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extended mean-value theorem

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Related topic	MeanValueTheorem

Let  $f : [a, b] \rightarrow \mathbb{R}$  and  $g : [a, b] \rightarrow \mathbb{R}$  be continuous on  $[a, b]$  and differentiable on  $(a, b)$ . Then there exists some number  $\xi \in (a, b)$  satisfying:

$$(f(b) - f(a))g'(\xi) = (g(b) - g(a))f'(\xi).$$

If  $g$  is linear this becomes the usual mean-value theorem.