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Euclidean field

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Related topic ConstructibleNumbers Related topic EuclideanNumberField

Defines Euclidean

An ordered field F is Euclidean if every non-negative element a $(a \ge 0)$ is a square in F (there exists $b \in F$ such that $b^2 = a$).

1 Examples

- \mathbb{R} is Euclidean.
- \mathbb{Q} is not Euclidean because 2 is not a square in \mathbb{Q} (http://planetmath.org/lei.e., $\pm \sqrt{2} \notin \mathbb{Q}$).
- ullet C is not a Euclidean field because http://planetmath.org/MathbbCIsNotAnOrderedFieldC is not an ordered field.
- The http://planetmath.org/ConstructibleNumbersfield of real constructible numbers is Euclidean.

A Euclidean field is an ordered Pythagorean field. There are ordered fields that are Pythagorean but not Euclidean.