

planetmath.org

Math for the people, by the people.

perfect and semiperfect rings

Canonical name PerfectAndSemiperfectRings

Date of creation 2013-03-22 19:17:56 Last modified on 2013-03-22 19:17:56

Owner joking (16130) Last modified by joking (16130)

Numerical id 4

Author joking (16130) Entry type Definition Classification msc 16D40 A ring R is called **left/right perfect** if for any left/right R-module M there exists a projective cover $p: P \to M$.

A ring R is called **left/right semiperfect** if for any left/right finitely-generated R-module M there exists a projective cover $p: P \to M$.

It can be shown that there are rings which are left perfect, but not right perfect. However being semiperfect is left-right symmetric property.

Some examples of semiperfect rings include:

- 1. perfect rings;
- 2. left/right Artinian rings;
- 3. finite-dimensional algebras over a field k.