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definable type

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Defines	definable type
Defines	defining scheme

Let  $M$  be a first order structure. Let  $A$  and  $B$  be sets of parameters from  $M$ . Let  $p$  be a complete  $n$ -type over  $B$ . Then we say that  $p$  is an *A-definable* type iff for every formula  $\psi(\bar{x}, \bar{y})$  with  $\text{ln}(\bar{x}) = n$ , there is some formula  $d\psi(\bar{y}, \bar{z})$  and some parameters  $\bar{a}$  from  $A$  so that for any  $\bar{b}$  from  $B$  we have  $\psi(\bar{x}, \bar{b}) \in p$  iff  $M \models d\psi(\bar{b}, \bar{a})$ .

Note that if  $p$  is a type over the model  $M$  then this condition is equivalent to showing that  $\{\bar{b} \in M : \psi(\bar{x}, \bar{b}) \in p\}$  is an  $A$ -definable set.

For  $p$  a type over  $B$ , we say  $p$  is *definable* if it is  $B$ -definable.

If  $p$  is definable, we call  $d\psi$  the *defining formula* for  $\psi$ , and the function  $\psi \mapsto d\psi$  a defining scheme for  $p$ .