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Golomb's sequence

Canonical name GolombsSequence
Date of creation 2013-03-22 17:47:07
Last modified on 2013-03-22 17:47:07
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Last modified by PrimeFan (13766)

Numerical id 4

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Entry type Definition Classification msc 03E10

Synonym Golomb sequence
Synonym Silverman's sequence
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Golomb's sequence is a self-referential ascending order sequence of integers a in which the number of times each number n occurrs is given by a_n . The sequence begins 1, 2, 2, 3, 3, 4, 4, 4, 5, 5, 5, 6, 6, 6, 6, 7, 7, 7, 7, 8, 8, 8, 8, 9, 9, 9, 9, 10, 10, 10, 10, 10, ... (see A001462 in Sloane's OEIS). For example, $a_3 = 2$ and indeed 3 occurs twice in the sequence. $a_4 = 3$, so 4 occurs thrice.

The recurrence relation for the sequence is $a_1 = 1$ and $a_n = a_{n-a_{a_{n-1}}} + 1$. Sometimes recurrence relations for this sequence are given which also explicitly set $a_2 = 2$. The *n*th term of the sequence can be obtained by the calculating $\phi^{2-\phi}n^{\phi-1}$ (with

$$\phi = \frac{1 + \sqrt{5}}{2}$$

being the golden ratio) and rounding off to the nearest integer. For example, with precision to five decimal places: 1.20178, 1.84448, 2.36975, 2.83087, 3.24948, 3.63706, 4.0006, 4.34477, 4.67284, 4.98724, 5.28984, 5.58209, 5.86518, 6.14005, 6.40753, 6.66827, 6.92286, 7.17178, 7.41548, etc.