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## tube domain

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Author jirka (4157) Entry type Definition Classification msc 32A07 **Definition.** Suppose  $S \subset \mathbb{R}^n$  is an open set (usually connected), then we define

$$T_S := \{ z \in \mathbb{C}^n \mid \operatorname{Re} z \in S \}.$$

We call  $T_S$  the *tube domain* associated to S.

Basically the idea is that these domains give you complete freedom in the imaginary coordinates. An interesting fact about these domains is that  $T_S$  is pseudoconvex if and only if  $T_S$  is convex in the geometric sense, and this is true if and only if S itself is convex.

## References

[1] Steven G. Krantz. , AMS Chelsea Publishing, Providence, Rhode Island, 1992.