Gas HALE Model

```
#inPDF:skip

from numpy import pi
from gpkit import VectorVariable, Variable, Model, units
from gpkit.tools import te_exp_minus1
import gpkit
exec gpkit.mdmake("gas_hale_rebuild5.md")
import numpy as np
gpkit.settings['latex_modelname'] = False

class GasPoweredHALE(Model):
    def setup(self):
        constraints = []
```

Flight segment definitions

```
# define number of segments
NSeg = 9 # number of flight segments
NCruise = 2 # number of cruise segments
NClimb = 2 # number of climb segments
NLoiter = NSeg - NCruise - NClimb# number of loiter segments
iCruise = [1,-1] # cuise index
iLoiter = [3] # loiter index
for i in range(4,NSeg-1): iLoiter.append(i)
iClimb = [0,2] # climb index
```

Fuel weight model

- end of first segment weight + first segment fuel weight must be greater
- than MTOW. Each end of segment weight must be greater than the next
- of segment weight + the next segment fuel weight. The last end segment
- weight must be greater than the zero fuel weight

Steady level flight model

Climb model

Engine Model

```
W_eng = Variable('W_{eng}', 'lbf', 'Engine weight')
W_engtot = Variable('W_{eng-tot}', 'lbf', 'Installed engine weight')
W_engref = Variable('W_{eng-ref}', 4.4107, 'lbf', 'Reference engine weight')
P_shaftref = Variable('P_{shaft-ref}', 2.295, 'hp', 'reference shaft power')
```

Weight breakdown

Breguet Range

BSFC model

• BSFC data was taken from http://www.3w-international.com/Drone_Engines_Sale/engine-details-test-data/engine-data-3W-28i-HFE-FI.php

Aerodynamics model

Atmosphere model

• http://en.wikipedia.org/wiki/Density_of_air#Altitude

```
h = VectorVariable(NSeg, 'h', 'ft', 'Altitude')
gamma = Variable(r'\gamma',1.4,'-', 'Heat capacity ratio of air')
p_sl = Variable('p_{sl}', 101325, 'Pa', 'Pressure at sea level')
T_sl = Variable('T_{sl}', 288.15, 'K', 'Temperature at sea level')
L_atm = Variable('L_{atm}', 0.0065, 'K/m', 'Temperature lapse rate')
T_atm = VectorVariable(NSeg, 'T_{atm}', 'K', 'Air temperature')
a_atm = VectorVariable(NSeg, 'a_{atm}', 'm/s', 'Speed of sound at altitude')
R_spec = Variable('R_{spec}', 287.058, 'J/kg/K', 'Specific gas constant of air')
TH = (g/R_spec/L_atm).value.magnitude # dimensionless
```

```
constraints.extend([#h \le [20000, 20000] * units.m, # Model valid to top of T_sl >= T_atm + L_atm*h, # Temp decreases w/ altitude rho == p_sl*T_atm**(TH-1)/R_spec/(T_sl**TH)])
```

altitude constraints

wind speed model

```
V_wind = VectorVariable(NLoiter, 'V_{wind}', [20,25,30,10,15], 'm/s', 'wind speed')
constraints.extend([V[iLoiter] >= V_wind])
```

Conclusion

```
objective = 1/t_station
    return objective, constraints

if __name__ == '__main__':
    M = GasPoweredHALE()
    M.solve()
```

Solution

```
#inPDF: replace with sol.generate.tex
with open("sol.generated.tex", "w") as f:
    f.write(M.solution.table(latex=True))
```