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## Fatou's lemma

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If  $f_1, f_2, \dots$  is a sequence of nonnegative measurable functions in a measure space  $X$ , then

$$\int_X \liminf_{n \rightarrow \infty} f_n \leq \liminf_{n \rightarrow \infty} \int_X f_n$$