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zero divisor

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Related topic	CancellationRing
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Related topic	Unity
Defines	left zero divisor
Defines	right zero divisor
Defines	regular element

Let  $a$  be a nonzero element of a ring  $R$ .

The element  $a$  is a *left zero divisor* if there exists a nonzero element  $b \in R$  such that  $a \cdot b = 0$ . Similarly,  $a$  is a *right zero divisor* if there exists a nonzero element  $c \in R$  such that  $c \cdot a = 0$ .

The element  $a$  is said to be a *zero divisor* if it is both a left and right zero divisor. A nonzero element  $a \in R$  is said to be a *regular element* if it is neither a left nor a right zero divisor.

**Example:** Let  $R = \mathbb{Z}_6$ . Then the elements 2 and 3 are zero divisors, since  $2 \cdot 3 \equiv 6 \equiv 0 \pmod{6}$ .