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categorical diagrams as functors

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0.1 Introduction: categorical diagrams defined by functors

Any *categorical diagram* can be defined *via* a corresponding functor (associated with a diagram as shown by Mitchell, 1965, in ref. [?]). Such functors associated with diagrams are very useful in the categorical theory of representations as in the case of <http://planetmath.org/CategoricalAlgebra>. As a particularly useful example in (commutative) homological algebra let us consider the case of an exact categorical sequence that has a correspondingly defined *exact functor* introduced for example in Abelian category theory.

0.2 Examples

Consider a scheme Σ as defined in ref. [?]. Then one has the following short list of important examples of diagrams and functors:

1. Diagrams of adjoint situations: Adjoint functors
2. Equivalence of categories
3. Natural equivalence diagrams
4. Diagrams of natural transformations
5. Category of diagrams and 2-functors
6. Monad on a category

References

- [1] Barry Mitchell., *Theory of Categories.*, Academic Press: New York and London (1965), pp.65-70.