

Let \mathfrak{g} be a finite dimensional complex solvable Lie algebra, and V a representation of \mathfrak{g} . Then there exists an element of V which is a simultaneous eigenvector for all elements of \mathfrak{g} .

Applying this result inductively, we find that there is a basis of V with respect to which all elements of \mathfrak{g} are upper triangular.