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upward Lowenheim-Skolem theorem

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Let  $L$  be a first-order language and let  $\mathcal{A}$  be an infinite  $L$ -structure. Then if  $\kappa$  is a cardinal with  $\kappa \geq \text{Max}(|\mathcal{A}|, |L|)$  then there is an  $L$ -structure  $\mathcal{B}$  such that  $|\mathcal{B}| = \kappa$  and  $\mathcal{A} \preccurlyeq \mathcal{B}$ .