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isomorphism of varieties

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**Definition 1.** *Let  $V_1$  and  $V_2$  be algebraic varieties. We say that  $V_1$  and  $V_2$  are isomorphic, and write  $V_1 \cong V_2$ , if there are regular maps*

$$\phi: V_1 \rightarrow V_2, \quad \psi: V_2 \rightarrow V_1$$

*such that the compositions  $\psi \circ \phi$  and  $\phi \circ \psi$  are the identity maps on  $V_1$  and  $V_2$  respectively.*

**Definition 2.** *Let  $V_1$  and  $V_2$  be varieties defined over a field  $K$ . We say that  $V_1/K$  and  $V_2/K$  are isomorphic over  $K$  if  $V_1$  and  $V_2$  are isomorphic as in Definition 1 and the regular maps  $\phi$  and  $\psi$  can be defined over  $K$ .*