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commuting matrices are simultaneously  
triangularizable

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**Theorem 1.** *All matrices in the below are complex  $n \times n$  matrices.  
Let  $A, B$  be matrices and  $AB = BA$ . Then there exists a unitary matrix  $Q$   
such that*

$$Q^H A Q = T_1, Q^H B Q = T_2$$

*where  $^H$  is the conjugate transpose and  $T_1, T_2$ , are upper triangular matrices.*