

# WORD2VEC APPLIED TO THE YALE CORPUS

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## ABSTRACT

We apply a word embedding model to a large corpus of classical music to learn an embedding space where chords are represented by real-valued vectors. The first two principal components of the embeddings of major triads are arranged on a circle. In music from earlier composers, this circular topology is more evident than in later composers who used less counterpoint. Remarkably, the order in which major triads are arranged on this structure corresponds to their order in the circle of fifths. The emergence of this structure is justified by reasoning about the probabilistic embedding model and the composition of classical music. We situate our results in the context of current statistical research into functional harmony in common practice music. We show how this technique can be used for large-scale, quantitative stylistic analysis of music.

## 1. INTRODUCTION

### 1.1 Word embeddings

Probabilistic models such as Latent Dirichlet Allocation [4] are standard tools for analyzing text data. However, such models use bag-of-words representations. Therefore they extract meaning from word co-occurrence counts on the document level, and ignore the sequential nature of language. Syntax, punctuation, and grammar are intrinsically sequential, and a good model of natural language or tree structures should be able to capture both information from co-occurrence counts and information across time. While Latent Dirichlet Allocation has been used to model music (Q:citation?), music is inherently sequential. For in-depth analysis of style in music, we need embedding models.

Word embeddings, or real-valued vectors representing words in a vocabulary, were first introduced by [3] but popularized by [11]. Such models typically have a log-bilinear form [12], and are trained using negative sampling with a fixed size context window [11]. This is equivalent to matrix factorization of a shifted pointwise mutual information word-context matrix [9]. To see this, construct a co-occurrence matrix of words, where the rows and columns are the words in the vocabulary. Each entry  $i, j$  in the matrix is the count of how many times

word  $i$  (e.g. ‘dog’) occurred in the context of word  $j$  (e.g. ‘the’). Word embedding models such as the skip-gram model (word2vec) can be viewed as performing singular value decomposition on a transformed version of this matrix. Compositional word embeddings for learning paragraph or document embeddings have also been proposed [5, 8]. However, [10] suggests that much of the success of these types of distributed representations of words is due to the tricks needed to train such models such as noise contrastive estimation. [1] and (todo: cite arora 2016 polysemy, <http://arxiv.org/pdf/1601.03764.pdf>) show that word embedding models can also be thought of as random walks in the embedding space.

As useful models of discrete data, word embedding models are starting to be used in domains outside of natural language. For example, [2] embed protein sequences for classification, and [6] develop an embedding model to build a recommendation system (for example, for recommending movies to users). There exists some prior work on applying word embedding models to music. [7] trained an embedding model on a corpus of 200 rock songs for the task of recommending chords to composers.

### 1.2 Quantitative stylistic analysis of music

## 2. METHODOLOGY

### 2.1 Corpus

The Yale/Classical Archives Corpus (YCAC) is a database of pitch-class and time data from MIDI files contributed by users of classicalarchives.com encoding 8,980 distinct pieces of music [?]. Each piece is represented by a sequence of time-coded chroma vectors obtained by “salami slicing” the original MIDI file.

### 2.2 Embedding space

A word2vec algorithm was used to create a number of word-embedding spaces for the entire corpus and for corpora consisting only of the works of a single composer.<sup>1</sup> The algorithm treats each chroma vector as a word in a sentence. It returns an  $n$ -dimensional real-valued vector for each word. t-SNE dimensionality reduction was applied to the resultant word-embedding space to demonstrate its plausibility. PCA was applied to the resultant



<sup>1</sup> The implementation used was the word2vec model provided by the Python module ‘gensim’, which uses a skip-gram negative sampling (SGNS) model which has been shown to be effective on large textual corpora. [?]

word-embedding space, and the locations of chroma vectors corresponding to major triads were plotted.

### 3. DISCUSSION

As shown in Figure ??, we can see that the circle of fifths emerges from the structure of the learned vector space of chords in classical music. This is not an intuitive result at first. However, to see that this is a reasonable result of applying the skip-gram word2vec model, consider the log-likelihood of the model. Gradients of the log-likelihood with respect to the embeddings are used to train the model. The log-likelihood means the model will maximize the probability of correctly classifying the context given the training example. If the model assigns too high a probability to correct contexts, it will be overconfident on other (incorrect) contexts, and the derivative of the log-likelihood will push the embeddings further apart. But if the model assigns too low a probability to correct contexts, the gradient of the log-likelihood will flip signs and pull the embeddings closer together. The minimal geometric structure that minimizes these constraints is a circle. If the parts of the circle are perturbed (e.g. imagine shifting the values of an embedding in the circle by a large amount), the above arguments show that it will return to a circular structure by virtue of the gradients of the objective function. We thus expect a circle from the principal components of highly stable embeddings (such as the embeddings of chords in the circle of fifths). To see why the circle of fifths respects the ordering, we consider the context window (**(size 5? in our case)**). Chords in the circle of fifths occur in each others' contexts, but usually only nearest neighbors (e.g. it is rare to see C major followed by B major). Therefore C major and G major occur in each others' contexts and will be pushed closer together during training. But they will be pushed apart from their non-nearest-neighbors (such as B major). This shows they will respect the ordering apparent in classical music where common practices such as counterpoint result in transitions prevalent on the circle of fifths.

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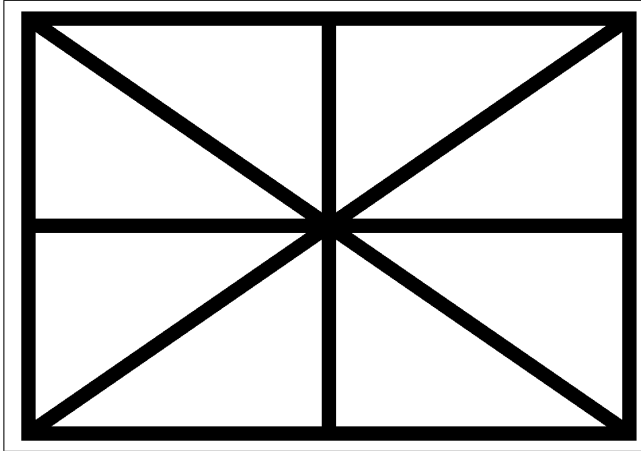
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## 10. ACKNOWLEDGMENTS

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