

3.1)

a. Which nodes are leaves?

D, M, N, J, K, L, F

b. Which node is the root?

A

c. What is the parent of node **C**?

A

d. Which nodes are children of **C**?

F, G, H

e. Which nodes are ancestors of **E**?

B, A

f. Which nodes are descendants of **E**?

I, M, N

g. What are the right siblings of **D** and **E**?

F, G, H

h. Which nodes are to the left and to the right of **G**?

F, H

i. What is the depth of node **C**?

1

j. What is the height of node **C**?

2

3.2)

6

3.6)

$\text{preorder}(n) < \text{preorder}(m)$	$\text{inorder}(n) < \text{inorder}(m)$	$\text{Postorder}(n) < \text{postorder}(m)$
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n is to the left of m

Check	Check	Check
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n is to the right of m

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n is a proper ancestor of m

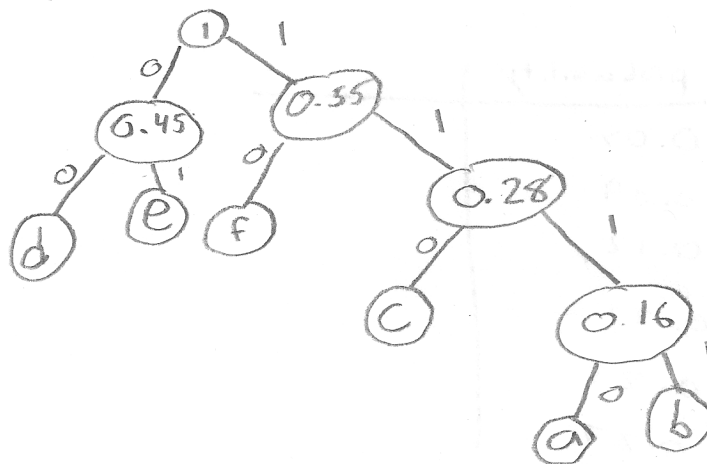
Check		
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n is a proper descendant of m

	Check	Check
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3.20

Symbol	probability
a	0.07
b	0.09
c	0.12
d	0.22
e	0.23
f	0.27



Symbol		
a	1110	$4 \times 0.07 = 0.28$
b	1111	$4 \times 0.09 = 0.36$
c	110	$3 \times 0.12 = 0.36$
d	00	$2 \times 0.22 = 0.44$
e	01	$2 \times 0.23 = 0.46$
f	10	$2 \times 0.27 = 0.54$
		$\frac{2.45}{6} = \boxed{0.41}$

3.21

- 1) Suppose the probability of symbol b is less than the probability of a and symbol a has a greater depth than a .

When choosing from the queue the symbol with the lower probability will be chosen, in this case it will be b . Therefore b has greater depth.

Thus we have a contradiction, b probability can not be less than a 's probability.

Analyze Implementation

The run time of a recursive function is 2^n . The graph seen verifies this. As the function calls itself over and over it slows down.

Memorization is a list of results so that the recursive presses is sped up. Instead of re-running the recursion each time the value is taken from the list if it exists.

The runtime of a recursive function with memorization depends on how specific the analyzer wants to go. Technically it is a decrease graph when analyzed really close. That is because if the “n” is not in the memorized list the runtime is $O(n)$, but if it is it is $O(1)$. When looking at the graph from far away it looks constant. It depends on the scale. So yes, technically it is a decreasing line.

My graph and data is consistent with this analysis.