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generalized continuum hypothesis

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The *generalized continuum hypothesis* states that for any infinite cardinal λ there is no cardinal κ such that $\lambda < \kappa < 2^\lambda$.

An equivalent condition is that $\aleph_{\alpha+1} = 2^{\aleph_\alpha}$ for every ordinal α . Another equivalent condition is that $\aleph_\alpha = \beth_\alpha$ for every ordinal α .

Like the continuum hypothesis, the generalized continuum hypothesis is known to be independent of the axioms of ZFC.