

example of conformal mapping

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 ${\it Related topic} \qquad {\it Category Of Riemannian Manifolds}$

Consider the four curves $A = \{t\}$, $B = \{t+it\}$, $C = \{it\}$ and $D = \{-t+it\}$, $t \in [-10,10]$. Suppose there is a mapping $f : \mathbb{C} \mapsto \mathbb{C}$ which maps A to D and B to C. Is f conformal at $z_0 = 0$? The size of the angles between A and B at the point of intersection $z_0 = 0$ is preserved, however the orientation is not. Therefore f is not conformal at $z_0 = 0$. Now suppose there is a function $g : \mathbb{C} \mapsto \mathbb{C}$ which maps A to C and B to D. In this case we see not only that the size of the angles is preserved, but also the orientation. Therefore g is conformal at $z_0 = 0$.