

## HW-9

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**Problem 1.** Beginning with  $(\mathbf{x}, \mathbf{w}, \mathbf{y}, \mathbf{z}) = (\mathbf{e}, \mathbf{e}, \mathbf{e}, \mathbf{e})$  and using  $\delta = \frac{1}{10}$  and  $r = \frac{9}{10}$  compute  $(\bar{\mathbf{x}}, \bar{\mathbf{w}}, \bar{\mathbf{y}}, \bar{\mathbf{z}})$  after one step of the path following method for each of the following problems.

(1) Exercise 2.3

(2) Exercise 2.4

(3) Exercise 2.5

(4) Exercise 2.10

*Proof.* With  $(\mathbf{x}, \mathbf{w}, \mathbf{y}, \mathbf{z}) = (\mathbf{e}, \mathbf{e}, \mathbf{e}, \mathbf{e})$ ,  $X = W = Y = Z = I$ . Thus  $\Delta(\mathbf{x}, \mathbf{w}, \mathbf{y}, \mathbf{z}) =$

$$\begin{bmatrix} -A & I & O & O \\ O & O & A^T & I \\ I & O & O & I \\ O & I & I & O \end{bmatrix}^{-1} \begin{bmatrix} \mathbf{b} - A\mathbf{e} - \mathbf{e} \\ \mathbf{c} - A^T\mathbf{e} + \mathbf{e} \\ \frac{11}{10}\mathbf{e} \\ \frac{11}{10}\mathbf{e} \end{bmatrix} = \begin{bmatrix} -A^{-1} & X & O & A^{-1} \end{bmatrix} \begin{bmatrix} -A & I & O & O \\ O & O & A^T & I \\ I & O & O & I \\ O & I & I & O \end{bmatrix} \quad \square$$