Artifact: A Computational Interpretation of Compact Closed Categories:

Reversible Programming with Negative and Fractional Types

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This document contains a list of claims in the paper and corresponding code.

2 Core Reversible Language: Π

• The syntax of Π in Fig.1 is formalized in Pi/Syntax.agda.

2.1 Abstract Machine Semantics

- The δ function in Fig.2 is defined in **Pi/Opsem.agda:L47**.
- The well-formed continuation stacks in Fig.3 are defined in Pi/Opsem.agda:L71.
- The machine states in Def.1 are defined in Pi/Opsem.agda:L81.
- The reduction relation in Fig.4 is defined in Pi/Opsem.agda:L86.
- Lem.2 is proved in Pi/NoRepeat.agda:L13.
- Lem.3 is proved in Pi/NoRepeat.agda:L29.
- Def.4 is defined in Pi/Eval.agda:L76.
- Def.5 is defined in Pi/Eval.agda:L121.
- Thm.6 is proved in Pi/Properties.agda:L31.

2.2 Interpreter

- The interpreter in Fig.5 is defined in Pi/Interp.agda:L9.
- Thm.7 is proved in Pi/Properties.agda:L49.

3 Termination of Reversible Abstract Machines

- The reversible abstract machine in Def.8 is defined in RevMachine.agda:L8.
- Lem.9 is proved in **RevNoRepeat.agda:L125**.
- Lem.10 is proved in Pi/Eval.agda:L13.
- Thm.11 is proved in Pi/Eval.agda:L76.
- The partial reversible abstract machine in Def.12 is defined in RevMachine.agda:L15.
- Lem.13 is proved in PartialRevNoRepeat.agda:L136.

4 Space and Time Resources and Trade-Offs

- $\#\sigma$ is defined in **TimeSpace.agda:L71**.
- The examples at the end of this section are in **TimeSpace.agda:L80-87**.

5 Negative Types: Π^m

5.1 Abstract Machine Semantics

- The syntax of Π^m is formalized in **Pi-/Syntax.agda**.
- Def.14 is defined in Pi-/Opsem.agda:L84.
- The transition rules in Fig.6 are defined in Pi-/Opsem.agda:L91.

5.2 Properties

- Lem.15 is proved in Pi-/NoRepeat.agda:L20.
- Lem.16 is proved in Pi-/NoRepeat.agda:L119.
- Lem.17 is proved in Pi-/Eval.agda:L23.
- Π^m is a reversible abstract machine is proved in Pi-/NoRepeat.agda:L223.
- Def.18 is generalized in Def.20.
- Def.20 and generalized Thm.19 are in **Pi-/Eval.agda:L172**. The proof relies on the finitness of execution traces for Π^m which follows from the finitness of Π^m machine states and the non-repeating lemma for reversible abstract machines (Lem.9).
- Def.21 is defined in Pi-/Eval.agda:L177.
- Thm.22 is proved in Pi-/Properties.agda:L133.

5.3 Interpreter

- The interpreter is defined in Pi-/Interp.agda:L12.
- Thm.23 is proved in Pi-/Properties.agda:L193.

5.4 Compact Closed Category

- Thm.24 is proved in Pi-/Category.agda:L297.
- Thm.25 is proved in Pi-/Category.agda:L301.
- The code for the remark in the end is in Pi-/Category.agda:L306-363.

6 Fractional Types: Π^d

6.1 Abstract Machine Semantics

- The syntax of Π^d is formalized in **PiFrac/Syntax.agda**.
- Def.26 is defined in PiFrac/Opsem.agda:L103.
- The transition rules in Fig.8 are defined in PiFrac/Opsem.agda:L109.

6.2 Properties

- Lem.27 is proved in PiFrac/NoRepeat.agda:L17.
- Lem.28 is proved in PiFrac/NoRepeat.agda:L38.
- Lem.29 is proved in PiFrac/Eval.agda:L18.
- Π^d is a partial reversible abstract machine is proved in **PiFrac/NoRepeat.agda:L113**.
- Def.30 and Thm.31 is in PiFrac/Eval.agda:L96.
- Def.32 and Thm.33 is in PiFrac/Eval.agda:L153.
- Thm.34 is proved in PiFrac/Properties.agda:L20.

6.3 Interpreter

- The interpreter is defined in PiFrac/Interp.agda:L15.
- Thm.35 is proved in PiFrac/Properties.agda:L40.

6.4 Compact Closed Category

• Thm.36 is proved in **PiFrac/Category.agda:L110**.

7 Combining Negative and Fractional Types: $\Pi^{\mathbb{Q}}$

7.1 Abstract Machine Semantics

- The syntax of $\Pi^{\mathbb{Q}}$ is defined in **PiQ/Syntax.agda**.
- Def.37 is defined in PiQ/Opsem.agda:L115.
- The transition rules in Fig.9 are defined in PiQ/Opsem.agda:L123.

7.2 Properties

- Lem.38 is proved in PiQ/NoRepeat.agda:L17.
- Lem.39 is proved in PiQ/NoRepeat.agda:L135.
- Lem.40 is proved in PiQ/Eval.agda:L24.
- $\Pi^{\mathbb{Q}}$ is a partial reversible abstract machine is proved in PiQ/NoRepeat.agda:L250.
- Def.41 and Thm.42 is in PiQ/Eval.agda:L196. This proof relies on the finitness of execution traces for $\Pi^{\mathbb{Q}}$ which follows from the finitness of $\Pi^{\mathbb{Q}}$ machine states and the non-repeating lemma for partial reversible abstract machines (Lem.13).
- Def.43 is in PiQ/Eval.agda:L201.
- Thm.44 is proved in PiQ/Properties.agda:L217.

7.3 Interpreter

- The interpreter is defined in PiQ/Interp.agda:L20.
- The equivalence between interpreter and machine semantics is proved in PiQ/Properties.agda:L402.

8 Programming with Negative and Fractional Types

- All examples except for the SAT solver are in PiQ/Examples.agda.
- The implementation of the SAT solver is in PiQ/SAT.agda.