

## Question 1.21

a) I did this using code from Example 1.8. According to Example 1.19, since I used the same moving average filter of 3 observations, the  $p(h)$  should be 0 for any lags greater than 2. My  $p\_hat(h)$  was -.081 for lag = 20. This isn't unexpected per se since the  $p\_hat(h)$  is calculated from actual sample data, so it wasn't that far off

```
# a)
set.seed(1)
w = rnorm(1600, 0, 1)
v = filter(w, sides = 2, filter=rep(1/3,3))
v = v[2:501]

samp_acf = acf(v, 20, plot=F)
print(samp_acf[20])
# Should be 0 for h > 2
```

b) I repeated part a for  $n=50$ . The results for lag 20 actually got closer to 0, which is a little surprising. Typically I'd expect with a larger  $n$  the results to be more "normal" or close to the theoretical values, but this was not the case. I got a  $p\_hat(h)$  of .037, which is actually closer in absolute value to 0 than the result with  $n=500$

## Question 2.1

a & b) I copied the book's code, and printed the output. The resulting trend is an increase of .167 per year

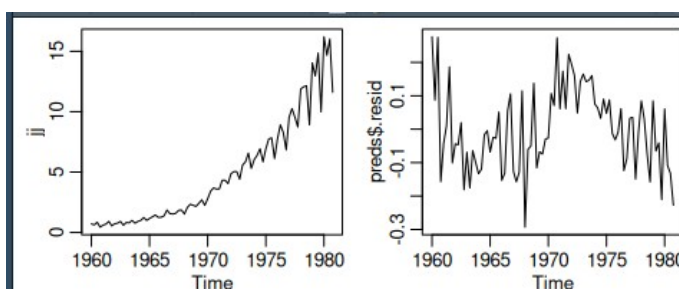
```
> print(summary$coefficients)
              Estimate Std. Error t value Pr(>|t|)
trend 0.1671722 0.002259113  73.99902 9.919298e-75
Q1    1.0527931 0.027359218  38.48038 6.215327e-53
Q2    1.0809159 0.027365047  39.49987 8.711575e-54
Q3    1.1510242 0.027382526  42.03499 7.974132e-56
Q4    0.8822665 0.027411632  32.18584 3.608412e-47
```

c) They decrease from Q3 → Q4, by a percentage of 23.3%, as shown by the summary output here

d) Including an intercept term removes quarter 1 from the model, and it also makes everything significantly less significant (lol)

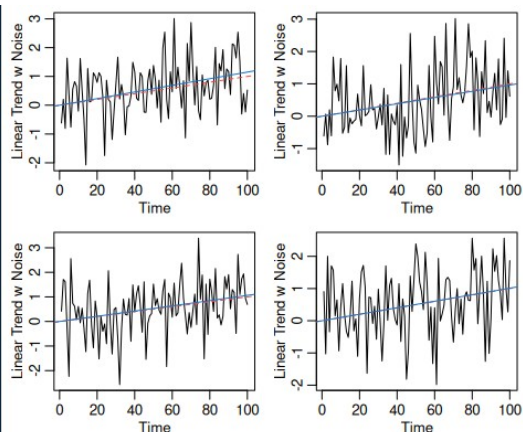
```
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  1.052793  0.027359  38.480 < 2e-16 ***
trend        0.167172  0.002259  73.999 < 2e-16 ***
Q2           0.028123  0.038696   0.727  0.4695
Q3           0.098231  0.038708   2.538  0.0131 *
Q4          -0.170527  0.038729  -4.403 3.31e-05 ***
```

e) I couldn't get the graph exactly, but I was able to plot the residuals. The residuals showed no apparent pattern, so we can assume that the model is a decent fit



## Question 2.3

a) I copied the book's code from the problem, and plotted the results. The first graph seems to model the fit very well (in terms of the fitted line), but the rest of them do not model the series well



b) Same, but instead I made a linear trend. The fitted and mean lines fit the data much better, and it's sometimes almost impossible to distinguish between the two.

