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proof of sum rule

Canonical name	ProofOfSumRule
Date of creation	2013-03-22 12:28:13
Last modified on	2013-03-22 12:28:13
Owner	mathcam (2727)
Last modified by	mathcam (2727)
Numerical id	5
Author	mathcam (2727)
Entry type	Proof
Classification	msc 26A24
Related topic	Derivative
Related topic	FixedPointsOfNormalFunctions

$$\begin{aligned}
\frac{d}{dx} [f(x) + g(x)] &= \lim_{h \rightarrow 0} \frac{f(x+h) + g(x+h) - f(x) - g(x)}{h} \\
&= \lim_{h \rightarrow 0} \left[ \frac{f(x+h) - f(x)}{h} + \frac{g(x+h) - g(x)}{h} \right] \\
&= f'(x) + g'(x)
\end{aligned}$$