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ordered integral domain with well-ordered
positive elements

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Theorem. If (R, \leq) is an <http://planetmath.org/OrderedRingordered> integral domain and if the set $R_+ = \{r \in R : 0 < r\}$ of its <http://planetmath.org/PositivityIn> elements is well-ordered, then R and R_+ can be expressed as sets of multiples of the unity as follows:

- $R = \{m \cdot 1 : m \in \mathbb{Z}\},$
- $R_+ = \{n \cdot 1 : n \in \mathbb{Z}_+\}.$

The theorem may be interpreted so that such an integral domain is isomorphic with the ordered ring \mathbb{Z} of rational integers.