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finite

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Defines	finite set

A set S is *finite* if there exists a natural number n and a bijection from S to n. Note that we are using the set theoretic definition of natural number, under which the natural number n equals the set $\{0, 1, 2, \ldots, n-1\}$. If there exists such an n, then it is unique, and we call n the *cardinality* of S.

Equivalently, a set S is finite if and only if there is no bijection between S and any proper subset of S.