

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile
Cluster Geometry

Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions



Dark Matter in Galaxy Clusters

Shape, Projection, and Environment

Austen M. Groener

Drexel University

September 10, 2015

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

Cluster Shape
& Orientation

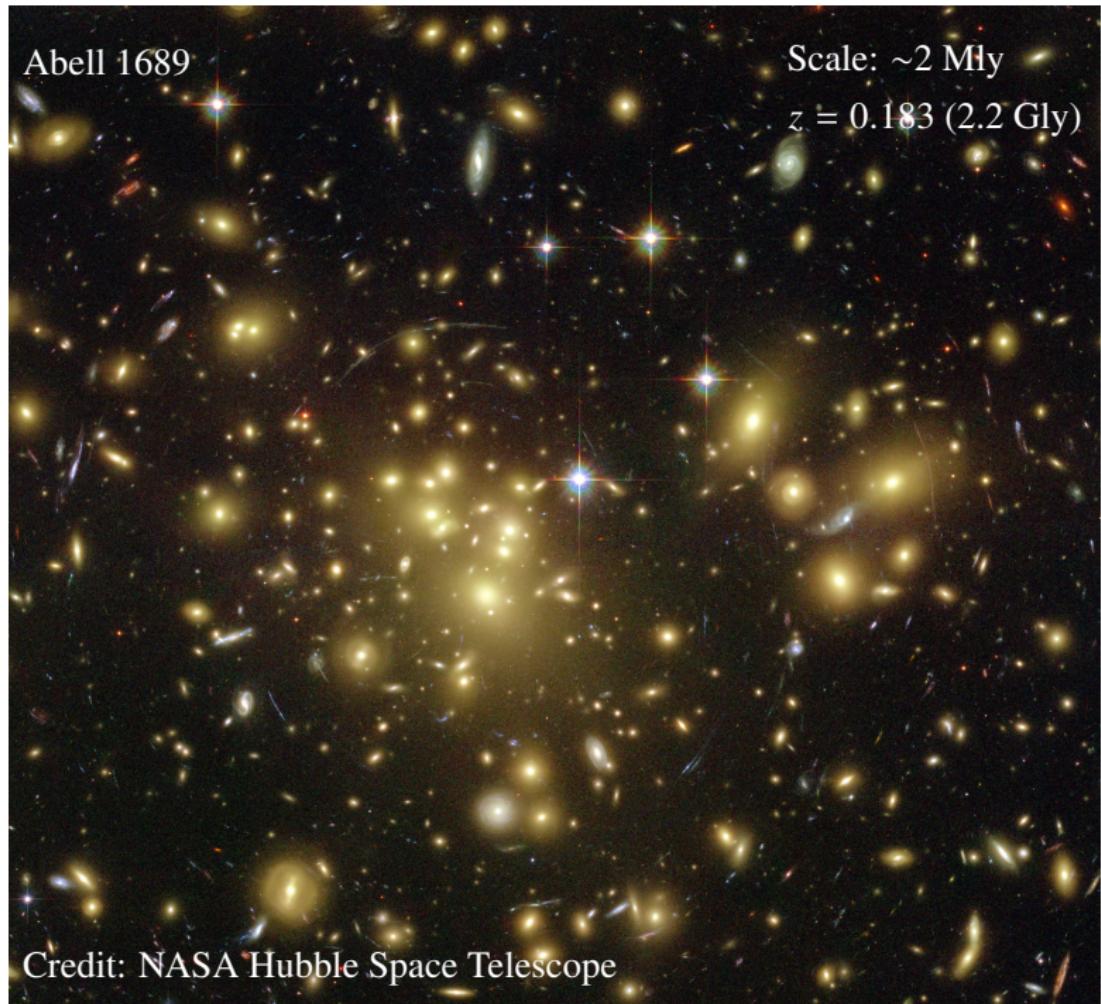
The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

Abell 1689

Scale: ~ 2 Mly
 $z = 0.183$ (2.2 Gly)



Credit: NASA Hubble Space Telescope

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

Cluster Shape
& Orientation

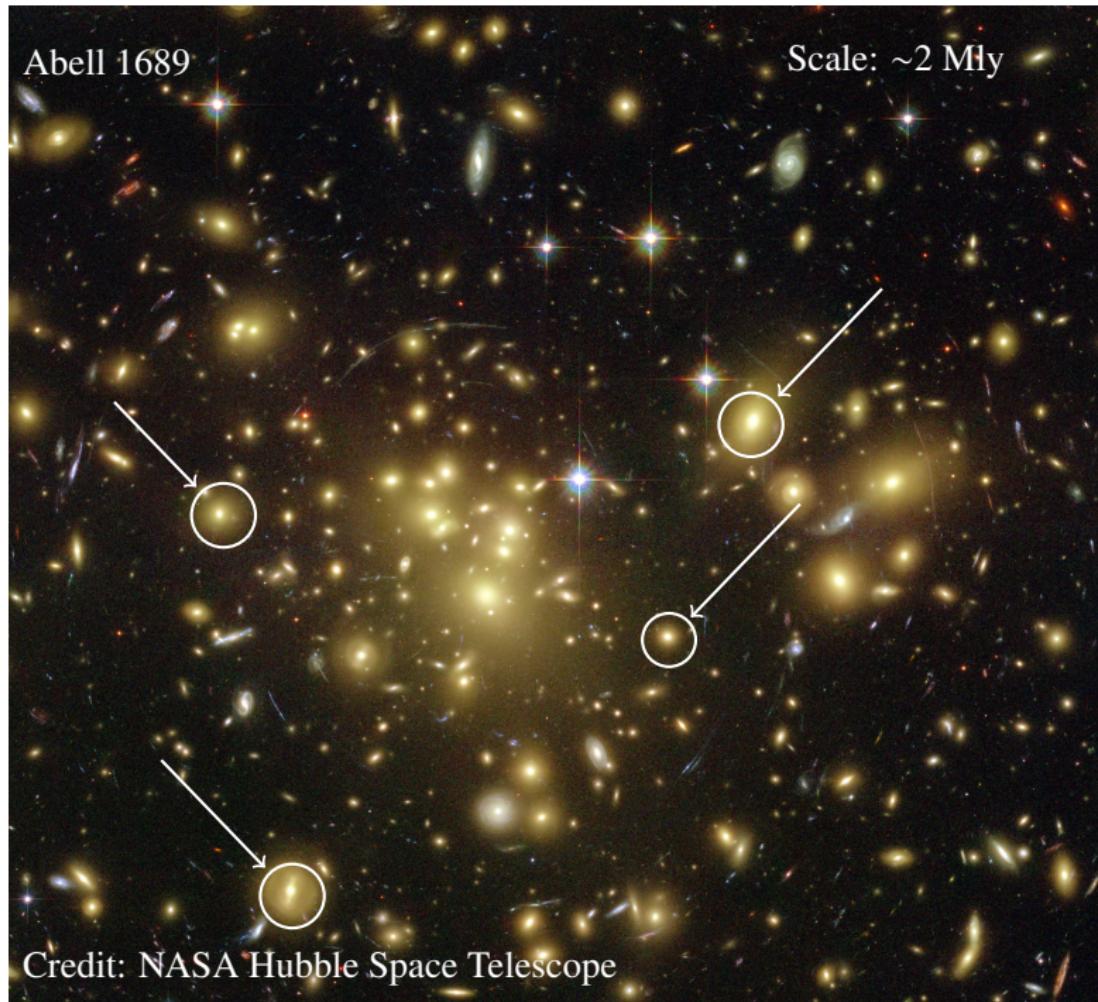
The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

Abell 1689

Scale: ~2 Mly



Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

Cluster Shape
& Orientation

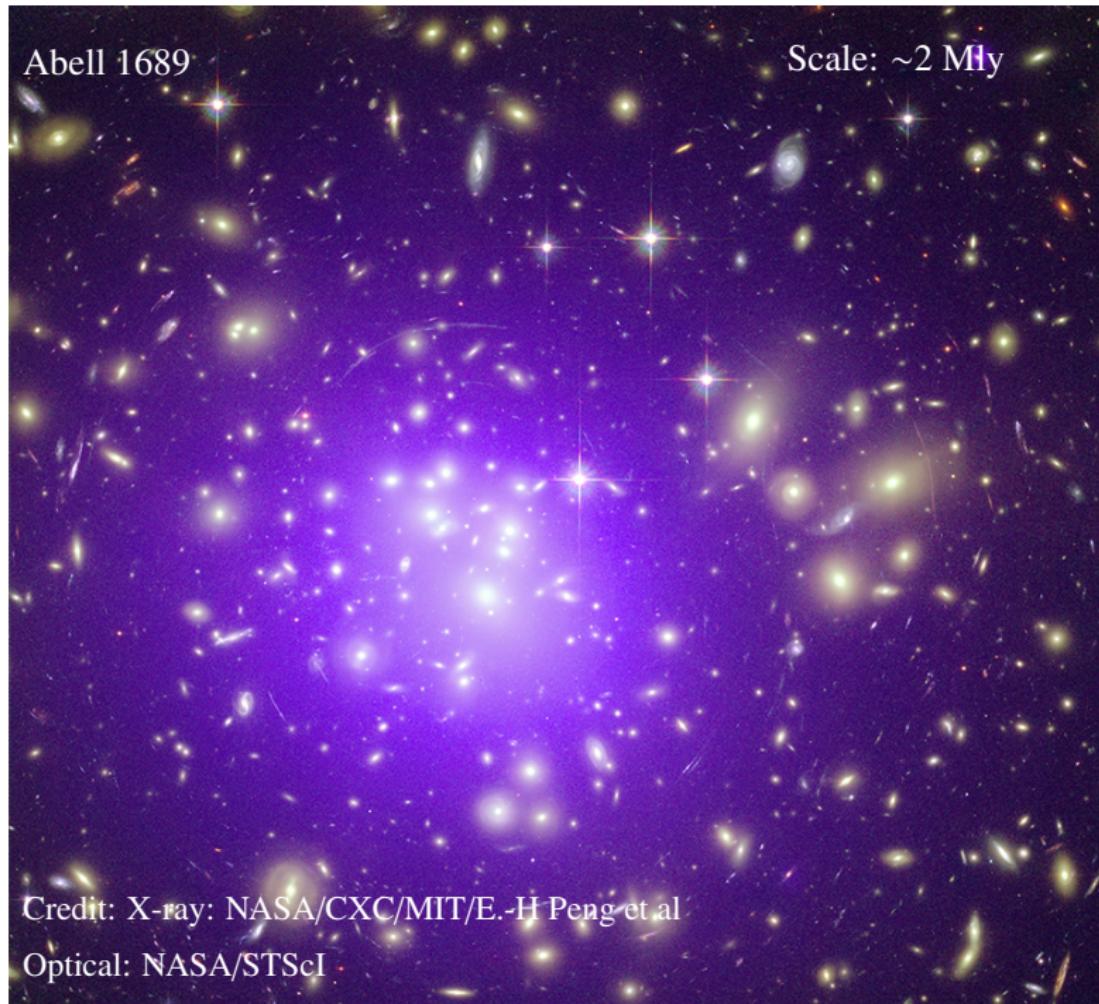
The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

Abell 1689

Scale: ~2 Mly



Credit: X-ray: NASA/CXC/MIT/E.-H Peng et al

Optical: NASA/STScI

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

Cluster Shape
& Orientation

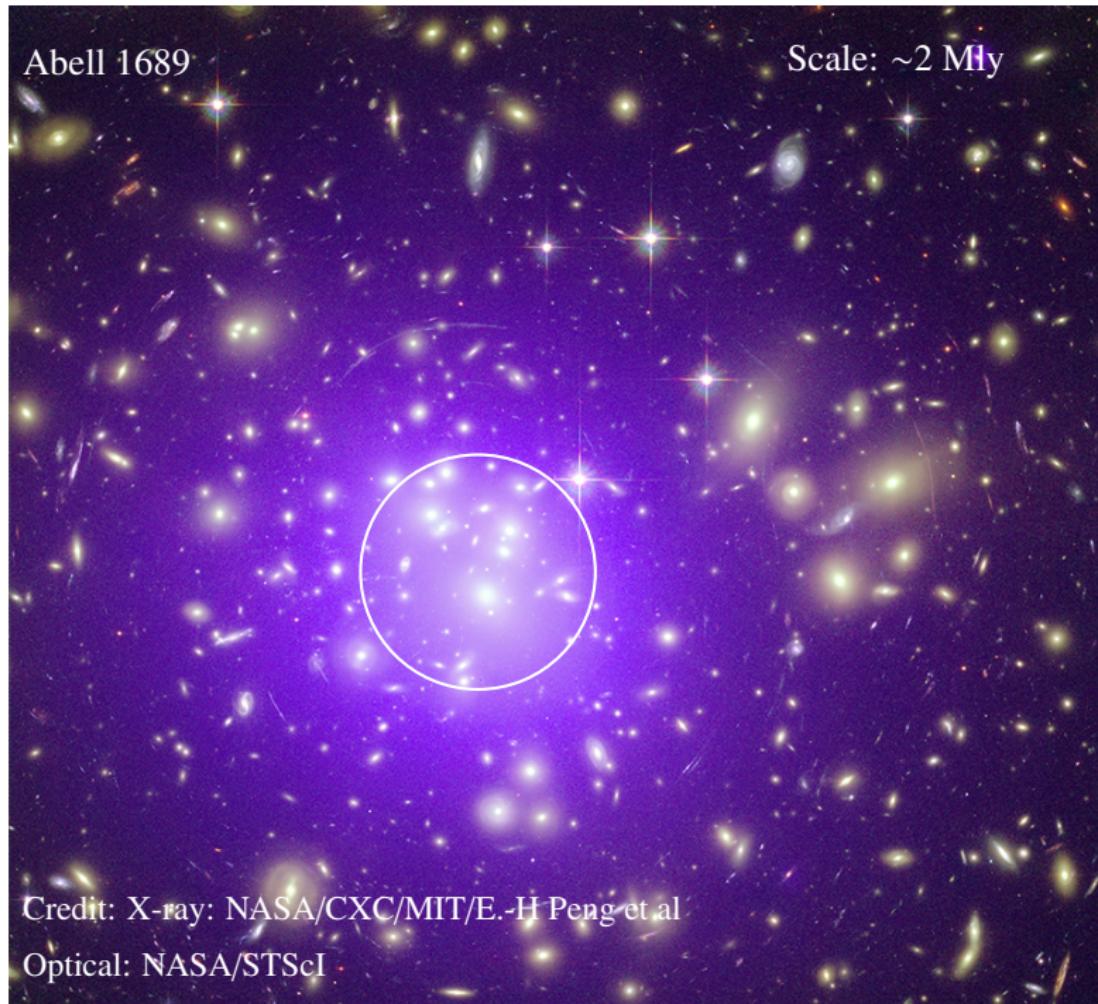
The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

Abell 1689

Scale: ~2 Mly



Credit: X-ray: NASA/CXC/MIT/E.-H Peng et al

Optical: NASA/STScI

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

Cluster Shape
& Orientation

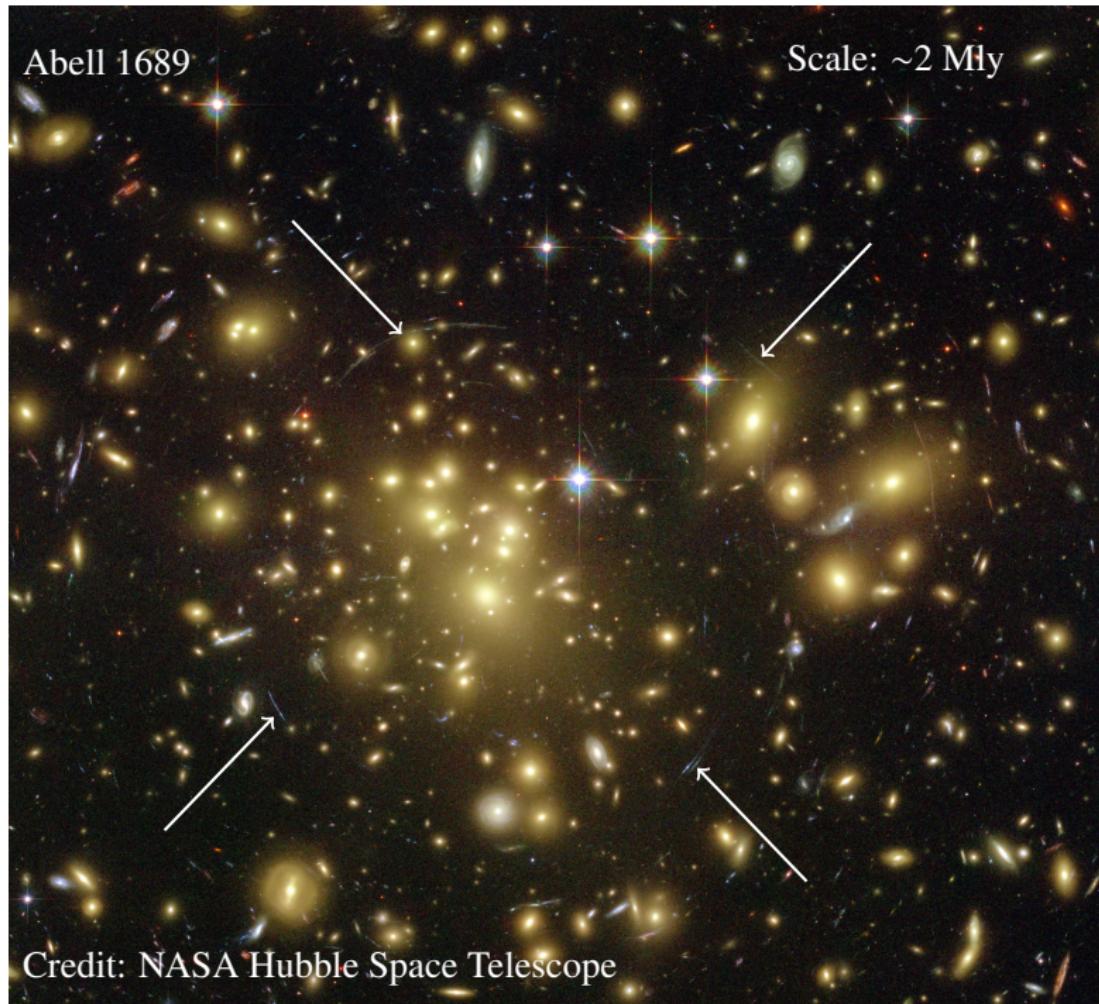
The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

Abell 1689

Scale: ~2 Mly



Credit: NASA Hubble Space Telescope

Dark Matter in Galaxy Clusters

Austen M.
Groener

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

Cluster Shape
& Orientation

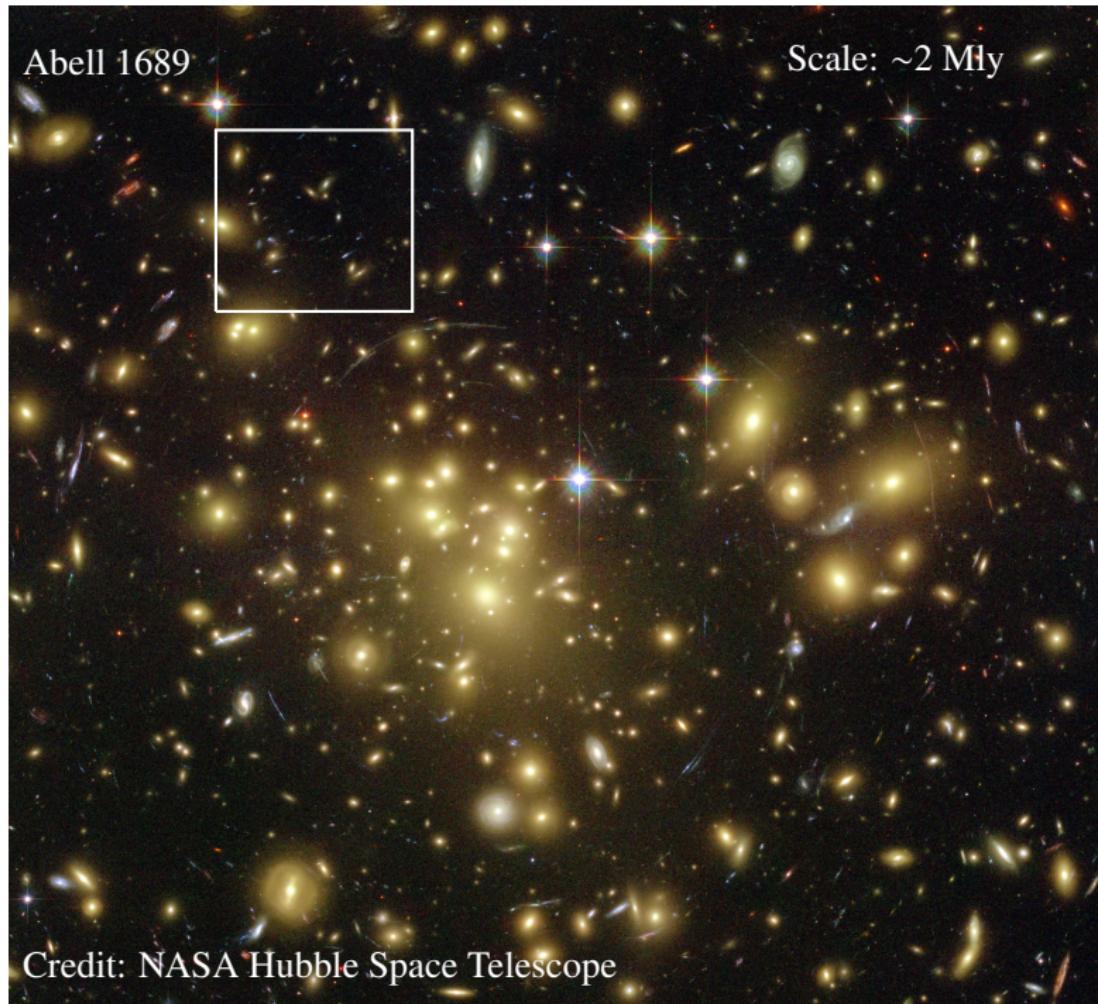
The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

Abell 1689

Scale: ~2 Mly



Credit: NASA Hubble Space Telescope

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

Cluster Shape
& Orientation

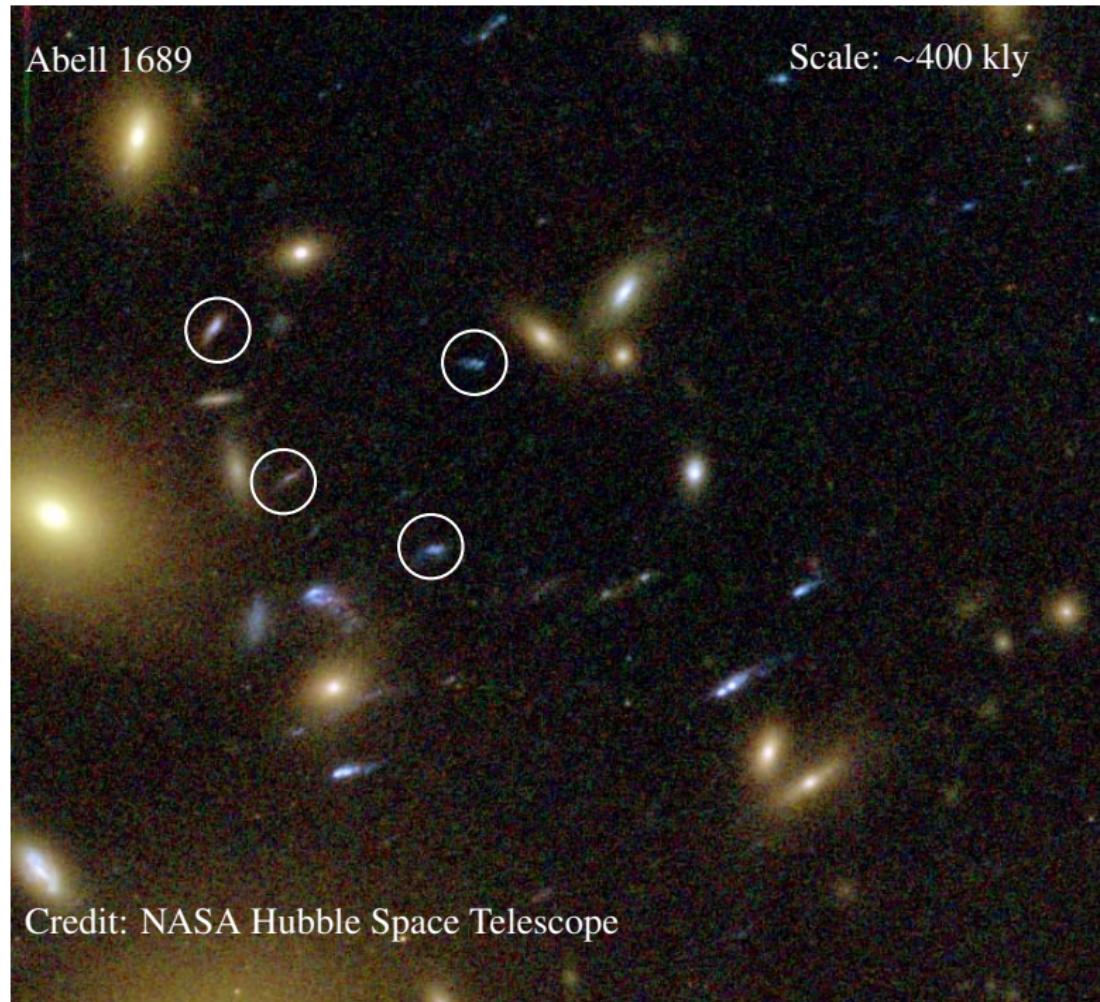
The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

Abell 1689

Scale: ~400 kly



Credit: NASA Hubble Space Telescope

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

Cluster Shape
& Orientation

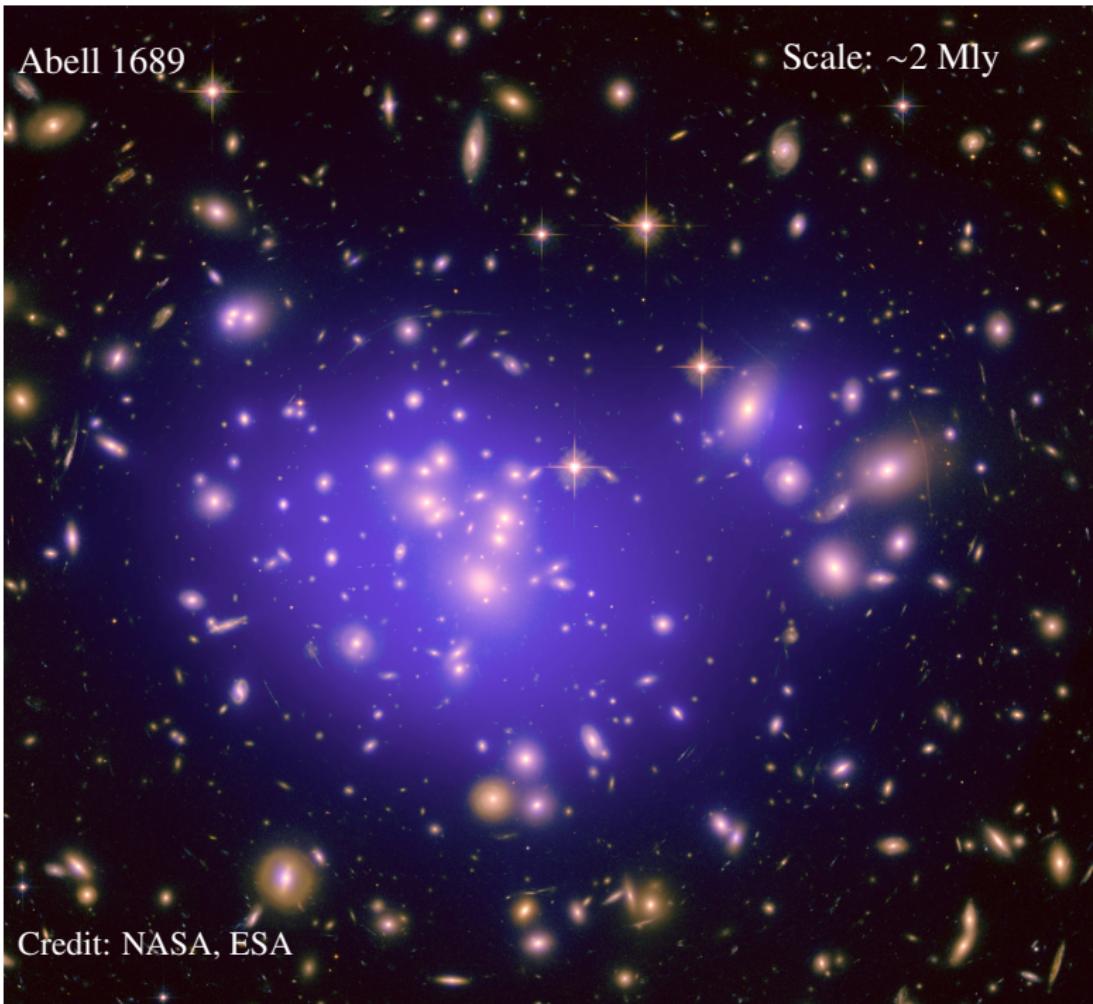
The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

Abell 1689

Scale: ~2 Mly



Credit: NASA, ESA

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

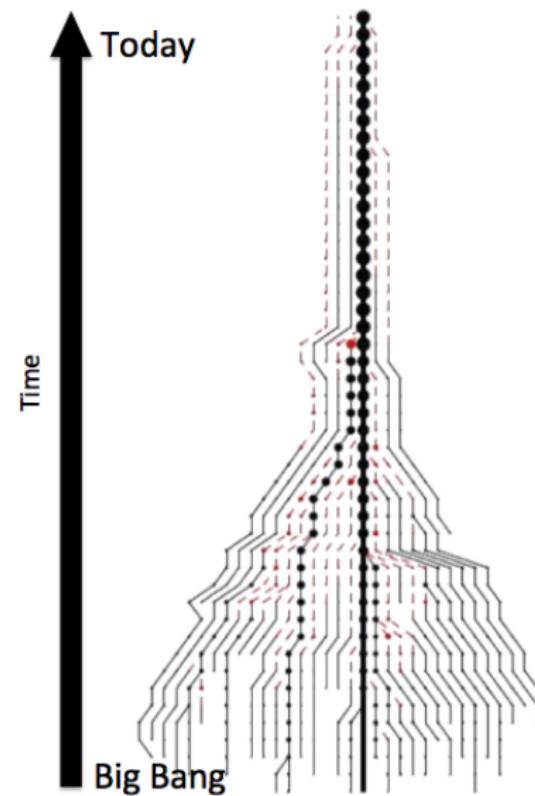
Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

Hierarchical Structure Formation



Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

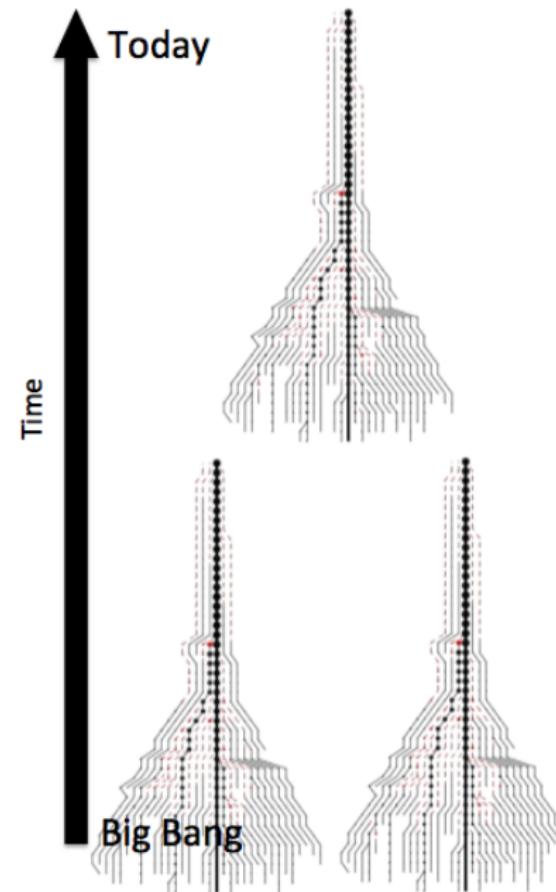
Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

Hierarchical Structure Formation



The Navarro-Frenk-White Profile

NFW (1996)

Introduction

The Anatomy of a Cluster

The Radial Density Profile

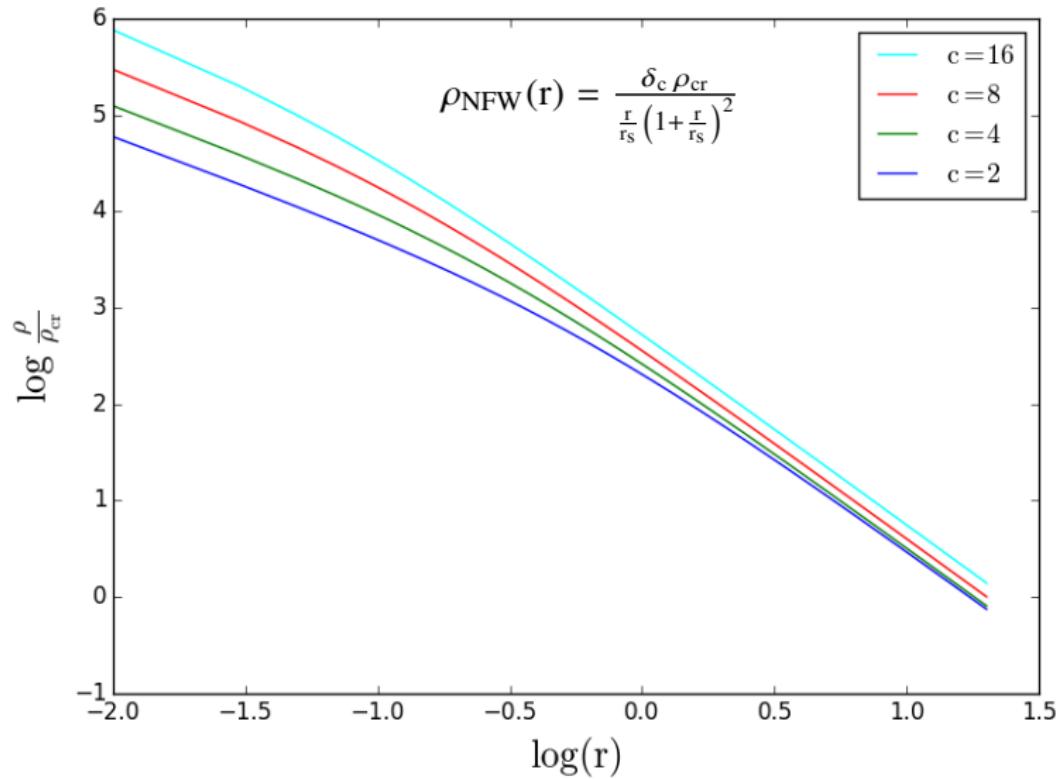
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

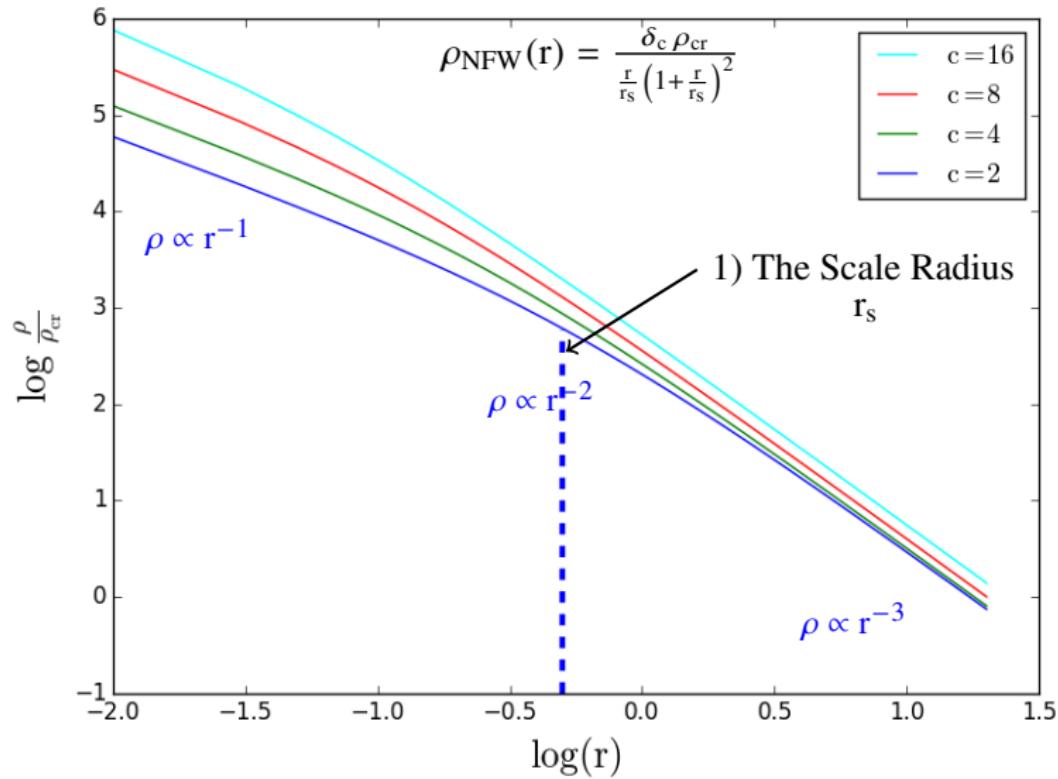
Clusters and the LSS of the Universe

Conclusions



The Navarro-Frenk-White Profile

NFW (1996)



Introduction
The Anatomy of a Cluster

The Radial Density Profile
Cluster Geometry

Cluster Shape & Orientation

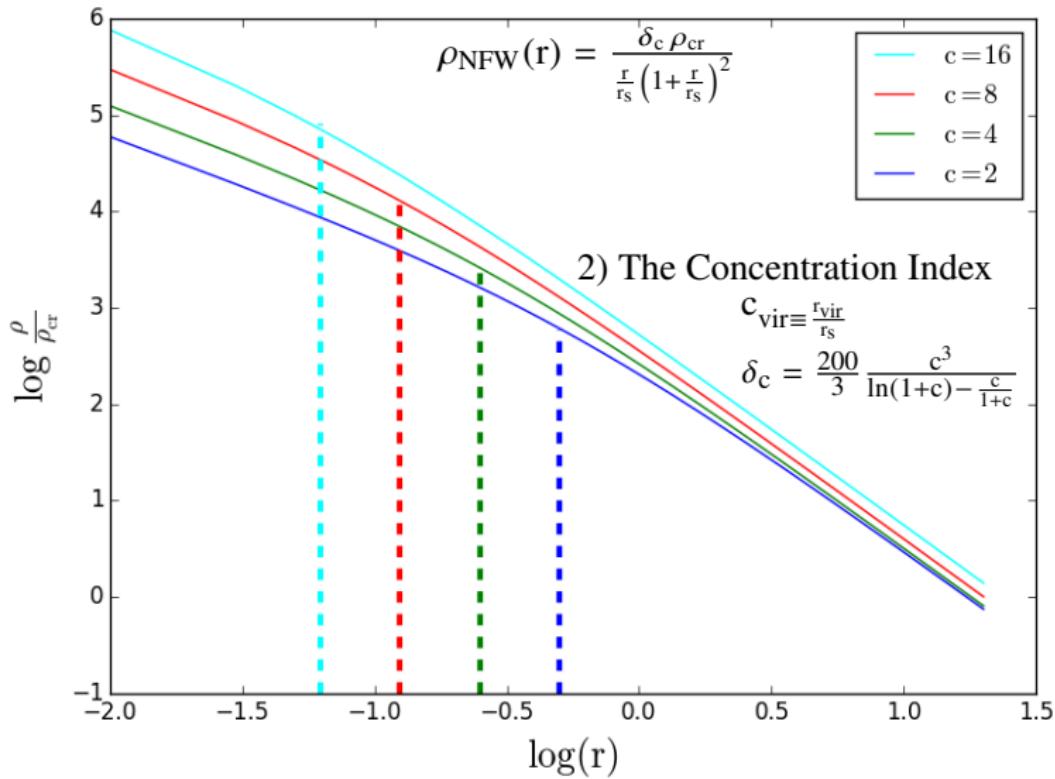
The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions

The Navarro-Frenk-White Profile

NFW (1996)



The Cuspy Halo Problem

(The Over-Concentration Problem)

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

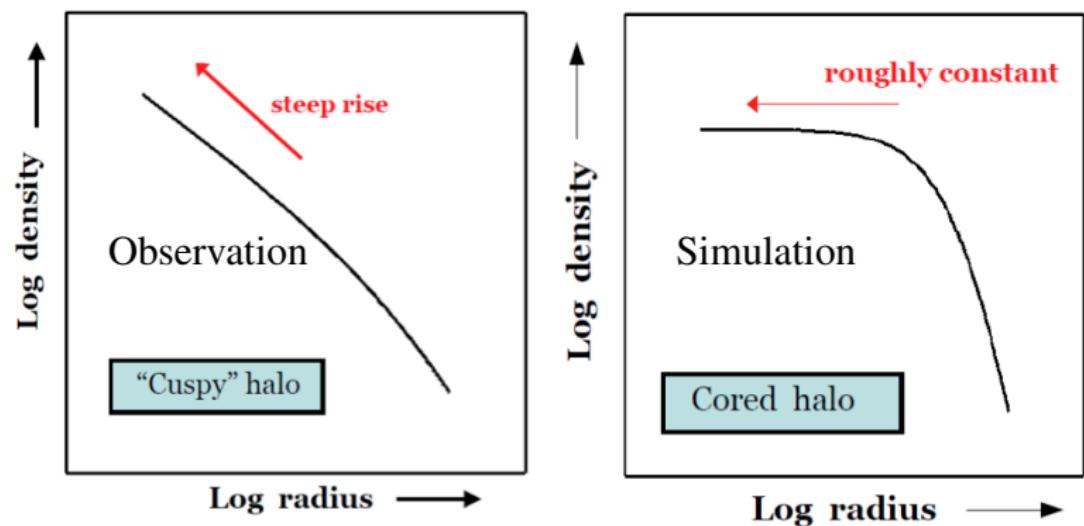
Cluster Geometry

Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions



- Observed clusters:
 $c_{\text{vir}} = 8 - 12$
- Simulated clusters:
 $c_{\text{vir}} = 4 - 6$

The Concentration-Mass (c-M) Scaling Relation

Austen M.
Groener

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

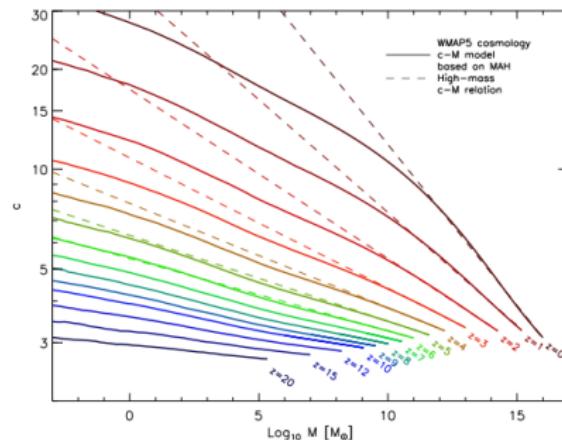
Cluster Geometry

Cluster Shape
& Orientation

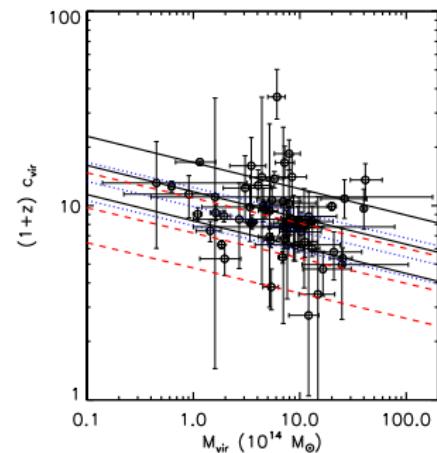
The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions



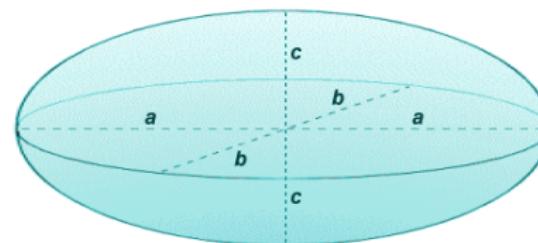
Simulation (Correa et al. 2015)



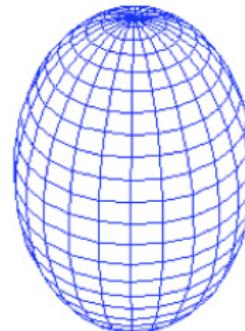
Observational (Comerford & Natarajan
2007)

Clusters Are *Not* Spherical

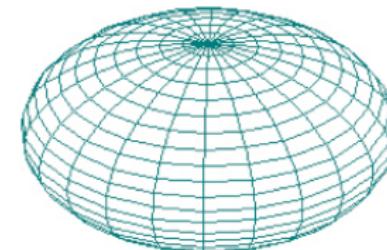
Triaxial Ellipsoid



Prolate $a < b = c$



Oblate $a = b > c$



Triaxial Projection Biases 2D Observables

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

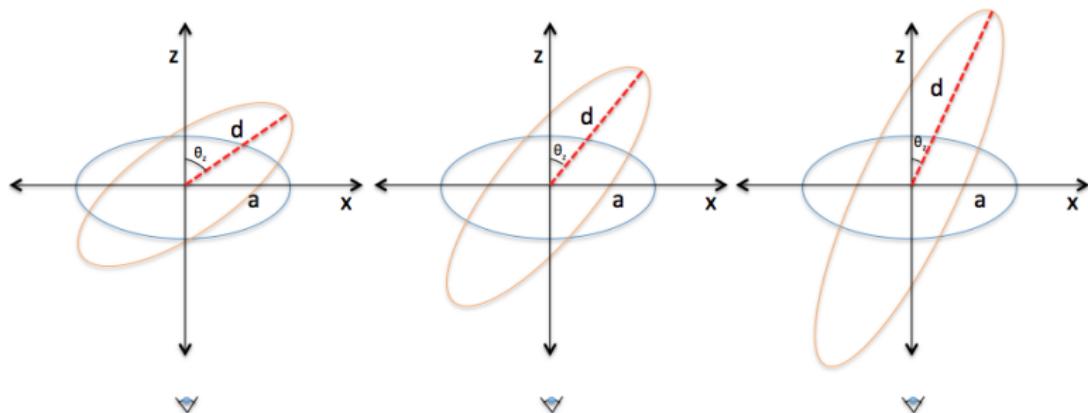
Cluster Geometry

Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions



Simulated Halo Isodensities Are Not Constant On All Scales

Austen M.
Groener

Introduction

The Anatomy of a Cluster

The Radial Density Profile

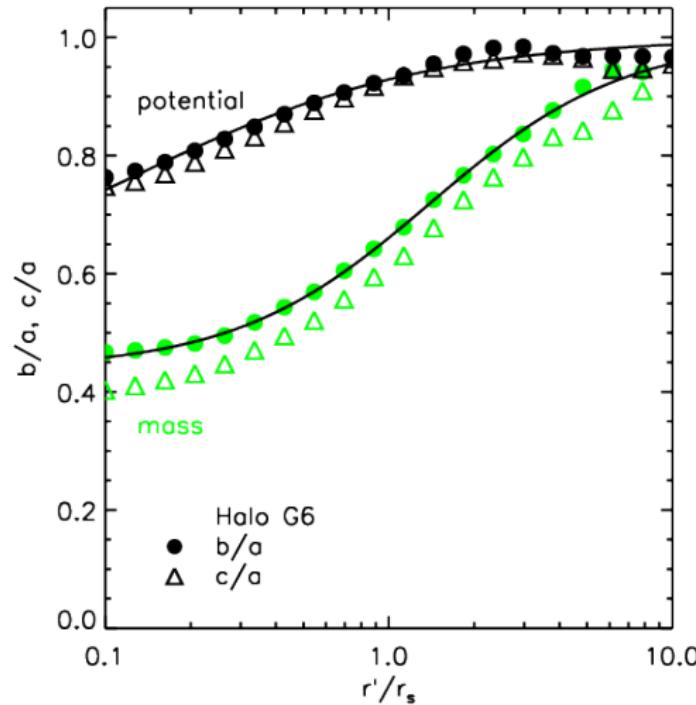
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



Implications For Cluster Mass Reconstruction

Austen M.
Groener

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

- Does the changing of isodensity shape affect the concentration parameter *differently* as a function of cluster scale?
- Is the 2D concentration even a well-defined quantity?

Groener & Goldberg (2014)

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

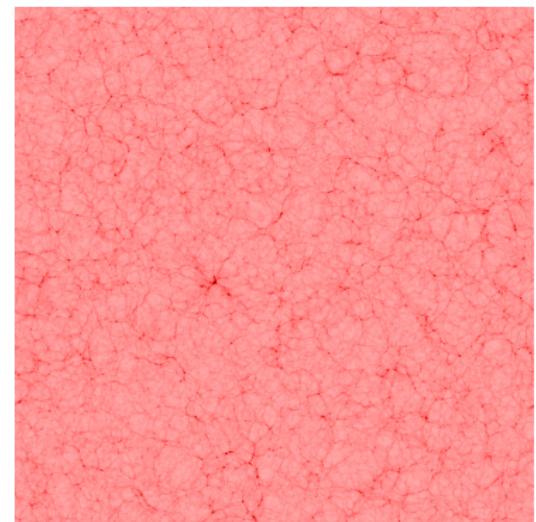
Clusters and the LSS of the Universe

Conclusions

The MDR1 Simulation

(Prada et al.
2012)

- Dark matter only, 2048^3 particles
- Adaptive-Refinement-Tree (ART) (Kravtsov et al. 1997)
- Cosmology: WMAP5
- Mass resolution: $8.721 \times 10^9 M_\odot/h$
- Force resolution: 7.0 kpc/h
- Box: 1000 Mpc/h (on a side)
- Mass range: $(1.7 \times 10^{11} - 1.6 \times 10^{15}) M_\odot/h$



MDR1 Simulated Cluster Halos

Introduction

The Anatomy of a
Cluster

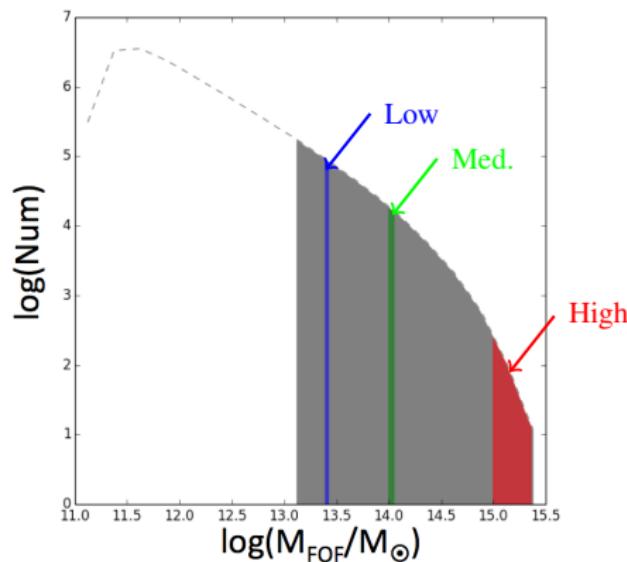
The Radial Density
Profile
Cluster Geometry

Cluster Shape & Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions



The Sample ($z=0$)

- Low Mass: $(2.5 - 2.6) \times 10^{13} M_{\odot}/h$ [6007]
- Med. Mass: $(1.0 - 1.1) \times 10^{14} M_{\odot}/h$ [2905]
- High Mass: $> 1.0 \times 10^{15} M_{\odot}/h$ [121]

Sample Selection Criteria

Clustering and Virialization Criteria

Introduction

The Anatomy of a Cluster

The Radial Density Profile

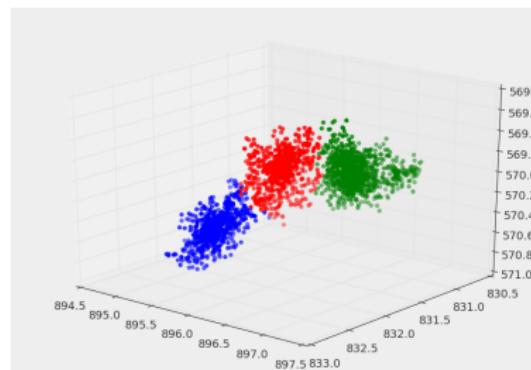
Cluster Geometry

Cluster Shape & Orientation

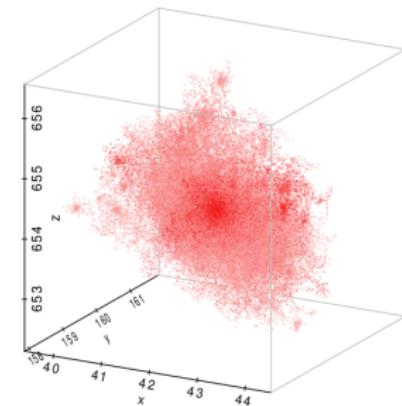
The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



Merging, unrelaxed cluster



The Final Product

- MDR1 Friends of Friends (FOF) Catalog
- Apply MeanShift/K-Means Algorithms

- Find Dynamically Relaxed Halos Shaw et al. (2006)

Full Distribution of Shapes

Introduction

The Anatomy of a Cluster

The Radial Density Profile

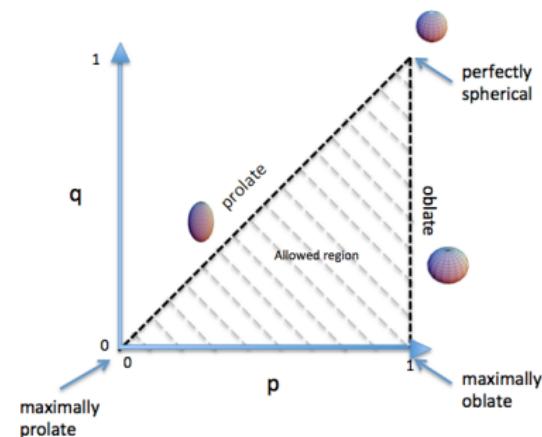
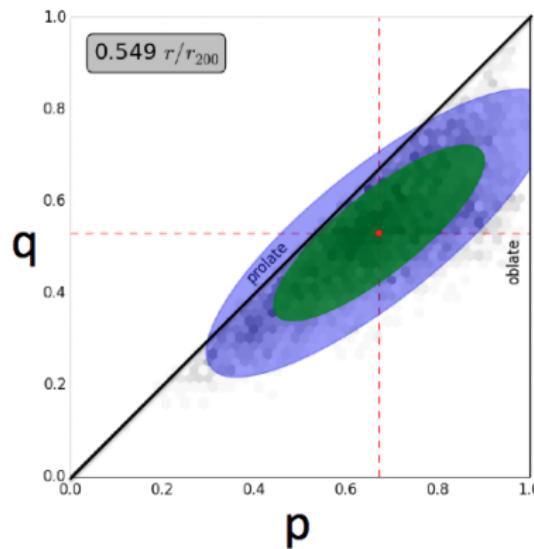
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



Changing Shape of Isodensities

Introduction

The Anatomy of a Cluster

The Radial Density Profile

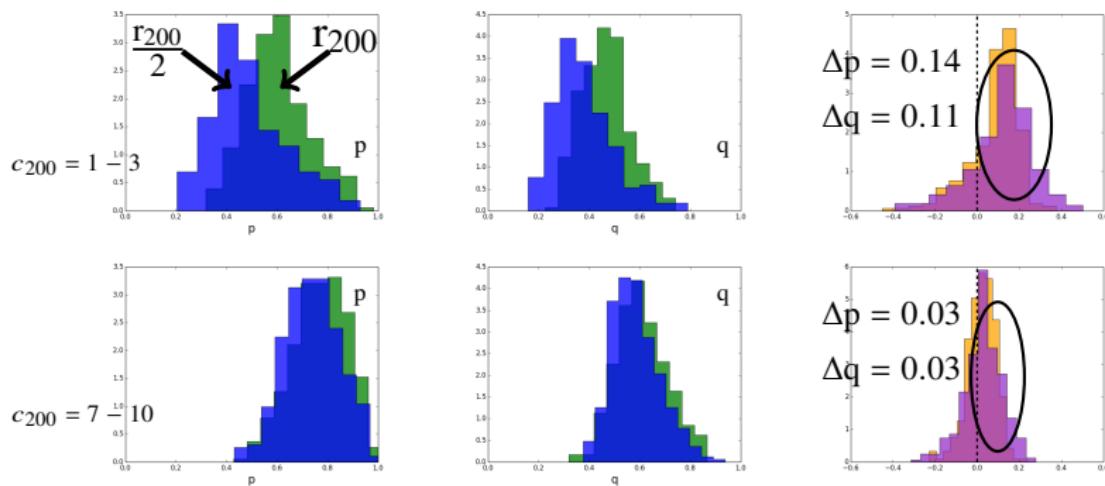
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



Along the Top: Distribution of axial ratios p, q , on characteristic scales $r_{200}/2$ (blue), and r_{200} (green) for $c_{200} = 1 - 3$. Difference in axial ratios p (purple) and q (orange) on these scales. *Along the Bottom:* Similar plots for $c_{200} = 7 - 10$.

Concentrations In Projection

Introduction

The Anatomy of a Cluster

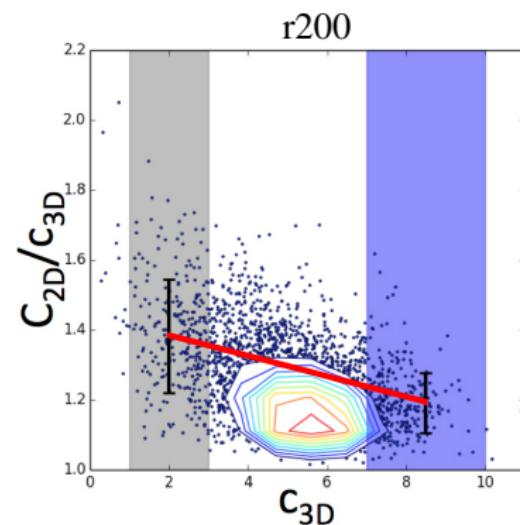
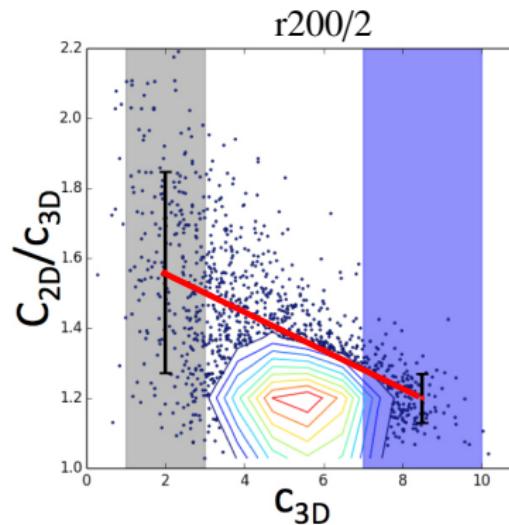
The Radial Density Profile
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



- Trend 1: Projected concentration is a function of intrinsic concentration, and is fractionally larger for low concentrations.

Concentrations In Projection

Introduction

The Anatomy of a Cluster

The Radial Density Profile

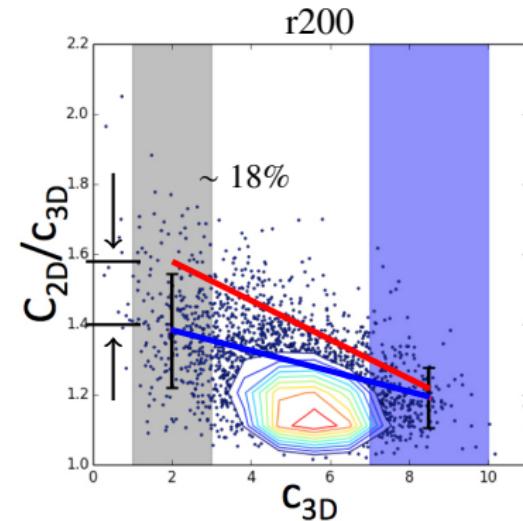
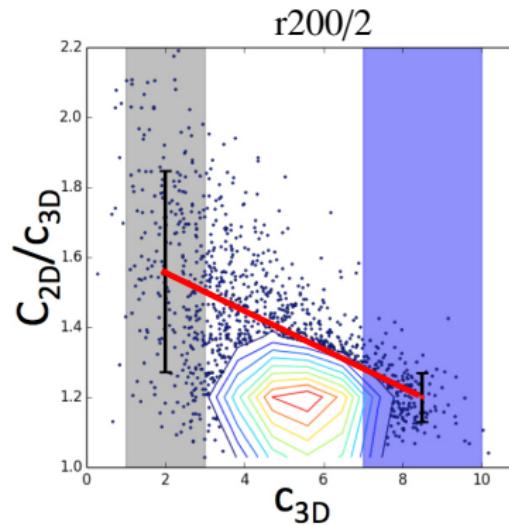
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



- Trend 2: Projected concentration is a function of radius, and changes the most for intrinsically low concentrations.

Conclusions

- Relaxed MDR1 cluster halos are prolate spheroidal in shape, and move toward sphericity at larger radii.
- Due to analytical projection, line-of-sight oriented halos are over-concentrated.
- This over-concentration is stronger on SL scales than on WL scales ($\sim 20\%$).
- Lower mass halos ($\sim 3 \times 10^{13} h^{-1} M_{\odot}$) are *more* affected by this difference than high mass halos are.

THE ASTROPHYSICAL JOURNAL

SHAPE PROFILES AND ORIENTATION BIAS FOR WEAK AND
STRONG LENSING CLUSTER HALOS



A. M. Groener and D. M. Goldberg

Published 2014 October 23 • © 2014. The American Astronomical Society. All rights reserved. • [The Astrophysical Journal, Volume 795, Number 2](#)

The c-M Relation: What To Expect

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

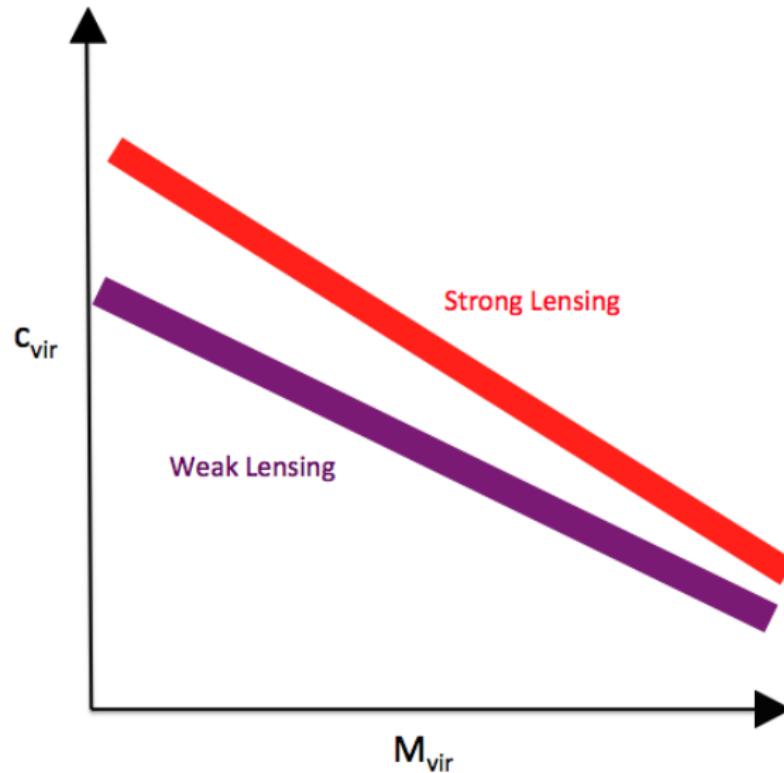
Cluster Geometry

Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions



Groener, Goldberg, & Sereno (2015)

Introduction

The Anatomy of a Cluster

The Radial Density Profile
Cluster Geometry

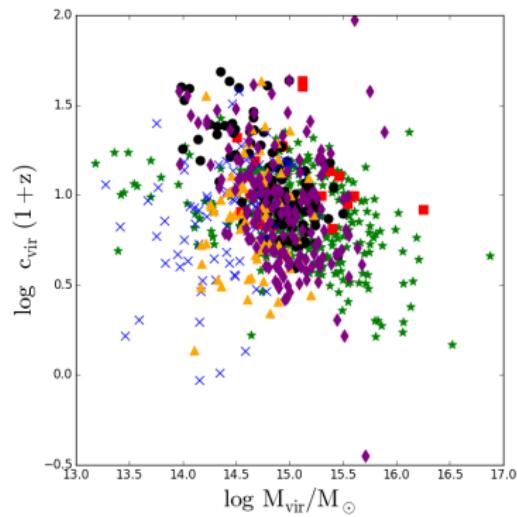
Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions

- 81 papers
- 781 cluster measurements
- 361 unique clusters
- Methods:
(arranged roughly from small to large scale)
 - X-ray
 - Strong Lensing (SL)
 - Weak + Strong Lensing (WL+SL)
 - Weak Lensing (WL)
 - Line of sight velocity dispersion (LOSVD)
 - Caustic Method (CM)



Lensing Reconstruction Techniques

Weak Lensing (WL), Strong Lensing (SL), and WL+SL

Introduction

The Anatomy of a Cluster

The Radial Density Profile

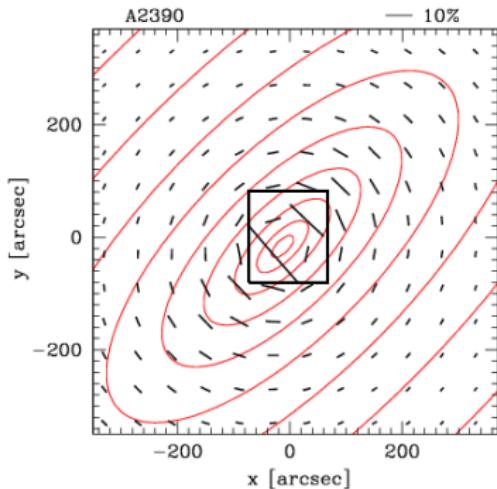
Cluster Geometry

Cluster Shape & Orientation

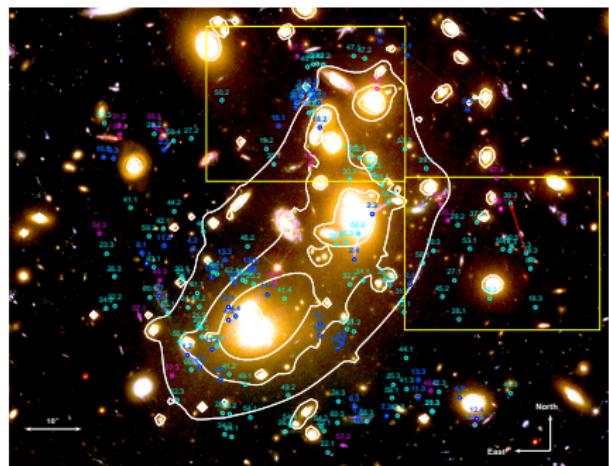
The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



Abell 2390 ($z=0.228$) Oguri et al.
(2010)



Abell 2744 ($z=0.308$) Jauzac et al. (2014)

Introduction

The Anatomy of a Cluster

The Radial Density Profile

Cluster Geometry

Cluster Shape & Orientation

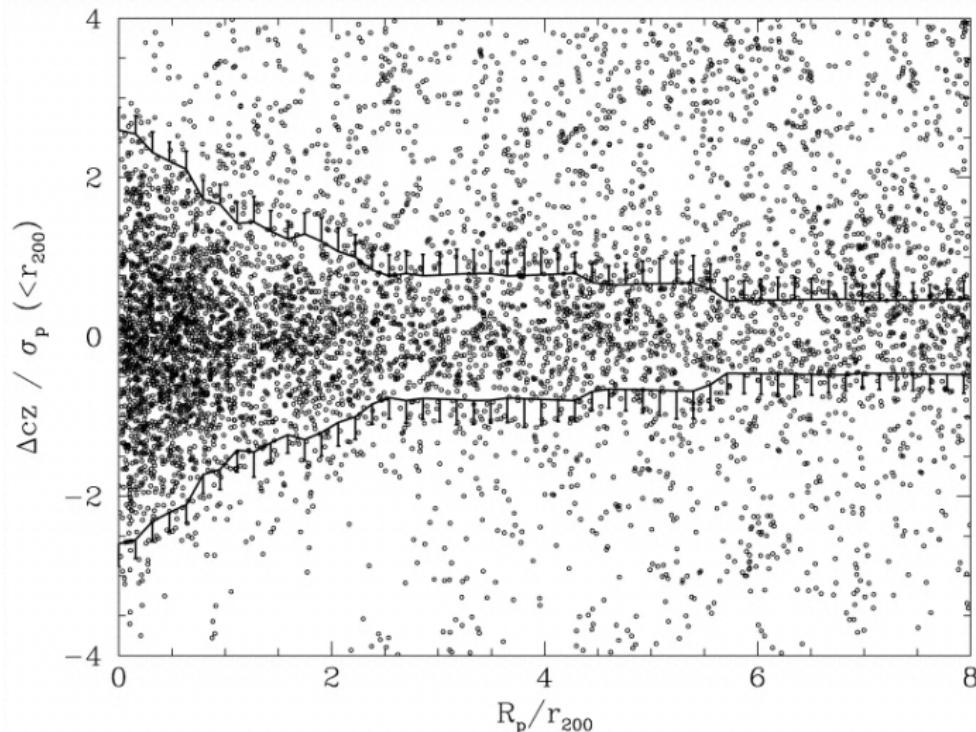
The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions

Galaxy-Based Reconstruction Techniques

The Caustic Method (CM) and Line-of-sight Velocity Dispersion (LOSVD)



The Caustic Method Rines et al. (2006)

X-ray Reconstruction Techniques

Austen M.
Groener

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

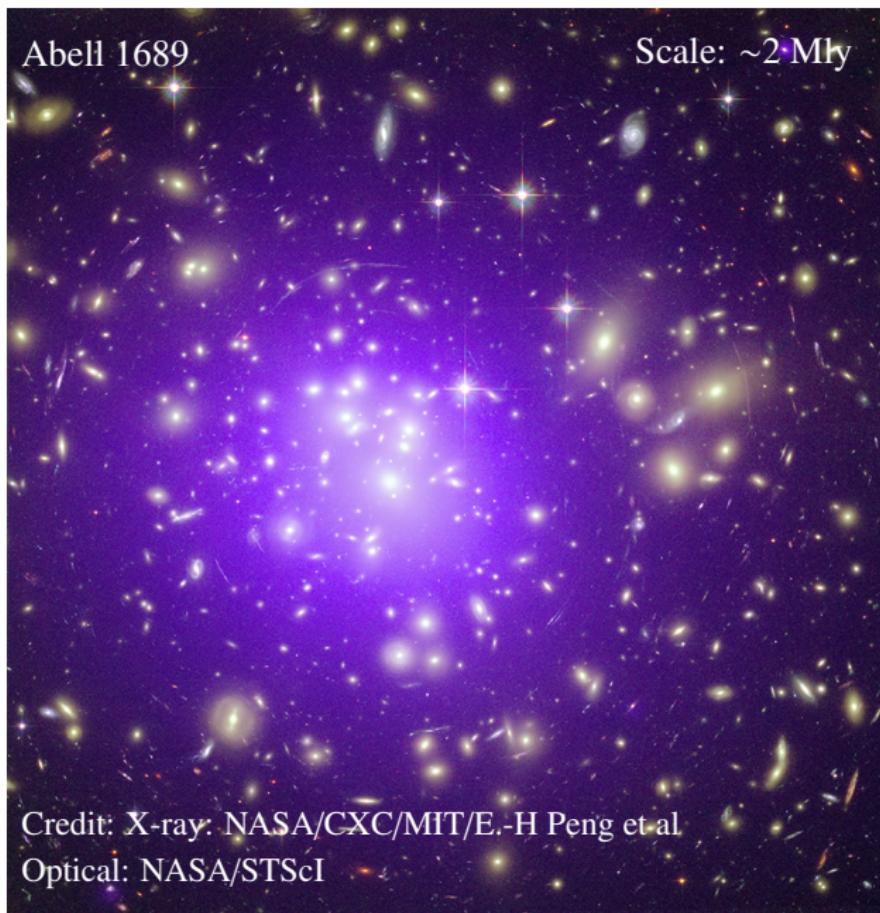
Cluster Geometry

Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions



Reconstruction-Dependent Results

Introduction

The Anatomy of a Cluster

The Radial Density Profile

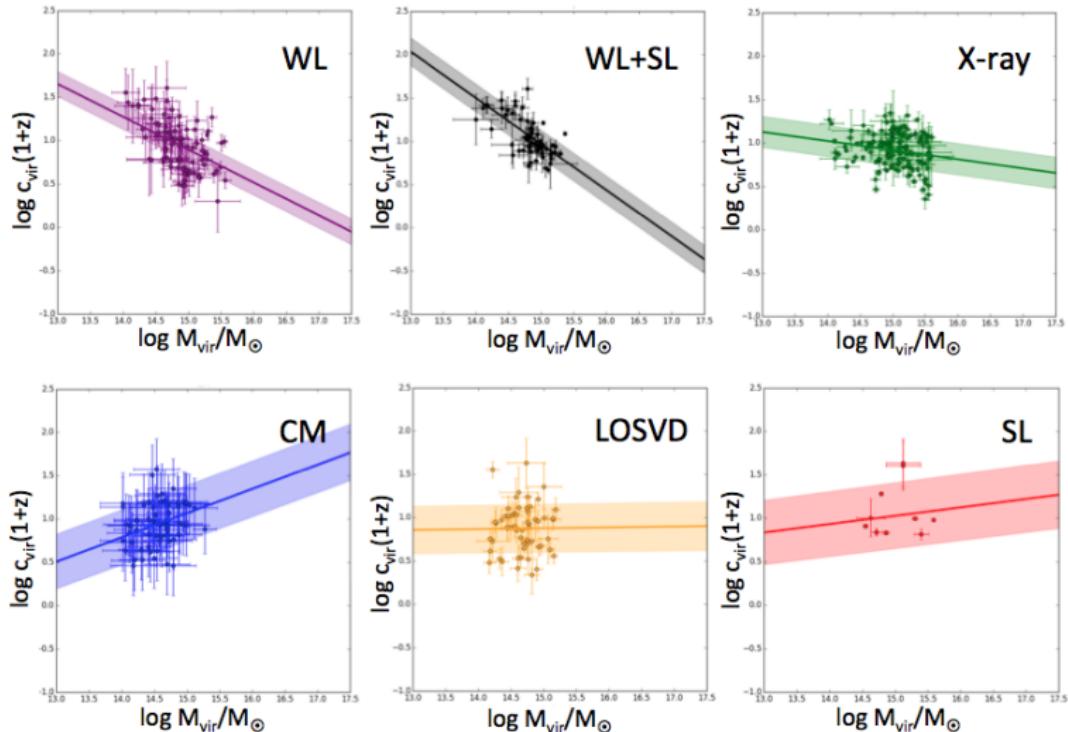
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



Comparison of c-M relations

Introduction

The Anatomy of a Cluster

The Radial Density Profile

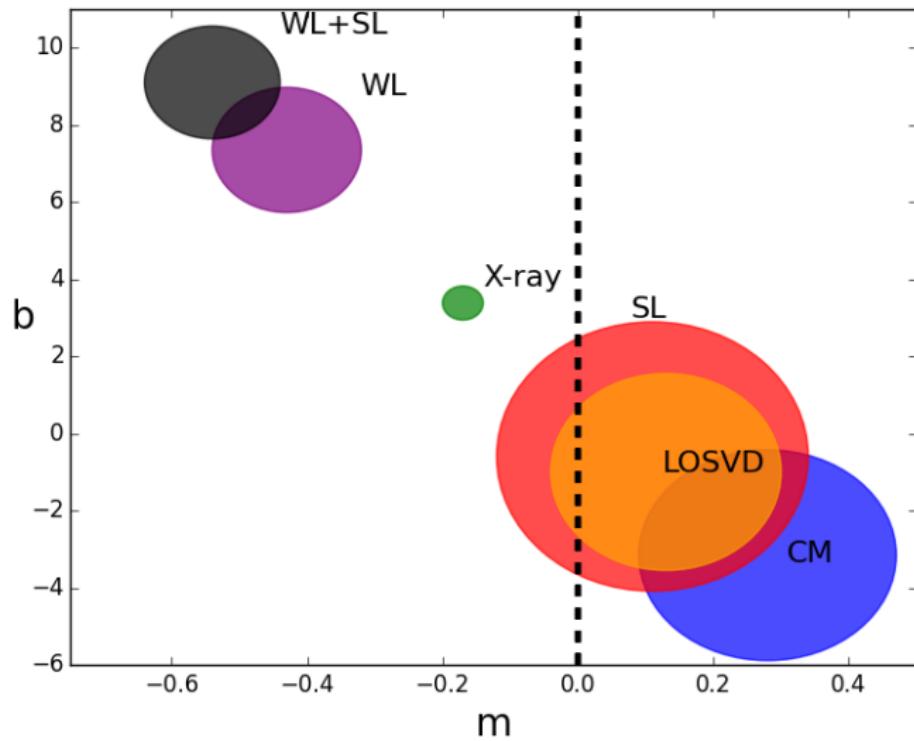
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



Introduction

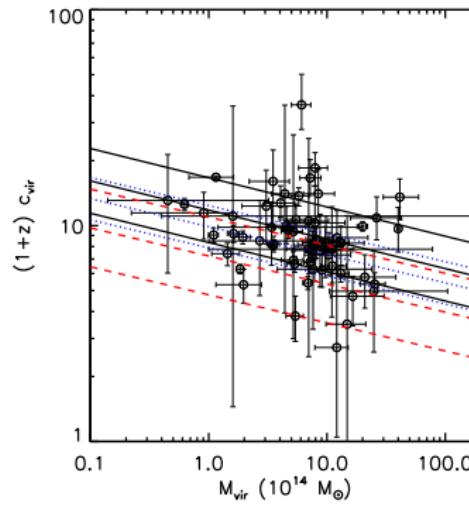
The Anatomy of a
ClusterThe Radial Density
Profile

Cluster Geometry

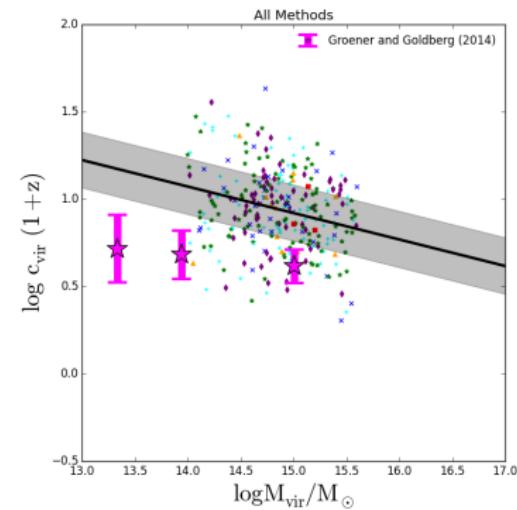
Cluster Shape
& OrientationThe Observed
c-M RelationClusters and the
LSS of the
Universe

Conclusions

Fit To All Data



Comerford & Natarajan (2007) - All Methods.



This work - All Methods.

Comparison Revisited

Introduction

The Anatomy of a Cluster

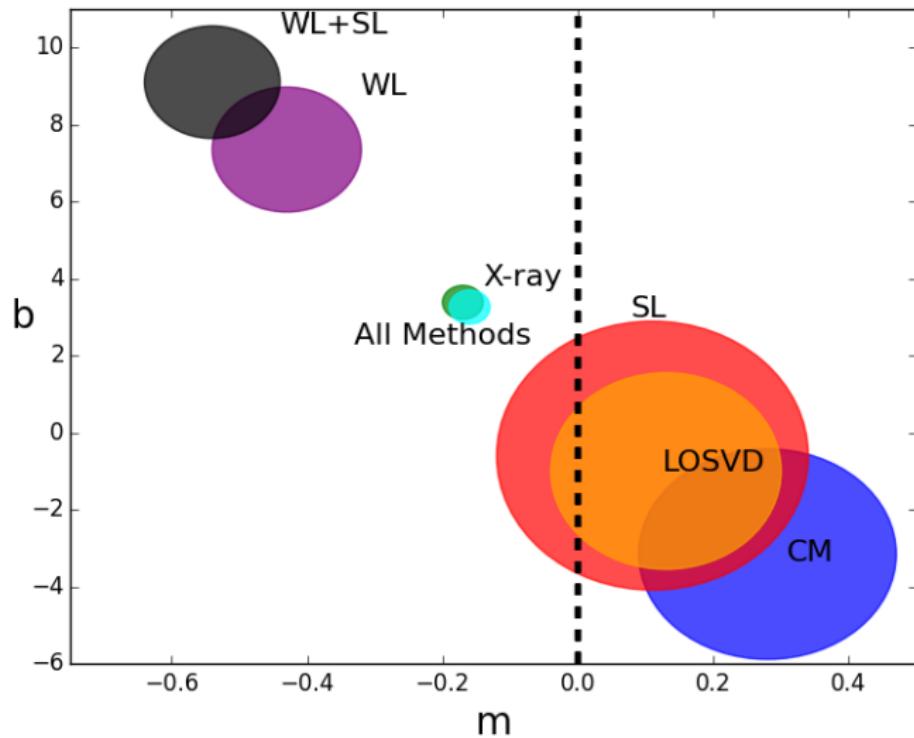
The Radial Density Profile
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



Information about the halo is lost!

Comparison With CLASH

Merten et al. (2014)

Introduction

The Anatomy of a Cluster

The Radial Density Profile

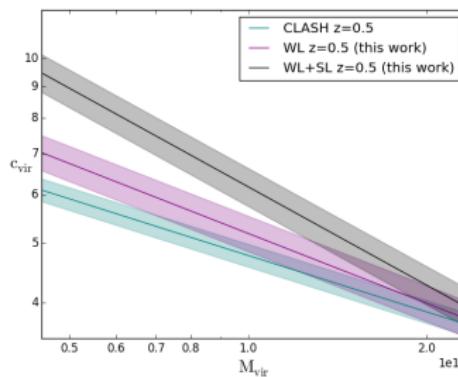
Cluster Geometry

Cluster Shape & Orientation

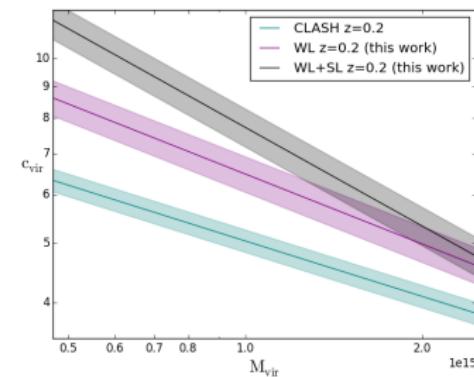
The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



$$z = 0.5$$



$$z = 0.2$$

- Low redshift cluster concentrations are off by $\sim 50\%$ for WL, but $\sim 100\%$ for WL+SL.
- High redshift cluster concentrations are nearly in agreement with WL, but still off by $\sim 50\%$ with WL+SL.

Comparison With Simulations

Introduction

The Anatomy of a Cluster

The Radial Density Profile

Cluster Geometry

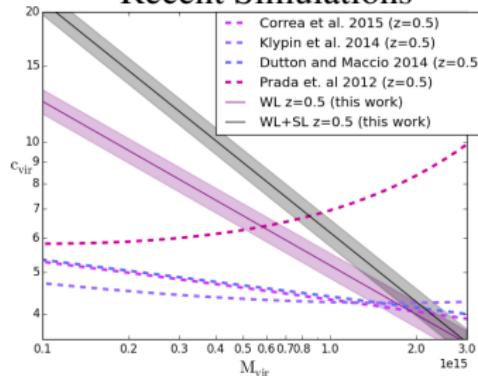
Cluster Shape & Orientation

The Observed c-M Relation

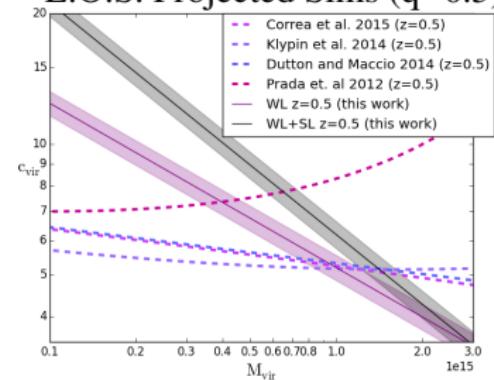
Clusters and the LSS of the Universe

Conclusions

Recent Simulations



L.O.S. Projected Sims ($q=0.5$)



- Projection is not enough. Still off by almost a factor of 2!
- Selection effects are likely responsible.

Conclusions

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

- The c-M relation varies from technique to technique.
- The steepest relations are WL and WL+SL.
- The WL+SL relation is steeper (though consistent) with WL.
- The SL, CM, and LOSVD relations are not well-constrained, and are consistent with a slope of zero.

Look for us in MNRAS!

The Large-Scale Cluster Environment

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

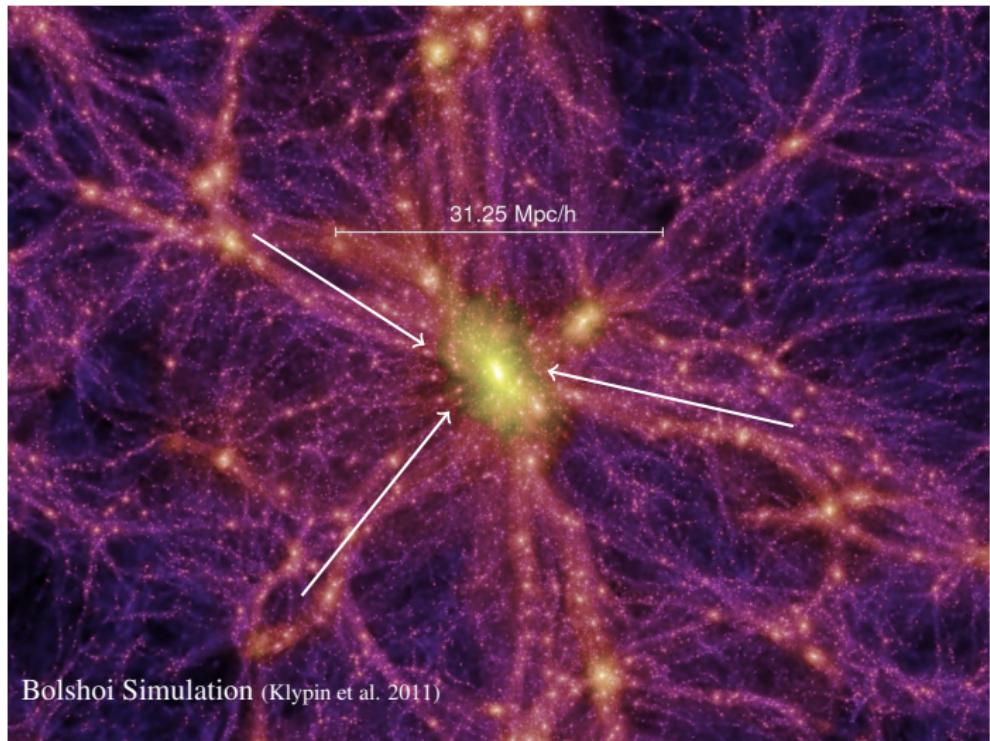
Cluster Geometry

Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions



The SDSS DR10 Sample

Austen M.
Groener

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

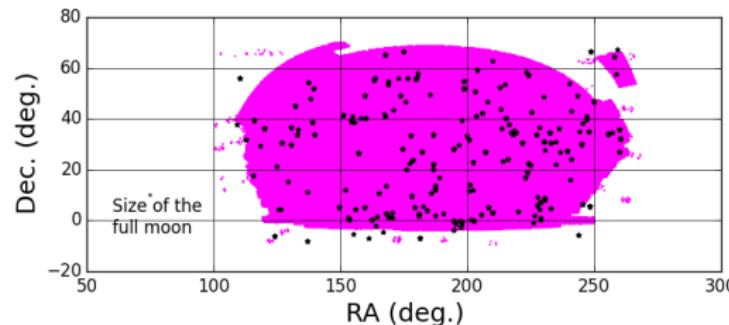
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



- ~ 1.4 million spectroscopically confirmed galaxies
- $z \lesssim 0.7$.
- 203 of 361 clusters are within the survey volume.

Clusters Within the LSS

Austen M.
Groener

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

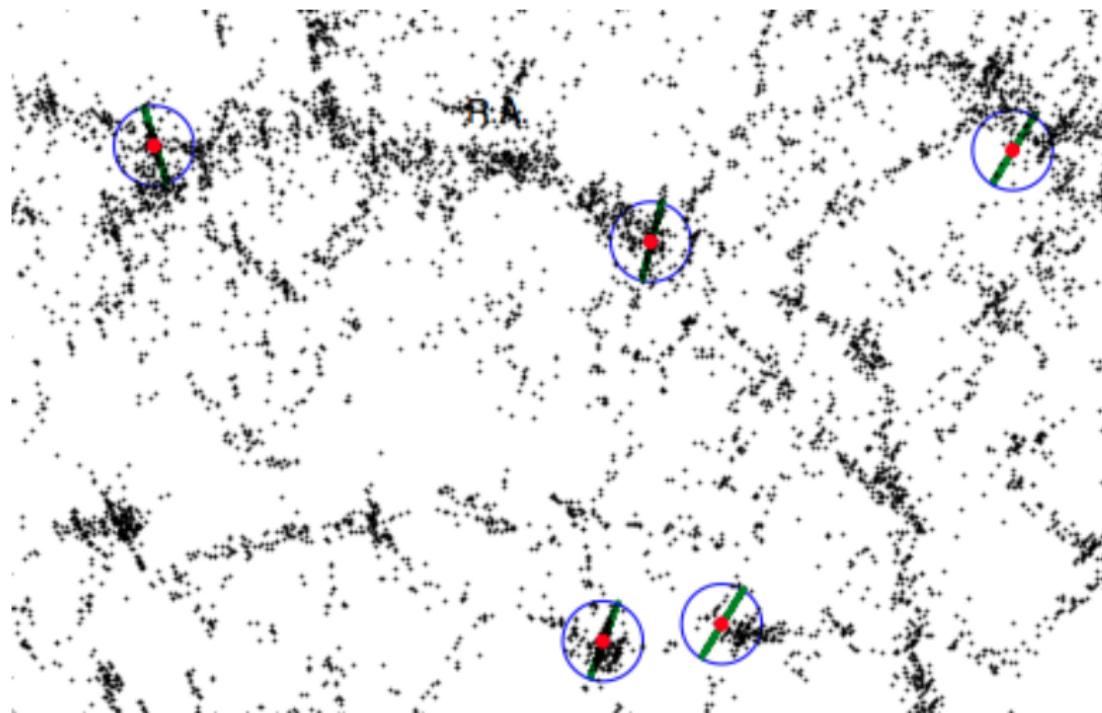
Cluster Geometry

Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions



Selecting SDSS Galaxies Around Clusters

Austen M.
Groener

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

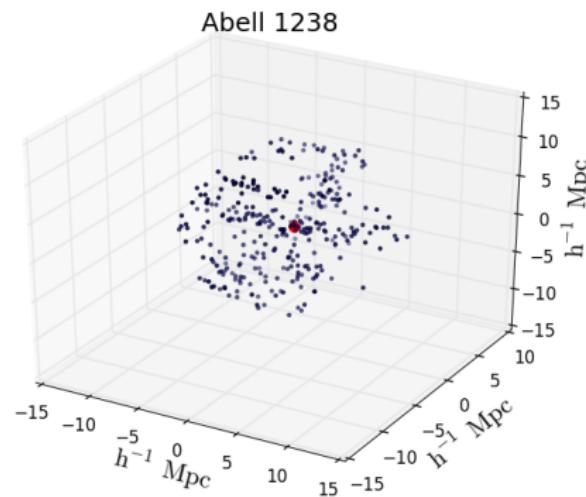
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



Cluster Concentration - LSS Orientation Correlation

Austen M.
Groener

Introduction

The Anatomy of a
ClusterThe Radial Density
Profile

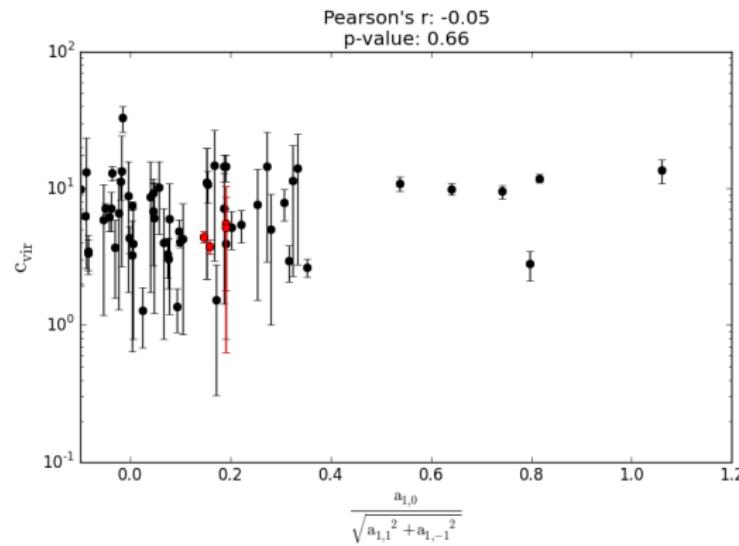
Cluster Geometry

Cluster Shape & Orientation

The Observed c-M Relation

Clusters and the LSS of the Universe

Conclusions



- No correlation between LSS orientation and mass and concentration.
- Techniques: WL (5), X-ray (33), CM (62), and LOSVD (34).

Future Work

- Explore alternate ways of quantifying the directionality of LSS around clusters.
- More data - particularly lensing measurements.
- Correct for redshift space distortions like Finger of God Effect, and the Kaiser Effect, which may alter the distribution of galaxies (e.g. - use cluster membership catalogs like maxBCG).

Conclusions

- Cluster halos are prolate spheroidal on small scales, and become spherical on larger scales.
- The changing of shape alters the 2D concentration on WL and SL scales differently.
- Low-mass clusters are affected by this difference the most.

Introduction

The Anatomy of a
Cluster

The Radial Density
Profile

Cluster Geometry

Cluster Shape
& Orientation

The Observed
c-M Relation

Clusters and the
LSS of the
Universe

Conclusions

-
- The c-M relation for clusters varies significantly from technique-to-technique.
 - WL and WL+SL are the steepest relations.
 - WL and WL+SL are inconsistent with theory, even after projection effects are taken into account. This likely points to selection effects as the cause.

-
- Cluster concentrations and masses show no correlation with the line-of-sight orientation of large scale structure (scales of $10 h^{-1} \text{Mpc}$).

Thank you!

- Advisor: Dr. David Goldberg
- Collaborator: Dr. Mauro Sereno
- Committee: Dr. Michael Vogeley, Dr. Gordon Richards, Dr. Luis Cruz, Dr. Andrew Hicks
- Research Group (Current and Past): Justin Bird and Markus Rexroth
- My Friends and Family
- This work was also supported by the NSF (Grant 0908307).



The Connection Between c_{vir} and M_{vir}

- Low-mass halos form halos earlier than massive ones
- The core density (concentration) of the halo reflects the density of the universe at the formation time
- Since the density of the universe decreases with time, low-mass halos tend to have higher concentrations

Shape and Density profiles are obtained for all clusters which meet our selection criteria.

Density Profiles

Iterative, Moment of Inertia Tensor

$$I_{ij} = \sum w_g(\zeta) m_p(r_{i,n} - \bar{r}_i)(r_{j,n} - \bar{r}_j)$$

Gaussian weighting function $w_g(\zeta)$, which matches shape and orientation at each step

Model Fitting

Using Maximum-Likelihood Methods, we fit the NFW profile to halo density profiles obtained through our analysis

$$\rho_{\text{NFW}}(r) = \frac{\delta c_{200} \rho_{\text{cr}}}{\frac{r}{r_s} \left(1 + \frac{r}{r_s}\right)^2}$$

Cluster Timescales

- Two-Body Relaxation:

$$t_{relax} = 2 \times 10^{10} \left(\frac{V_r}{1000 \text{ km/s}} \right) \left(\frac{M_g}{10^{12} M_\odot} \right)^{-2} \left(\frac{N_d}{1000 \text{ gal/Mpc}^3} \right)^{-1}$$

V_r is the radial component of the 3D velocity dispersion ($\approx 1000 \text{ km/s}$), M_g is the mass of the galaxy (or particle), and N_d is the number of galaxies (or particles) per Mpc^3 .

- Cooling Timescale:

$$\tau_{cool} = 9 \times 10^7 (T_8)^{1/2} (n_e)^{-1} \text{ years}$$

T_8 is the temperature in units of 10^8 K , and n_e is measured in particles per cm^{-3} (typically $n_e \leq 10^{-3}$).

- Dynamical Timescale:

$$\tau_{dyn} = 6 \times 10^{11} \left(\frac{R}{\text{Mpc}} \right) \left(\frac{V_r}{1000 \text{ km/s}} \right) \text{ years}$$

Modeling The Observed c-M Relations

Power-Law Model

- $c_{\text{vir}} = \frac{A}{1+z} \left(\frac{M_{\text{vir}}}{M_*} \right)^\alpha$
- Constant: M_*
- Free parameters: A, α

Linear Model

- $\mathcal{Y} = mX + b + \epsilon$
- $\mathcal{Y} \equiv \log c(1+z)$
- $X \equiv \log M$
- $m = \alpha$
- $b = \log A - \alpha \log M_*$
- $\epsilon \sim \mathcal{N}(0, \sigma_{\text{int}})$

Measurement Uncertainty

...and other considerations.

- Arbitrary propagation of uncertainty (assuming errors are not independent):

$$\delta q \leq \left| \frac{\partial q}{\partial x} \right| + \dots + \left| \frac{\partial q}{\partial z} \right|$$

This applies when we fit the c-M relation as a linear model (instead of the original power-law model). We also apply this for re-calculating the uncertainties for $c(1+z)$ (e.g. - $q = Bx; \delta q = |B|\delta x$).

- Best-fit values and confidence intervals to expectation values and standard deviations (D'Agostini 2004). Starting with $\theta_m^{\Delta_+}_{\Delta_-}$.

$$\sigma_\theta \approx \frac{\Delta_+ + \Delta_-}{2}$$

$$E[\theta] \approx \theta_m + O(\Delta_+ - \Delta_-)$$

Measurement Uncertainty

...and other considerations.

- Concentration Convention: Renormalize the concentration (and mass) based upon a different definition of r_{vir} (see procedure along with fitting formulae from Hu & Kravtsov 2002).
- Correct for cosmology: We develop our own cosmology correction. This turns out to be a rather small correction (of order a few percent), unless cosmology is extremely different from the assumed fiducial cosmology $\Omega_m = 0.3$, $\Omega_\Lambda = 0.7$.

Quantifying The Angular Distribution

Spherical Harmonics

- Series: $f(\theta, \phi) = \sum_{l=0}^{\infty} \sum_{m=0}^l A_l^m Y_l^m(\theta, \phi)$
- $A_l^m = \frac{4\pi}{N} \sum_{i=1}^{N_{\text{gal}}} \tilde{Y}_l^m(\theta_i, \phi_i)$

$$Y_1^1 = -\sqrt{\frac{3}{8\pi}} \sin \theta e^{i\phi}$$

$$Y_1^0 = \sqrt{\frac{3}{4\pi}} \cos \theta$$

$$Y_1^{-1} = \sqrt{\frac{3}{8\pi}} \sin \theta e^{-i\phi}$$

- Compute for each cluster: $\frac{A_1^0}{\sqrt{A_1^{02} + A_1^{02}}}$
- A_1^0 tells us about line-of-sight direction.