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maximality principle

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Let S be a collection of sets. If, for each chain $C \subseteq S$, there exists an $X \in S$ such that every element of C is a subset of X , then S contains a maximal element. This is known as the *maximality principle*.

The maximality principle is equivalent to the axiom of choice.