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## pole

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Related topic EssentialSingularity

Defines simple pole befines simple

Let  $U \subset \mathbb{C}$  be a domain and let  $a \in \mathbb{C}$ . A function  $f: U \to \mathbb{C}$  has a *pole* at a if it can be represented by a Laurent series centered about a with only finitely many terms of negative exponent; that is,

$$f(z) = \sum_{k=-n}^{\infty} c_k (z-a)^k$$

in some nonempty deleted neighborhood of a, with  $c_{-n} \neq 0$ , for some  $n \in \mathbb{N}$ . The number n is called the *order* of the pole. A *simple pole* is a pole of order 1