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affine algebraic group

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An affine algebraic group over a field k is quasi-affine variety G (a locally closed subset of affine space) over k, which is a equipped with a group—such that the multiplication map $m: G \times G \to G$ and inverse map $i: G \to G$ are algebraic.

For example, k is an affine algebraic group over itself with the group law being addition, and as is $k^* = k - \{0\}$ with the group law multiplication. Other common examples of affine algebraic groups are GL_nk , the general linear group over k (identifying matrices with affine space) and any algebraic torus over k.