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## inverse number

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Defines reciprocal number

The *inverse number* or *reciprocal number* of a non-zero real or complex number a may be denoted by  $a^{-1}$ , and it the quotient  $\frac{1}{a}$  (so, it is really the -1<sup>th</sup> power of a).

- Two numbers are inverse numbers of each other if and only if their product is equal to 1 (cf. opposite inverses).
- If  $a \neq 0$  is given in a quotient form  $\frac{b}{c}$ , then its inverse number is simply

$$\left(\frac{b}{c}\right)^{-1} = \frac{c}{b}.$$

• Forming the inverse number is also a multiplicative function, i.e.

$$(bc)^{-1} = b^{-1}c^{-1}$$

(to be more precise, it is an automorphism of the multiplicative group of  $\mathbb R$  resp.  $\mathbb C$ ).