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linear isomorphism

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Synonym invertible linear map Synonym bijective linear map Synonym non-singular linear map **Definition 1.** Suppose V and W are vector spaces and $L: V \to W$ is a linear map. Then L is a linear isomorphism if L is bijective.

Properties

- 1. Compositions and of linear isomorphisms is a linear isomorphism.
- 2. The inverse of a linear isomorphisms is a linear isomorphism.
- 3. If either V or W if finite dimensional, then $\dim V = \dim W$. (This is a consequence of the rank-nullity theorem.)