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## complex mean-value theorem

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**Theorem** [?] Suppose  $\Omega$  is an open convex set in  $\mathbb{C}$ , suppose  $f$  is a holomorphic function  $f : \Omega \rightarrow \mathbb{C}$ , and suppose  $a, b$  are distinct points in  $\Omega$ . Then there exist points  $u, v$  on  $L_{ab}$  (the straight line connecting  $a$  and  $b$  not containing the endpoints), such that

$$\Re\left\{\frac{f(b) - f(a)}{b - a}\right\} = \Re\{f'(u)\},$$

$$\Im\left\{\frac{f(b) - f(a)}{b - a}\right\} = \Im\{f'(v)\},$$

where  $\Re$  and  $\Im$  are the <http://planetmath.org/RealPart> real and imaginary parts of a complex number, respectively.

## References

- [1] J.-Cl. Evard, F. Jafari, *A Complex Rolle's Theorem*, American Mathematical Monthly, Vol. 99, Issue 9, (Nov. 1992), pp. 858-861.