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## inclusion mapping

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**Definition** Let  $X$  be a subset of  $Y$ . Then the **inclusion map** from  $X$  to  $Y$  is the mapping

$$\begin{aligned}\iota : X &\rightarrow Y \\ x &\mapsto x.\end{aligned}$$

In other words, the inclusion map is simply a fancy way to say that every element in  $X$  is also an element in  $Y$ .

To indicate that a mapping is an inclusion mapping, one usually writes  $\hookrightarrow$  instead of  $\rightarrow$  when defining or mentioning an inclusion map. This hooked arrow symbol  $\hookrightarrow$  can be seen as combination of the symbols  $\subset$  and  $\rightarrow$ . In the above definition, we have not used this convention. However, examples of this convention would be:

- Let  $\iota : X \hookrightarrow Y$  be the inclusion map from  $X$  to  $Y$ .
- We have the inclusion  $S^n \hookrightarrow \mathbb{R}^{n+1}$ .