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first primitive Pythagorean triplets

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Synonym least coprime Pythagorean triplets

Related topic PythagorasTheorem

Related topic IncircleRadiusDeterminedByPythagoreanTriple
Related topic ContraharmonicMeansAndPythagoreanHypotenuses
Related topic PythagoreanHypotenusesAsContraharmonicMeans

Defines Egyptian triangle

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(odd \ cathetus)^2 + (even \ cathetus)^2 = (hypotenuse)^2
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3^2 + 4^2 = 5^2 (\leftarrow these form the so-called Egyptian triangle, known by the
pyramid builders)
5^2 + 12^2 = 13^2
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$$5^2 + 12^2 = 13^2$$

$$15^2 + 8^2 = 17^2$$

$$7^2 + 24^2 = 25^2$$

$$21^2 + 20^2 = 29^2$$

$$9^2 + 40^2 = 41^2$$

$$35^2 + 12^2 = 37^2$$

$$11^2 + 60^2 = 61^2$$

$$45^2 + 28^2 = 53^2$$

$$33^2 + 56^2 = 65^2$$

$$13^2 + 84^2 = 85^2$$

$$63^2 + 16^2 = 65^2$$

$$55^2 + 48^2 = 73^2$$

$$39^2 + 80^2 = 89^2$$

$$15^2 + 112^2 = 113^2$$

$$77^2 + 36^2 = 85^2$$

$$65^2 + 72^2 = 97^2$$

$$17^2 + 144^2 = 145^2$$

$$99^2 + 20^2 = 101^2$$

$$91^2 + 60^2 = 109^2$$

$$51^2 + 140^2 = 149^2$$

$$19^2 + 180^2 = 181^2$$

$$117^2 + 44^2 = 125^2$$

$$105^2 + 88^2 = 137^2$$

$$85^2 + 132^2 = 157^2$$

$$57^2 + 176^2 = 185^2$$

$$21^2 + 220^2 = 221^2$$

$$143^2 + 24^2 = 145^2$$

$$119^2 + 120^2 = 169^2$$

$$95^2 + 168^2 = 193^2$$

$$23^2 + 264^2 = 265^2$$

$$165^2 + 52^2 = 173^2$$

$$153^2 + 104^2 = 185^2$$

$$133^2 + 156^2 = 205^2$$

$$105^2 + 208^2 = 233^2$$

$$69^2 + 260^2 = 269^2$$
 $25^2 + 312^2 = 313^2$
 $195^2 + 28^2 = 197^2$
 $187^2 + 84^2 = 205^2$
 $171^2 + 140^2 = 221^2$
 $115^2 + 252^2 = 277^2$
 $75^2 + 308^2 = 317^2$
 $27^2 + 364^2 = 365^2$
 $221^2 + 60^2 = 229^2$
 $209^2 + 120^2 = 241^2$
 $161^2 + 240^2 = 289^2$
 $29^2 + 420^2 = 421^2$
 $255^2 + 32^2 = 257^2$
 $247^2 + 96^2 = 265^2$
 $231^2 + 160^2 = 281^2$
 $207^2 + 224^2 = 305^2$
 $175^2 + 288^2 = 337^2$
 $135^2 + 352^2 = 377^2$
 $87^2 + 416^2 = 425^2$
 $31^2 + 480^2 = 481^2$
 $285^2 + 68^2 = 293^2$
 $273^2 + 136^2 = 305^2$
 $253^2 + 204^2 = 325^2$
 $225^2 + 272^2 = 353^2$
 $189^2 + 340^2 = 389^2$
 $145^2 + 408^2 = 433^2$
 $93^2 + 476^2 = 485^2$
 $33^2 + 36^2 = 325^2$
 $299^2 + 180^2 = 349^2$
 $275^2 + 252^2 = 373^2$
 $203^2 + 396^2 = 445^2$
 $35^2 + 612^2 = 613^2$
 $357^2 + 76^2 = 365^2$
 $345^2 + 152^2 = 377^2$
 $325^2 + 228^2 = 397^2$
 $297^2 + 304^2 = 425^2$

$$261^{2} + 380^{2} = 461^{2}$$

$$217^{2} + 456^{2} = 505^{2}$$

$$165^{2} + 532^{2} = 557^{2}$$

$$105^{2} + 608^{2} = 617^{2}$$

$$37^{2} + 684^{2} = 685^{2}$$

$$399^{2} + 40^{2} = 401^{2}$$

$$391^{2} + 120^{2} = 409^{2}$$

$$351^{2} + 280^{2} = 449^{2}$$

$$319^{2} + 360^{2} = 481^{2}$$

$$279^{2} + 440^{2} = 521^{2}$$

$$231^{2} + 520^{2} = 569^{2}$$

$$111^{2} + 680^{2} = 689^{2}$$

$$39^{2} + 760^{2} = 761^{2}$$

$$437^{2} + 84^{2} = 445^{2}$$

$$425^{2} + 168^{2} = 457^{2}$$

$$377^{2} + 336^{2} = 505^{2}$$

$$341^{2} + 420^{2} = 541^{2}$$

$$185^{2} + 672^{2} = 697^{2}$$

$$41^{2} + 840^{2} = 841^{2}$$

$$483^{2} + 44^{2} = 485^{2}$$

$$475^{2} + 132^{2} = 493^{2}$$

$$459^{2} + 220^{2} = 509^{2}$$

$$435^{2} + 308^{2} = 533^{2}$$

$$403^{2} + 396^{2} = 565^{2}$$

$$315^{2} + 572^{2} = 653^{2}$$

$$259^{2} + 660^{2} = 709^{2}$$

$$195^{2} + 748^{2} = 773^{2}$$

$$123^{2} + 836^{2} = 845^{2}$$

$$43^{2} + 924^{2} = 925^{2}$$

$$525^{2} + 92^{2} = 533^{2}$$

$$513^{2} + 184^{2} = 545^{2}$$

$$493^{2} + 276^{2} = 565^{2}$$

$$465^{2} + 368^{2} = 593^{2}$$

$$429^{2} + 460^{2} = 629^{2}$$

$$385^{2} + 552^{2} = 673^{2}$$

$$333^{2} + 644^{2} = 725^{2}$$

$$273^{2} + 736^{2} = 785^{2}$$

$$205^{2} + 828^{2} = 853^{2}$$

$$129^{2} + 920^{2} = 929^{2}$$

$$45^{2} + 1012^{2} = 1013^{2}$$

$$575^{2} + 48^{2} = 577^{2}$$

$$551^{2} + 240^{2} = 601^{2}$$

$$527^{2} + 336^{2} = 625^{2}$$

$$455^{2} + 528^{2} = 697^{2}$$

$$407^{2} + 624^{2} = 745^{2}$$

$$287^{2} + 816^{2} = 865^{2}$$

$$215^{2} + 912^{2} = 937^{2}$$

$$47^{2} + 100^{2} = 629^{2}$$

$$609^{2} + 200^{2} = 641^{2}$$

$$589^{2} + 300^{2} = 661^{2}$$

$$561^{2} + 400^{2} = 689^{2}$$

$$481^{2} + 600^{2} = 769^{2}$$

$$429^{2} + 700^{2} = 821^{2}$$

$$369^{2} + 800^{2} = 881^{2}$$

$$301^{2} + 900^{2} = 949^{2}$$

$$141^{2} + 1100^{2} = 1109^{2}$$

$$49^{2} + 1200^{2} = 1201^{2}$$

$$675^{2} + 52^{2} = 677^{2}$$

$$667^{2} + 156^{2} = 685^{2}$$

$$651^{2} + 260^{2} = 701^{2}$$

$$627^{2} + 364^{2} = 725^{2}$$

$$595^{2} + 468^{2} = 757^{2}$$

$$555^{2} + 572^{2} = 797^{2}$$

$$451^{2} + 780^{2} = 901^{2}$$

$$387^{2} + 884^{2} = 965^{2}$$

$$315^{2} + 988^{2} = 1037^{2}$$

$$235^{2} + 1092^{2} = 1117^{2}$$

$$147^{2} + 1196^{2} = 1205^{2}$$

$$51^{2} + 1300^{2} = 1301^{2}$$

$$725^{2} + 108^{2} = 733^{2}$$

$$713^{2} + 216^{2} = 745^{2}$$

$$665^{2} + 432^{2} = 793^{2}$$

$$629^{2} + 540^{2} = 829^{2}$$

$$533^{2} + 756^{2} = 925^{2}$$

$$473^{2} + 864^{2} = 985^{2}$$

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329^2 + 1080^2 = 1129^2

245^2 + 1188^2 = 1213^2

53^2 + 1404^2 = 1405^2
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N.B. that the lengths of the even cathetus and the hypotenuse are consecutive integers (as 1404 and 1405) always when the corresponding seed numbers m and n (see the http://planetmath.org/PythagoreanTripletparent entry) are successive integers.