

A Lie algebra \mathfrak{g} is semi-simple if and only if its Killing form $B_{\mathfrak{g}}$ is nondegenerate.