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quantum geometry

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Defines	a mathematical approach to quantum gravity based on noncommutative geom

Description: *Quantum geometry (or quantum geometries)* are approaches to Quantum Gravity based on either noncommutative geometry and SUSY (the ‘Standard’ Model of current Physics) [?, ?] or modified or ‘deformed’ Riemannian, ‘quantum’ geometry, with additional assumptions regarding a generalized ‘Dirac’ operator, the ‘spectral triplet’ with non-Abelian structures of quantized space-times.

Remarks. Other approaches to Quantum Gravity include: Loop Quantum Gravity (LQG), AQFT approaches, Topological Quantum Field Theory (TQFT)/ Homotopy Quantum Field Theories (HQFT; Tureaev and Porter, 2005), Quantum Theories on a Lattice (QTL), string theories and spin network models.

An interesting, but perhaps limiting approach, involves ‘*quantum*’ *Riemannian geometry* [?] in place of the classical Riemannian manifold that is employed in the well-known, Einstein’s classical approach to General Relativity (GR).

References

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- [2] Connes, A. 1985 .Non-commutative differential geometry I–II. *Publication Mathématiques IHES*, **62**, 41–144.
- [3] Abhay Ashtekar and Jerzy Lewandowski. 2005. Quantum Geometry and Its Applications. <http://cgpg.gravity.psu.edu/people/Ashtekar/articles/qgfinal.pdf> Available PDF download.