Data for the Pattern Recognition paper, including a comparison with state-of-the-art methods and images used for medical analysis.

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## 1 Appendix B. Comparison of state-of-the-art methods with our method.

This document presents Tables 1, 2, and 3, which compare state-of-the-art methods with our approach for the 66 voxelized objects used in Experiment 3. The results demonstrate identical values for shape descriptors, simplexes, and tetravoxels. Only 12 objects from the sample are shown to verify the accuracy of these formulas, but the complete dataset can be requested via email at Cesareduardomucha@hotmail.com.

Additionally, Tables 4, 5, 6, 7, and 8 provide a comparison with Experiment 4, which focused on medical images from the BraTS 2020 dataset. In this case, the results also show that our method achieved 100% accuracy across all cases.

In Figure 1, some of the images of specimens from the BraTS 2020 dataset are displayed, featuring six tumor samples.

Table 1: Comparison between the state-of-the-art approach and the formulas discovered for each model. Part 1  $\,$ 

discovered for eac	11 1110 (1011) 1 (110 1	Results	
Test images	Descriptors and Simplexes	Traditional methods	All formulas found
Axolotl	Euler ES CS Volume Points Edges	-1 $248648$ $9461726$ $3195350$ $3321260$ $9836285$	-1 248648 9461726 3195350 3321260 9836285
	Faces Tetravoxels	9710374 0	9710374 $0$
Babydragon	Euler ES CS Volume Points Edges Faces Tetravoxels	-8 61306 768799 266484 298021 861650 830105 739038	-8 61306 768799 266484 298021 861650 830105 739038
Bird	Euler ES CS Volume Points Edges Faces Tetravoxels	-1 21880 301003 103981 115438 334341 322883 290581	-1 21880 301003 103981 115438 334341 322883 290581
Cheese	Euler ES CS Volume Points Edges Faces Tetravoxels	$ \begin{array}{r} -2 \\ 81148 \\ 2143672 \\ 728082 \\ 769004 \\ 2265744 \\ 2224820 \\ 2103448 \end{array} $	-2 81148 2143672 728082 769004 2265744 2224820 2103448

Table 2: Comparison between the state-of-the-art approach and the formulas

discovered for each model. Part 2

iiscovered for each	n moder. 1 art 2	Results		
Test images	Descriptors and Simplexes	Traditional methods	All formulas found	
	Euler	0	0	
	ES	5788	5788	
	$\operatorname{CS}$	12520	12520	
C	Volume	5138	5138	
$\mathbf{Cup}$	Points	8120	8120	
	Edges	21290	21290	
	Faces	18308	18308	
	Tetravoxels	9714	9714	
	Euler	0	0	
	ES	6538	6538	
	$^{\mathrm{CS}}$	26137	26137	
m.	Volume	9802	9802	
Torus	Points	13294	13294	
	Edges	36167	36167	
	Faces	32675	32675	
	Tetravoxels	23091	23091	
	Euler	-1	-1	
	ES	6712	6712	
	$\operatorname{CS}$	25687	25687	
Torush	Volume	9681	9681	
iorusn	Points	13255	13255	
	Edges	35974	35974	
	Faces	32399	32399	
	Tetravoxels	22550	22550	
	Euler	0	0	
	ES	20440	20440	
	$\operatorname{CS}$	34672	34672	
Vase	Volume	14964	14964	
vase	Points	25226	25226	
	Edges	65374	65374	
	Faces	55112	55112	
	Tetravoxels	24494	24494	

Table 3: Comparison between the state-of-the-art approach and the formulas discovered for each model. Part 3  $\,$ 

		Results	
Test images	Descriptors and Simplexes	Traditional methods	All formulas found
	Euler	-1	-1
	ES	21880	21880
	CS	301003	301003
Bird	Volume	103981	103981
Dira	Points	115438	115438
	Edges	334341	334341
	Faces	322883	322883
	Tetravoxels	290581	290581
	Euler	1	1
	ES	40248	40248
	CS	646761	646761
T21 1 4	Volume	222295	222295
Elephant	Points	242931	242931
	Edges	707644	707644
	Faces	687009	687009
	Tetravoxels	627148	627148
	Euler	-7	-7
	ES	23422	23422
	CS	215719	215719
Gun	Volume	75810	75810
Gun	Points	87922	87922
	Edges	251260	251260
	Faces	239141	239141
	Tetravoxels	204416	204416
	Euler	1	1
	ES	77350	77350
	$\operatorname{CS}$	3199273	3199273
Moon	Volume	1079316	1079316
Moon	Points	1118377	1118377
	Edges	3315683	3315683
	Faces	3276623	3276623
	Tetravoxels	3160983	3160983

Table 4: Comparison of four images from the BRATS dataset and demonstration of the most effective formulas using the OMP model, achieving a perfect accuracy of 100%. Samples 1 through 4 are presented.

·	•	Results	
Brain tumor Images	Descriptors and Simplexes	Traditional methods	Best Formulas Found
	Euler ES	-12 55120	-12 55120
	CS	608377	608377
G	Volume	211979	211979
Specimen 1	Points	240094	240094
	Edges	691624	691624
	Faces	663497	663497
	Tetravoxels	581384	581384
	Euler	-16	-16
	ES	25402	25402
	$\operatorname{CS}$	188323	188323
C	Volume	67008	67008
Specimen 2	Points	80316	80316
	Edges	227049	227049
	Faces	213725	213725
	Tetravoxels	176245	176245
	Euler	10	10
	ES	16468	16468
	CS	81187	81187
Specimen 3	Volume	29807	29807
specimen 3	Points	38466	38466
	Edges	106304	106304
	Faces	97655	97655
	Tetravoxels	73368	73368
	Euler	10	10
	ES	27556	27556
	CS	296710	296710
C • 4	Volume	103496	103496
Specimen 4	Points	117567	117567
	Edges	338327	338327
	Faces	324266	324266
	Tetravoxels	283215	283215

Table 5: Comparison of four images from the BRATS dataset and demonstration of the most effective formulas using the OMP model, achieving a perfect accuracy of 100%. Samples 5 through 8 are presented.

<u></u>	•	Results	
Brain tumor Images	Descriptors and Simplexes	Traditional methods	Best Formulas Found
Specimen 5	Euler ES CS Volume Points Edges Faces	5 10430 60674 21963 27460 76596 71104	5 10430 60674 21963 27460 76596 71104
	Tetravoxels Euler	55736	55736 -5
Specimen 6	ES CS Volume Points Edges Faces Tetravoxels	42586 396397 139230 161332 461090 438983 375918	42586 396397 139230 161332 461090 438983 375918
Specimen 7	Euler ES CS Volume Points Edges Faces Tetravoxels	10 17536 110548 39772 49054 137356 128084 102284	10 17536 110548 39772 49054 137356 128084 102284
Specimen 8	Euler ES CS Volume Points Edges Faces Tetravoxels	-23 21736 89470 33446 44560 122343 111206 78871	-23 21736 89470 33446 44560 122343 111206 78871

Table 6: Comparison of four images from the BRATS dataset and demonstration of the most effective formulas using the OMP model, achieving a perfect accuracy of 100%. Samples 9 through 12 are presented.

v	•	Results	
Brain tumor Images	Descriptors and Simplexes	Traditional methods	Best Formulas Found
Specimen 9	Euler ES CS Volume Points Edges Faces	-30 62614 517975 183094 215244 612769 580589	-30 62614 517975 183094 215244 612769 580589
Specimen 10	Euler ES CS Volume Points Edges Faces Tetravoxels	-26 28744 119374 44582 60014 163576 148118 106088	-26 28744 119374 44582 60014 163576 148118 106088
Specimen 11	Euler ES CS Volume Points Edges Faces Tetravoxels	-4 19214 155783 55130 65250 185121 174997 146693	-4 19214 155783 55130 65250 185121 174997 146693
Specimen 12	Euler ES CS Volume Points Edges Faces Tetravoxels	-38 17624 87341 32051 41632 114584 104965 79336	-38 17624 87341 32051 41632 114584 104965 79336

Table 7: Comparison of four images from the BRATS dataset and demonstration of the most effective formulas using the OMP model, achieving a perfect accuracy of 100%. Samples 13 through 16 are presented.

	_	Results	
Brain tumor Images	Descriptors and Simplexes	Traditional methods	Best Formulas Found
	Euler	-44	-44
	ES	21922	21922
	CS	128056	128056
Specimen 19	Volume	46339	46339
Specimen 13	Points	57960	57960
	Edges	161643	161643
	Faces	149978	149978
	Tetravoxels	117799	117799
	Euler	41	41
	ES	30630	30630
	$\operatorname{CS}$	225873	225873
G • 14	Volume	80396	80396
Specimen 14	Points	95889	95889
	Edges	271955	271955
	Faces	256503	256503
	Tetravoxels	210695	210695
	Euler	48	48
	ES	36146	36146
	$\operatorname{CS}$	357788	357788
G · 1F	Volume	125287	125287
Specimen 15	Points	143807	143807
	Edges	412406	412406
	Faces	393934	393934
	Tetravoxels	340114	340114
	Euler	14	14
	ES	46408	46408
	$\operatorname{CS}$	358363	358363
Crasiman 16	Volume	127189	127189
Specimen 16	Points	150931	150931
	Edges	428499	428499
	Faces	404771	404771
	Tetravoxels	335683	335683

Table 8: Comparison of four images from the BRATS dataset and demonstration of the most effective formulas using the OMP model, achieving a perfect accuracy of 100%. Samples 17 through 20 are presented.

	1	Results	
Brain tumor Images	Descriptors and Simplexes	Traditional methods	Best Formulas Found
Specimen 17	Euler ES CS Volume Points Edges Faces Tetravoxels	$ \begin{array}{c} 1\\ 35146\\ 284701\\ 100758\\ 118848\\ 337936\\ 319847\\ 267644 \end{array} $	1 35146 284701 100758 118848 337936 319847 267644
Specimen 18	Euler ES CS Volume Points Edges Faces Tetravoxels	-7 28772 120968 45118 60233 164862 149740 107318	-7 28772 120968 45118 60233 164862 149740 107318
Specimen 19	Euler ES CS Volume Points Edges Faces Tetravoxels	-55 18638 122072 43797 53825 150793 140710 113517	-55 18638 122072 43797 53825 150793 140710 113517
Specimen 20	Euler ES CS Volume Points Edges Faces Tetravoxels	18 47606 503222 175675 200110 575245 550828 480033	18 47606 503222 175675 200110 575245 550828 480033

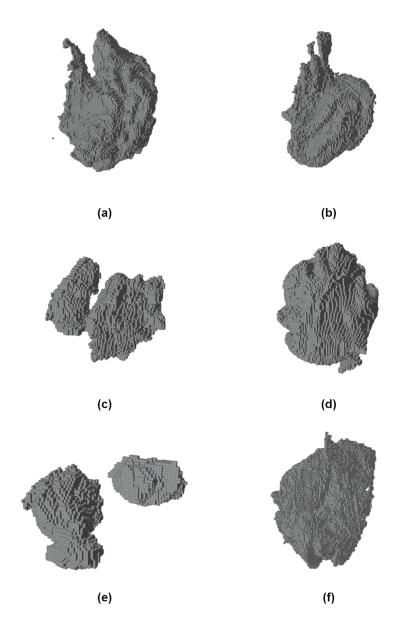


Figure 1: The images featured in the study by Menze et al. [1] illustrate brain tumors from the BRATS dataset. Specimen 1 is shown in image (a), Specimen 2 in image (b), Specimen 3 in image (c), Specimen 4 in image (d), Specimen 5 in image (e), and Specimen 6 in image (f). We extracted descriptors from all images in the dataset, with six representative images displayed here.

## References

[1] B. H. Menze et al., 'The Multimodal Brain Tumor Image Segmentation Benchmark (BRATS)', IEEE Transactions on Medical Imaging, vol. 34, no. 10, pp. 1993–2024, 2015.