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## measurable space

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Defines measurable set

A measurable space is a set E together with a collection  $\mathcal{B}$  of subsets of E which is a sigma algebra.

The elements of  $\mathcal{B}$  are called *measurable sets*.

A measurable space is the correct object on which to define a measure;  $\mathcal{B}$  will be the collection of sets which actually have a measure. We normally want to ensure that  $\mathcal{B}$  contains all the sets we will ever want to use. We usually cannot take  $\mathcal{B}$  to be the collection of all subsets of E because the axiom of choice often allows one to construct sets that would lead to a contradiction if we gave them a measure (even zero). For the real numbers, Vitali's theorem states that  $\mathcal{B}$  cannot be the collection of all subsets if we hope to have a measure that returns the length of an open interval.