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Riesz' Lemma

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Let E be a normed space, $S \subset E$ a closed proper vector subspace, and $0 < \alpha < 1$. Then there is $x_{\alpha} \in E \setminus S$ such that $||x_{\alpha}|| = 1$ and $||s - x_{\alpha}|| > \alpha$ for every $s \in S$.