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**commutative ring**

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Let  $(X, +, \cdot)$  be a ring. Since  $(X, +)$  is required to be an abelian group, the operation “+” necessarily is commutative.

This needs not to happen for “ $\cdot$ ”. Rings  $R$  where “ $\cdot$ ” is commutative, that is,  $x \cdot y = y \cdot x$  for all  $x, y \in R$ , are called commutative rings.

The commutative rings are rings which are more like the fields than other rings are, but there are certain dissimilarities. A field has always a multiplicative inverse for each of its nonzero elements, but the same needs not to be true for a commutative ring. Further, in a commutative ring there may exist zero divisors, i.e. nonzero elements having product zero. Since the ideals of a commutative ring are <http://planetmath.org/Ideals> two-sided, the these rings are more comfortable to handle than other rings.

The study of commutative rings is called *commutative algebra*.