Im2mesh_GUI Tutorial

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This is a tutorial for Im2mesh_GUI v2.23, which is developed by Jiexian Ma. Im2mesh_GUI is a graphical user interface (GUI) version of Im2mesh, an open-source MATLAB/Octave package.¹ It's used to generate finite element mesh based on two-dimensional (2D) segmented multi-phase image. With GUI, Im2mesh becomes much easier to use. User-friendly! It has incorporated many features, such as polyline smoothing and simplification. Through this tutorial, you will understand the workflow and the parameters of Im2mesh_GUI.

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 $^{^{1}}$ https://github.com/mjx888/im2mesh

1 Installation

Im2mesh_GUI can be installed in two ways: MATLAB app or standalone desktop application.

For using as MATLAB app, you need to install MATLAB software (R2017b or later; version higher than R2018b is preferred), Image Processing Toolbox, and Mapping Toolbox. When MATLAB software is opened, you can install Im2mesh_GUI by running "Im2mesh_GUI.mlappinstall". After installation, you should be able to find Im2mesh_GUI in the APPS tab of MATLAB. If you find the window of Im2mesh_GUI cannot display completely, you can change the display scaling setting in your operating system to fix that.

For standalone desktop application, you don't need to install MATLAB software or any MATLAB toolbox. However, you need to install MATLAB Runtime (version 9.11). When you open "Installer_Im2mesh_GUI.exe", the installer will automatically download and install MATLAB Runtime for you. Please send me a brief email to get the exe file. Note that MATLAB Runtime is free. After installation, you can find the application in the following file directory: C:\Program Files \Im2mesh_GUI\application\Im2mesh_GUI.exe. When you start the application, it may take a while to initialize. Just be patient.

2 Workflow

Figure 1 shows the workflow of Im2mesh. The workflow is straightforward. The GUI window has been organized according to the workflow (Figure 2). The workflow consists of 9 steps. Some steps are optional: Step 2, Step 5, and Step 7. When running Im2mesh_GUI, you can skip those optional steps if they do not work for your image. If you plan to use pixelMesh (pixel-based quadrilateral mesh) as mesh generator, the workflow would be much simpler: Step 1-3 and 7-9.

3 Step-by-step Guide

Step 0. Image processing. It is often necessary to perform digital image processing to your raw image. For example, converting to 8-bit grayscale image, noise removal, and image segmentation. You can refer to the following links on how to perform image processing in MATLAB:

```
https://www.mathworks.com/videos/search.html?q=Image+Processing
https://www.mathworks.com/help/images/noise-removal.html
https://www.mathworks.com/discovery/image-segmentation.html
https://www.mathworks.com/videos/image-segmentation-app-1504291389509.html
https://www.mathworks.com/help/images/image-segmentation.html
```

You can also use ImageJ to perform digital image processing. There are many videos on how to use ImageJ.

```
https://www.youtube.com/@johanna.m.dela-cruz
https://www.youtube.com/watch?v=HnTehD-H3t8
```

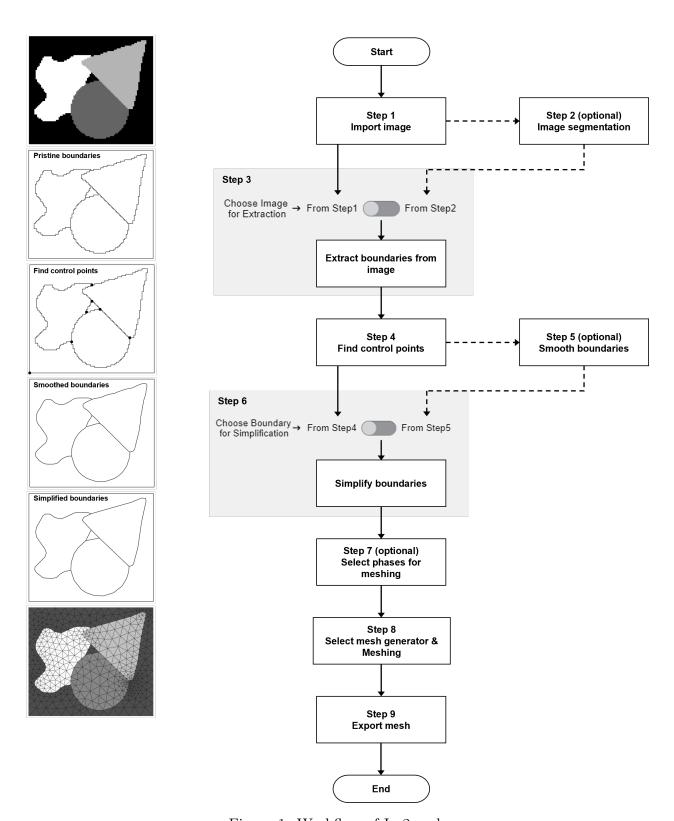


Figure 1: Workflow of Im2mesh

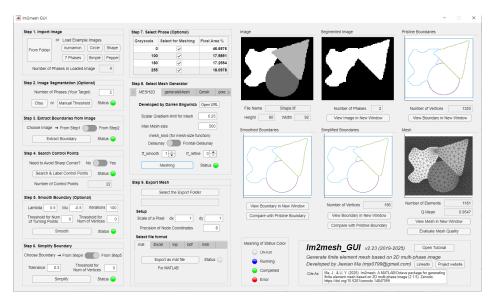


Figure 2: Im2mesh GUI

Step 1. Import image. You can import from your folder or just load one of the example images. An ideal input image for Im2mesh is a segmented grayscale image. That is because Im2mesh identifies different material phases in an image by their grayscales. Different grayscales correspond to different material phases. If you have 4 levels of grayscale in an image, the resulting mesh will contain 4 phases.

If your image is a grayscale image without segmentation, you can perform image segmentation in Step 2.

For RGB images, Im2mesh_GUI will automatically convert the imported RGB image to a 8-bit grayscale image. Therefore, some info in the RGB image will be lost. You may perform color thresholding before importing into Im2mesh.

https://www.mathworks.com/videos/search.html?q=Color%20Thresholding

Step 2. Image segmentation. This step is optional. This step is included only for convenience. If you do not need segmentation, just skip this step.

Before pressing button "Otsu" or "Manual Threshold", you need to enter *Number of Phases (Your Target)*. The value of *Number of Phases (Your Target)* has to be smaller than *Number of Phases in Loaded Image*.

For Otsu's method, Number of Phases (Your Target) can be 2-20.

For manual multi-thresholding, Number of Phases (Your Target) can be 2-4 or higher.

Im2mesh_GUI currently supports two image segmentation methods: Otsu's method and manual multi-thresholding, which are the simplest multi-thresholding methods. The GUI of manual multi-thresholding is developed by me. Note that manual multi-thresholding does not work in MATLAB versions before R2018b.

Ater pressing button "Manual Threshold", you should be able to see the interface as shown in Figure 3a. Then, you can press button "Update Overlay" to display the overlaid labels (Figure 3b). The initial threshold values are computed based on Otsu's method.

In this example (Pepper.png), Thresh1 is 82 and Thresh2 is 149. Thus, grayscale from 0 to 82 is considered as Phase 1, grayscale from 82 to 149 is considered as Phase 2, and

grayscale from 149 to 255 is considered as Phase 3. Note that the background (grayscale from 0 to 82) is considered as a phase in the image.

You can drag the threshold slider to manually change threshold values. You can press button "No overlay" and "Update Overlay" alternately to check the effect of thresholding. In addition to changing threshold values by the threshold slider, you can also enter threshold values directly and press "Update Overlay". To change the transparency of overlay, you can drag the transparency slider and then press "Update Overlay".

After you get satisfied results, press button "Done" to return to the main app.

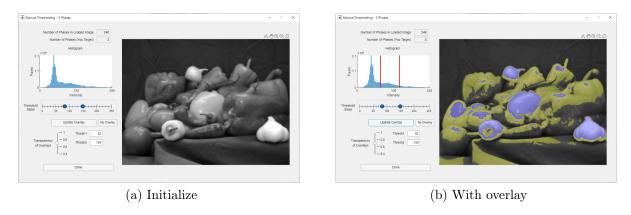


Figure 3: Manual multi-thresholding

Step 3. Extract polygonal boundaries from image. You can choose your input for this step by clicking the Switch. For example, if your input is from Step 2, just click the right side of the switch. This step uses a subroutine (getExactBounds.m) developed by me to extract the exact boundary from the image.²

Step 4. Search & label control points. Here, control point is defined as the intersection or meeting point between edges in the images (Figure 4). These control points will not change their positions (x, y coordinates) in the following steps. This step uses a subroutine (getCtrlPnts.m) developed by me to search and label control points.

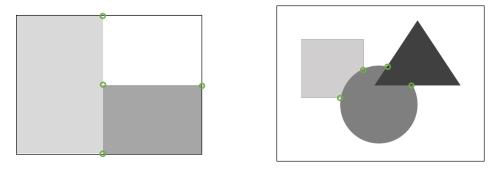


Figure 4: Examples of control points, which are marked with small circles.

²https://www.mathworks.com/matlabcentral/fileexchange/72436-getexactbounds-get-exact-boundary

I include an option "Need to Avoid Sharp Corners?" in this step. You can set this option to "Yes" in the following cases:

- If you want to avoid sharp corner during boundary smoothing and simplification
- If you find the step of mesh generation has failed for your image
- To avoid bugs

Step 5. Smooth boundary. This step is optional. If your polygonal boundaries don't need smoothing, just skip this step. Note that I found boundary smoothing is beneficial in most cases. This step uses 2D Taubin smoothing method (taubinSmooth.m), which can remove noise in polyline without shrinkage. Please refer to the course slide of Dr. Tao Ju if you'd like to learn about Taubin smoothing method.³

There are 5 parameters in this step: Lambda, Mu, Iterations, Threshold for Num of Turning Points, and Threshold for Num of Vertices. The meaning and value range of these parameters are listed as follows.

- Lambda: How far each node is moved toward the average position of its neighbours during every second iteration. Type: Float. Range: 0 < Lambda < 1.
- Mu: How far each node is moved opposite the direction of the average position of its neighbours during every second iteration. Type: Float. Range: -1 < Mu < 0.
- *Iterations*: Number of iterations in Taubin smoothing. If you don't need polyline smoothing, set *Iterations* to 0. Type: Integer. Range: ≥ 0 .
- Threshold for Num of Turning Points: Threshold value for the number of turning points in a polyline. Only those polylines with number of turning points greater than this threshold will be smoothed. Type: Integer. Range: ≥ 0 .
- Threshold for Num of Vertices: Threshold value for the number of vertices in a polyline. Only those polylines with number of vertices greater than this threshold will be smoothed. Type: Integer. Range: ≥ 0 .

Lambda, Mu, and Iterations are parameters for Taubin smoothing. The default value is Lambda = 0.5, Mu = -0.5, Iterations = 100. You can increase Iterations if you want smoother boundary. You can reduce Iterations if you want rough boundary.

In this step, there are two thresholds: Threshold for Num of Turning Points, and Threshold for Num of Vertices. These two parameters are introduced by me to avoid over-smoothing of simple polylines or polygons (Figure 5). Here, a turning point is defined as a vertex where the plane angle between two connected edges is not 180 degrees (Figure 6). By setting a threshold, those polylines with less turning points or less vertices will be skipped in this step so they will not be smoothed (Figure 7). If you want to perform smoothing to all the polylines, set the thresholds to 0.

 $^{^3}$ CSE554 lecture slides

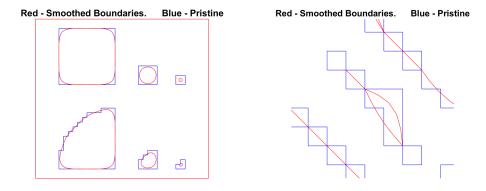


Figure 5: Examples of over-smoothing

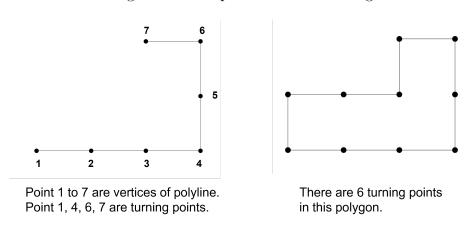


Figure 6: Examples of turning point

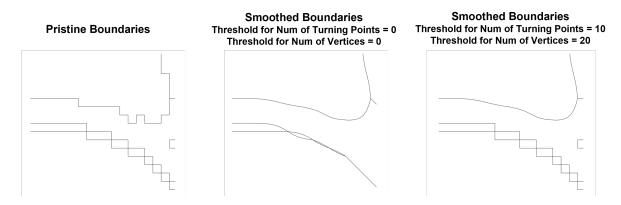


Figure 7: Set thresholds to avoid over-smoothing of simple polylines or polygons

Step 6. Simplify boundary. You can choose your input for this step by clicking the Switch. For example, if your input is from Step 5, just click the right side of the switch. This step uses Douglas-Peucker algorithm to simplify polylines. The subroutine (dpsimplify.m) is written by Wolfgang Schwanghart. There are 2 parameters in this step: *Tolerance*, and *Threshold for Num of Vertices*.

• Tolerance: The maximum allowable deviation of a vertex from the simplified curve.

It's for Douglas-Peucker algorithm. Type: Float. Range: ≥ 0 .

• Threshold for Num of Vertices: Threshold value for the number of vertices in a polyline. Only those polylines with number of vertices greater than this threshold will be simplified. Type: Integer. Range: ≥ 0 .

If you don't need to simplify polylines, set *Tolerance* to 0 or a small value, such as 1e-10. Note that in some MATLAB version, setting *Tolerance* to 0 may cause error.

Higher *Tolerance* means fewer points are retained in polyline and worse approximation to the pristine boundary. The reasonable value of *Tolerance* depends on your workflow and your image.

- When you're using the boundaries from Step 4 as input, the typical value of *Tolerance* is 0.8 2.
- When you're using the boundaries from Step 5 as input, the typical value of *Tolerance* is 0.2 0.8.

In this step, there is a parameter called *Threshold for Num of Vertices*. This parameter is used to avoid over-simplification of polyline. Figure 8 shows examples of over-simplification. Some of the over-simplified polygons even have zero area. By setting a threshold, those polylines with less vertices will be skipped in this step so they will not be simplified. **If you want to perform simplification to all the polylines, set the threshold to 0.**

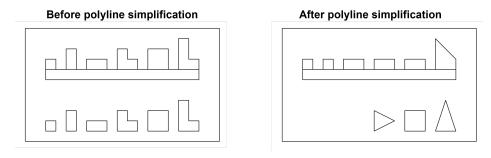


Figure 8: Example of over-simplification

Once you got the simplified boundaries. You can press button "View Boundary in New Window" or "Compare with Pristine Boundary" and zoom in to check the results. If the resulted boundary is not ideal, you can change parameters of Step 6 and press the button "Simplify" again to obtained new results.

Step 7. Select phase. All the phases are selected in the default case. If you don't need certain phases for meshing, un-check them in the table.

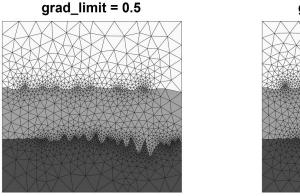
Step 8. Select mesh generator & meshing. There are four mesh generators available in Im2mesh: MESH2D, generateMesh, Gmsh, and pixelMesh.

MESH2D is an open source mesh generator developed by Darren Engwirda.⁴ It's the default mesh generator of Im2mesh GUI. It can generate high-quality finite element

 $^{^4}$ https://github.com/dengwirda/mesh2d

mesh. You are not required to install any MATLAB Toolbox when using MESH2D. If you have questions about the algorithm, please refer to the MESH2D program. If you use MESH2D as mesh generator, you can cite the thesis of Darren Engwirda. There are 5 parameters for MESH2D: *Gradient-limit*, *Max Mesh-size*, *mesh_kind*, *tf_smooth*, and *tf_refine*. The meanings of them are listed below for your reference.

- *Gradient-limit*: A limit on the gradient of mesh-size function (Figure 9).⁵ Type: Float. Range: > 0. Typical value: 0.15 0.4.
- Max Mesh-size: Maximum mesh edge lengths. This is an approximate upper bound on the mesh edge lengths (Figure 10). Type: Float. Range: > 0.
- $mesh_kind$: Method used to create mesh-size functions based on an estimate of the "local-feature-size" associated with a polygonal domain. Value: Delaunay or Frontal-Delaunay.
- *tf_smooth*: Boolean. Value: 0 or 1. Whether improve triangulation quality by adjusting the vertex positions and mesh topology (hill-climbing type optimisation). Default value: 1.
- tf_refine: Boolean. Value: 0 or 1. Whether refine mesh (quadtree-type). Each triangle is split into four new sub-triangles, and smooth. Default value: 0.



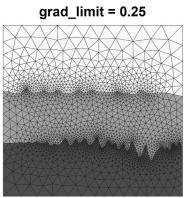


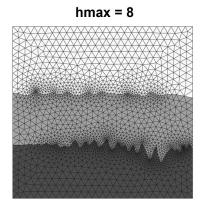
Figure 9: Effect of Gradient-limit

generateMesh is a MATLAB built-in function. It requires installation of MAT-LAB Partial Differential Equation Toolbox. If you encounter the following error, please update MATLAB to a newer version: Parameter name must be 'SolidBoundaryOrientation' or 'Simplify'. Because function generateMesh has poor support for multi-part geometry, it may occasionally cause MATLAB to crash. Please be cautious.

There are 3 parameters for generateMesh: Mesh Growth Rate, Max Mesh Edge Length, and Min Mesh Edge Length.

⁵http://persson.berkeley.edu/pub/persson04gradlim.pdf

 $^{^6}$ https://www.mathworks.com/help/pde/ug/pde.pdemodel.generatemesh.html



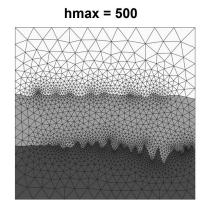


Figure 10: Effect of Max Mesh-size

- Mesh Growth Rate. The rate at which the mesh transitions between regions of different edge size. Type: Float. Range: $1 \le Mesh$ Growth Rate ≤ 2 . Typical value: 1.2 1.5.
- Max Mesh Edge Length: An approximate upper bound on the mesh edge lengths. Type: Float. Range: > 0.
- Min Mesh Edge Length: An approximate lower bound on the mesh edge lengths. Type: Float. Range: ≥ 0 .

Gmsh is a powerful open-source finite element mesh generator. Please go to section 4 of this tutorial to learn about how to use Gmsh in Im2mesh.

pixelMesh is used to generate pixel-based quadrilateral mesh. It's written by me many years ago. It's for some special applications.

The step of meshing is the most time-consuming step in Im2mesh. The computation time of meshing is dependent on the number of vertices in the simplified boundaries. I ran tests on my desktop computer with 4-phase images and with option "Need to Avoid Sharp Corners?" = Yes. For 15,000 vertices in the simplified boundaries, MESH2D took 40-50 seconds. For 80,000 vertices in the simplified boundaries, MESH2D took 300-450 seconds.

What to do if the mesh generation has failed for your images?

- Set the thresholds in Step 5 or 6 to a higher value (e.g., 20), and re-run Step 5 to Step 8
- Set the option "Need to Avoid Sharp Corners?" to Yes, and re-run Step 4 to Step 8

Once you obtain the mesh from MESH2D or generateMesh. You can press button "View Mesh in New Window" or "Evaluate Mesh Quality" to check the results. "Evaluate Mesh Quality" use a subroutine (tricost.m) written by Darren Engwirda to evaluate mesh quality. "Evaluate Mesh Quality" has 3 outputs (Figure 11). The definition of Q and θ are as follows.

- Q: Area-length measure of a triangle. $Q = \frac{4A}{\sqrt{3} \, l_{rms}^2}$, where A is the area of a triangle and l_{rms} is the root-mean-squared edge length in a triangle. Q achieve a score of 1 for ideal elements. Q approaches zero as an element distorts toward degeneracy.
- θ : The plane angle between adjacent edges.

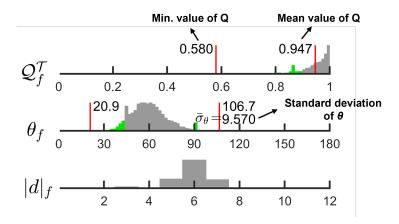


Figure 11: An example of mesh quality. A few statistics can be obtained from the plot.

If the resulted mesh is not ideal, you can change parameters of Step 8 and press the button "Meshing" again to obtained new results. You may also go back to Step 5 or 6 to change parameters. But once you do that, you need to re-run all the steps after Step 5 or 6 to get the updated results.

What are the critical parameters that affect the number of triangular mesh?

- Tolerance in Step 6.
- Gradient-limit in Step 8, if you are using MESH2D.
- Mesh Growth Rate and Min Mesh Edge Length in Step 8, if you are using generateMesh.

My suggestion for choosing the value of these critical parameters:

- First, try different *Tolerance* value in an ascending order and press button "Compare with Pristine Boundary" to view the corresponding simplified boundaries. Identify the largest *Tolerance* value that provides an acceptable approximation to the pristine boundaries. With a larger *Tolerance* value, the number of generated triangles in Step 8 will decrease.
- After that, try different *Gradient-limit* and evaluate the corresponding mesh quality Q. Increasing the *Gradient-limit* will reduce the number of generated triangles. However, a higher *Gradient-limit* will also lower the mesh quality Q. You may perform a mesh convergence analysis to find the largest acceptable *Gradient-limit* for your cases.

Step 9. Export mesh. Im2mesh_GUI supports exporting linear element and quadratic element. You can export mesh as the following files.

- mat file (MATLAB)
- xls file (Excel)
- inp file (Abaqus)
- bdf file (Nastran bulk data, compatible with COMSOL)

Before exporting file, you need to setup some parameters, such as dx, dy, and Precision of $Node\ Coordinates$.

dx and dy are the scales of a pixel. dx is the column direction, and dy is the row direction. In most cases, dx and dy are equal. The value of dx and dy depends on the scale of your image and the unit in your finite element simulation. For example, the scale of your image is 0.11 mm/pixel, you can set dx = 0.11 and dy = 0.11.

Precision of Node Coordinates is the number of digits to the right of the decimal point when writing node coordinates to inp file and bdf file.

MAT file

If you use MESH2D or pixelMesh as mesh generator, the exported mat file would have the following variables: vertL, eleL, pcode, vertQ, eleQ.

If you use generateMesh as mesh generator, the exported mat file would have the following variables: vertL, eleL, pcode, vertQ, eleQ, meshL, meshQ.

- vertL, eleL, pcode define a model with linear elements.
- vertQ, eleQ, pcode define a model with quadratic elements.

When the element is triangular, the meanings of variables in the mat file are listed as follows. When the element is quadrilateral, the meanings are the same. Just the number of columns in eleL and eleQ will increase.

- vertL: Mesh nodes (for linear element). It's a Nn-by-2 matrix, where Nn is the number of nodes in the mesh. Each row of vertL contains the x, y coordinates for that mesh node.
- eleL: Mesh elements (for linear element). For triangular elements, it's a Ne-by-3 matrix, where Ne is the number of elements in the mesh. Each row in eleL contains the indices of the nodes for that mesh element.
- pcode: Label of phase. Ne-by-1 array, where Ne is the number of elements

pcode(j,1) = k; means the j-th element belongs to the k-th phase.

• vertQ: Mesh nodes (for quadratic element). It's a Nn-by-2 matrix.

- eleQ: Mesh elements (for quadratic element). For triangular elements, it's a Ne-by-6 matrix.
- meshL, meshQ: MATLAB FEMesh objects (with linear or quadratic elements).⁷ If you're familiar with MATLAB Partial Differential Equation Toolbox, you can use MATLAB FEMesh object to solve PDE.⁸

After loading the mat file into MATLAB, you can use the following function to plot the mesh. It works for linear and quadratic element. Syntax: plotMeshes(vertL,eleL,pcode); or plotMeshes(vertQ,eleQ,pcode);

```
function plotMeshes( vert, ele, pcode )
% plotMeshes: plot mesh
    ele_wid = size(ele,2);
    if ele_wid == 3
                            % linear triangle
        range_vec = 1:3;
    elseif ele_wid == 6
                            % quadratic triangle
        range_vec = [1 4 2 5 3 6];
                            % linear quadrilateral
    elseif ele_wid == 4
        range_vec = 1:4;
    elseif ele_wid == 8
                            % quadratic quadrilateral
        range_vec = [1 5 2 6 3 7 4 8];
    else
        error("ele - wrong size")
    end
    figure; hold on; axis image off;
    tvalue = unique( pcode );
    num_phase = length( tvalue );
    % setup color
    if num_phase == 1
        col = 0.98;
    elseif num_phase > 1
        col = 0.3: 0.68/(num_phase-1): 0.98;
    else
        error("num_phase < 1")</pre>
    end
    % use function patch to plot
    for i = 1: num_phase
        current_phase = tvalue(i);
        patch( 'faces',ele( pcode==current_phase, range_vec ), ...
            'vertices', vert, ...
            'facecolor',[ col(i), col(i), col(i)], ...
            'edgecolor',[.1,.1,.1] ...
            );
    end
    hold off
end
```

⁷https://www.mathworks.com/help/pde/ug/pde.femesh.html

⁸https://www.mathworks.com/help/pde/index.html

XLS file

In the exported XLS file, there are 5 sheets: vertL, eleL, pcode, vertQ, eleQ. Their meanings have been explained above.

INP file

When exporting inp file, you need to specify *Element Type*. You can check the Abaqus manual to find out which element type is suitable for your simulation. Im2mesh will automatically export two inp files: one for a model with linear elements and the other for a model with quadratic elements. Typically, models with quadratic elements are better. If you encounter issues when doing simulation with quadratic elements, please contact me. It may be a bug. If you use pixelMesh as mesh generator, please set the Element Type to quadrilateral elements in Abaqus; otherwise, error will occur when importing the inp file into Abaqus.

The exported inp file would have a model with one part, which contains multiple sections. Each section corresponds to one phase in your image. After importing the inp file into Abaqus, you can view different sections (please check Figure 12).

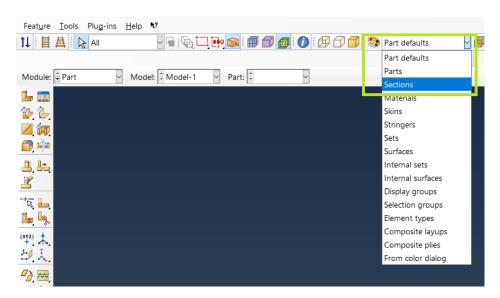


Figure 12: Abaqus

It's possible to export the mesh as a model with multiple parts, where each part corresponds to one phase in the image. However, that function (written by me in 2018) maybe outdated so I didn't incorporate it into Im2mesh_GUI.

How to import BDF file into COMSOL

Please refer to the following figures about how to import bdf file into COMSOL and assign material properties to different phases.

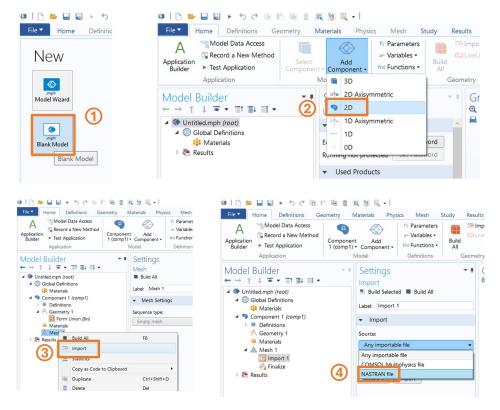


Figure 13: Import bdf file into COMSOL

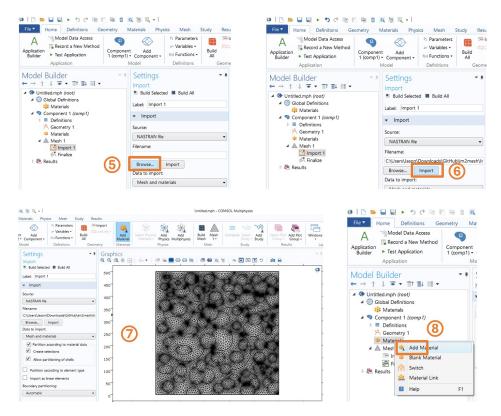


Figure 14: Import bdf file into COMSOL

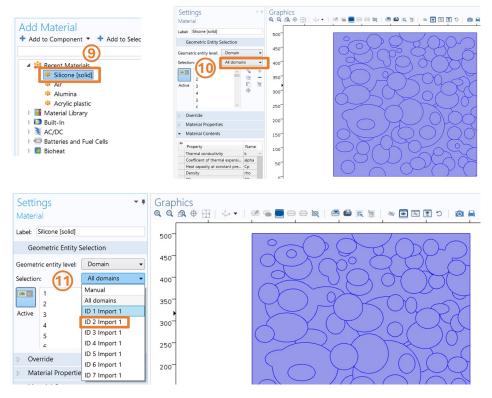


Figure 15: Import bdf file into COMSOL

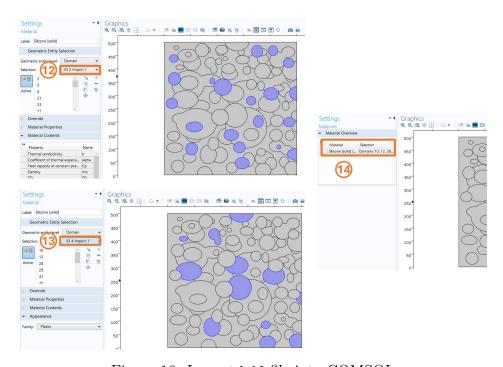


Figure 16: Import bdf file into COMSOL

4 Gmsh

Before starting, you need to download Gmsh (https://gmsh.info) and un-zip. Then, in the interface of Im2mesh_GUI, you need to "Locate gmsh.exe". I have tested with MATLAB 2021b and gmsh 4.13.1 on Windows system. I'm not sure whether it works on Linux or macOS. On Linux or macOS, you may try to locate other executable files of gmsh. Each time you restart Im2mesh_GUI, you will have to "Locate gmsh.exe" again. To save some time, I suggest you create a shortcut of gmsh.exe and when you "Locate gmsh.exe", you can click that shortcut.

In Im2mesh_GUI, there are six parameters for Gmsh. The meanings of them are listed in the manual of Gmsh 4.13.1 (https://gmsh.info/doc/texinfo/gmsh.html). I list them below for your reference.

- MeshSizeMin: Minimum mesh element size. Default value of Gmsh: 0.
- MeshSizeMax: Maximum mesh element size. Default value of Gmsh: 1e+22.
- Algorithm: 2D mesh algorithm (1: MeshAdapt, 2: Automatic, 3: Initial mesh only, 5: Delaunay, 6: Frontal-Delaunay, 7: BAMG, 8: Frontal-Delaunay for Quads, 9: Packing of Parallelograms, 11: Quasi-structured Quad). Default value of Gmsh: 6.
- ElementOrder: 1 or 2.
- Recombine All: Boolean. Value: 0 or 1. Whether apply recombination algorithm to all surfaces, ignoring per-surface spec. Default value of Gmsh: 0.
- RecombinationAlgorithm: Mesh recombination algorithm (0: simple, 1: blossom, 2: simple full-quad, 3: blossom full-quad). Default value of Gmsh: 1.

To generate triangular mesh, you can set Algorithm to 1-7 and set RecombineAll to 0. To generate unstructured quadrilateral mesh, you can set Algorithm to 8 and set RecombineAll to 1. You can try different RecombinationAlgorithm.

To generate quasi-structured quadrilateral mesh, you can set Algorithm to 11 and set Recombine All to 0.

Once you press "Meshing", Im2mesh_GUI will write a geo file (gmshTemp.geo) to your current working folder of MATLAB and MATLAB will send this file to gmsh.exe for mesh generation. Once meshed, you will find an m file (gmshTemp.m) in your current working folder and a struct variable (msh) in your MATLAB workspace.

After you got the generated mesh, you can check "Q mean". For quadrilateral element, Im2mesh_GUI use a subroutine (MeshQualityQuads.m) written by Allan P. Engsig-Karup to evaluate mesh quality. Here, Q is defined as $\operatorname{prod}(1-\operatorname{abs}((\operatorname{pi}/2 - \operatorname{angles})/(\operatorname{pi}/2)))$, where angles are the interior angles of the quadrilateral. 0 <= Q <= 1, where Q = 1 for rectangles (good quality) and Q = 0 for quadrilaterals with triangular shape (four unique vertices

 $^{^9} https://www.mathworks.com/matlabcentral/file$ exchange/33108-unstructured-quadrilateral-mesh-quality-assessment

assumed). Usually, you will have to adjust the value of MeshSizeMax to achieve better mesh quality. Typical value of MeshSizeMax is 5 to 20.

When you generate unstructured quadrilateral mesh, there may exist some triangles that are failed to recombine into quad mesh. Please be cautious. You can check the struct variable (msh) in your MATLAB workspace to confirm whether it has some triangles left. If msh.TRIANGLES or msh.TRIANGLES6 exist, it means there are some triangles left in the quad mesh. To remove those triangles from the quad mesh, you can set *MeshSizeMax* to a smaller value and mesh again. It should help.

If you're not satisfied with with the mesh quality, you can open the gmshTemp.geo file in Gmsh and improve it. Specify a mesh size field may improve the mesh quality. You can add more mesh nodes in Gmsh. There are a lot of videos on how to use Gmsh.

Once you're ok with the mesh, you can export it by pressing "Export to File". You can specify export format by setting *File Name Suffix for Output*, which corresponds to Mesh.Format in Gmsh. Gmsh support a lot of output formats. I list below for your reference.

```
1: msh, 2: unv, 10: auto, 16: vtk, 19: vrml, 21: mail, 26: pos stat, 27: stl, 28: p3d, 30: mesh, 31: bdf, 32: cgns, 33: med, 34: diff, 38: ir3, 39: inp, 40: ply2, 41: celum, 42: su2, 47: tochnog, 49: neu, 50: matlab
```

For example, if you want stl file, set *File Name Suffix for Output* to stl. If you want matlab file, set *File Name Suffix for Output* to m. Please refer to the manual of Gmsh if you have questions about the format. Once you press "Export to File", a file named "gmshExport" will be created in your MATLAB current working folder.

If you plan to work with the matlab file (m file) generated by Gmsh, please be cautious. You may need to adjust the node order in the mesh element. Please refer to demo13 in Im2mesh package about how to do that.

demo13: https://mjx888.github.io/im2mesh_demo_html/demo13.html

5 Edit Polygonal Boundary

It is possible to edit the polygonal boundary before mesh generation. We can achieve many things by editing the boundary. For instance, we can add a notch or other shape to the geometry; we can add mesh nodes to the boundary; we can refine the mesh near a specific polyline or polygon. Check Figure 17.

Please refer to demo04 and demo14-16 in Im2mesh package about how to edit polygonal boundary before mesh generation.

```
demo04: https://mjx888.github.io/im2mesh_demo_html/demo04.html demo14: https://mjx888.github.io/im2mesh_demo_html/demo14.html demo15: https://mjx888.github.io/im2mesh_demo_html/demo15.html demo16: https://mjx888.github.io/im2mesh_demo_html/demo16.html
```

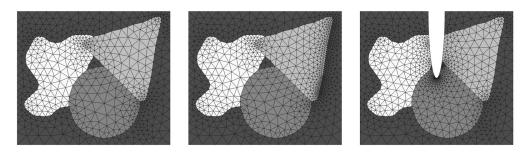


Figure 17: Edit Polygonal Boundary