

FP

Lez 5

Property-based testing
&
tagged values

Recap: PM su liste

- Sia $f: 'a \text{ list} \rightarrow 'b$.

– Il PM tipico è:

```
let f xs =
```

```
  match xs with
```

```
    | [] -> e1
```

```
    | y::ys -> e2
```

dove y, ys tipicamente occorrono in $e2$

- Si possono fare PM più articolati

PM su liste 2

```
let rec ordered xs =  
  match xs with  
  | [] -> true  
  | [x] -> true  
  | x :: (y :: ys) -> x <= y &&  
                        ordered (y :: ys)
```

- Nota: `[x]` è sy-sugar per `x :: []`

PM su liste 3

- Anche PM non esaustivo da funzioni parziali:

```
let rec last xs =  
  match xs with  
  | [y] → y  
  | _ :: ys → last ys
```

```
last : 'a list → 'a
```

Mini F#

Il nostro linguaggio, per adesso

- $p ::= c \mid id \mid (p, p) \mid [] \mid (p :: p)$
- $e ::= c \mid id \mid fun\ p \rightarrow e \mid e\ e \mid (e, e) \mid ()$
| $let\ p = e \mid let\ p = e\ in\ e$
| $let\ rec\ id = e\ in\ e \mid e :: e \mid []$
| $match\ e\ with\ p_1 \rightarrow e_1 \dots p_n \rightarrow e_n$
- $t ::= b \mid \alpha \mid t \rightarrow t \mid \alpha list \mid t * t \mid unit$
- $b ::= int \mid float \mid string \mid bool \dots$

TESTING

Why it matters ...

Go to `fscheck.fsx`

Dijkstra's ghost

“Program testing can at best show the presence of errors, but never their absence” [*Notes On Structured Programming*, 1970]

“None of the program in this monograph, *needless to say*, has been tested on a machine”
[Introduction to *A Discipline of Programming*, 1980]



Software testing

Most common approach to SW quality

- Very labour-intensive
 - up to 50% of SW development
- Even after testing, a bug remains on average per 100 lines of code, costing 60 billions \$ (2002)
- Need of *automatic* testing tools
 - To complete tests in shorter time
 - To test better
 - To repeat tests more easily
 - *To generate test cases automatically*

Testing: the dominant paradigm

- By far the most widely used style of testing today is *unit testing*.
 - Invent a "state of the world".
 - Run the unit we're testing – a function/method
 - Check the modified state of the world to see if it looks like it should
 - Ericsson's ATM switch controlled by 1.5 mil LOC + 700.000 lines of UT
 - More modestly ...

The dominant paradigm

```
public class TestAdder {  
    public void testSum() {  
        Adder adder = new AdderImpl();  
        assert(adder.add(1, 1) == 2);  
        assert(adder.add(1, 2) == 3);  
        assert(adder.add(2, 2) == 4);  
        assert(adder.add(0, 0) == 0);  
        assert(adder.add(-1, -2) == -3);  
        assert(adder.add(-1, 1) == 0);  
        assert(adder.add(1234, 988) == 2222);  
    }  
}
```

The dominant paradigm

Problem: unit testing is only as good as your patience

- The previous example contains 7 tests.
- Typically we lose the will to continue inventing new unit tests long before we've exhausted our search of the space of possible bugs.
- (One) **solution:** property-based testing – PBT
 - A property is nothing more than a predicate that should always hold.

PBT: Quickcheck

- Quickcheck was introduced by Claessen & Hughes (2000)
 - Voted “most influential ICFP'00 paper”
- A tool for testing Haskell programs automatically.
- The programmer provides a specification of the program, in the form of *properties* that functions should satisfy
- QuickCheck then tests that the properties hold in a large number of *randomly generated cases*.

PBT

Quickcheck is now available for many PLs, including imperative ones, such as *Java*, *C(++)*, *JavaScript*, *Objective-C*, *Perl*, *Erlang*, *Prolog*, *Python*, *Ruby*, *Scala* ...

- **Quickcheck** is based on *random testing*
- There are alternatives such as **(Lazy) Smallcheck**, based on *exhaustive testing* and *symbolic execution*, but just for FP right no
 - We will see and use **FsCheck**
 - Random testing only

Commercial uses of PBT

- Mostly within [QuviQ](#), Hughes' start-up commercializing Quickcheck for *Erlang* – [here](#) a free version
 - See paper “[Quickcheck for fun and profit](#)”
- Some success stories:
 - Ericsson's 4G radio base stations
 - Database reliability at Basho
 - Mission-critical gateway at Motorola
 - AUTOSAR Basic Software
 - Google's LevelDB database ...

Commercial uses of FsCheck

- Credit Suisse
- BlueMountainCapital
- Tachyus
- Digital Furnace Games
- 15below

Details [here](#)

Back to code

Quickcheck: how

- Checking $\forall x : \tau. C(x)$ means trying to find an assignment $x \rightarrow a$ at type τ such that $\neg C(a)$ holds
 - e.g. checking $\forall xs : 'a \text{ list}. \text{rev } xs = xs$ means finding $xs \rightarrow [a2, a1]$ for which $\text{rev } xs \neq xs$
- Quickcheck generates *pseudo-random* values of size k and stops when
 - a counterexample is found, or
 - the maximum size of test values has been reached, or
 - a default timeout expires

Conditional laws

- More interesting are *conditional laws*:
 - $\forall x: 'a, xs: 'a \text{ list. } \text{ordered } xs \implies \text{ordered } (\text{insert } x \text{ } xs)$
- Here we generate random list that may or may not be sorted and then check if insertion preserves ordered-ness
- If a candidate list does not satisfies the condition it is discarded
 - *Coverage is an issue*: what's the likelihood of randomly generating lists (of length > 1) that are *sorted*?
- Quickcheck gives combinator to *monitor* test data distribution – but in the end one has to write an ad-hoc generator, here yielding only ordered lists

Quickcheck's design decisions

- A lightweight tool – originally 300 lines of Haskell code, then extended to deal with the monadic fragment
- Spec are written via a DSL in the very module under test
- Adoption of random testing
- Put distribution of test data in the hand of the user
 - API for writing generators and observe distributions
- Emphasis on *shrinking* failing test cases to facilitate debugging