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essential monomorphism

 ${\bf Canonical\ name} \quad {\bf Essential Monomorphism}$

Date of creation 2013-03-22 18:27:30 Last modified on 2013-03-22 18:27:30

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Numerical id 9

Author jocaps (12118) Entry type Definition Classification msc 18A20

Synonym essential extension Related topic essential extension

Defines essential monomorphism

Let $\mathcal C$ be a category and $A,B\in \mathrm{Ob}(\mathcal C)$. Then a monomorphism $f\in \mathcal C(A,B)$ is said to be an essential extension (or essential monomorphism) iff .

If $g \in \mathcal{C}(B,C)$ be such that $g \circ f : A \to B \to C$ is a monomorphism then g is a monomorphism.

Some examples:

- Consider the category of commutative rings. One way to redefine essential extension in this category is in the following way:
 - If A is a subring of another ring B then B is an essential extension of A iff for any $b \in B \setminus \{0\}$ there exists a $c \in B$ such that $bc \in A \setminus \{0\}$.
- In the category of modules see http://planetmath.org/EssentialSubmoduleessential submodules.
- In the category of groups see essential subgroups.