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PID

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Entry type	Definition
Classification	msc 16D25
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Synonym	principal ideal domain
Related topic	UFD
Related topic	Irreducible
Related topic	Ideal
Related topic	IntegralDomain
Related topic	EuclideanRing
Related topic	EuclideanValuation
Related topic	ProofThatAnEuclideanDomainIsAPID
Related topic	WhyEuclideanDomains

A *principal ideal domain* is an integral domain where every ideal is a principal ideal.

In a PID, an ideal (p) is maximal if and only if p is irreducible (and prime since <http://planetmath.org/PIDsAreUFDs> any PID is also a UFD).

Note that subrings of PIDs are not necessarily PIDs. (There is an example of this within the entry biquadratic field.)