Michael Burton

March 17, 2016

Assumptions

- 1. Fixed Engine Weight $W_{eng-tot} \leftarrow 6$ lbf $P_{shaft-maxMSL} \leftarrow 2.189$ kW. Also assuming that engine performance is affected by altitude and RPM. This BSFC model is technically fit for a single propellor. We are assuming that the the variance in BSFC curves in the family of propellers is small.
- 2. Fixed propller 18x8
- 3. Fixed range to station $R \leftarrow 200$ nmi
- 4. Fixed payload $W_{pay} \leftarrow 10$ lbf $Vol_{pay} \leftarrow 0.5$ ft³
- 5. Fixed altitude at cruise $h_{cruise} \leftarrow 5000 \text{ ft}$
- 6. Fixed altitude at station $h_{station} \leftarrow 1.5 \times 10^4 \text{ ft}$
- 7. Fixed avonics $Vol_{avionics} \leftarrow 0.125 \text{ ft}^3 \ W_{avionics} \leftarrow 8 \text{ lbf}$
- 8. Fixed climb rate $h_{dot} \leftarrow 125 \frac{\text{ft}}{\text{min}}$
- 9. Fixed time to get on station $t_{cruise} \leq 1$ day
- 10. Constant wind speed during loiter $V_{wind} \leftarrow 25 \text{ m/s}$
- 11. Fuselage fineness ratio $fr \leftarrow 3.5$
- 12. Power during climb/cuise $P_{avn} \leftarrow 40$ watts
- 13. Power during loiter $P_{avn} \leftarrow 50$ watts

Performance Curves

The following curves are performance curves. They assume that the weight of the aircraft is fixed. All of the above assumptions hold.

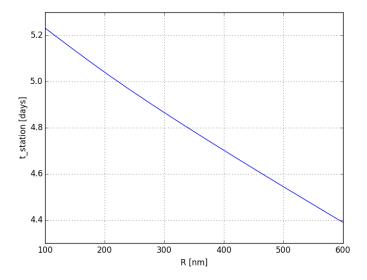


Figure 1: Time on station vs R. Assumes fixed weight of MTOW = 87 [lbf].

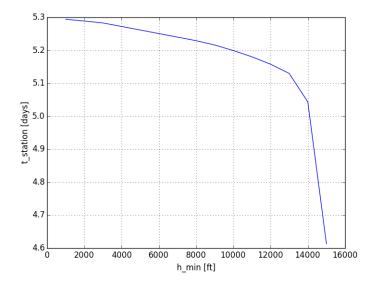


Figure 2: Time on station vs cruise altitude. Assumes fixed weight of MTOW=87 [lbf].

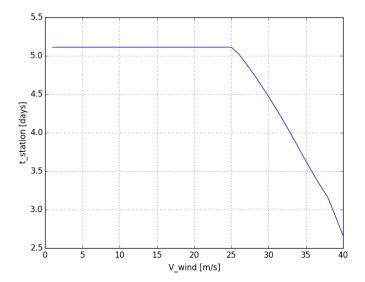


Figure 3: Time on station vs wind velocity. Assumes fixed weight of MTOW = 87 [lbf].

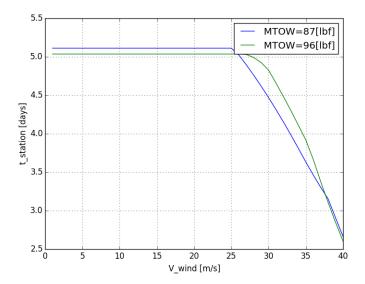


Figure 4: Time on station vs wind velocity.

Solution

```
Cost
----
83.13 [lbf]
```

```
AR : 27.87
                                                                                        Aspect ratio
               A_{capcent} : 9.979e-05
                                                                    [m**2]
                                                                                        Cap area at center
                 C_{D-fuse}: 0.003734
                                                                                        fueslage drag
                 C_{f-fuse}: 0.006756
                                                                                       Fuselage skin friction coefficient
                                   F : 1633
                                                                    [N]
                                                                                       Load on wings
                         LoverA : 5.225
                                                                    [lbf/ft**2] Wing loading
                             MTOW: 83.13
                                                                    [lbf]
                                                                                       max take off weight
                         M_cent : 1310
                                                                    [N*m]
                                                                                        Center bending moment
                       P_{cap}: 4.74e+04
                                                                                        Cap load
                                                                    [N]
                                   S: 15.91
                                                                    [ft**2]
                                                                                        wing area
                                                                    [ft**2]
                     S_{\text{fuse}} : 7.994
                                                                                        Fuselage surface area
                   Vol_{cap}: 0.0002135
                                                                    [m**3]
                                                                                        Cap volume
                 Vol_{fuel} : 0.02653
                                                                    [m**3]
                                                                                        Fuel Volume
                 Vol_{fuse} : 0.04423
                                                                    [m**3]
                                                                                        fuselage volume
                     W_{cent} : 73.41
                                                                    [lbf]
                                                                                        Center aircraft weight
             W_{\text{fuel-tot}}: 42.13
                                                                    [lbf]
                                                                                        total fuel weight
                     W_{\text{fuse}} : 4.284
                                                                    [lbf]
                                                                                        fuselage weight
                     W_{\text{wing}} : 7.514
                                                                    [lbf]
                                                                                        Total wing structural weight
                       W_{zfw} : 41
                                                                    [lbf]
                                                                                        Zero fuel weight
             \delta_{tip} : 4.211
                                                                                        Tip deflection
                                                                    [ft]
                   \rho_{sl} : 1.225
                                                                    [kg/m**3]
                                                                                       density at sea level
                                   b: 21.06
                                                                    [ft]
                                                                                        Span
                                   c: 0.7556
                                                                    ſftl
                                                                                        Wing chord
                     h_{spar}: 0.02764
                                                                    [m]
                                                                                        Spar height
                     1_{cent}: 2.675
                                                                    [ft]
                                                                                        center fuselage length
                     1_{fuse} : 3.316
                                                                    [ft]
                                                                                        fuselage length
                       m_{cap} : 0.3757
                                                                    [kg]
                                                                                        Cap mass
                     m_{\text{fuse}} : 0.7427
                                                                    [kg]
                                                                                        fuselage mass
                     m_{skin} : 2.956
                                                                    [kg]
                                                                                        Skin mass
                       w_{cap} : 5.524
                                                                    [in]
                                                                                        Spar cap width
                     w_{cent} : 0.7642
                                                                    [ft]
                                                                                        center fuselage width
                  \sqrt{BSFC}: [ 0.507
                                                                   0.681
                                                                                        0.507
                                                                                                            0.649
                                                                                                                              ...]
                                                                                                                                            [lb/hp/hr] brake specific fu
                   \sqrt{C_D} : [ 0.0304
                                                                   0.0131
                                                                                        0.0299
                                                                                                            0.0274
                                                                                                                              ...]
                                                                                                                                                        Drag coefficient
                   \sqrt{C_L} : [1.08]
                                                                                        1.06
                                                                                                            0.991
                                                                   0.498
                                                                                                                              ...]
                                                                                                                                                        Lift coefficient
         \sqrt{L_factor}: [ 0.188
                                                                                        0.518
                                                                                                                              ...]
                                                                                                                                                        Max shaft power loss fa
                                                                   0.189
                                                                                                            0.518
\sqrt{P_{shaft-max}}: [ 2.38
                                                                   2.37
                                                                                        1.41
                                                                                                            1.41
                                                                                                                               ...]
                                                                                                                                            [hp]
                                                                                                                                                                Max shaft power at
       \sqrt{P_{shaft}} : [2.38]
                                                                   0.66
                                                                                        1.41
                                                                                                            0.448
                                                                                                                              ...]
                                                                                                                                            [hp]
                                                                                                                                                                Shaft power
                    \sqrt{RPM} : [ 8.44e+03
                                                                   5.82e+03
                                                                                       8.44e+03 6.1e+03
                                                                                                                              ...]
                                                                                                                                            [rpm]
                                                                                                                                                                Engine operating RF
       \sqrt{Re_{fuse}} : [ 1.49e+06
                                                                   2.18e+06
                                                                                      1.24e+06
                                                                                                           1.24e+06 ... ]
                                                                                                                                                        fuselage Reynolds number
                     \sqrt{Re} : [ 3.38e+05
                                                                   4.97e+05
                                                                                       2.83e+05
                                                                                                         2.83e+05 ... ]
                                                                                                                                                        Reynolds number
                       \sqrt{T} : [ 9.54
                                                                                        4.74
                                                                                                                             ...]
                                                                                                                                                                Thrust
                                                                   2.16
                                                                                                                                            [lbf]
                                                                                                                      ...] [m/s]
                       \vec{V} : [20.9]
                                                                   30.7
                                                                                        25
                                                                                                        25
                                                                                                                                                        cruise speed
           \ensuremath{\mbox{vec}\{\ensuremath{\mbox{W}_{=}}\}} : [82.8]
                                                                                                                                            [lbf]
                                                                   81.4
                                                                                       80.6
                                                                                                           71.6
                                                                                                                              ...]
                                                                                                                                                                segment-end weight
          \c {W_{fuel}} : [ 0.288]
                                                                                                        9.06
                                                                                                                                      [lbf]
                                                                   1.4
                                                                                   0.83
                                                                                                                          ...]
                                                                                                                                                            segment-fuel weight
    \ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath{\ensuremath}\amb}\amb}\amb}}}}}}}}}}}}}}
                                                               0.6
                                                                                               0.7
                                                                                                                                            propulsive efficiency
                                                                                                                  ...]
                  \vec{\rho} : [ 1.05
                                                                    1.05
                                                                                        0.738
                                                                                                            0.738
                                                                                                                              ...]
                                                                                                                                            [kg/m**3]
                                                                                                                                                                    air density
             \sqrt{c_{dp}} : [ 0.0117
                                                                   0.00622
                                                                                        0.012
                                                                                                            0.0112
                                                                                                                              ...]
                                                                                                                                                        wing profile drag coeff
```

```
\sqrt{h} : [5e+03]
                                   5e+03
                                             1.5e+04
                                                       1.5e+04 ...] [ft]
                                                                                  altitude
                                                                                   time per flight seg
            \sqrt{t} : [0.00973]
                                   0.126
                                             0.047
                                                        1.2
                                                                 ...]
                                                                        [day]
      \sqrt{z_{bre}} : [ 0.0034
                                   0.0167
                                             0.01
                                                       0.117
                                                                 ...]
                                                                              breguet coefficient
Constants
_____
        BSFC_{min} : 0.32
                                   [kg/hr/kWMinimum BSFC
         C_{L-max}: 1.5
                                             Maximum lift coefficient
           E_{cap} : 2e+07
                                   [pound_force_per_square_inch] Youngs modulus of CF cap
       FuelOilFrac : 0.98
                                             Fuel-oil fraction
          K_{\text{fuse}} : 1.1
                                             Fuselage form factor
           N_{\max} : 5
                                             Load factor
  P_{shaft-maxMSL} : 2.93
                                   [hp]
                                             Max shaft power at MSL
                 R: 200
                                   [nmi]
                                             range to station
         RPM_{max}: 9000
                                   [rpm]
                                             Maximum RPM
        R_{cruise} : 180
                                   [nmi]
                                             range to station during climb
          Re_{ref}: 3e+05
                                             Reference Re for cdp
          V_{\text{wind}}: 25
                                   [m/s]
                                             wind speed
    Vol_{avionics} : 0.125
                                   [ft**3]
                                             Avionics volume
         Vol_{pay} : 0.5
                                   [ft**3]
                                             Payload volume
      W_{avionics} : 8
                                   [lbf]
                                             Avionics weight
       W_{eng-tot}: 6
                                   [lbf]
                                             Installed engine weight
           W_{pay}: 10
                                   [lbf]
                                             Payload weight
                                             skid weight
          W_{skid}: 3
                                   [lbf]
  \delta_{tip-max} : 0.2
                                             max tip deflection ratio
 \eta_{prop-climb} : 0.5
                                             propulsive efficiency in climb
\eta_{prop-cruise} : 0.6
                                             propulsive efficiency in cruise
\eta_{prop-loiter} : 0.7
                                             propulsive efficiency in loiter
               \mu : 1.5e-05
                                   [N*s/m**2] Dynamic viscosity
        \rho_{cap} : 1.76
                                   [g/cm**3] Density of CF cap
       \rho_{fuel} : 6.01
                                   [lbf/liquid_gallon]
                                                            density of 100LL
       \rho_{skin} : 0.1
                                   [g/cm**2] Wing Skin Density
      \sigma_{cap} : 4.75e+08
                                   [Pa]
                                             Cap stress
              \tau : 0.12
                                             Airfoil thickness ratio
                 e : 0.9
                                             Spanwise efficiency
                fr: 3.5
                                             fineness ratio fuselage
                 g: 9.81
                                   [m/s**2]
                                             Gravitational acceleration
           h_{\min} : 5000
                                   ſftl
                                             minimum cruise altitude
       h_{station}: 1.5e+04
                                   [ft]
                                             minimum altitude at station
        k-\{2-fuse\} : 5.938
                                             fuselage form factor 2
        k_{1-fuse}: 2.858
                                             fuselage form factor 1
           m_{\text{rib}}: 1.2
                                   [kg]
                                             rib mass
          m_{tail} : 1
                                             tail mass
                                   [kg]
           t_{cap} : 0.028
                                   [in]
                                             Spar cap thickness
t_{cruise} : 1
                           [day]
                                     time to station
       t_{station} : 6
                                             time on station
                                   [day]
```

 $\sqrt{h_{dot}} : [357]$

148

]

[ft/min]

Climb rate