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## Borel subgroup

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Author CWoo (3771) Entry type Definition Classification msc 17B20 Let  $G = \operatorname{GL}_n\mathbb{C}$ , the group of all automorphisms of the *n*-dimensional vector space over the field of complex numbers  $\mathbb{C}$ , and  $H \leq G$  a subgroup of G. The *standard Borel subgroup* of H is the subgroup of H consisting of all upper triangular matrices (in H). A *Borel subgroup* of H is a conjugate (in H) of the standard Borel subgroup of H.

The notion of a Borel subgroup can be generalized. Let G be a complex semi-simple Lie group. Then any maximal solvable subgroup  $B \leq G$  is called a Borel subgroup. All Borel subgroups of a given group are conjugate. Any Borel group is connected and equal to its own normalizer, and contains a unique Cartan subgroup. The intersection of B with a maximal compact subgroup K of G is the maximal torus of K.