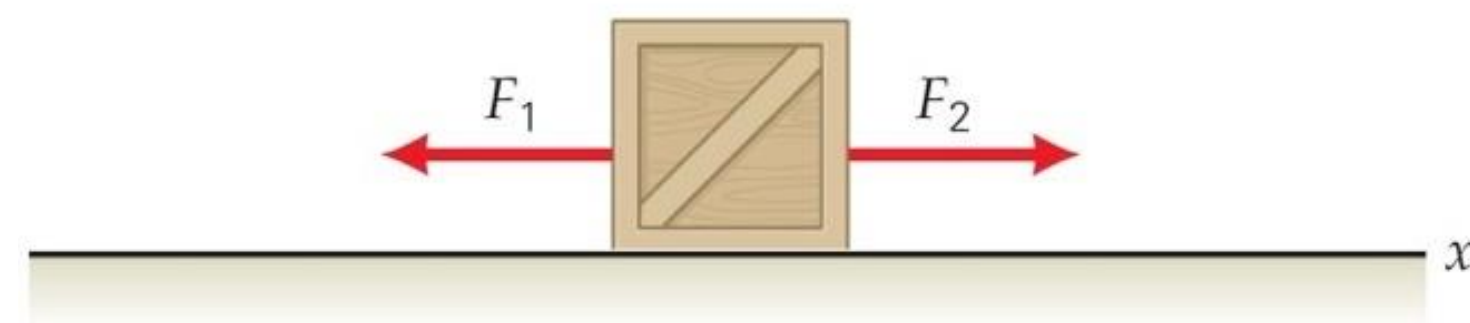
Newton's first law

If $\vec{F}_{\text{net}} = 0$, then $\vec{a} = 0$.

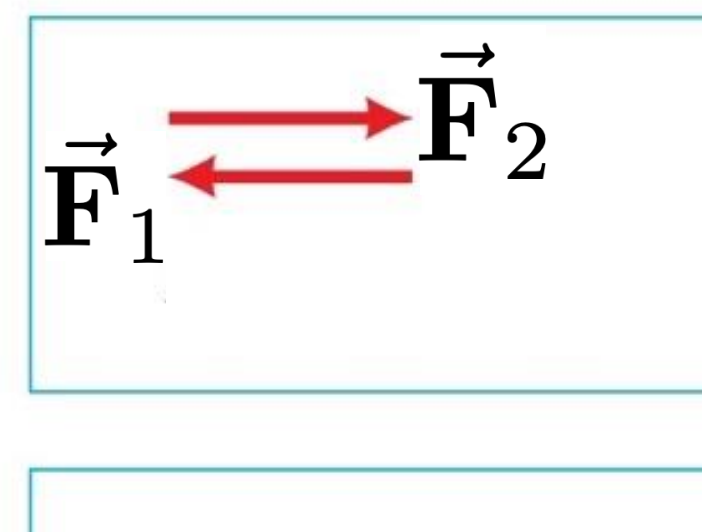
If $\vec{a} = 0$, then $\vec{F}_{\text{net}} = 0$.

- If $\vec{F}_{\text{net}} = \sum_i \vec{F}_i$ on the object is 0, then $\vec{a} = 0$ and $\vec{v} = v_0$, vice versa

- If initially at rest, object remains at rest
- If initially moving, moves at a constant velocity



(b) Zero net force (balanced forces)



$$\vec{F}_{\text{net}} = \vec{F}_1 + \vec{F}_2 = 0$$
$$\vec{a} = 0$$

Clicker question 2

$$\vec{a} = 0$$

A hockey puck slides on ice at constant velocity.

What is the *net* force acting on the puck?

Newton's First Law

- ☒ A Zero
- ☐ B Equal to its weight
- ☐ C Less than its weight but more than zero
- ☐ D Depends on the speed of the puck

If $\vec{a} = 0$, then \vec{F}_{net} is 0

Example 1

Given: 3 \vec{F} 's, $\vec{a} = 0$, \vec{F}_1 , \vec{F}_2
Goal: \vec{F}_3

- Three forces work on an object moving with a constant velocity. One force is $\vec{F}_1 = 1.0\text{ N}\hat{i} + 2.0\text{ N}\hat{j}$, another force is $\vec{F}_2 = -1.0\text{ N}\hat{j} + 3.0\text{ N}\hat{k}$. What is the third force?

Step 1: $\vec{a} = 0$, Newton's 1st law: $\vec{F}_{\text{net}} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 = 0$

Rewrite: $\vec{F}_3 = -\vec{F}_1 - \vec{F}_2$

Step 2: $\vec{F}_3 = -(1.0\text{ N}\hat{i} + 2.0\text{ N}\hat{j}) - (-1.0\text{ N}\hat{j} + 3.0\text{ N}\hat{k})$
 $= -1.0\text{ N}\hat{i} - 1.0\text{ N}\hat{j} - 3.0\text{ N}\hat{k}$

Mass

- Inertia = tendency of an object to remain at rest or to remain at const velocity
 - How much an object “resists” accelerating
- Mass = measure of inertia (units kg)
 - Example: Mass of electronic devices,

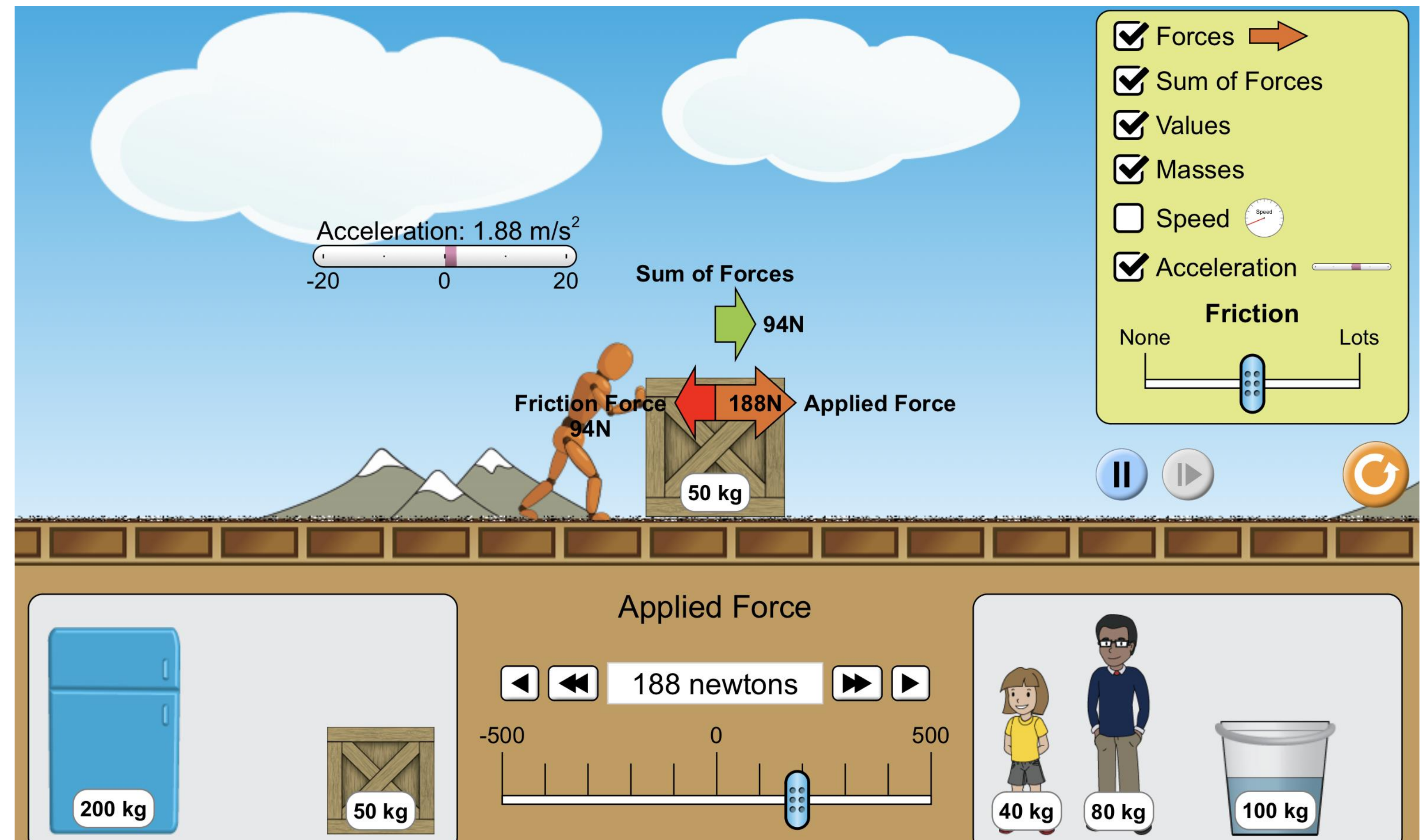


2004
Power Mac
G5
18 kg



2012
iPhone 5
0.1 kg

Simulation demo



https://phet.colorado.edu/sims/html/forces-and-motion-basics/latest/forces-and-motion-basics_all.html

Newton's second law

- If the net force on an object of mass m is \vec{F}_{net} , then:

Unit: N \rightarrow $\vec{F}_{net} = m\vec{a}$ $\text{kg} \cdot \text{m} \cdot \text{s}^{-2}$

Unit: kg Unit: m/s²

$N = \text{kg} \cdot \text{m/s}^2$
Newton

- Vector equation
- Acceleration of an object is in the same direction as the net force on it

Clicker question 3

- The **net force** on a box is in the positive x direction. Which of the following statements best describes the motion of the box?

A

Its velocity is parallel to the x axis.

B

Its acceleration is parallel to the x axis.

C

Both its velocity and its acceleration are parallel to the x axis.

D

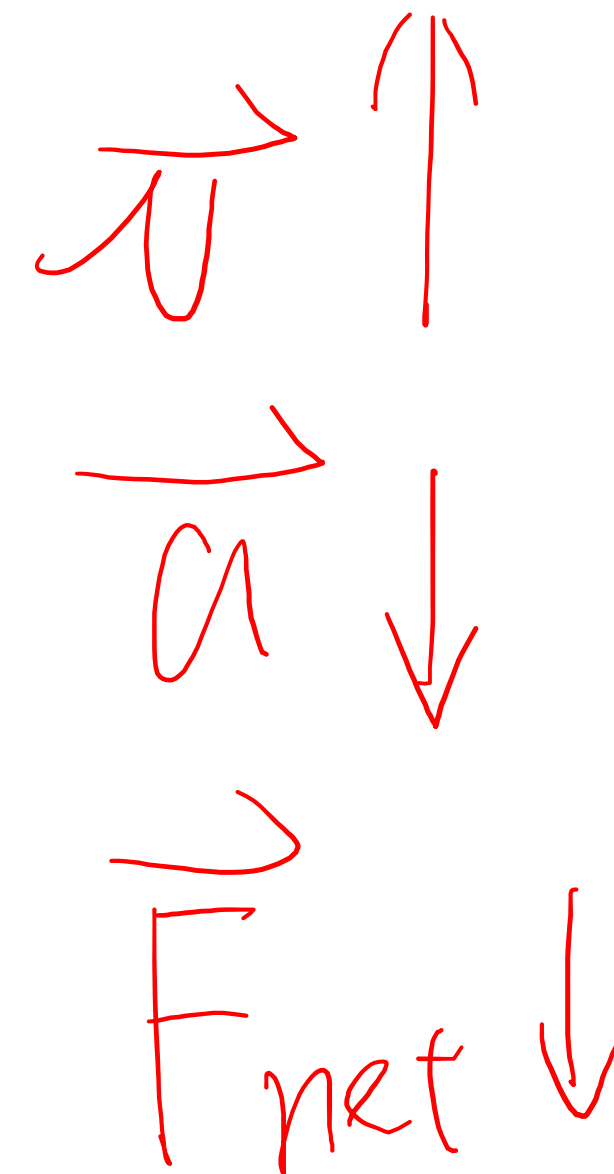
Neither its velocity nor its acceleration need to be parallel to the x axis.



Examples

Throwing balls

Free fall : Rising



Example

Given: $\sum \vec{F}'s$, m , \vec{F}_1 , \vec{F}_2

Goal: \vec{a}

- There are only two forces on the 2.43 kg box in the following figure. For $F_1 = 26.2 \text{ N } \hat{i}$, and $F_2 = -37.92 \text{ N } \hat{i} - 25.4 \text{ N } \hat{j}$. Express the acceleration, \vec{a} , in unit-vector notation.

Step 1: Newton's 2nd law:

$$\vec{F}_{\text{net}} = m \vec{a}$$

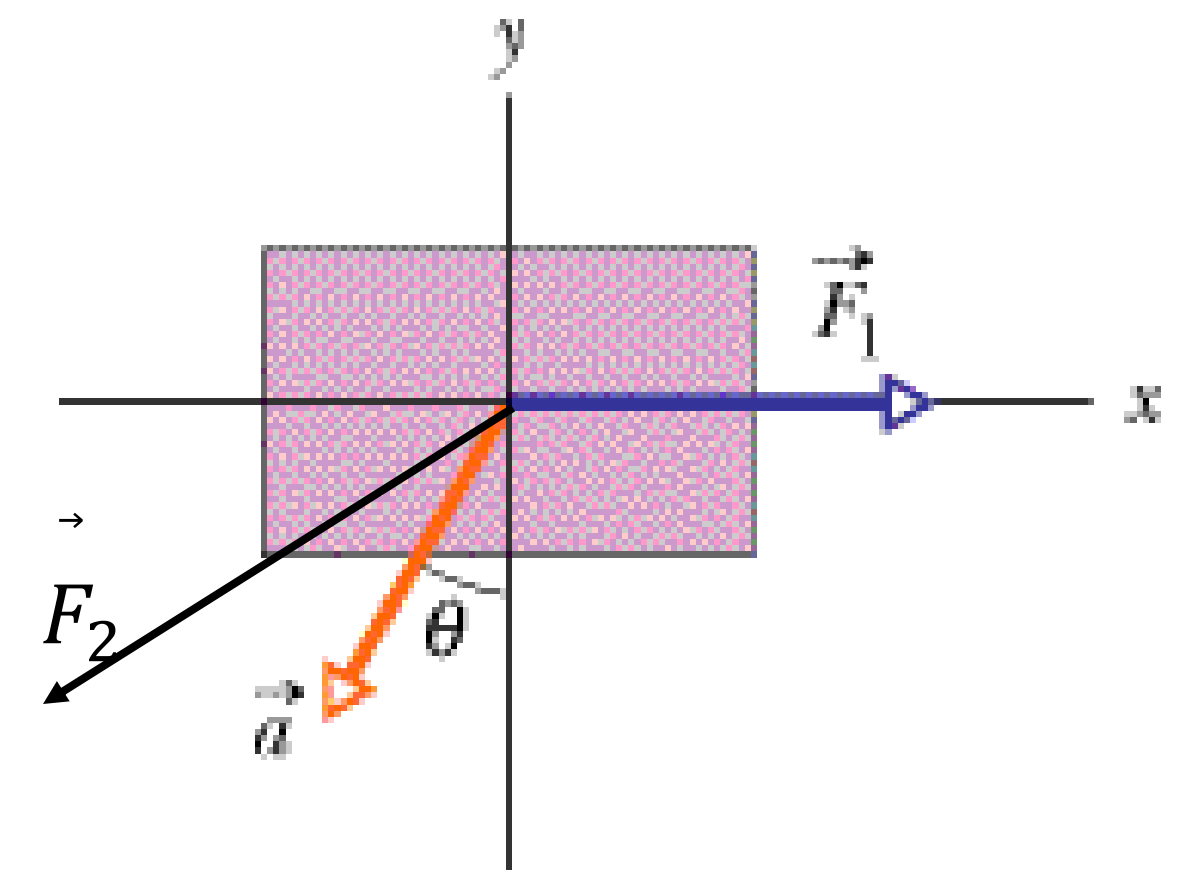
Step 2: $\vec{F}_1 + \vec{F}_2 = m \vec{a}$

$$\rightarrow \vec{a} = \frac{\vec{F}_1 + \vec{F}_2}{m}$$

$$= \frac{26.2 \text{ N } \hat{i} + (-37.92 \text{ N } \hat{i} - 25.4 \text{ N } \hat{j})}{2.43 \text{ kg}}$$

$$\approx -4.82 \text{ m s}^{-2} \hat{i} - 10.45 \text{ m s}^{-2} \hat{j}$$

$$\text{N} \sim \text{kg} \cdot \text{m} \cdot \text{s}^{-2}$$

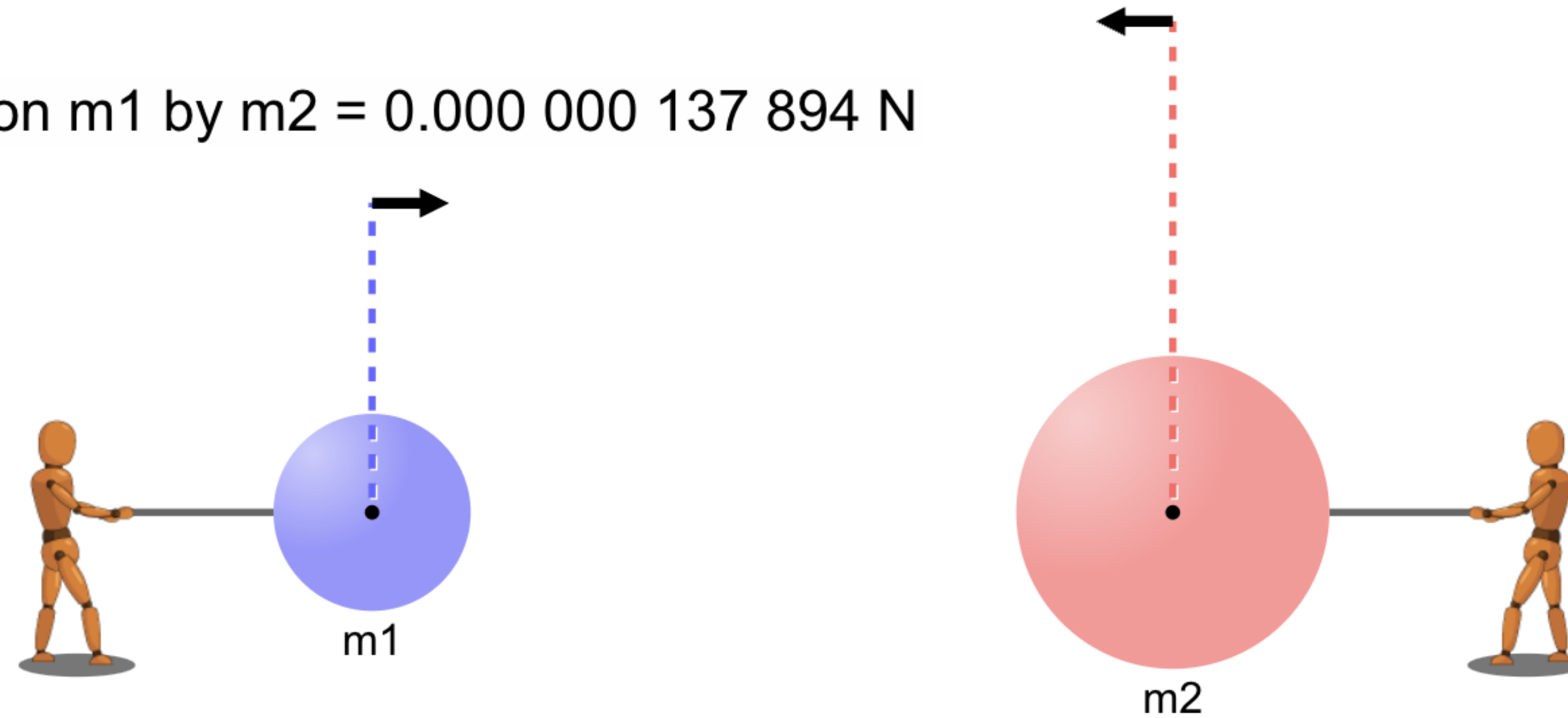


Example

Simulation demo

Force on m2 by m1 = 0.000 000 137 894 N

Force on m1 by m2 = 0.000 000 137 894 N



https://phet.colorado.edu/sims/html/gravity-force-lab/latest/gravity-force-lab_all.html

Newton's third law

$$\vec{F}_{\text{on B by A}} = -\vec{F}_{\text{on A by B}}$$

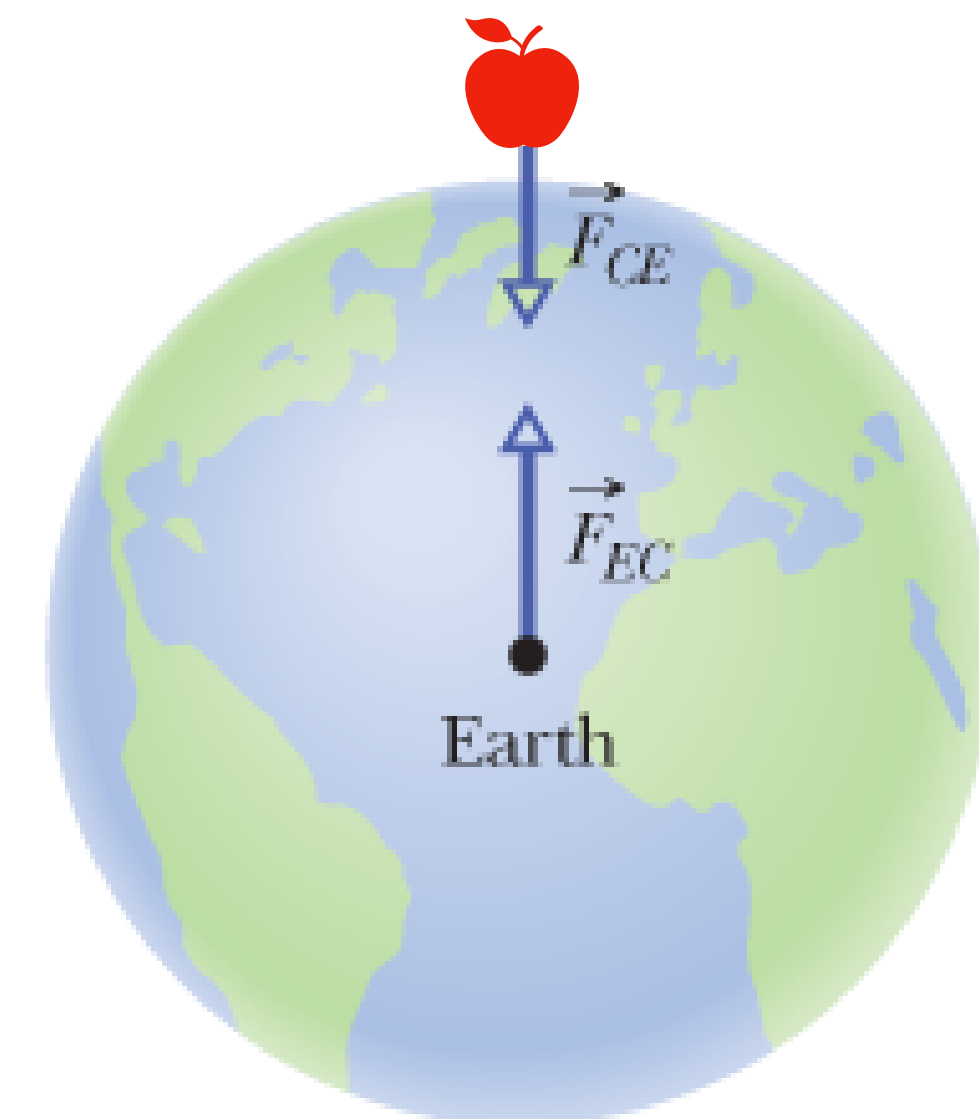
- **Newton's third law:** When two bodies A and B interact, if force *on A by B* is \vec{F}_{AB} , then Force *on B by A* is $\vec{F}_{BA} = -\vec{F}_{AB}$.
- Example: when the car hits the wall, the wall also pushes the car.

$$\vec{F}_{\text{on car by wall}} = -\vec{F}_{\text{on wall by car}}$$



Force pairs in Newton's third law

- **Newton's 3rd law:** "For every force on A by B , there is an equal but opposite force on B by A "
 - This pair of forces is called a force pair
 - The two forces in such force pair must be
 - ▶ acting on two different objects
 - ▶ and must be reciprocal



These are
third-law force
pairs.

Clicker question 4 (checkpoint)

Force pair: 1) On two different
obj.
2) reciprocal

- A 50-kg student pushes a 2-kg box that moves at constant speed along a smooth surface, as shown. Which of the following is a force pair?

A

The friction between the box and the surface, and the horizontal component of the push on the box.

Not reciprocal

B

The normal force on the box and the weight of the box.

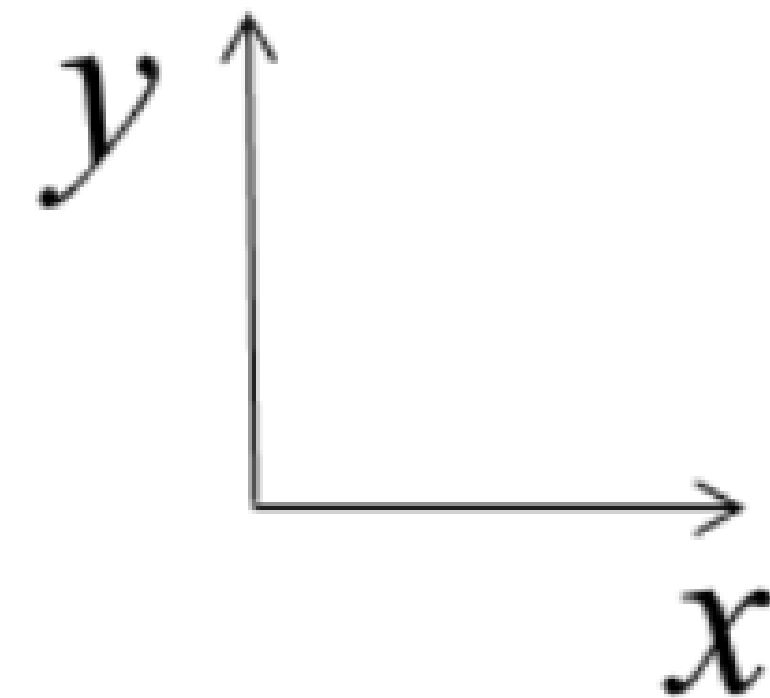
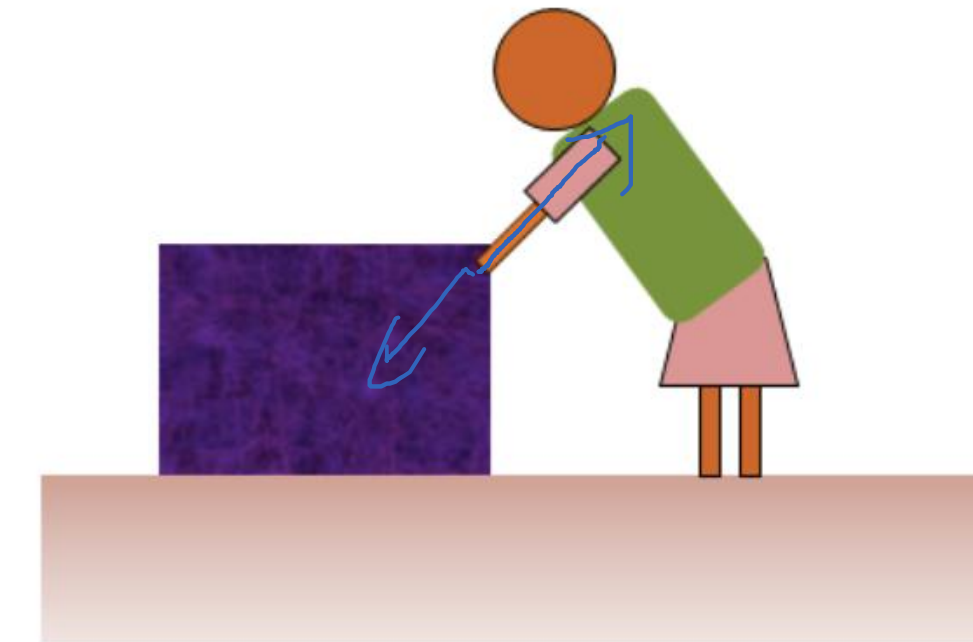
1 obj.

C

The push on the box by the student and the push on the student by the box.

D



The vertical component of the push applied by the student and the weight of the box.

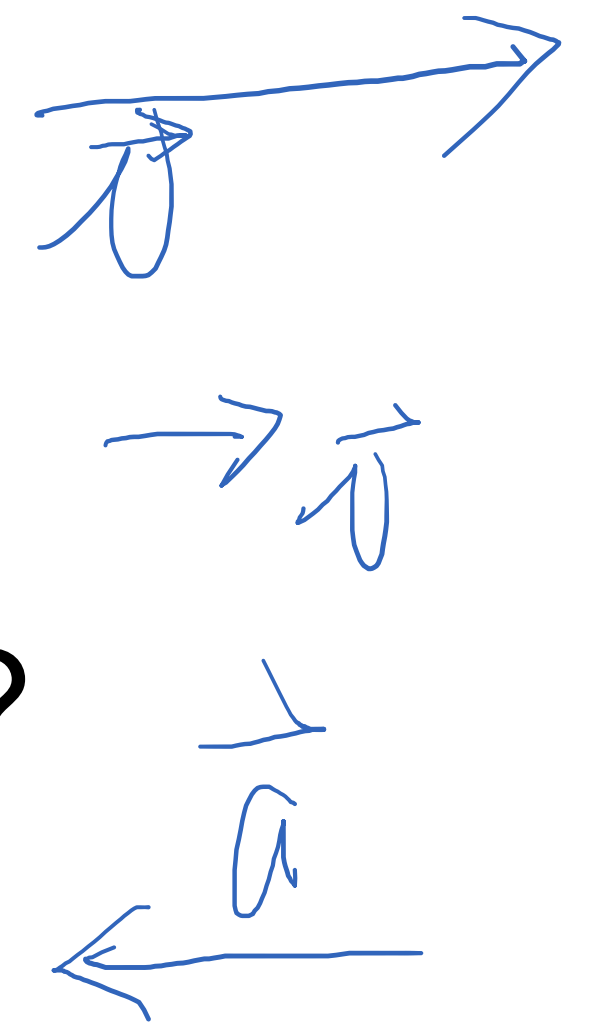




Clicker question 5

- WALL-E is moving rightward and wants to slow down. Which direction is his desired acceleration?

			Not enough info
			Not sure



Clicker question 6

- WALL-E wants to accelerate left. Which direction should be force **on** Wall-E by the fire extinguisher?

A	→	C	Not enough info
B	←	D	Not sure

$F_{\text{net}} = m \vec{a}$



Clicker question 7

Newton's 3rd
law

- WALL-E is moving rightward and wants to slow down. Which way should he aim?

			Not enough info
			Not sure



<http://www.youtube.com/watch?v=hHXx8AmBwXg>

Summary: Newton's three laws

- Newton's 1st law:
 - If $\vec{F}_{net} = 0$ on an object, then $\vec{a} = 0$ for the object, vice versa.
- Newton's 2nd law:
 - $\vec{F}_{net} = m\vec{a}$
- Newton's 3rd law:
 - “For a force on A **by** B , there is an equal and opposite force on B **by** A ”:
$$\vec{F}_{AB} = -\vec{F}_{BA}$$