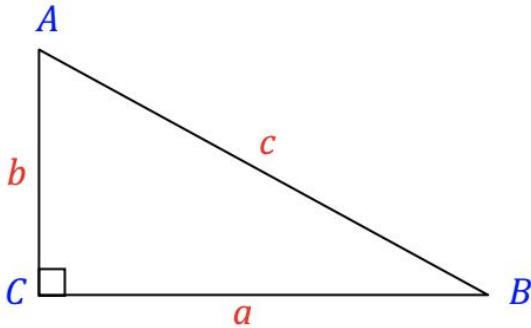


Pythagoras Theorem and Trigonometry

Pythagoras Theorem

In a right-angled triangle (one of the angles is 90°), the longest side is known as the hypotenuse. The other two shorter sides are known as the leg of the right-angled triangle.

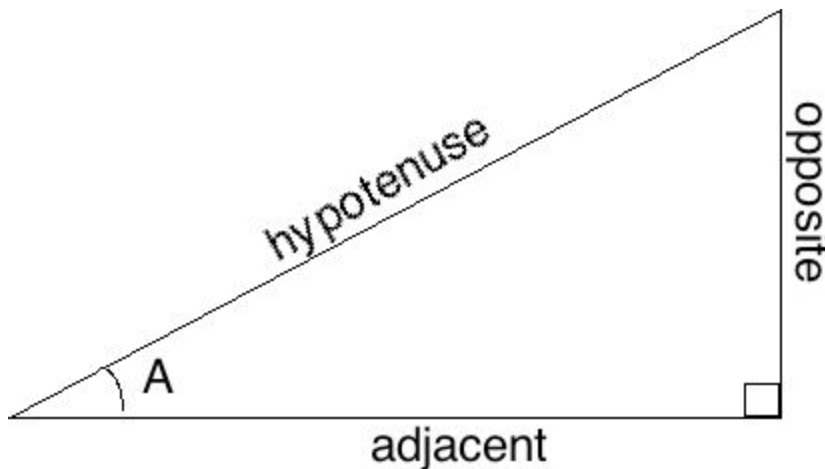


$$C^2 = b^2 + a^2$$

Trigonometry

Trigonometry refers to the mathematical discipline dealing with the relationships between the sides and angles of triangles.

Trigonometric: Basic Terminology



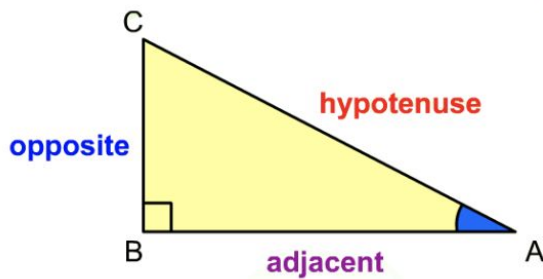
Adjacent is adjacent(next to) the angle A

Opposite is opposite the angle A

The longest side is the hypotenuse

Trigonometric ratios: Sin, Cos, Tan

The 3 basic Trigonometric Ratios are namely, **Sine** Ratio, **Cosine** Ratio and **Tangent** Ratio.



$$\sin A = \frac{CB(\text{opp})}{CA(\text{HYP})}$$

$$\cos A = \frac{BA(\text{adj})}{CA(\text{HYP})}$$

$$\tan A = \frac{CB(\text{opp})}{BA(\text{adj})}$$

Finding Unknown Angles in Right-Angled Triangles Given Trigonometric Ratios

\sin^{-1} (inverse sine) goes the other way opposite to sine. It takes in the ratio of "Opposite/hypotenuse" and gives us an angle.

$\sin^{-1}(\dots)$ takes a ratio whereas $\sin(\dots)$ takes an angle. So x can be the input of both $\sin^{-1}(\dots)$ and $\sin(\dots)$ at the same time.

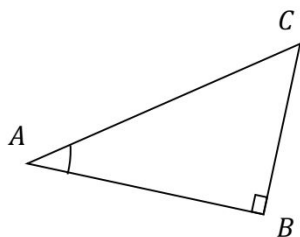


Diagram 1

The ratio $\frac{\text{Opposite}}{\text{Hypotenuse}}$ is also known as the **sine** of angle A or $\sin A$.

The ratio $\frac{\text{Adjacent}}{\text{Hypotenuse}}$ is also known as the **cosine** of angle A or $\cos A$.

The ratio $\frac{\text{Opposite}}{\text{Adjacent}}$ is also known as the **tangent** of angle A or $\tan A$.

From Diagram 1

$$\tan A = \frac{\text{opp.}}{\text{adj.}} = \frac{BC}{AB} \quad \text{TOA}$$

$$\cos A = \frac{\text{adj.}}{\text{hyp.}} = \frac{AB}{AC} \quad \text{CAH}$$

$$\sin A = \frac{\text{opp.}}{\text{hyp.}} = \frac{BC}{AC} \quad \text{SOH}$$

Note:

Angles sum of triangle = 90°

similarly ...

$$\tan(90 - A) = \frac{\text{opp.}}{\text{adj.}} = \frac{AB}{BC} \quad \text{TOA}$$

$$\cos(90 - A) = \frac{\text{adj.}}{\text{hyp.}} = \frac{BC}{AC} \quad \text{CAH}$$

$$\sin(90 - A) = \frac{\text{opp.}}{\text{hyp.}} = \frac{AB}{AC} \quad \text{SOH}$$

Note:

$90^\circ - A = C$