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filter basis

Canonical name FilterBasis

Date of creation 2013-03-22 14:41:34 Last modified on 2013-03-22 14:41:34

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Numerical id 11

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Entry type Definition
Classification msc 03E99
Classification msc 54A99
Synonym filter base
Defines filter subbasis
Defines equivalent

A filter subbasis for a set S is a collection of subsets of S which has the finite intersection property.

A filter basis B for a set S is a non-empty collection of subsets of S which does not contain the empty set such that, for every $u \in B$ and every $v \in B$, there exists a $w \in B$ such that $w \subset u \cap v$.

Given a filter basis B for a set S, the set of all supersets of elements of B forms a filter on the set S. This filter is known as the filter generated by the basis.

Given a filter subbasis B for a set S, the set of all supersets of finite intersections of elements of B is a filter. This filter is known as the filter generated by the subbasis.

Two filter bases are said to be *equivalent* if they generate the same filter. Likewise, two filter subbases are said to be equivalent if they generate the same filter.

Note: Not every author requires that filters do not contain the empty set. Because every filter is a filter basis then accordingly some authors allow that a filter base can contain the empty set.