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generating function for the reciprocal
alternating central binomial coefficients

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It is also not very well known this relation:

$$\frac{4 \left(\sqrt{x+4} - \sqrt{x} \operatorname{arcsinh}\left(\frac{\sqrt{x}}{2}\right) \right)}{\sqrt{(x+4)^3}} = 1 - \frac{x}{2} + \frac{x^2}{6} - \frac{x^3}{20} + \frac{x^4}{70} - \frac{x^5}{252} + \frac{x^6}{924} - \dots$$

where one clearly appreciate that the function on LHS generates the sequence $(-1)^n \binom{2n}{n}^{-1}$.

To obtain the relation above one should use some kind of software because for the function is “terrible” to calculate derivatives of any order. It is a little challenge to give a recursive formula that gives the inverses of these alternating central binomial numbers, when evaluated at $x = 0$ at those derivatives.