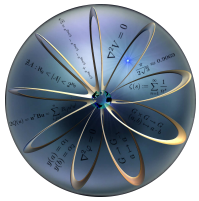

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example of universe

Canonical name	ExampleOfUniverse
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The simplest example of a universe consists of all sets gotten by starting with the empty set and repeatedly aggregating sets already known to lie in the universe. That is to say, starting with $\emptyset$, we first form $\{\emptyset\}$. Given these two elements of our universe, we can then form $\{\{\emptyset\}\}$ and $\{\emptyset, \{\emptyset\}\}$. Given these four elements, we then can form $\{\{\{\emptyset\}\}\}$, $\{\emptyset, \{\{\emptyset\}\}\}$, $\{\{\emptyset, \{\emptyset\}\}\}$ and several other sets. We can repeat this process to obtain an infinite collection of finite sets.

The set considered here also happens to be the set V_ω in the cumulative hierarchy.