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## index set theorem

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Index Set Theorem: If A is an index set and  $A \neq \emptyset, \omega$ , then either  $K \leq_1 A$  or  $K \leq_1 A^{\complement}$ .

In the statement of the theorem, K is the halting set  $\{x : \varphi_x(x) converges\}$ ,  $\leq_1$  is the one-one reducibility (or 1-reducibility) relation symbol, and  $A^{\complement}$ stands for the complement of the set A (relative to  $\omega$ ).