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index of category theory

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# 1 Foundations

## 1.1 Basic Definitions

1. category theory
2. precategory
3. category
4. alternative definition of category
5. subcategory
6. automorphism
7. commutative diagram
8. concrete category
9. dual category
10. duality principle
11. endomorphism
12. epi
13. monic
14. extremal monomorphism
15. source
16. sink
17. initial source
18. final sink
19. isomorphism-closed subcategory
20. locally finite category
21. preimage of category
22. product of categories
23. types of morphisms
24. wellpowered category
25. zero object
26. <http://planetmath.org/node/5658>U-small
27. equalizer
28. subobject
29. quotient object
30. categorical direct product
31. categorical direct sum
32. categorical pullback
33. direct limit
34. limiting cone
35. complete category
36. groupoid (category theoretic)

## 1.2 Maps of Categories

1. functor
2. autofunctor
3. category isomorphism
4. diagonal functor
5. endofunctor
6. forgetful functor
7. identity functor
8. isomorphism
9. multifunctor
10. natural transformation
11. essentially surjective
12. faithful functor
13. full functor
14. natural equivalence
15. adjoint functor
16. equivalence of categories
17. <http://planetmath.org/CategoryIsomorphism>  
categories
18. universal property
19. representable functor
20. Equivalent definition of a Representable Functor
21. simplicial object

## 1.3 Fundamental Theorems

1. properties of monomorphisms and epimorphisms
2. properties of regular and extremal monomorphisms
3. monomorphisms are pullback stable
4. proof that an equalizer is a monomorphism
5. Yoneda lemma
6. categorical direct product is an inverse limit
7. kernel is an inverse limit

## 1.4 Examples of Categories

1. discrete category
2. category example (arrow category)
3. category associated to a partial order
4. category of matrices
5. Category of pseudomorphisms
6. Category of intermorphisms
7. examples of initial objects and terminal objects and zero objects

8. category of sets	5. exact sequence
9. monomorphisms of category of sets	6. exact functor
10. monoid as a category	7. Grothendieck spectral sequence
11. comma category	8. enough projectives
12. category of pointed topological spaces	9. enough injectives
13. simplicial category	10. projective object
	11. injective object
	12. derived functor
<b>1.5 Micellaneous</b>	13. derived category
1. algebra formed from a category	14. Algebraic K-theory
2. monad	15. examples of algebraic K-theory groups
3. comonad	16. Grothendieck group
4. monoidal category	17. delta functor
5. group object	18. horseshoe lemma
6. nerve	19. syzygy
	20. Ext
<b>2 Additive Categories and Homology</b>	21. Tor
1. preadditive category	22. projective dimension
2. additive category	23. 5-lemma
3. Abelian category	24. proof of 5-lemma
4. supplemental axioms for an Abelian category	25. 9-lemma
	26. snake lemma
	27. <a href="http://planetmath.org/ProofOfSnakeLemmaproof">http://planetmath.org/ProofOfSnakeLemmaproof</a> of snake lemma

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|---------------------------------|---------------------------|
| 28. chain homotopy              | 5. stalk                  |
| 29. chain homotopy equivalence  | 6. Étale space            |
| 30. chain map                   | 7. resolution of a sheaf  |
| 31. homology of a chain complex | 8. site                   |
| 32. Leray spectral sequence     | 9. small site on a scheme |
| 33. spectral sequence           | 10. topos                 |

### **3 Sheaves, Topoi, and the like**

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|------------------------------------|-------------------------------|
| 1. presheaf                        | 11. cosmos                    |
| 2. sheaf                           | 12. subobject classifier      |
| 3. sheafification                  | 13. well-pointed topos        |
| 4. presheaf of a topological basis | 14. power object              |
|                                    | 15. natural numbers object    |
|                                    | 16. Cartesian closed category |
|                                    | 17. exponential object        |