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## irreducible component

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Defines reducible analytic variety

Let  $G \subset \mathbb{C}^N$  be an open set.

**Definition.** A locally analytic set (or an analytic variety)  $V \subset G$  is said to be *irreducible* if whenever we have two locally analytic sets  $V_1$  and  $V_2$  such that  $V = V_1 \cup V_2$ , then either  $V = V_1$  or  $V = V_2$ . Otherwise V is said to be . A maximal irreducible subvariety of V is said to be an *irreducible component* of V. Sometimes irreducible components are called *ircomps*.

Note that if V is an analytic variety in G, then a subvariety W is an irreducible component of V if and only if  $W^*$  (the set of regular points of W) is a connected complex analytic manifold. This means that the irreducible components of V are the closures of the connected components of  $V^*$ .

## References

[1] Hassler Whitney. Addison-Wesley, Philippines, 1972.