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biharmonic equation

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Definition. 1. A real-valued function $V: \mathbb{R}^n \rightarrow \mathbb{R}$ of <http://planetmath.org/http://planetmath.org> C^4 , and satisfying the equation

$$\nabla^4 V = 0, \tag{1}$$

also defines a biharmonic function, and (1) is called the biharmonic equation. Biharmonic operator is defined as

$$\nabla^4 := \sum_{k=1}^n \frac{\partial^4}{\partial x_k^4} + 2 \sum_{k=1}^{n-1} \sum_{l=k+1}^n \frac{\partial^4}{\partial x_k^2 \partial x_l^2}.$$