## **Chemicals required for various hardness constituents**

### **Key Points:**

- 1. Substances such as NaCl, Na<sub>2</sub>SO<sub>4</sub>, NaNO<sub>3</sub>, KCl, K<sub>2</sub>SO<sub>4</sub>, KNO<sub>3</sub>, SiO<sub>2</sub>, Fe<sub>2</sub>O<sub>3</sub>, etc. do not consume any L & S and should therefore be excluded from the calculation of L & S requirements.
- 2. All substances must be converted into their respective CaCO<sub>3</sub> equivalents.
- 3. Ca-hardness is precipitated as CaCO<sub>3</sub>, while Mg-hardness is precipitated as Mg(OH)<sub>2</sub>.

#### Chemicals requirement for Temporary hardness constituents:

- A.  $Ca(HCO_3)_2 + Ca(OH)_2 \rightarrow 2CaCO_3 + 2H_2O$  ------ needs 1 mole of L (1L) B. (i)  $Mg(HCO_3)_2 + Ca(OH)_2 \rightarrow Ca(HCO_3)_2 + Mg(OH)_2$  ----- 1L (ii)  $Ca(HCO_3)_2 + Ca(OH)_2 \rightarrow 2CaCO_3 + 2H_2O$  ----- 1L Or by combining eq. (i) and (ii) we get  $Mg(HCO_3)_2 + 2Ca(OH)_2 \rightarrow 2CaCO_3 + Mg(OH)_2 + 2H_2O$  ---- 2L
- ✓ 1 mole of  $Ca(HCO_3)_2$  needs 1 mole of Lime whereas 1 mole of  $Mg(HCO_3)_2$  needs 2 moles of Lime.

#### Chemicals requirement for Permanent hardness constituents:

- A. Calcium permanent hardness (CaCl<sub>2</sub>, Ca(NO<sub>3</sub>)<sub>2</sub>, CaSO<sub>4</sub>)
- (i)  $CaCl_2 + Na_2CO_3 \rightarrow CaCO_3 + 2 NaCl$  ----- needs 1 mole of Soda (1S)
- (ii)  $Ca(NO_3)_2 + Na_2CO_3 \rightarrow CaCO_3 + 2 NaNO_3$  ---- needs 1 mole of Soda (1S)
- (iii)  $CaSO_4 + Na_2CO_3 \rightarrow CaCO_3 + Na_2SO_4 ---- needs 1 mole of Soda (1S)$
- ✓ \*\*\* All Calcium permanent hardness constituents [CaCl<sub>2</sub>, CaSO<sub>4</sub>, Ca(NO<sub>3</sub>)<sub>2</sub>] need only 1- mole of Soda (1S)
- B. Magnesium permanent hardness (MgCl<sub>2</sub>, Mg(NO<sub>3</sub>)<sub>2</sub>, MgSO<sub>4</sub>)
- (i)  $MgCl_2 + Ca(OH)_2 + \rightarrow Mg(OH)_2 + CaCl_2$  ----- needs 1 mole of Lime (1L) but releasing 1 mole of CaCl2. For its removal we need 1 mole of Soda  $CaCl_2 + Na_2CO_3 \rightarrow CaCO_3 + 2 NaCl$  ----- needs 1 mole of Soda (1S)
- ✓ So, 1 mole of Magnesium permanent hardness needs 1 mole of lime and 1 mole of Soda (1L + 1S).

#### Chemicals requirement for coagulants (FeSO<sub>4</sub>, Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub>):

- (i) FeSO<sub>4</sub> + Ca(OH)<sub>2</sub> +  $\rightarrow$  Fe(OH)<sub>2</sub> + CaSO<sub>4</sub> ----- needs 1 mole of Lime (1L) but releasing 1 mole of CaSO<sub>4</sub>. Its removal needed 1 mole of Soda CaSO<sub>4</sub> + Na<sub>2</sub>CO<sub>3</sub>  $\rightarrow$  CaCO<sub>3</sub> + Na<sub>2</sub>SO<sub>4</sub> ----- needs 1 mole of Soda (1S)
- ✓ So, FeSO<sub>4</sub> needs 1 mole of lime and 1 mole of Soda (1L + 1S).
  - (ii)  $Al_2(SO_4)_3 + 3Ca(OH)_2 + \rightarrow 2Al(OH)_3 + 3CaSO_4 3$  moles of Lime (3L)  $3CaSO_4 + 3Na_2CO_3 \rightarrow 3CaCO_3 + 3Na_2SO_4 \dots$  needs 3 mole of Soda (3S)
- ✓ So,  $Al_2(SO_4)_3$  needs 3 mole of lime and 3 mole of Soda (3L + 3S).

Q.1 Give reason that 1 mole of  $Ca(HCO_3)_2$  needs 1 mole of Lime whereas 1 mole of  $Mg(HCO_3)_2$  needs 2 moles of Lime. (write chemical reactions)

Ans.

A. 
$$Ca(HCO_3)_2 + Ca(OH)_2 \rightarrow 2CaCO_3 + 2H_2O$$
 ----- needs 1 mole of L (1L)  
B. (i)  $Mg(HCO_3)_2 + Ca(OH)_2 \rightarrow Ca(HCO_3)_2 + Mg(OH)_2$  ----- 1L   
(ii)  $Ca(HCO_3)_2 + Ca(OH)_2 \rightarrow 2CaCO_3 + 2H_2O$  ----- 1L }

Q. 2. Give reason that Calcium permanent hardness constituents need only 1- mole of Soda (1S).

Ans.

- (i)  $CaCl_2 + Na_2CO_3 \rightarrow CaCO_3 + 2 NaCl$  ----- needs 1 mole of Soda (1S)
- (ii)  $Ca(NO_3)_2 + Na_2CO_3 \rightarrow CaCO_3 + 2 NaNO_3$  ---- needs 1 mole of Soda (1S)
- (iii)  $CaSO_4 + Na_2CO_3 \rightarrow CaCO_3 + Na_2SO_4 ---- needs 1 mole of Soda (1S)$

Q.3. Give reason that 1 mole of Magnesium permanent hardness needs 1 mole of lime and 1 mole of Soda (1L + 1S).

**Ans.** (i)  $MgCl_2 + Ca(OH)_2 + \rightarrow Mg(OH)_2 + CaCl_2$  ----- needs 1 mole of Lime (1L) but releasing 1 mole of CaCl<sub>2</sub>. For removal of CaCl<sub>2</sub> we need 1 mole of Soda as per the following reaction

$$CaCl_2 + Na_2CO_3 \rightarrow CaCO_3 + 2 NaCl$$
 ----- needs 1 mole of Soda (1S)

Q.4. Give reason that lime is not consumed by CaCl<sub>2</sub> or any calcium-permanent hadness constituents.

Ans. 
$$CaCl_2 + Ca(OH)_2 \rightarrow CaCl_2 + Ca(OH)_2$$

See the above reaction, there is no change in reactant and product side. It means there is no reaction between these two constituents.

# **Solved Numerical**

#### Note:

- (A) Lime required for softening of 1L of hard water (mg) = 74/100 (Lime consuming substances as CaCO<sub>3</sub> eq.) x Vol. of water x (100/% purity of lime)
- (B) Soda required for softening of 1L of hard water (mg) = 106/100 (Soda consuming substances as CaCO<sub>3</sub> eq.) x Vol. of water x (100/% purity of soda)

Solved numerical on Lime-soda Process

Example-1 A sample of water on analysis has been found to contain 100 mg/L of KHCO<sub>3</sub> and 200 mg/L of  $K_2SO_4$ . Calculate the amount of lime and soda required for softening of 10,000 litres of hard water. (At. mass: K = 39, Ca = 40, H = 1, C = 12, O = 16, S = 32 g/mol)

**Ans.** The amount of lime and soda required = 0, as both are non hardness constituents.

Example-2 A sample of water on analysis has been found to contain 100 mg/L of  $Mg(HCO_3)_2$  and 200 mg/L of  $K_2SO_4$ . Calculate the amount of lime and soda required for softening of 10,000 litres of hard water. (At. mass: Na = 23, Mg= 24, H =1, C = 12, O =16, K=39 g/mol, S = 32 g/mol)

**Solution:** Na<sub>2</sub>SO<sub>4</sub> does not consume chemicals like lime and soda.

N.B: if purity of lime and soda is not mention then take % purity = 100

 $Mg(HCO_3)_2$  as  $CaCO_3$  eq. = 100 x (100/146) = 68.493 mg/L

 $Mg(HCO_3)_2$  require only 2L ( **no soda requirement**, that is soda amount = 0)

So, lime required for softening of 10,000 L of hard water =  $74/100(Ca(HCO_3)_2 CaCO_3 eq.) x V x (100/\% purity of lime)$ 

= (74/100) x 2 x 68.493 x 10,000 L x 100/100 (here purity of lime 100%)

= 1013696.4 mg = 1.013 Kg (Ans.)

Example-3 A sample of water on analysis has been found to contain 150 mg/L of  $Ca(HCO_3)_2$  and 100 mg/L of  $Na_2SO_4$ . Calculate the amount of lime and soda required for softening of 15,000 litres of hard water after boiling the water for 20 min. (At. mass: Na = 23, Ca = 40, H = 1, C = 12, O = 16, S = 32 g/mol)

**Solution:** As boiling removes Ca(HCO<sub>3</sub>)<sub>2</sub>, lime and soda required will be zero.

Example-4 Calculate the amount of lime and soda required for softening of 100 L of hard water having 95 mg/L of MgCl<sub>2</sub>.

Solution:  $MgCl_2$  needs 1L + 1S.

 $CaCl_2$  as  $CaCO_3$  eq. = 95 x (100/95) = 100 mg/L

- (A) Lime required = 74/100 (MgCl<sub>2</sub> as CaCO<sub>3</sub> eq.) x Vol. of water x (100/% purity of lime) = (74/100) x 100 x 100 x (100/100) = 7400 mg
- (B) Soda required =  $106/100 (MgCl_2 \text{ as as } CaCO_3 \text{ eq.}) \times Vol. \text{ of water } \times (100\% \text{ purity of soda}) = (106/100) \times 100 \times 100 \times (100/100) = 10600 \text{ mg}$

Example-6 Calculate the amount of lime required for softening of 100 L of hard water having 250 mg/L of CaCl<sub>2</sub> and 220 mg/L of KCl

**Ans.** KCl is a non hardness mass.

 $CaCl_2$  do not consume any lime. So, lime required = 0

Example-7 A sample of water on analysis has been found to contain 150 mg/L of  $Ca(HCO_3)_2$ , 100 mg/L of  $Mg(HCO_3)_2$  and 100 mg/L og KCl. Calculate the amount of soda required for softening of 15,000 litres of hard water.

Ans. Soda required = 0

Example-8 A sample of water on analysis has been found to contain 150 mg/L of  $Ca(HCO_3)_2$  and 100 mg/L of  $CaSO_4$ . Calculate the amount of lime and soda required for softening of 15,000 litres of hard water after boiling the water for 20 min. (At. mass: Ca = 40, H = 1, C = 12, O = 16, S = 32 g/mol)

**Solution: Boiling will remove the** Ca(HCO<sub>3</sub>)<sub>2.</sub> So only CaSO<sub>4</sub> will be remain in the hard water after boiling.

CaSO<sub>4</sub> consumes only soda (Mol .mass = 136 g)

 $CaSO_4$  as  $CaCO_3$  eq. = 100 x (100/136) = 73.529 mg/L

**Soda required** = 106/100 (CaSO<sub>4</sub> as CaCO<sub>3</sub> eq.) x V x (100/% purity of soda)

= 106/100 x 73.529 x 15,000 x 100/100 (purity of soda is 100%)

= 1169111.1 mg = 1.169 Kg (take  $1 \text{ mg} = 10^{-6} \text{ Kg}$ ).

Here, lime required = 0

Example-9 A sample of water on analysis has been found to contain 150 mg/L of  $Ca(HCO_3)_2$  and 200 mg/L of  $Ca(NO_3)_2$ . Calculate the amount of lime required for softening of 15,000 litres of hard water after boiling the water for 20 min. (At. mass: Ca = 40, H = 1, C = 12, O = 16, N = 14 g/mol)

**Solution:** Lime required = 0

Example-10 Calculate the amount of Lime and soda needed for the softening of 10 litres of hard water having 146 mg/l of Mg(HCO<sub>3</sub>)<sub>2</sub>.

**Solution:** We know that Mg(HCO<sub>3</sub>)<sub>2</sub> consumes 2 moles of lime and no soda.

 $Mg(HCO_3)_2$  as  $CaCO_3$  eq. = 146 x 100/146 = 100 mg/L or ppm

- (i) **Lime reqd.** = 74/100 (2 x Mg(HCO<sub>3</sub>)<sub>2</sub> as CaCO<sub>3</sub> eq.) x Vol. of hard water x (100/% purity) = (74/100) x 100 mg/L x 10 L x (100/100) = 1480 mg
- (ii) **Soda Reqd.** = 0 mg.

Example-11 Calculate the amount of Lime and soda needed for the softening of 50,000 litres of hard water having  $Mg(HCO_3)_2 = 144$  ppm,  $Ca(HCO_3)_2 = 25$  ppm,  $MgCl_2 = 95$  ppm,  $CaCl_2 = 111$  ppm,  $Fe_2O_3 = 25$  ppm, and  $Na_2SO_4 = 15$  ppm. Also find the cost of chemicals for softening. (Given that cost of lime = Rs.10 per Kg and cost of soda = Rs. 100 per Kg)

#### Solution:

As Fe<sub>2</sub>O<sub>3</sub> and Na<sub>2</sub>SO<sub>4</sub> are non-hardness constituents, they do not consume Lime (L) and Soda (S)

Constituents	Strength (ppm or	Mol. Mass	Chemical Need	CaCO <sub>3</sub> eq.
	mg/L)			(mg/L)
$Mg(HCO_3)_2$	144	146	2L	144 x (100/146)
				=98.63
Ca(HCO <sub>3</sub> ) <sub>2</sub>	25	162	1L	25 x (100/162)
			. (	=15.43
MgCl <sub>2</sub>	95	95	L+S	95 x (100/95)
				=100
CaCl <sub>2</sub>	111	111	S	111 x (100/111)
			4 1 7	=100

<sup>\*\*</sup>n-factor = 2 for all the salts

Remember that Lime is read. by  $Mg(HCO_3)_2$ ,  $Ca(HCO_3)_2$ , and  $MgCl_2$ 

(i) **Lime reqd.** =  $74/100 [(2 \text{ x Mg}(HCO_3)_2 + Ca(HCO_3)_2 + MgCl_2); all as CaCO_3 eq.] x Vol. of hard water x <math>(100/\% \text{ purity})$  = (74/100) x [2 x 98.63 + 15.43 + 100] mg/L x 50,000 L x (100/100) =  $11569530 \text{ mg} = 11569530 \text{ x } 10^{-6} \text{ Kg} = 11.5695 \text{ Kg}$ 

Soda is read. by only CaCl<sub>2</sub> and MgCl<sub>2</sub>

Cost of lime =  $11.5695 \times 10 = Rs. 115.695$ 

- (ii) Soda reqd. = 106/100 [(CaCl<sub>2</sub> + MgCl<sub>2</sub>); all as CaCO<sub>3</sub> eq.] x Vol. of hard water x (100/% purity)
  - $= (106/100) \times [100 + 100] \text{ mg/L} \times 50,000 \text{ L} \times (100/100)$
  - $= 10600000 \text{ mg} = 10600000 \text{ x } 10^{-6} \text{ Kg} = 10.6 \text{ Kg}$

**Cost of soda** =  $10.6 \times 100 = \text{Rs.} 1060$ 

Total cost of chemicals for softening of 50,000L of hard water = 115.695 = 1060 = Rs. 1175.695

**Example-12** 20,000 L of hard water to be softens by a chemist using a lime-soda softener. The budget allocated for the said purpose is Rs.500. Do you think the allocated amount is sufficient to get the job done? The sample contains  $Mg(HCO_3)_2 = 73$  ppm,  $Ca(HCO_3)_2 = 81$  ppm,  $MgCl_2 = 95$  ppm,  $CaSO_4 = 68$  ppm, and  $Na_2SO_4 = 30$  ppm. The purity of lime is 95% and that of soda is 90%. The costs per 1 Kg of lime and soda are Rs. 100 and Rs. 100, respectively.

**Solution:** As Na<sub>2</sub>SO<sub>4</sub> is a non-hardness constituent, it does not consume Lime (L) and Soda (S)

Constituents	Strength (ppm or	Mol. Mass	Chemical Need	CaCO <sub>3</sub> eq.
	mg/L)			(mg/L)
$Mg(HCO_3)_2$	73	146	2L	73 x (100/146)
				=50
Ca(HCO <sub>3</sub> ) <sub>2</sub>	81	162	1L	81 x (100/162)
				=50
MgCl <sub>2</sub>	95	95	L + S	95 x (100/95)
				=100
CaSO <sub>4</sub>	68	136	S	68 x (100/136)
				=50

Lime is read. by  $Mg(HCO_3)_2$ ,  $Ca(HCO_3)_2$ , and  $MgCl_2$ 

(i) Lime reqd. = 
$$74/100 [(2 \text{ x Mg(HCO}_3)_2 + \text{Ca(HCO}_3)_2 + \text{MgCl}_2); \text{ all as CaCO}_3 \text{ eq.}]$$
 x Vol. of hard water x ( $100/\%$  purity)

= 
$$(74/100)$$
 x  $[2 \times 50 + 50 + 100]$  mg/L x  $20,000$  L x  $(100/95)$ 

$$= 3894736.842 \text{ mg} = 3894736.842 \text{ x } 10^{-6} \text{ Kg} = 3.894 \text{ Kg}$$

 $(1 \text{ mg} = 10^{-6} \text{ Kg})$ 

Cost of lime =  $3.894 \times 100 = \text{Rs. } 389.4$ 

Soda is reqd. by only MgCl<sub>2</sub> and CaSO<sub>4</sub>

(i) **Soda reqd.** = 106/100 [(CaSO<sub>4</sub> + MgCl<sub>2</sub>); all as CaCO<sub>3</sub> eq.] x Vol. of hard water x (100/% purity)

= 
$$(106/100)$$
 x  $[50 + 100]$  mg/L x  $50,000$  L x  $(100/90)$ 

$$= 3533333.333 \text{ mg} = 35333333.333 \text{ x } 10^{-6} \text{ Kg} = 3.533 \text{ Kg}$$

Cost of soda =  $3.533 \times 100 = \text{Rs.} 353.3$ 

Now, total cost of chemicals = Rs. 389.4 + Rs. 353.3 = Rs. 742.7

No, the allocated amount is not sufficient to get the job done.

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