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ordinal number

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An ordinal number is a well ordered set S such that, for every $x \in S$,

$$x = \{z \in S \mid z < x\}$$

(where $<$ is the ordering relation on S).

It follows immediately from the definition that every ordinal is a transitive set. Also note that if $a, b \in S$ then we have $a < b$ if and only if $a \in b$.

There is a theory of ordinal arithmetic which allows construction of various ordinals. For example, all the numbers $0, 1, 2, \dots$ have natural interpretations as ordinals, as does the set of natural numbers (including 0), which in this context is often denoted by ω , and is the first infinite ordinal.