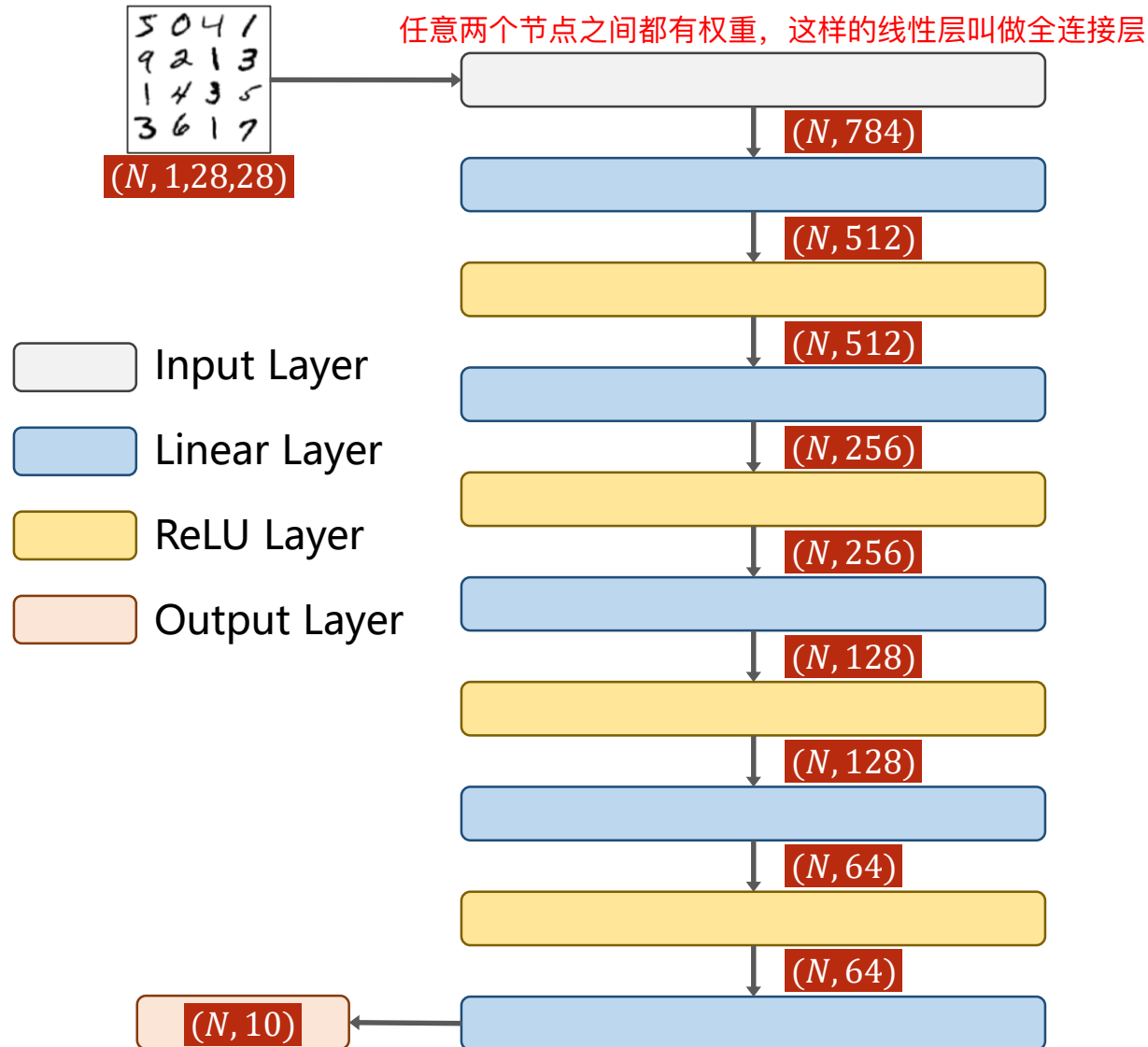




PyTorch Tutorial

10. Basic CNN

Revision: Fully Connected Neural Network



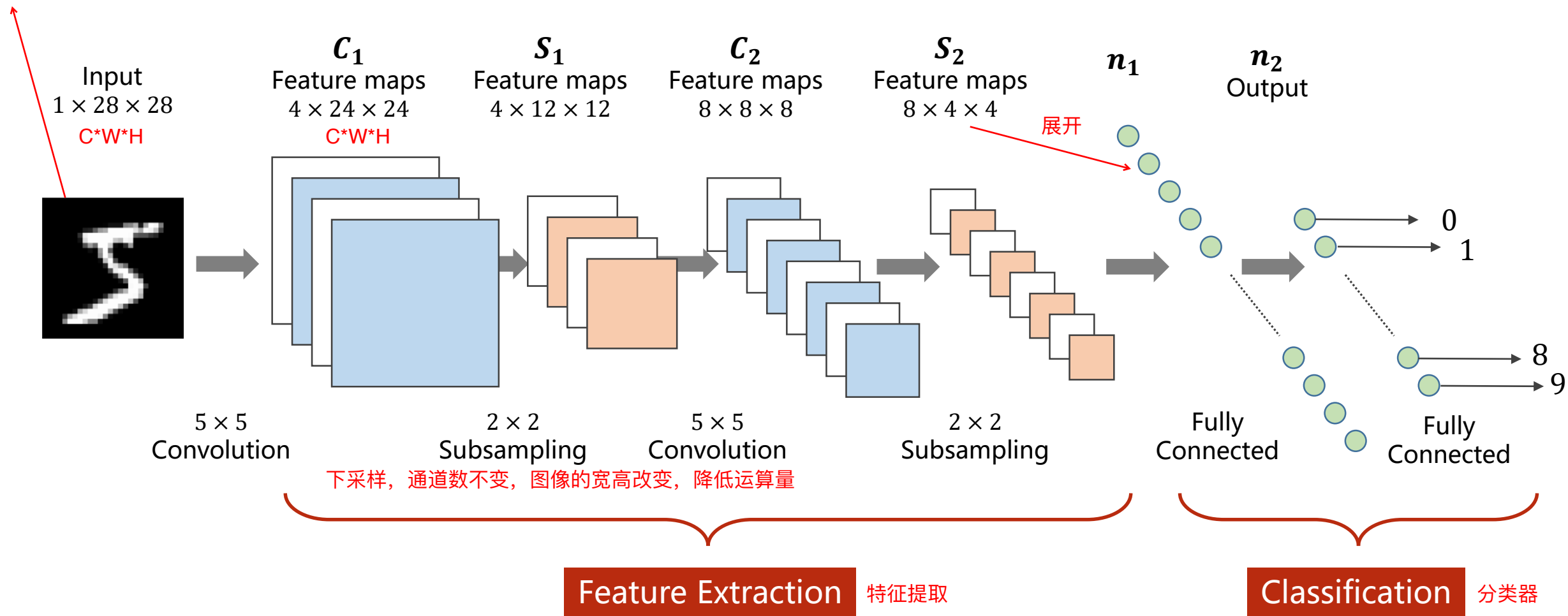
```
class Net(torch.nn.Module):
    def __init__(self):
        super(Net, self).__init__()
        self.l1 = torch.nn.Linear(784, 512)
        self.l2 = torch.nn.Linear(512, 256)
        self.l3 = torch.nn.Linear(256, 128)
        self.l4 = torch.nn.Linear(128, 64)
        self.l5 = torch.nn.Linear(64, 10)

    def forward(self, x):
        x = x.view(-1, 784)
        x = F.relu(self.l1(x))
        x = F.relu(self.l2(x))
        x = F.relu(self.l3(x))
        x = F.relu(self.l4(x))
        return self.l5(x)

model = Net()
```

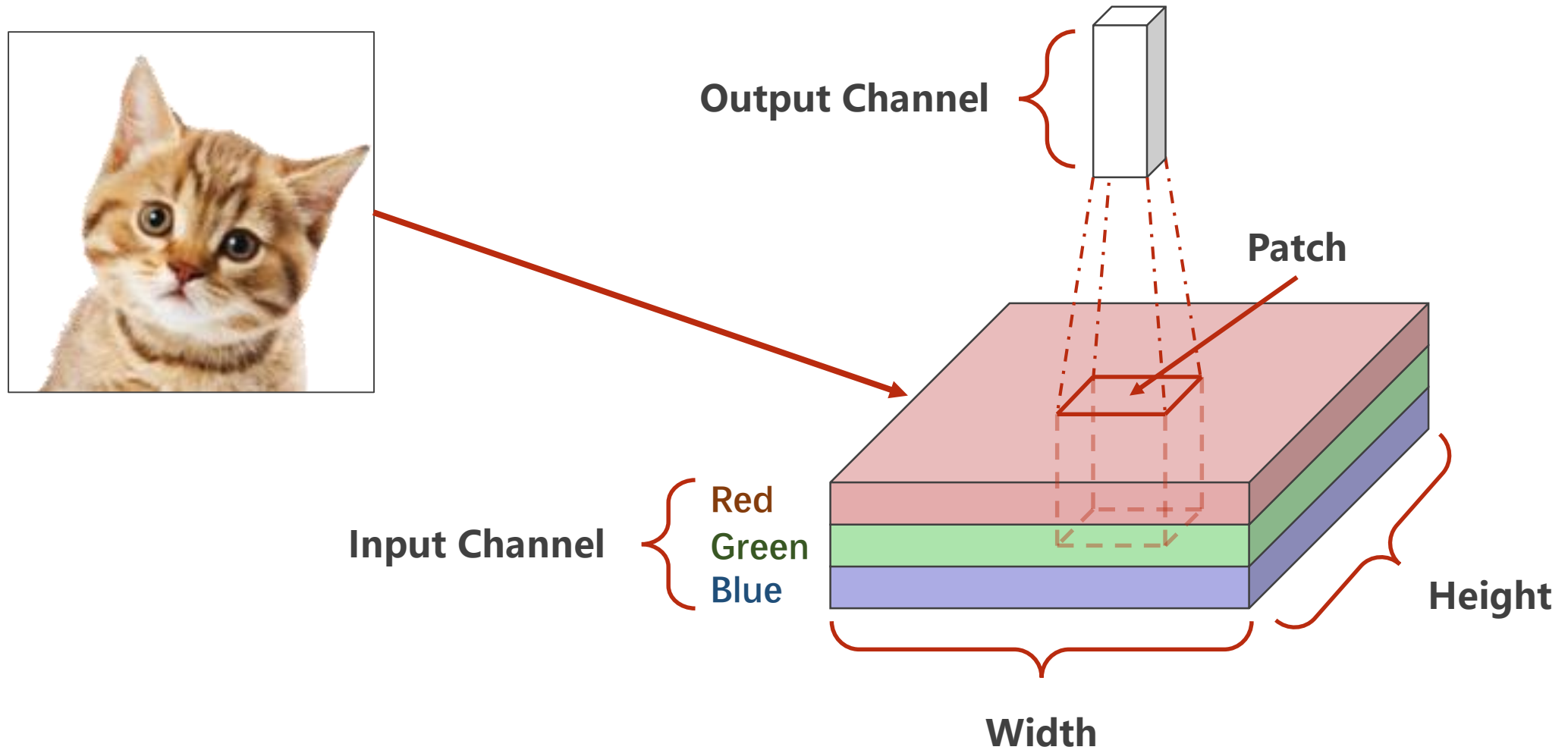
Convolutional Neural Network

之前用全连接做预测时，将图像所有像素直接变为一维向量，这个过程会丧失部分像素之间的位置关联。

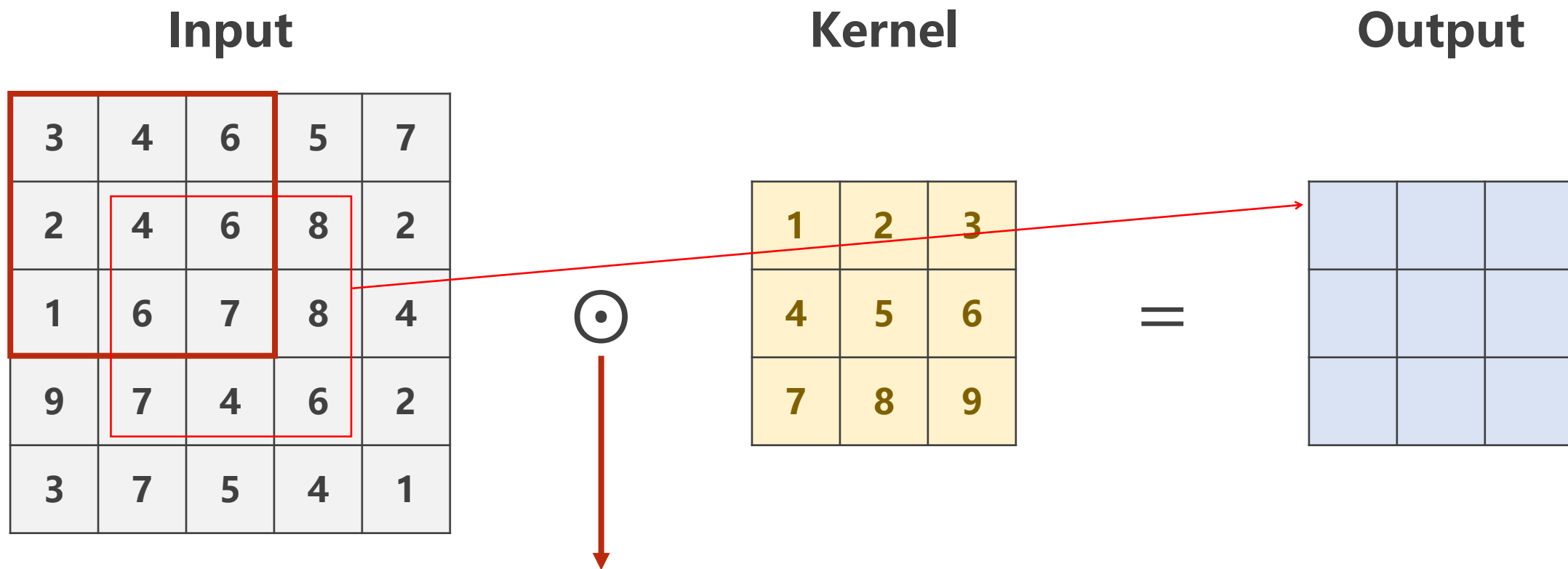


不断进行大小和维度的变化，直到成为一个1维的向量

Convolution



Convolution – Single Input Channel



$$3 \cdot 1 + 4 \cdot 2 + 6 \cdot 3 + 2 \cdot 4 + 4 \cdot 5 + 6 \cdot 6 + 1 \cdot 7 + 6 \cdot 8 + 7 \cdot 9 =$$
$$3 + 8 + 18 + 8 + 20 + 36 + 7 + 48 + 63 = \mathbf{211}$$

Convolution – Single Input Channel

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1

Kernel

1	2	3
4	5	6
7	8	9

Output

211		



=

$$3 \cdot 1 + 4 \cdot 2 + 6 \cdot 3 + 2 \cdot 4 + 4 \cdot 5 + 6 \cdot 6 + 1 \cdot 7 + 6 \cdot 8 + 7 \cdot 9 =$$
$$3 + 8 + 18 + 8 + 20 + 36 + 7 + 48 + 63 = \mathbf{211}$$

Convolution – Single Input Channel

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1

Kernel

1	2	3
4	5	6
7	8	9

Output

211		



$$4 \cdot 1 + 6 \cdot 2 + 5 \cdot 3 + 4 \cdot 4 + 6 \cdot 5 + 8 \cdot 6 + 6 \cdot 7 + 7 \cdot 8 + 8 \cdot 9 =$$
$$4 + 12 + 15 + 16 + 30 + 48 + 42 + 56 + 72 = \mathbf{295}$$

Convolution – Single Input Channel

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1

Kernel

1	2	3
4	5	6
7	8	9

Output

211	295	



=

$$4 \cdot 1 + 6 \cdot 2 + 5 \cdot 3 + 4 \cdot 4 + 6 \cdot 5 + 8 \cdot 6 + 6 \cdot 7 + 7 \cdot 8 + 8 \cdot 9 =$$
$$4 + 12 + 15 + 16 + 30 + 48 + 42 + 56 + 72 = \mathbf{295}$$

Convolution – Single Input Channel

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	295	262

Convolution – Single Input Channel

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	295	262
259		

Convolution – Single Input Channel

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	295	262
259	282	

Convolution – Single Input Channel

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	295	262
259	282	214

Convolution – Single Input Channel

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	295	262
259	282	214
251		

Convolution – Single Input Channel

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	295	262
259	282	214
251	253	

Convolution – Single Input Channel

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	295	262
259	282	214
251	253	169

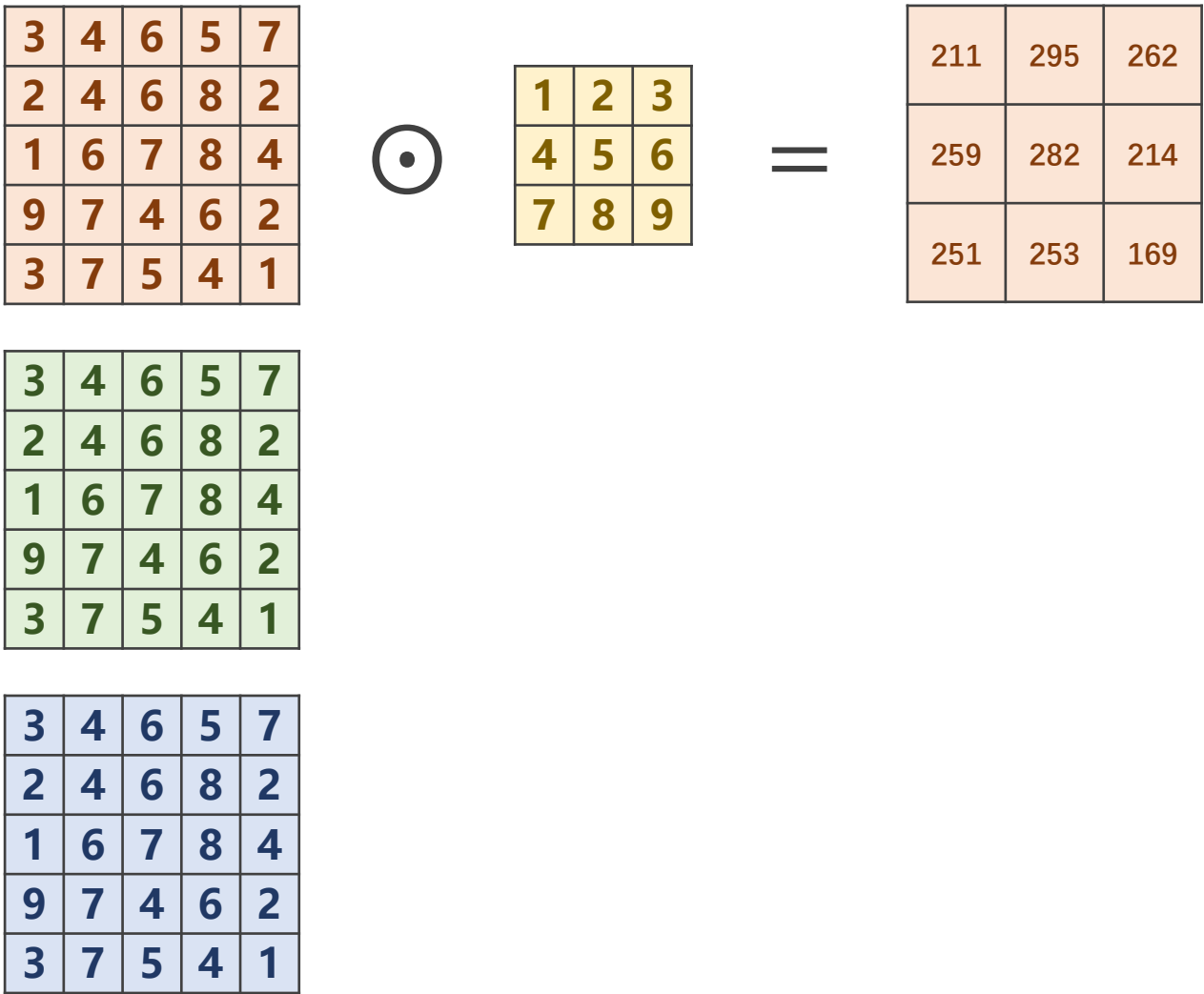
Convolution – 3 Input Channels

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1

Convolution – 3 Input Channels



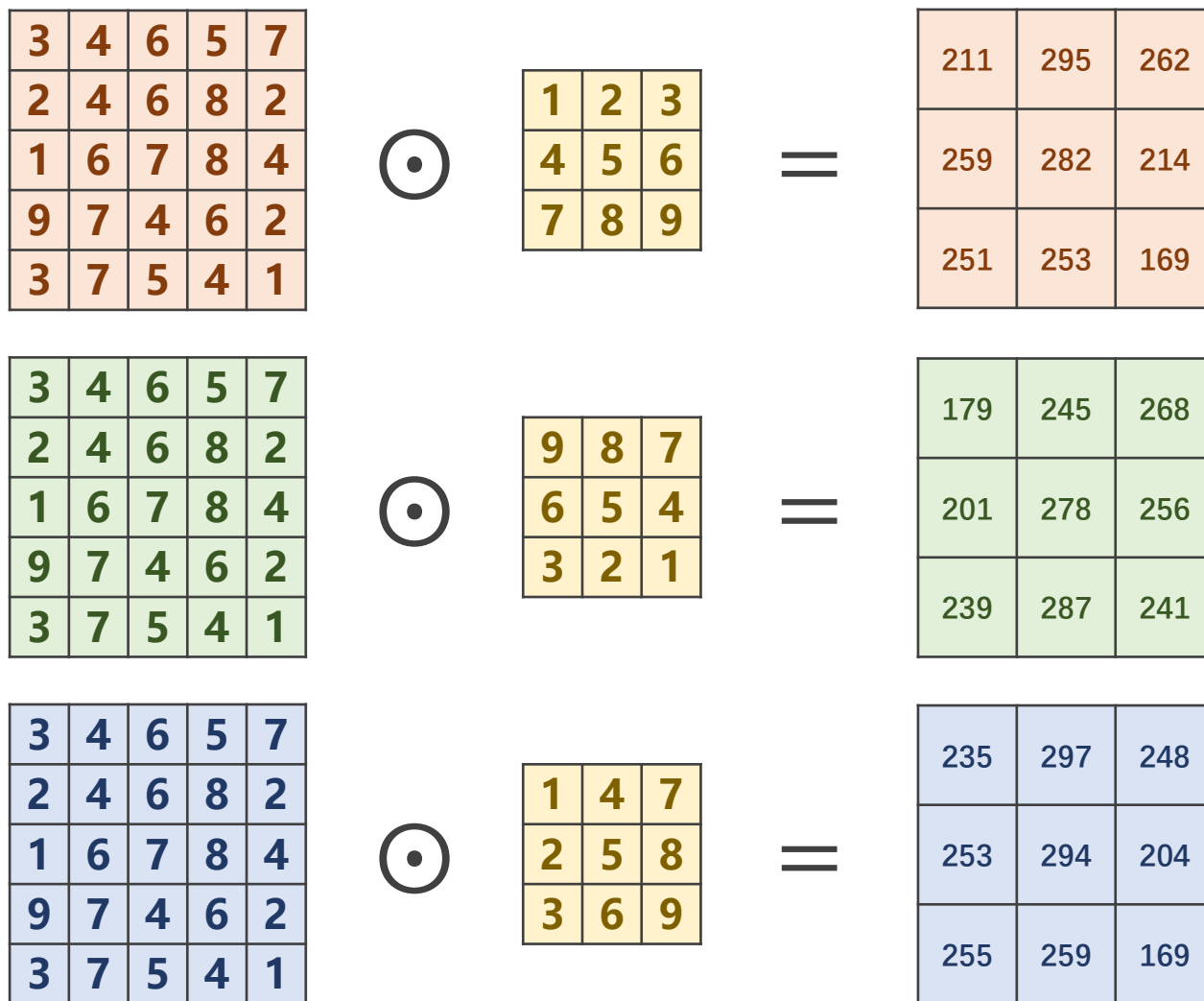
Convolution – 3 Input Channels

3	4	6	5	7	\odot	1	2	3	=	211	295	262
2	4	6	8	2		4	5	6		259	282	214
1	6	7	8	4		7	8	9		251	253	169
9	7	4	6	2								
3	7	5	4	1								

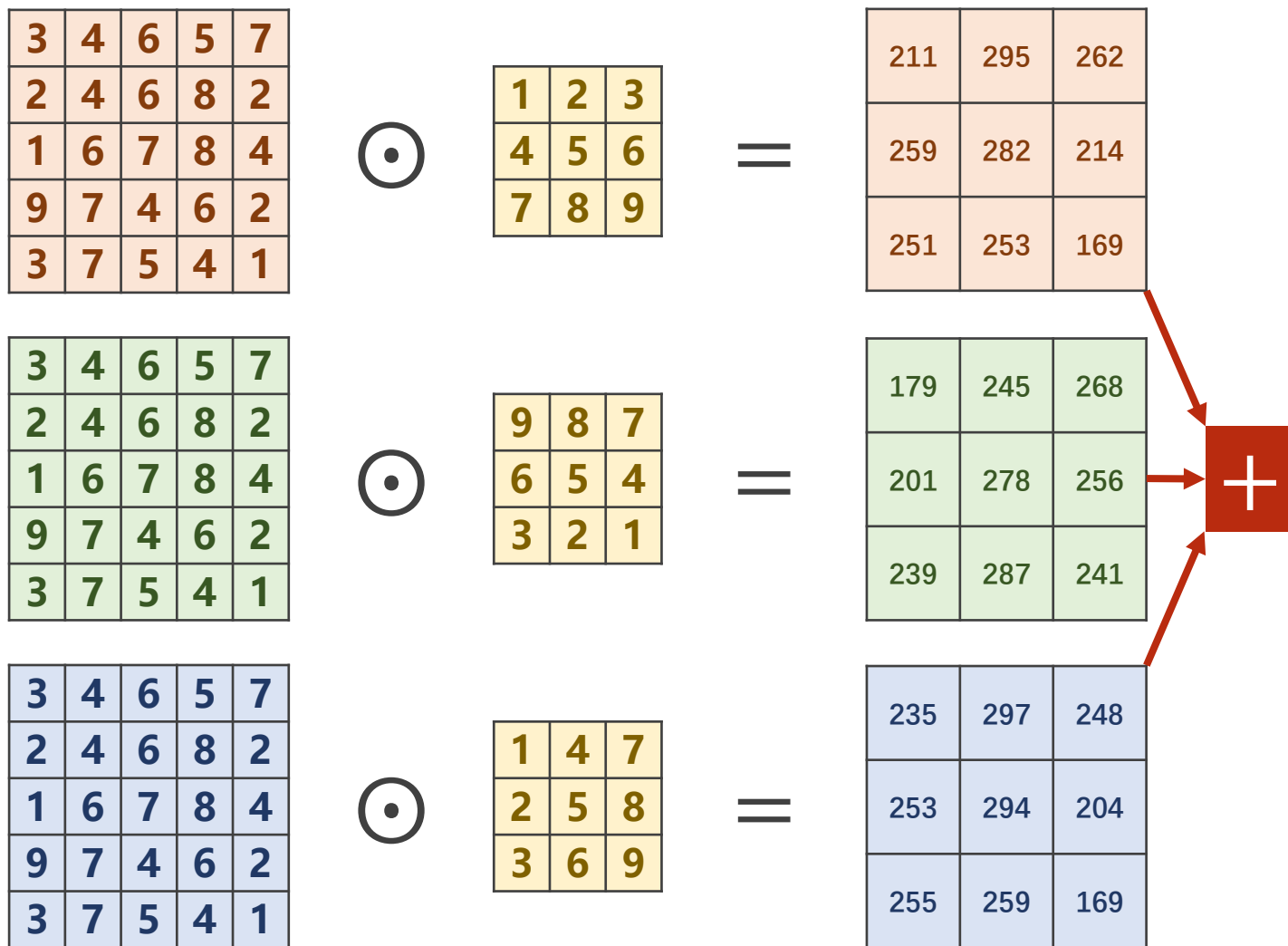
3	4	6	5	7	\odot	9	8	7	=	179	245	268
2	4	6	8	2		6	5	4		201	278	256
1	6	7	8	4		3	2	1		239	287	241
9	7	4	6	2								
3	7	5	4	1								

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1

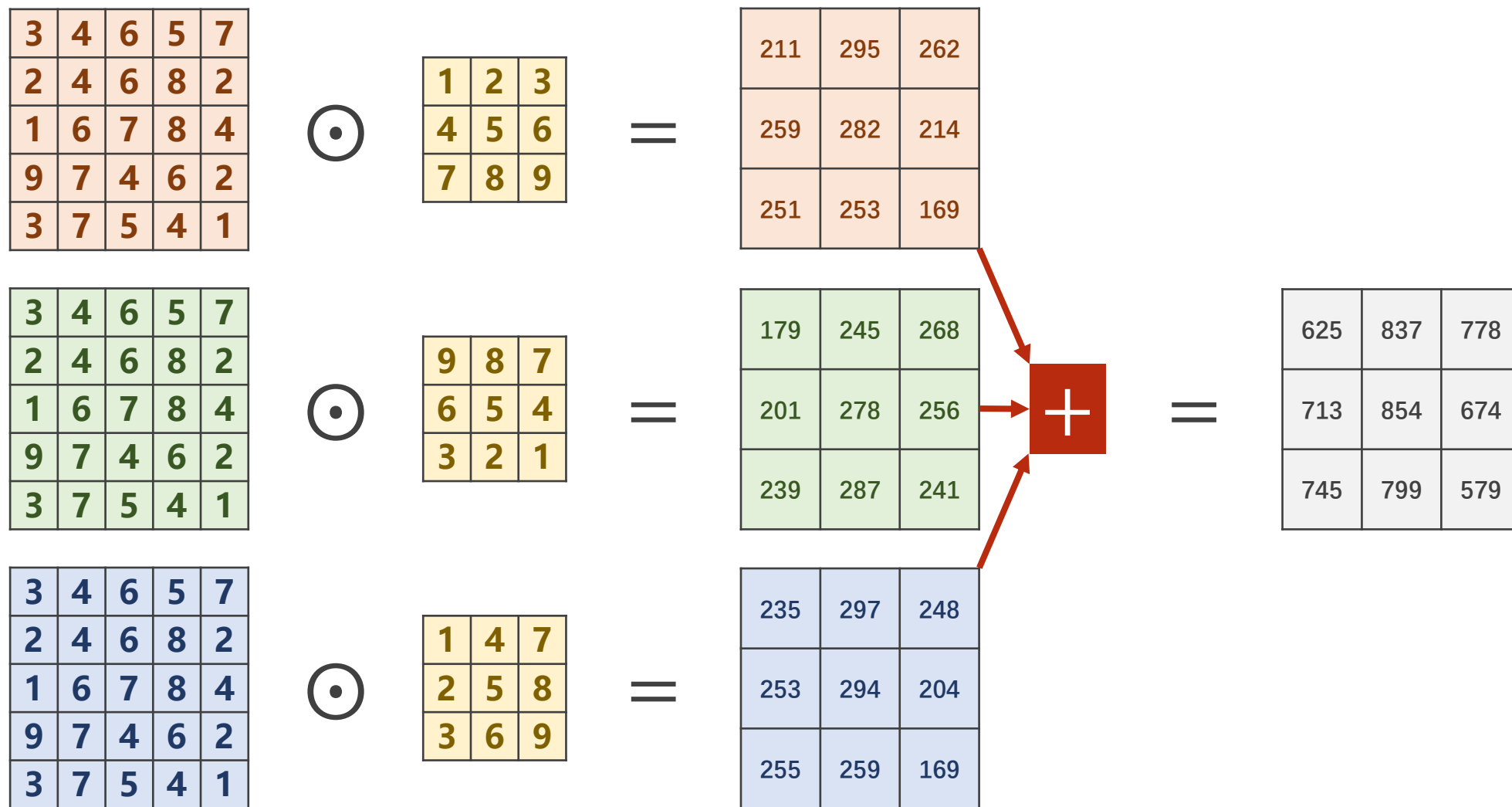
Convolution – 3 Input Channels



Convolution – 3 Input Channels



Convolution – 3 Input Channels



Convolution – 3 Input Channels

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



1	2	3
4	5	6
7	8	9

=

211	295	262
259	282	214
251	253	169



9	8	7
6	5	4
3	2	1

=

179	245	268
201	278	256
239	287	241



1	4	7
2	5	8
3	6	9

=

235	297	248
253	294	204
255	259	169

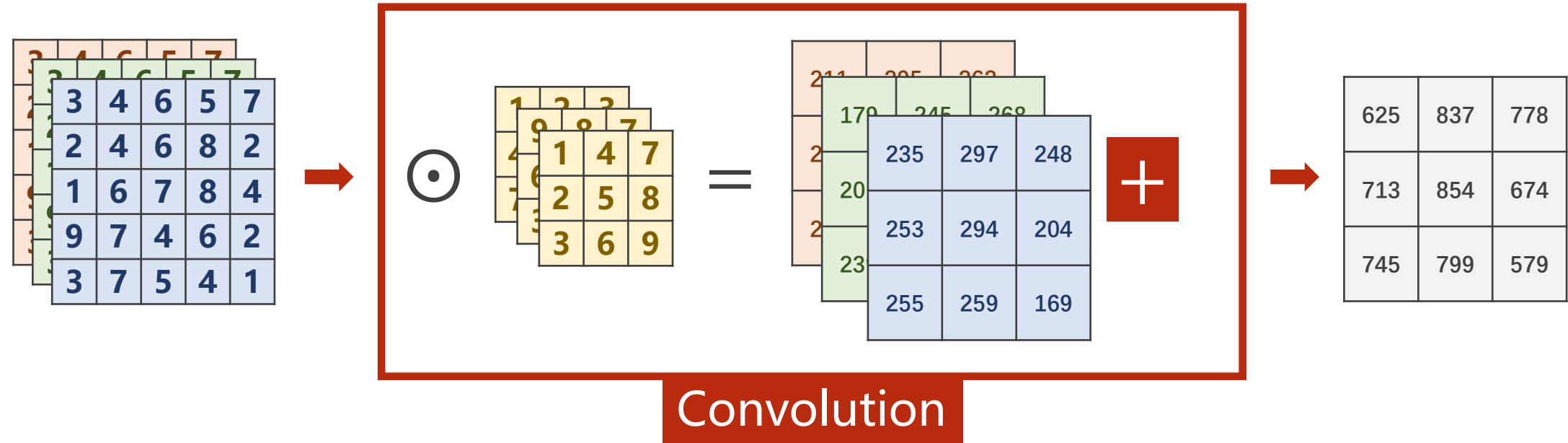


=

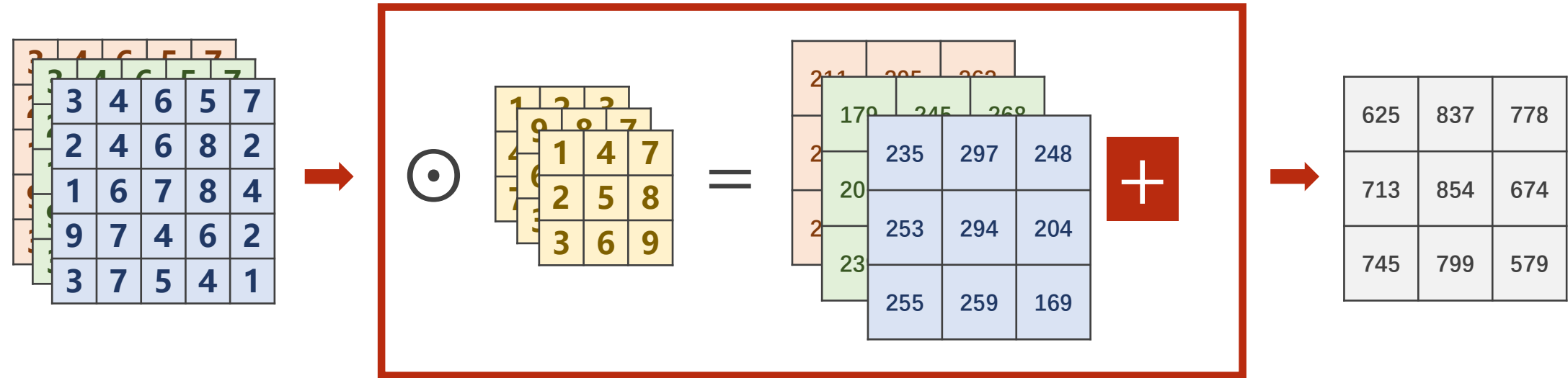
Convolution

625	837	778
713	854	674
745	799	579

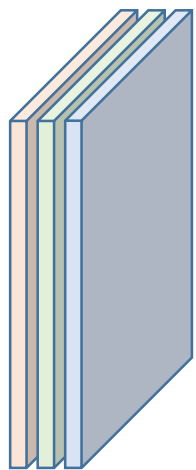
Convolution – 3 Input Channels



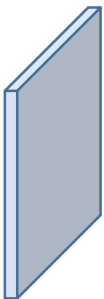
Convolution – 3 Input Channels



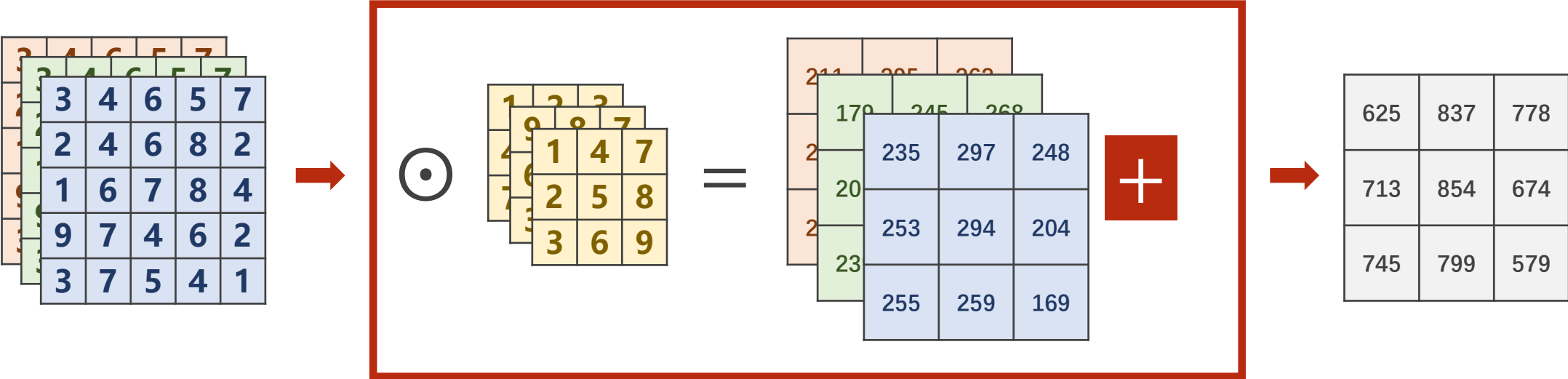
Convolution



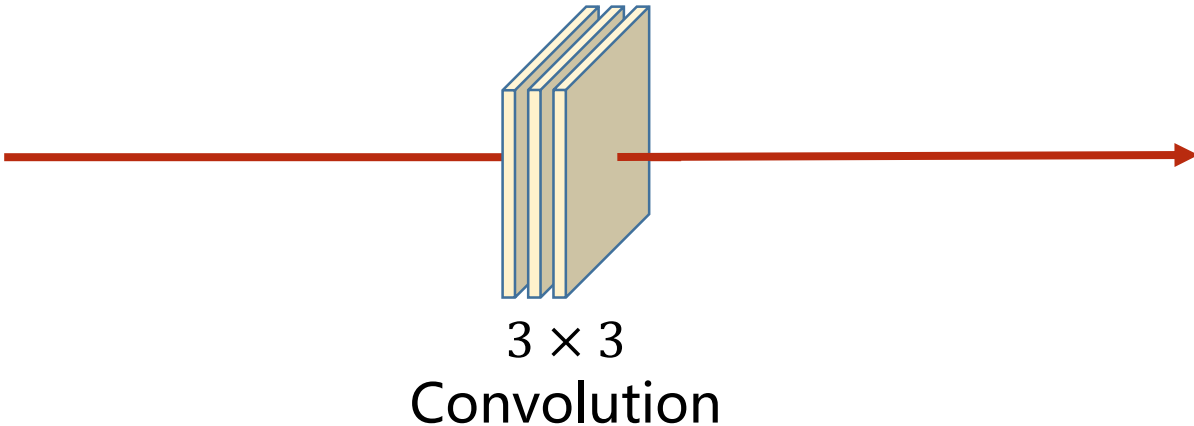
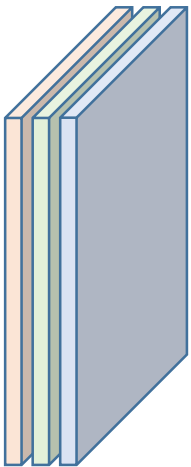
3×3
Convolution



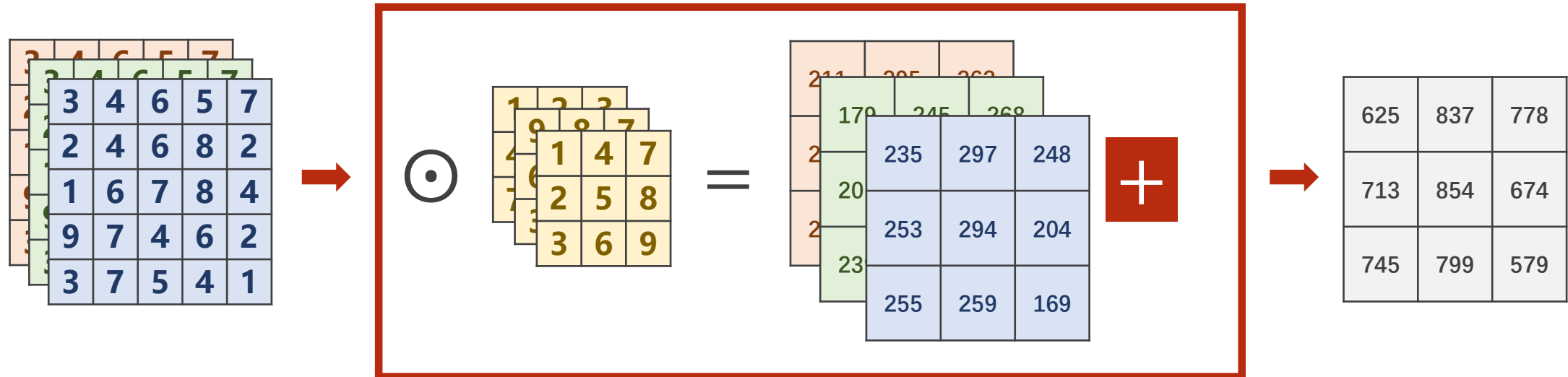
Convolution – 3 Input Channels



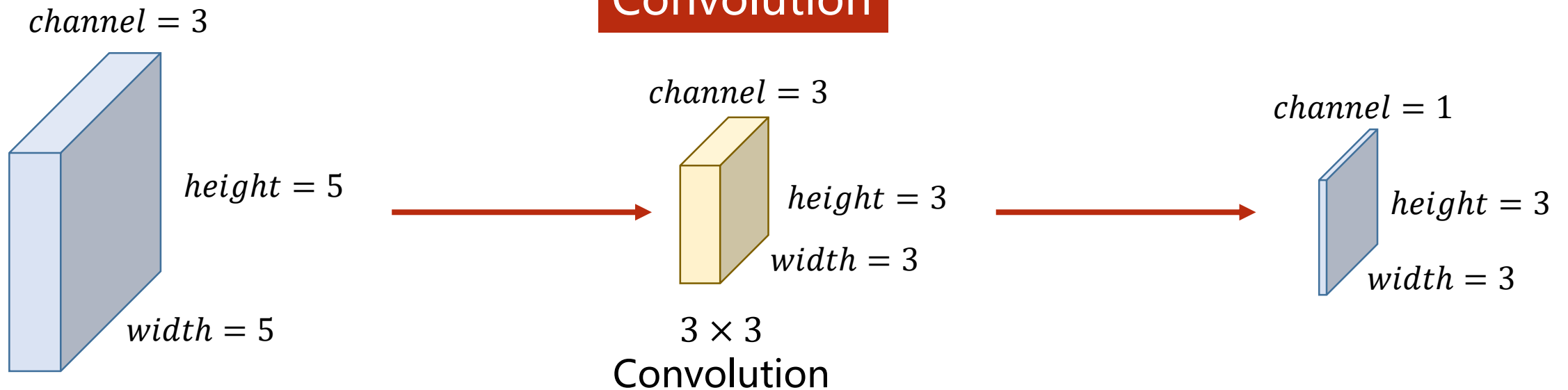
Convolution



Convolution – 3 Input Channels

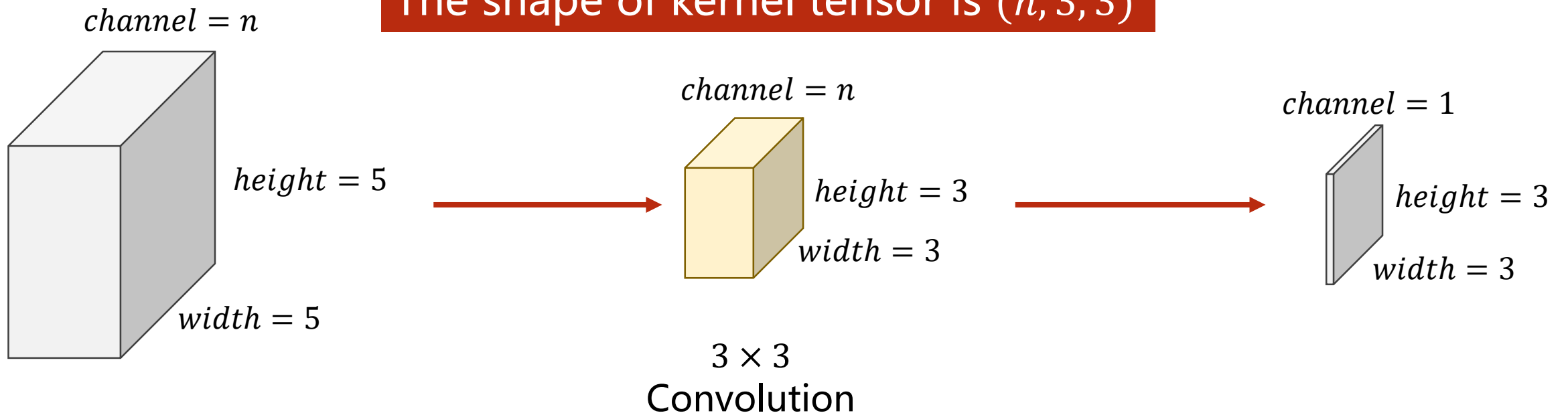


Convolution

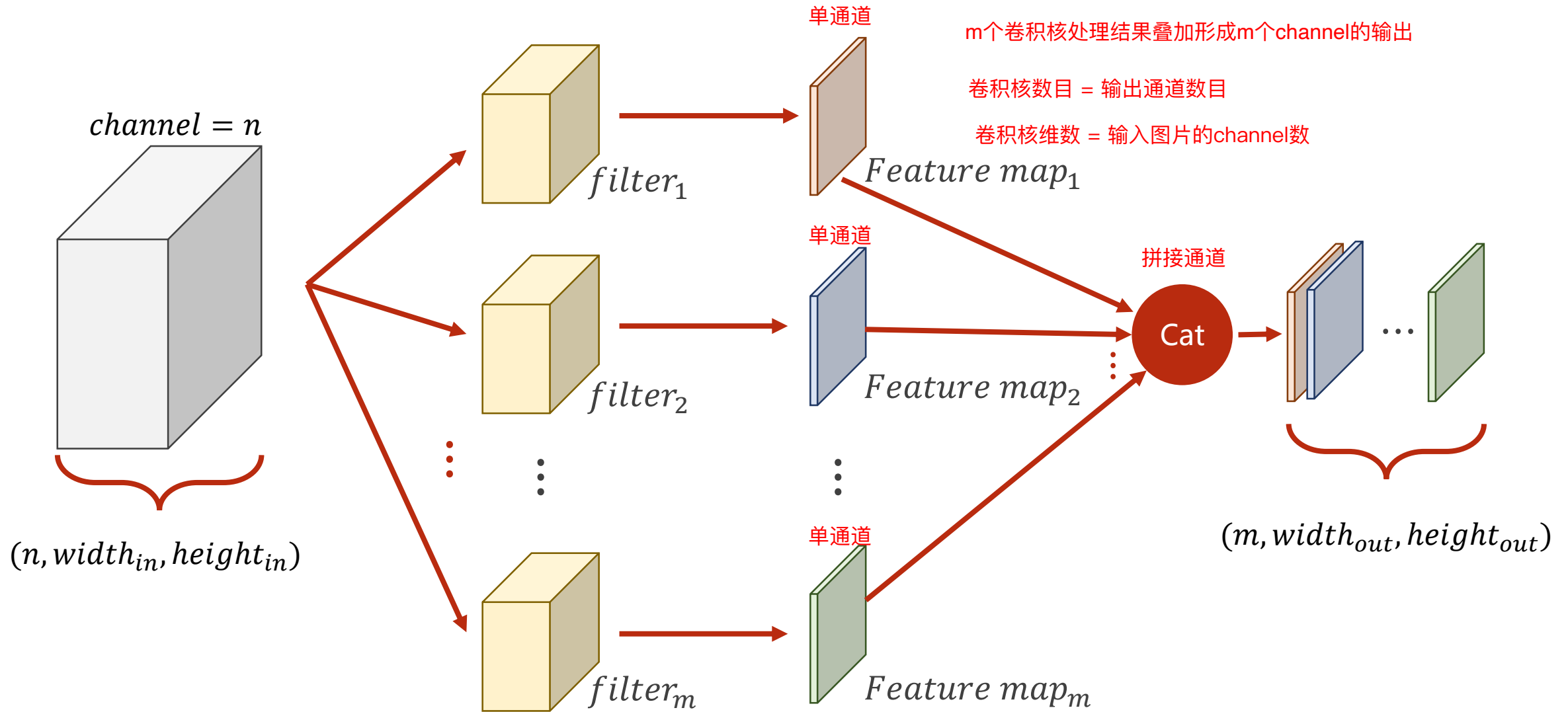


Convolution – N Input Channels

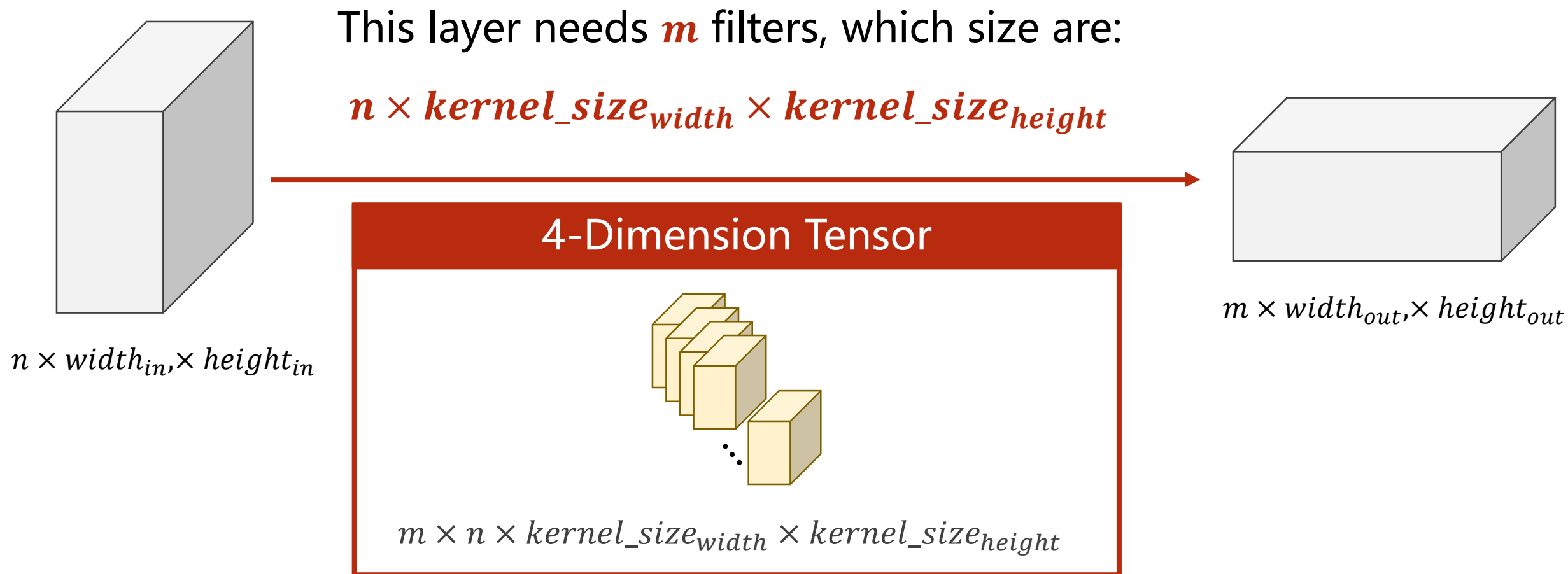
The shape of kernel tensor is $(n, 3, 3)$



Convolution – N Input Channels and M Output Channels



Convolutional Layer



Convolutional Layer

```
import torch
in_channels, out_channels= 5, 10
width, height = 100, 100
kernel_size = 3
batch_size = 1

input = torch.randn(batch_size,
                     in_channels,
                     width,
                     height)

conv_layer = torch.nn.Conv2d(in_channels,
                              out_channels,
                              kernel_size=kernel_size)

output = conv_layer(input)

print(input.shape)
print(output.shape)
print(conv_layer.weight.shape)
```

Convolutional Layer

```
import torch
in_channels, out_channels= 5, 10
width, height = 100, 100
kernel_size = 3
batch_size = 1

input = torch.randn(batch_size,
                     in_channels,
                     width,
                     height)

conv_layer = torch.nn.Conv2d(in_channels,
                              out_channels,
                              kernel_size=kernel_size)

output = conv_layer(input)

print(input.shape)
print(output.shape)
print(conv_layer.weight.shape)
```

Convolutional Layer

```
import torch
in_channels, out_channels= 5, 10
width, height = 100, 100
kernel_size = 3
batch_size = 1

input = torch.randn(batch_size,
                     in_channels,
                     width,
                     height)

conv_layer = torch.nn.Conv2d(in_channels,
                              out_channels,
                              kernel_size=kernel_size)

output = conv_layer(input)

print(input.shape)
print(output.shape)
print(conv_layer.weight.shape)
```


Convolutional Layer

```
import torch
in_channels, out_channels= 5, 10
width, height = 100, 100
kernel_size = 3
batch_size = 1

input = torch.randn(batch_size,
                     in_channels,
                     width,
                     height)

conv_layer = torch.nn.Conv2d(in_channels,
                              out_channels,
                              kernel_size=kernel_size)

output = conv_layer(input)

print(input.shape)
print(output.shape)
print(conv_layer.weight.shape)
```

Convolutional Layer

```
import torch
in_channels, out_channels= 5, 10
width, height = 100, 100
kernel_size = 3
batch_size = 1

input = torch.randn(batch_size,
                     in_channels,
                     width,
                     height)

conv_layer = torch.nn.Conv2d(in_channels,
                              out_channels,
                              kernel_size=kernel_size)

output = conv_layer(input)

print(input.shape)
print(output.shape)
print(conv_layer.weight.shape)
```

Convolutional Layer

```
import torch
in_channels, out_channels= 5, 10
width, height = 100, 100
kernel_size = 3
batch_size = 1

input = torch.randn(batch_size,
                     in_channels,
                     width,
                     height)

conv_layer = torch.nn.Conv2d(in_channels,
                              out_channels,
                              kernel_size=kernel_size)

output = conv_layer(input)

print(input.shape)
print(output.shape)
print(conv_layer.weight.shape)
```

torch.Size([1, 5, 100, 100])
torch.Size([1, 10, 98, 98])
torch.Size([10, 5, 3, 3])

Convolutional Layer – padding

边缘填充，扩展input大小，使output满足大小要求。
对于3*3的卷积核，如果需要output与input形态大小一样，则需要填充一圈。5*5则需要填充两圈

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1

Kernel

1	2	3
4	5	6
7	8	9



=

Output

211	295	262
259	282	214
251	253	169

Convolutional Layer – padding=1

Input

	3	4	6	5	7	
	2	4	6	8	2	
	1	6	7	8	4	
	9	7	4	6	2	
	3	7	5	4	1	



Kernel

1	2	3
4	5	6
7	8	9

=

Output

	211	295	262	
	259	282	214	
	251	253	169	

Convolutional Layer – padding=1

Input

0	0	0	0	0	0	0
0	3	4	6	5	7	0
0	2	4	6	8	2	0
0	1	6	7	8	4	0
0	9	7	4	6	2	0
0	3	7	5	4	1	0
0	0	0	0	0	0	0



Kernel

1	2	3
4	5	6
7	8	9

=

Output

	211	295	262	
	259	282	214	
	251	253	169	

Convolutional Layer – padding=1

Input

0	0	0	0	0	0	0
0	3	4	6	5	7	0
0	2	4	6	8	2	0
0	1	6	7	8	4	0
0	9	7	4	6	2	0
0	3	7	5	4	1	0
0	0	0	0	0	0	0

Kernel

1	2	3
4	5	6
7	8	9



=

Output

91				
	211	295	262	
	259	282	214	
	251	253	169	

Convolutional Layer – padding=1

Input

0	0	0	0	0	0	0
0	3	4	6	5	7	0
0	2	4	6	8	2	0
0	1	6	7	8	4	0
0	9	7	4	6	2	0
0	3	7	5	4	1	0
0	0	0	0	0	0	0

Kernel

1	2	3
4	5	6
7	8	9



=

Output

91	168	224	215	127
114	211	295	262	149
192	259	282	214	122
194	251	253	169	86
96	112	110	68	31

Convolutional Layer – padding=1

```
import torch

input = [3, 4, 6, 5, 7,
         2, 4, 6, 8, 2,
         1, 6, 7, 8, 4,
         9, 7, 4, 6, 2,
         3, 7, 5, 4, 1]
input = torch.Tensor(input).view(1, 1, 5, 5)

conv_layer = torch.nn.Conv2d(1, 1, kernel_size=3, padding=1, bias=False)

kernel = torch.Tensor([1, 2, 3, 4, 5, 6, 7, 8, 9]).view(1, 1, 3, 3)
conv_layer.weight.data = kernel.data

output = conv_layer(input)
print(output)
```

Convolutional Layer – stride=2

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

Convolutional Layer – stride=2

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1

Kernel

1	2	3
4	5	6
7	8	9



=

Output

211	

Convolutional Layer – stride=2

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	

Convolutional Layer – stride=2

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	262

Convolutional Layer – stride=2

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	262

Convolutional Layer – stride=2

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	262
251	

Convolutional Layer – stride=2

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	262
251	

Convolutional Layer – stride=2

Input

3	4	6	5	7
2	4	6	8	2
1	6	7	8	4
9	7	4	6	2
3	7	5	4	1



Kernel

1	2	3
4	5	6
7	8	9

=

Output

211	262
251	169

Convolutional Layer – stride=2

```
import torch

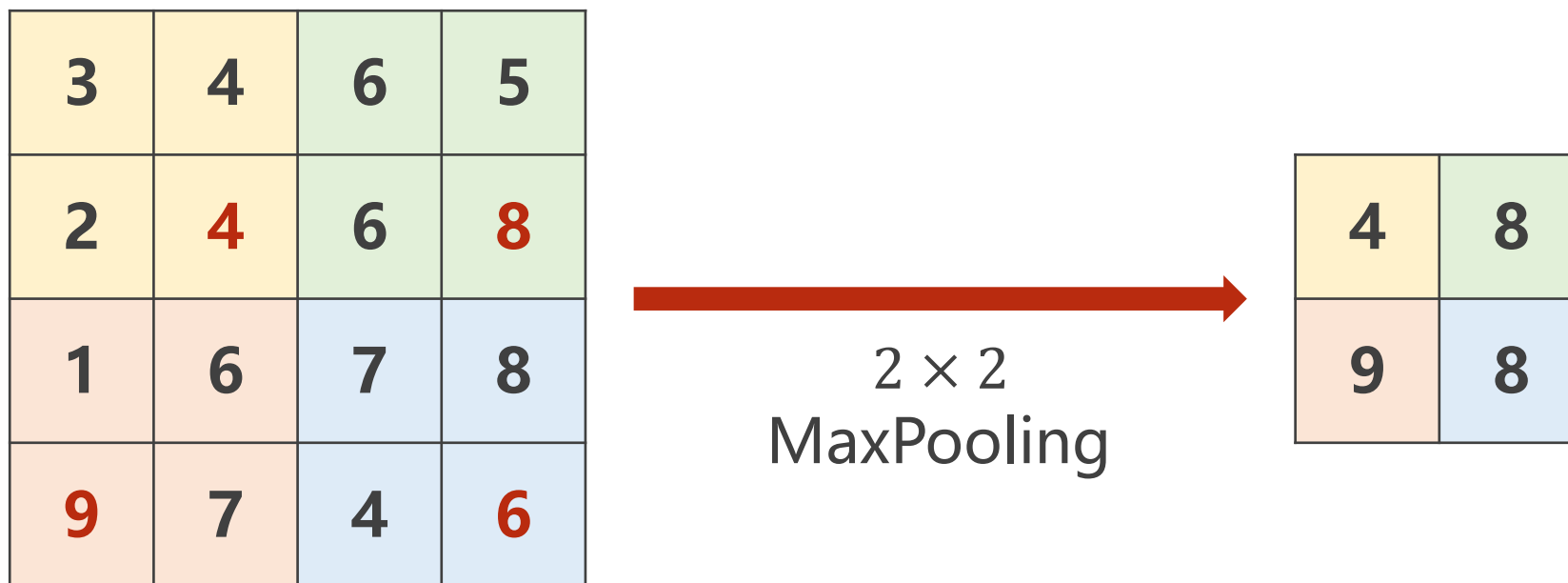
input = [3, 4, 6, 5, 7,
         2, 4, 6, 8, 2,
         1, 6, 7, 8, 4,
         9, 7, 4, 6, 2,
         3, 7, 5, 4, 1]
input = torch.Tensor(input).view(1, 1, 5, 5)

conv_layer = torch.nn.Conv2d(1, 1, kernel_size=3, stride=2, bias=False)

kernel = torch.Tensor([1, 2, 3, 4, 5, 6, 7, 8, 9]).view(1, 1, 3, 3)
conv_layer.weight.data = kernel.data

output = conv_layer(input)
print(output)
```

Max Pooling Layer



Max Pooling Layer

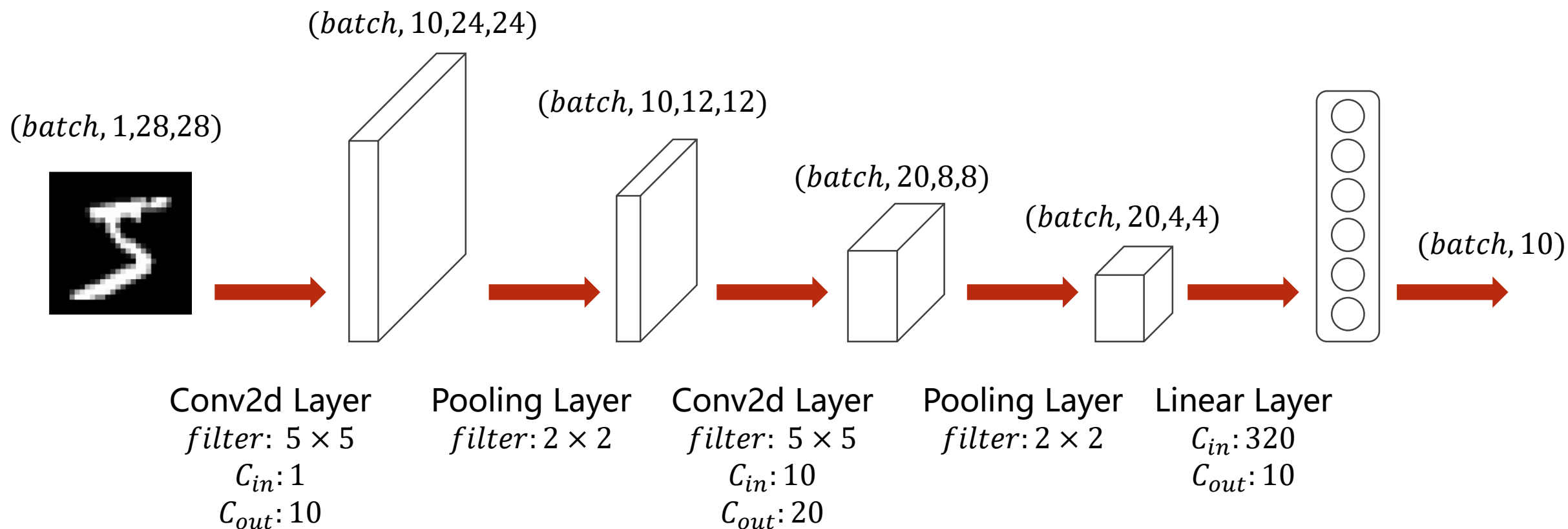
```
import torch

input = [3, 4, 6, 5,
         2, 4, 6, 8,
         1, 6, 7, 8,
         9, 7, 4, 6,
        ]
input = torch.Tensor(input).view(1, 1, 4, 4)

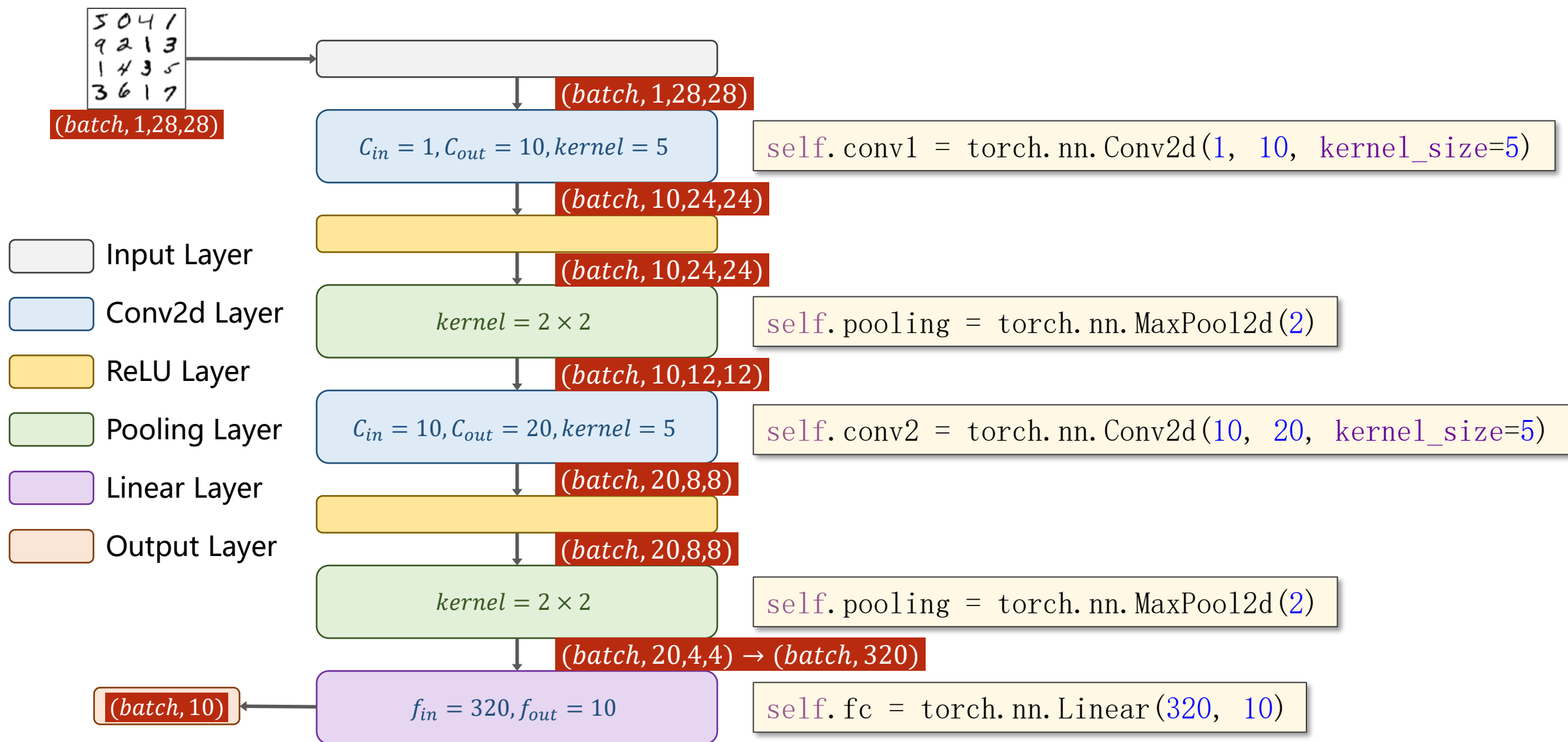
maxpooling_layer = torch.nn.MaxPool2d(kernel_size=2)

output = maxpooling_layer(input)
print(output)
```

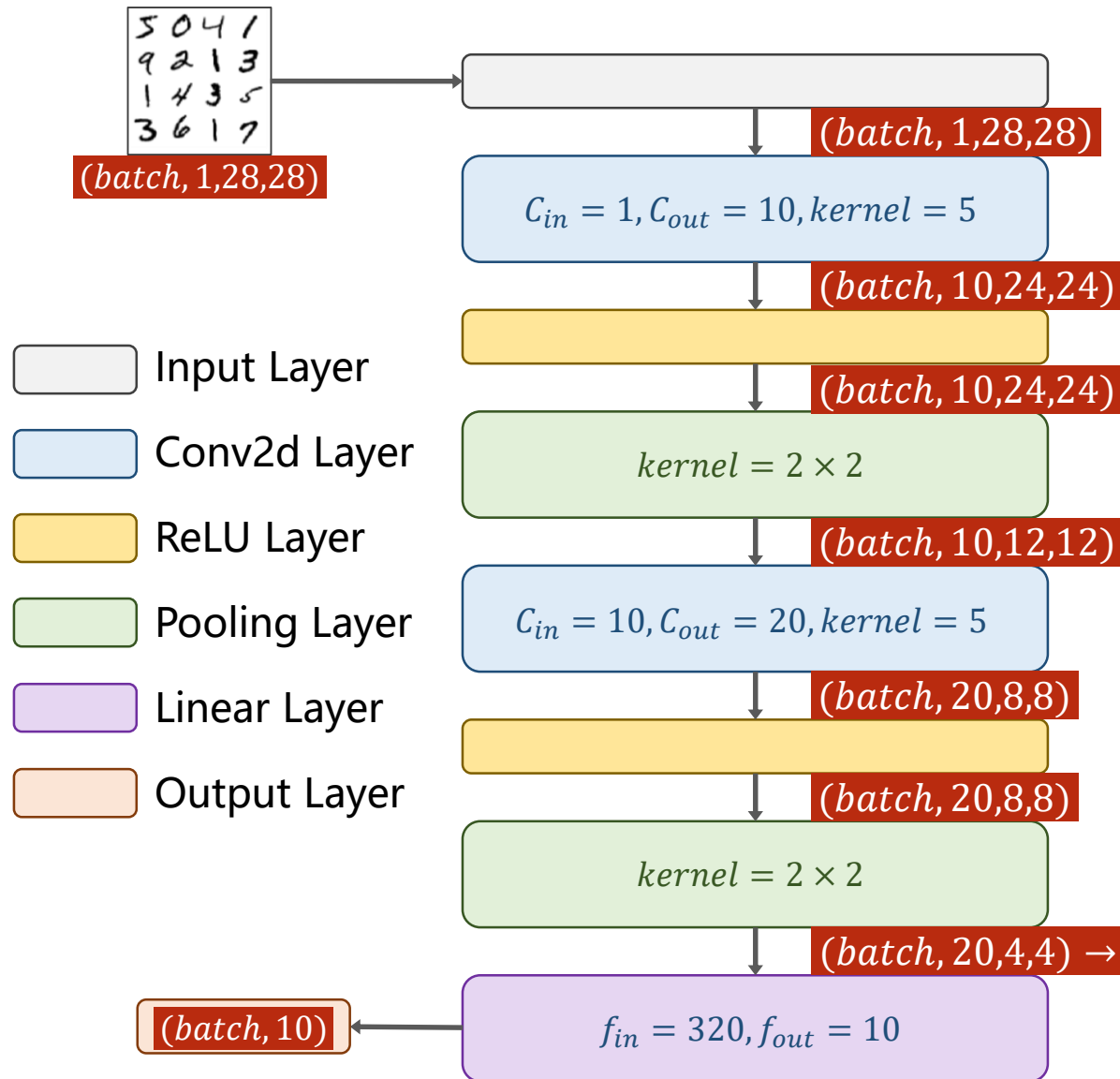
A Simple Convolutional Neural Network



Revision: Fully Connected Neural Network



Revision: Fully Connected Neural Network



```
class Net(torch.nn.Module):
    def __init__(self):
        super(Net, self).__init__()
        self.conv1 = torch.nn.Conv2d(1, 10, kernel_size=5)
        self.conv2 = torch.nn.Conv2d(10, 20, kernel_size=5)
        self.pooling = torch.nn.MaxPool2d(2)
        self.fc = torch.nn.Linear(320, 10)

    def forward(self, x):
        # Flatten data from (n, 1, 28, 28) to (n, 784)
        batch_size = x.size(0)
        x = F.relu(self.pooling(self.conv1(x)))
        x = F.relu(self.pooling(self.conv2(x)))
        x = x.view(batch_size, -1) # flatten
        x = self.fc(x)
        return x

model = Net()
```

How to use GPU – 1. Move Model to GPU

```
class Net(torch.nn.Module):
    def __init__(self):
        super(Net, self).__init__()
        self.conv1 = torch.nn.Conv2d(1, 10, kernel_size=5)
        self.conv2 = torch.nn.Conv2d(10, 20, kernel_size=5)
        self.pooling = torch.nn.MaxPool2d(2)
        self.fc = torch.nn.Linear(320, 10)

    def forward(self, x):
        # Flatten data from (n, 1, 28, 28) to (n, 784)
        batch_size = x.size(0)
        x = F.relu(self.pooling(self.conv1(x)))
        x = F.relu(self.pooling(self.conv2(x)))
        x = x.view(batch_size, -1) # flatten
        x = self.fc(x)
        return x

model = Net()
```


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        x = x.view(batch_size, -1)
        x = self.fc(x)
        return x

model = Net()
device = torch.device("cuda:0" if torch.cuda.is_available() else "cpu")
```

Define device as the first visible cuda device if we have CUDA available.

How to use GPU – 1. Move Model to GPU

```
class Net(torch.nn.Module):
    def __init__(self):
        super(Net, self).__init__()
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        x = x.view(batch_size, -1) # flatten
        x = self.fc(x)
        return x

model = Net()
device = torch.device("cuda:0" if torch.cuda.is_available() else "cpu")
model.to(device)
```

Convert parameters and buffers of all modules to CUDA Tensor.

How to use GPU – 2. Move Tensors to GPU

```
def train(epoch):
    running_loss = 0.0
    for batch_idx, data in enumerate(train_loader, 0):
        inputs, target = data
        optimizer.zero_grad()

        # forward + backward + update
        outputs = model(inputs)
        loss = criterion(outputs, target)
        loss.backward()
        optimizer.step()

        running_loss += loss.item()
        if batch_idx % 300 == 299:
            print('[%d, %5d] loss: %.3f' % (epoch + 1, batch_idx + 1, running_loss / 2000))
            running_loss = 0.0
```

How to use GPU – 2. Move Tensors to GPU

```
def train(epoch):
    running_loss = 0.0
    for batch_idx, data in enumerate(train_loader, 0):
        inputs, target = data
        inputs, target = inputs.to(device), target.to(device)
        optimizer.zero_grad()

        # forward + backward + update
        outputs = model(inputs)
        loss = criterion(outputs, target)
        loss.backward()
        optimizer.step()

        running_loss += loss.item()
        if batch_idx % 300 == 299:
            print('[%d, %5d] loss: %.3f' % (epoch + 1, batch_idx + 1, running_loss / 2000))
            running_loss = 0.0
```

Send the inputs and targets at every step to the GPU.

How to use GPU – 2. Move Tensors to GPU

```
def test():
    correct = 0
    total = 0
    with torch.no_grad():
        for data in test_loader:
            inputs, target = data
            outputs = model(inputs)
            _, predicted = torch.max(outputs.data, dim=1)
            total += target.size(0)
            correct += (predicted == target).sum().item()
    print('Accuracy on test set: %d %% [%d/%d]' % (100 * correct / total, correct, total))
```

How to use GPU – 2. Move Tensors to GPU

```
def test():
    correct = 0
    total = 0
    with torch.no_grad():
        for data in test_loader:
            inputs, target = data
            inputs, target = inputs.to(device), target.to(device)
            outputs = model(inputs)
            _, predicted = torch.max(outputs.data, dim=1)
            total += target.size(0)
            correct += (predicted == target).sum().item()
    print('Accuracy on test set: %d %% [%d/%d]' % (100 * correct / total, correct, total))
```

Send the inputs and targets at every step to the GPU.

Results

Accuracy on test set: 6 % [637/10000]

[1, 300] loss: 0.098

[1, 600] loss: 0.035

[1, 900] loss: 0.025

Accuracy on test set: 96 % [9605/10000]

[2, 300] loss: 0.021

[2, 600] loss: 0.017

[2, 900] loss: 0.015

Accuracy on test set: 97 % [9709/10000]

.....

[9, 300] loss: 0.006

[9, 600] loss: 0.006

[9, 900] loss: 0.007

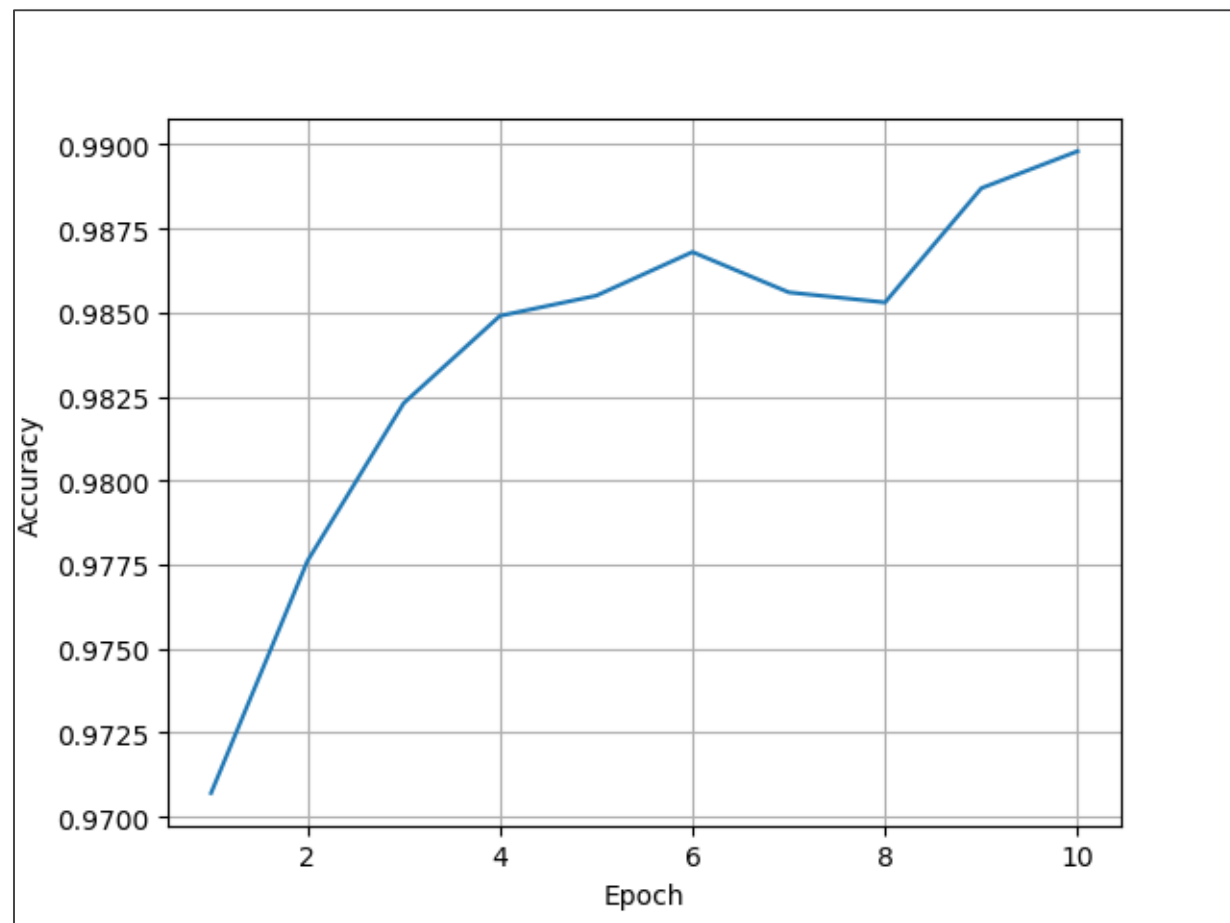
Accuracy on test set: 98 % [9857/10000]

[10, 300] loss: 0.006

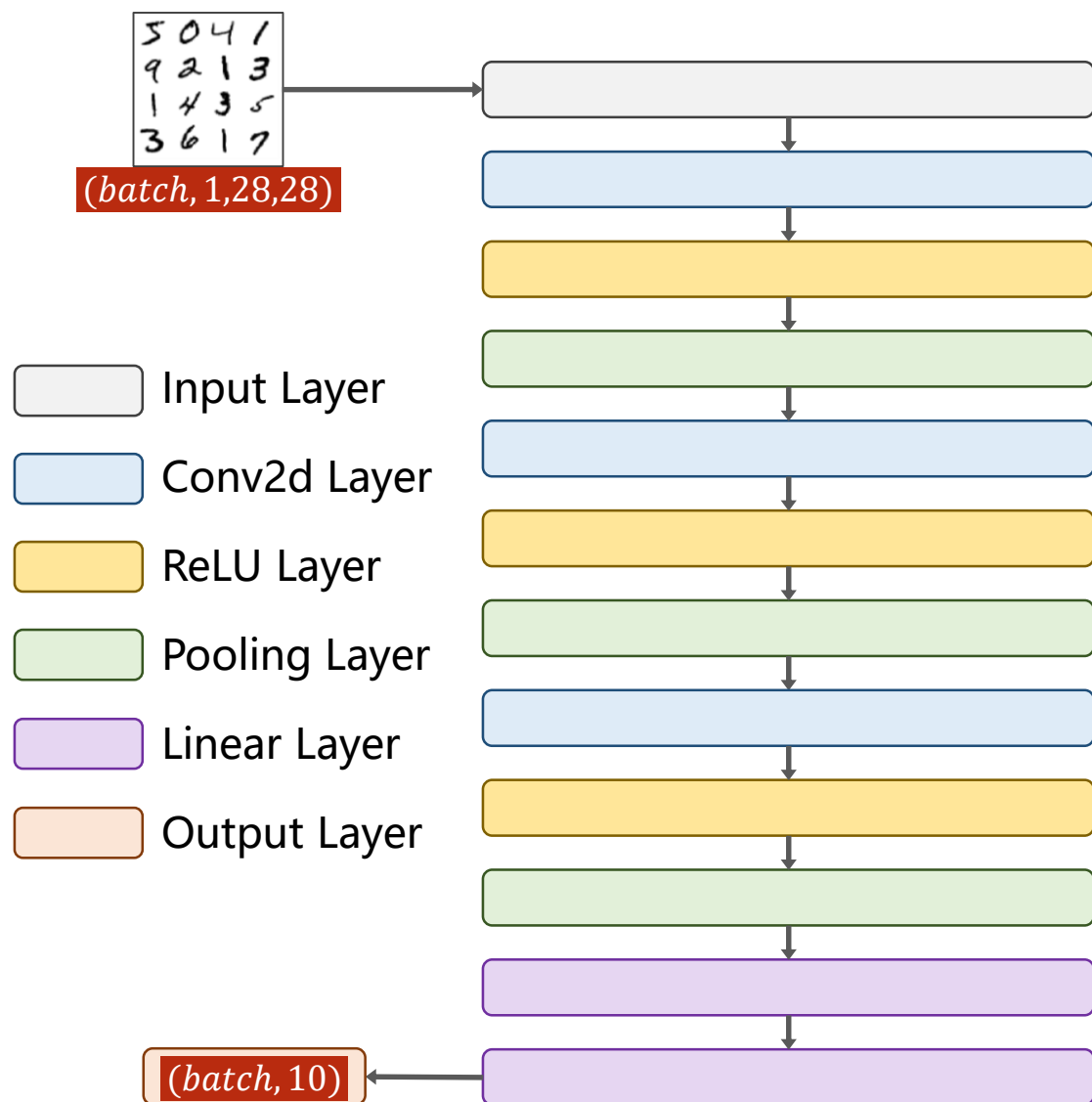
[10, 600] loss: 0.006

[10, 900] loss: 0.006

Accuracy on test set: 98 % [9869/10000]



Exercise 10-1



- Try a more complex CNN:
 - Conv2d Layer * 3
 - ReLU Layer * 3
 - MaxPooling Layer * 3
 - Linear Layer * 3
- Try different configuration of this CNN:
 - Compare their performance.



PyTorch Tutorial

10. Basic CNN