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## quantum category

Canonical name QuantumCategory
Date of creation 2013-03-22 18:16:52
Last modified on 2013-03-22 18:16:52

Owner bci1 (20947) Last modified by bci1 (20947)

Numerical id 30

Author bci1 (20947)
Entry type Definition
Classification msc 18-00
Classification msc 81P05
Classification msc 81P10

Synonym quantum groupoid category

Related topic QuantumGroupoids2 Related topic QuantumGroups

Related topic QuantumAutomataAndQuantumComputation2

Related topic QuantumTopos

Defines quantum groupoid homomorphism

Defines quantum category objects

Defines quantum category with Haar measures

**Definition 0.1.** A quantum category  $\mathcal{Q}$  is defined as the (non-Abelian) category of quantum groupoids,  $[Q_{\mathsf{G}}]_i$ , and quantum groupoid homomorphisms,  $[q_{\mathsf{G}}]_{ij}$ , where i and j are indices in an index class,  $\mathbf{I}$ , all subject to the usual ETAC axioms and their interpretations.

**Remark 0.1.** The category of quantum groupoids,  $[Q_{\mathsf{G}}]_i$ , is trivially a subcategory of the groupoid category, that can also be regarded as a functor category, or 2-category, if  $\mathsf{G}$  is small, that is, if  $G^0$  is a set rather than a class.

**Remark 0.2.** One notes that an alternative definition of quantum category has also been reported in physical mathematics as a rigid monoidal category, or its equivalent. A more general definition of *quantum category* is however necessary that has both quantum groups and locally compact quantum groupoids as particular cases. This would require a notion of quantum compactness in a category as well as the definition of associated Haar systems to a category.

## References

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