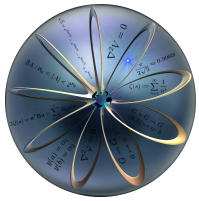

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Minkowski inequality

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If $p \geq 1$ and a_k, b_k are real numbers for $k = 1, \ldots,$ then

$$\left(\sum_{k=1}^{n} |a_k + b_k|^p \right)^{1/p} \leq \left(\sum_{k=1}^{n} |a_k|^p \right)^{1/p} + \left(\sum_{k=1}^{n} |b_k|^p \right)^{1/p}$$

The Minkowski inequality is in fact valid for all L^p norms with $p \geq 1$ on arbitrary measure spaces. This covers the case of $\mathbb{R}^n$ listed here as well as spaces of sequences and spaces of functions, and also complex L^p spaces.