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example of trace of a matrix

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$$\text{Let } A = \begin{bmatrix} 2 & 4 & 6 \\ 8 & 10 & 12 \\ 14 & 16 & 18 \end{bmatrix}, A' = \frac{1}{2}A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \text{ and } B = \begin{bmatrix} 9 & 8 & 7 \\ 6 & 5 & 4 \\ 3 & 2 & 1 \end{bmatrix}$$

then

$$\begin{aligned} \text{trace}(A + B) &= \text{trace}(A) + \text{trace}(B) \\ &= (2 + 10 + 18) + (9 + 5 + 1) \\ &= 45 \end{aligned}$$

$$\begin{aligned} \text{trace}(A) &= \text{trace}(2A') \\ &= 2 \cdot \text{trace}(A') \\ &= 2 \cdot \text{trace} \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \\ &= 2 \cdot (1 + 5 + 9) \\ &= 30 \end{aligned}$$