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Schur decomposition

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If A is a complex square matrix of order n (*i.e.* $A \in \text{Mat}_n(\mathbb{C})$), then there exists a unitary matrix $Q \in \text{Mat}_n(\mathbb{C})$ such that

$$Q^H A Q = T = D + N$$

where H is the conjugate transpose, $D = \text{diag}(\lambda_1, \dots, \lambda_n)$ (*the λ_i are eigenvalues of A*), and $N \in \text{Mat}_n(\mathbb{C})$ is strictly upper triangular matrix. Furthermore, Q can be chosen such that the eigenvalues λ_i appear in any order along the diagonal. [?]

References

[GVL] Golub, H. Gene, Van Loan F. Charles: Matrix Computations (*Third Edition*). The Johns Hopkins University Press, London, 1996.