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**integral**

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Let  $B$  be a ring with a subring  $A$ . We will assume that  $A$  is contained in the center of  $B$  (in particular,  $A$  is commutative). An element  $x \in B$  is *integral* over  $A$  if there exist elements  $a_0, \dots, a_{n-1} \in A$  such that

$$x^n + a_{n-1}x^{n-1} + \dots + a_1x + a_0 = 0.$$

The ring  $B$  is *integral* over  $A$  if every element of  $B$  is integral over  $A$ .