

## ⇒ Grammaire de base :

<file> ::= NEWLINE? <def>\* <stmt>+ EOF

<def> ::= def <ident> ( <ident>\*, ) : <suite>

<suite> ::= <simple\_stmt> NEWLINE

| NEWLINE BEGIN <stmt>+ END

<simple\_stmt> ::= return <expr>

| <ident> = <expr>

| <expr> [ <expr> ] = <expr>

| print ( <expr> )

| <expr>

<stmt> ::= <simple\_stmt> NEWLINE

| if <expr> : <suite>

| if <expr> : <suite> else : <suite>

| for <ident> in <expr> : <suite>

<expr> ::= <const> | <ident> | <expr> [ <expr> ] | - <expr> |  
not <expr> | <expr> <binop> <expr> | <ident> ( <expr>\*, ) |  
[ <expr>\*, ] | ( <expr> )

<binop> ::= + | - | \* | // | % | <= | >= | > | < | != | == | and | or

<const> ::= <integer> | <string> | True | False | None

## ⇒ Introduction des priorités et associativités des opérateurs

<expr> := or\_expr | <expr> [ <expr> ]

<or\_expr> := <and\_expr>\*<sub>or</sub>

<and\_expr> := <not\_expr>\*<sub>and</sub>

<not\_expr> := not? <comp\_expr>

<comp\_expr> := <add\_expr>\*<sub><binop\_comp></sub>

<add\_expr> := <mut\_expr>\*<sub><binop\_add></sub>

<mut\_expr> := <minus\_expr>\*<sub><binop\_mut></sub>

<minus\_expr> := - ? <terminal\_expr>

<binop\_comp> := <= | >= | > | < | != | ==

<binop\_add> := + | -

<binop\_mut> := \* | // | %

<terminal\_expr> := <const> | <ident>

| <ident> ( <expr>\*, )

| [ <expr>\*, ] | ( <expr> )

## ⇒ Explicitation des règles \* + et ? avec ou sans symbole:

<exemple>+	<exemple_plus> := <exemple> <exemple_plus_rest> <exemple_plus_rest> := ε   <exemple_plus>
<exemple>*	<exemple_etoile> -> ε   <exemple> <exemple_etoile>
<exemple>* <sub>symbole</sub>	<exemple_plus_symbole> := <exemple> <exemple_plus_symbole_rest> <exemple_plus_symbole_rest> := ε   symbole <exemple_plus_symbole>
<exemple>* <sub>symbole</sub>	<exemple_etoile_symbole> := ε   <exemple_plus_symbole>
exemple?	<exemple> := ε   exemple

⇒ **Elimination de la récursivité à gauche :**

$\langle \text{expr} \rangle ::= \langle \text{or\_expr} \rangle \mid \langle \text{expr} \rangle [ \langle \text{expr} \rangle ]$	$\langle \text{expr} \rangle ::= \langle \text{or\_expr} \rangle \langle \text{expr\_crochet\_etoile} \rangle$ $\langle \text{expr\_crochet\_etoile} \rangle ::= \varepsilon \mid [ \langle \text{expr} \rangle ] \langle \text{expr\_crochet\_etoile} \rangle$
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⇒ **Factorisation des règles :**

$\langle \text{stmt} \rangle ::= \text{if } \langle \text{expr} \rangle : \langle \text{suite} \rangle$ $\langle \text{stmt} \rangle ::= \text{if } \langle \text{expr} \rangle : \langle \text{suite} \rangle \text{ else } : \langle \text{suite} \rangle$	$\langle \text{stmt} \rangle ::= \text{if } \langle \text{expr} \rangle : \langle \text{suite} \rangle \langle \text{stmt\_else} \rangle$ $\langle \text{stmt\_else} \rangle ::= \varepsilon \mid \text{else } : \langle \text{suite} \rangle$
$\langle \text{terminal\_expr} \rangle ::= \dots \mid \langle \text{ident} \rangle \mid \langle \text{ident} \rangle ( \langle \text{expr} \rangle^*, ) \mid \dots$	$\langle \text{terminal\_expr} \rangle ::= \langle \text{ident} \rangle \langle \text{ident\_fact} \rangle$ $\langle \text{ident\_fact} \rangle ::= \varepsilon \mid ( \langle \text{expr} \rangle^*, )$

⇒ **Ambiguïté avec  $\langle \text{simple\_stmt} \rangle$  :**

On a :

$\langle \text{simple\_stmt} \rangle ::= \dots \mid \langle \text{expr} \rangle [ \langle \text{expr} \rangle ] = \langle \text{expr} \rangle$   
 $\mid \langle \text{expr} \rangle \mid \dots$

L'ambiguïté apparaît quand on lit le caractère « [ » :

- Doit-on utiliser la deuxième règle et ensuite utiliser la règle  $\langle \text{expr} \rangle ::= \langle \text{expr} \rangle [ \langle \text{expr} \rangle ]$
- Doit-on utiliser la première règle

**Pour lever cette ambiguïté on fait remonter les membres droits de la règle  $\langle \text{expr} \rangle$  :**

$\langle \text{simple\_stmt} \rangle ::= \dots \mid \langle \text{or\_expr} \rangle$   
 $\mid \langle \text{or\_expr} \rangle [ \langle \text{expr} \rangle ] \langle \text{expr\_crochet\_etoile} \rangle \mid \dots$

**On modifie aussi la première des règles de  $\langle \text{simple\_stmt} \rangle$  pour pouvoir factoriser le tout**

$\langle \text{simple\_stmt} \rangle ::= \dots \mid \langle \text{or\_expr} \rangle [ \langle \text{expr} \rangle ] \langle \text{expr\_crochet\_etoile} \rangle = \langle \text{expr} \rangle$   
 $\mid \langle \text{or\_expr} \rangle$   
 $\mid \langle \text{or\_expr} \rangle [ \langle \text{expr} \rangle ] \langle \text{expr\_crochet\_etoile} \rangle \mid \dots$

**On factorise**

$\langle \text{simple\_stmt} \rangle ::= \langle \text{or\_expr} \rangle \langle \text{simple\_stmt\_fact} \rangle$

$\langle \text{simple\_stmt\_fact} \rangle ::= [ \langle \text{expr} \rangle ] \langle \text{expr\_crochet\_etoile} \rangle \mid [ \langle \text{expr} \rangle ] \langle \text{expr\_crochet\_etoile} \rangle = \langle \text{expr} \rangle$

**On refactorise**

$\langle \text{simple\_stmt} \rangle ::= \langle \text{or\_expr} \rangle \langle \text{simple\_stmt\_fact} \rangle$

$\langle \text{simple\_stmt\_fact} \rangle ::= [ \langle \text{expr} \rangle ] \langle \text{expr\_crochet\_etoile} \rangle \langle \text{simple\_stmt\_fact\_fact} \rangle$

$\langle \text{simple\_stmt\_fact\_fact} \rangle ::= \varepsilon \mid = \langle \text{expr} \rangle$

**Il reste tout de même une ambiguïté avec la règle  $\langle \text{simple\_stmt} \rangle$  qui rend la grammaire ponctuellement LL(2) :**

$\langle \text{simple\_stmt} \rangle ::= \langle \text{or\_expr} \rangle \langle \text{simple\_stmt\_fact} \rangle$   
 $\langle \text{simple\_stmt} \rangle ::= \langle \text{ident} \rangle = \langle \text{expr} \rangle$

Sachant que :  
 $\langle \text{or\_expr} \rangle ::= {}_n \langle \text{ident} \rangle$

⇒ **Grammaire finale (syntaxe gramophone) :**

file -> opt\_newline def\_etoile stmt\_plus EOF .

opt\_newline -> .

opt\_newline -> NEWLINE .

def\_etoile -> .

def\_etoile -> def def\_etoile .

stmt\_plus -> stmt stmt\_plus\_rest .

stmt\_plus\_rest -> .

stmt\_plus\_rest -> stmt\_plus .

def -> def ident "(" ident\_etoile\_virgule ")" ":" suite .

ident\_etoile\_virgule -> .

ident\_etoile\_virgule -> ident\_plus\_virgule .

ident\_plus\_virgule -> ident ident\_plus\_virgule\_rest .

ident\_plus\_virgule\_rest -> .

ident\_plus\_virgule\_rest -> ";" ident\_plus\_virgule .

suite -> simple\_stmt NEWLINE .

suite -> NEWLINE BEGIN stmt\_plus END .

simple\_stmt -> return expr .

simple\_stmt -> print "(" expr ")" .

simple\_stmt -> ident "=" expr .

simple\_stmt -> or\_expr simple\_stmt\_fact .

simple\_stmt\_fact -> simple\_stmt\_fact\_fact .

simple\_stmt\_fact -> "[" expr "]" expr\_crochet\_etoile .

simple\_stmt\_fact\_fact -> .

simple\_stmt\_fact\_fact -> "=" expr .

stmt -> simple\_stmt NEWLINE .

stmt -> for ident in expr ":" suite .

stmt -> if expr ":" suite stmt\_else .

stmt\_else -> .

stmt\_else -> else ":" suite .

expr -> or\_expr expr\_crochet\_etoile .

expr\_crochet\_etoile -> .

expr\_crochet\_etoile -> "[" expr "]" expr\_crochet\_etoile .

or\_expr -> and\_expr or\_expr\_rest .

or\_expr\_rest -> .

or\_expr\_rest -> binop\_or or\_expr .

and\_expr -> not\_expr and\_expr\_rest .

and\_expr\_rest -> .

and\_expr\_rest -> binop\_and and\_expr .

not\_expr -> comp\_expr .

not\_expr -> not comp\_expr .

comp\_expr -> add\_expr comp\_expr\_rest .

comp\_expr\_rest -> .

comp\_expr\_rest -> binop\_comp comp\_expr .

add\_expr -> mut\_expr add\_expr\_rest .

add\_expr\_rest -> .

add\_expr\_rest -> binop\_add add\_expr .

mut\_expr -> terminal\_expr mut\_expr\_rest .

mut\_expr\_rest -> .

mut\_expr\_rest -> binop\_mut mut\_expr .

terminal\_expr -> "(" expr ")" .

terminal\_expr -> const .

terminal\_expr -> ident expr\_rest\_ident .

terminal\_expr -> "[" expr\_etoile\_virgule "]" .

expr\_rest\_ident -> "(" expr\_etoile\_virgule ")" .

expr\_rest\_ident -> .

expr\_etoile\_virgule -> .

expr\_etoile\_virgule -> expr\_plus\_virgule .

expr\_plus\_virgule -> expr expr\_plus\_virgule\_rest .

expr\_plus\_virgule\_rest -> .

expr\_plus\_virgule\_rest -> ";" expr\_plus\_virgule .

binop\_add -> "+" .

binop\_add -> "-" .

binop\_mut -> "\*" .

binop\_mut -> "/" .

binop\_mut -> "%" .

binop\_comp -> "<=" .

binop\_comp -> ">=" .

binop\_comp -> ">" .

binop\_comp -> "<" .

binop\_comp -> "!=" .

binop\_comp -> "==" .

binop\_and -> and .

binop\_or -> or .

const -> integer .

const -> string .

const -> True .

const -> False .

const -> None .