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infimum and supremum of sum and product

 ${\bf Canonical\ name} \quad {\bf Infimum And Supremum Of Sum And Product}$

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Suppose that the real functions f and g are defined on an interval $\Delta.$ Then on this interval

- $\inf(f+g) \ge \inf f + \inf g$
- $\sup(f+g) \le \sup f + \sup g$

If f and g are also nonnegative on Δ , we can write

- $\bullet \ \inf(fg) \ \geqq \ \inf f \cdot \inf g$
- $\sup(fg) \leq \sup f \cdot \sup g$