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 $Z_2$ 

Canonical name Z2

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Synonym Z Synonym Z2

Defines second order arithmetic

 $Z_2$  is the full system of second order arithmetic, that is, the full theory of numbers and sets of numbers. It is sufficient for a great deal of mathematics, including much of number theory and analysis.

The axioms defining successor, addition, multiplication, and comparison are the same as those of PA.  $\mathbb{Z}_2$  adds the full induction axiom and the full comprehension axiom.