

Mecânica dos Sólidos

Cargas combinadas

Vasos de pressão de paredes finas

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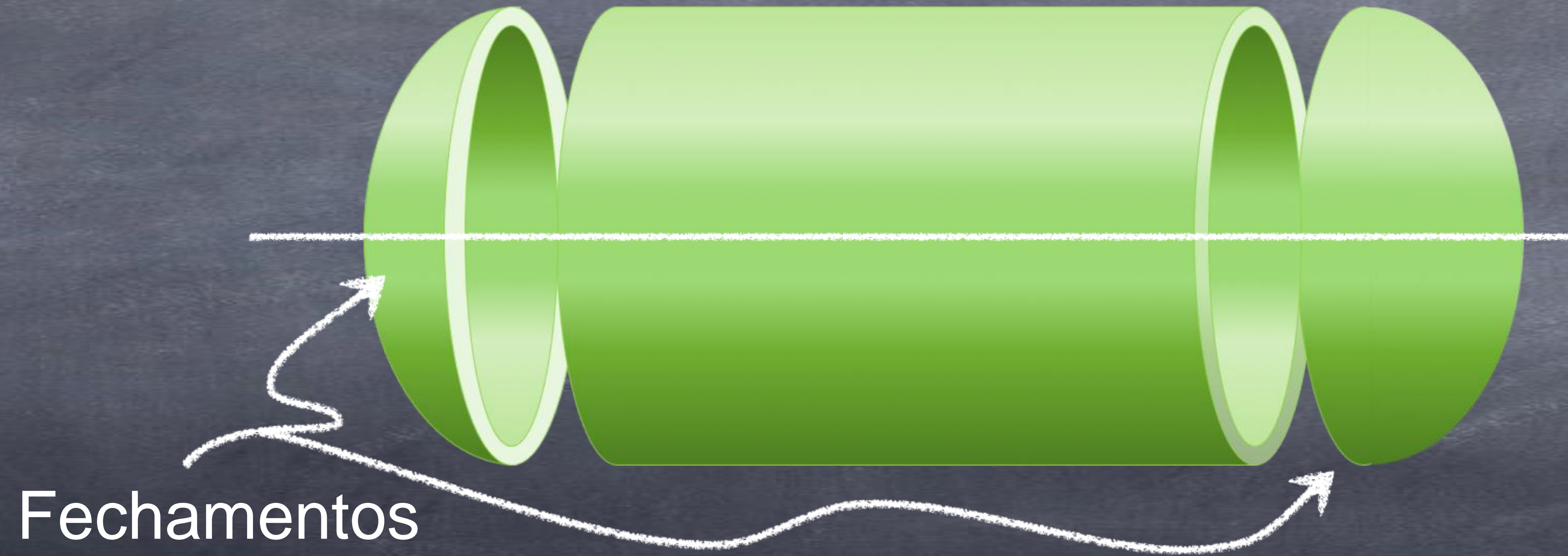
Vasos de pressão de paredes finas



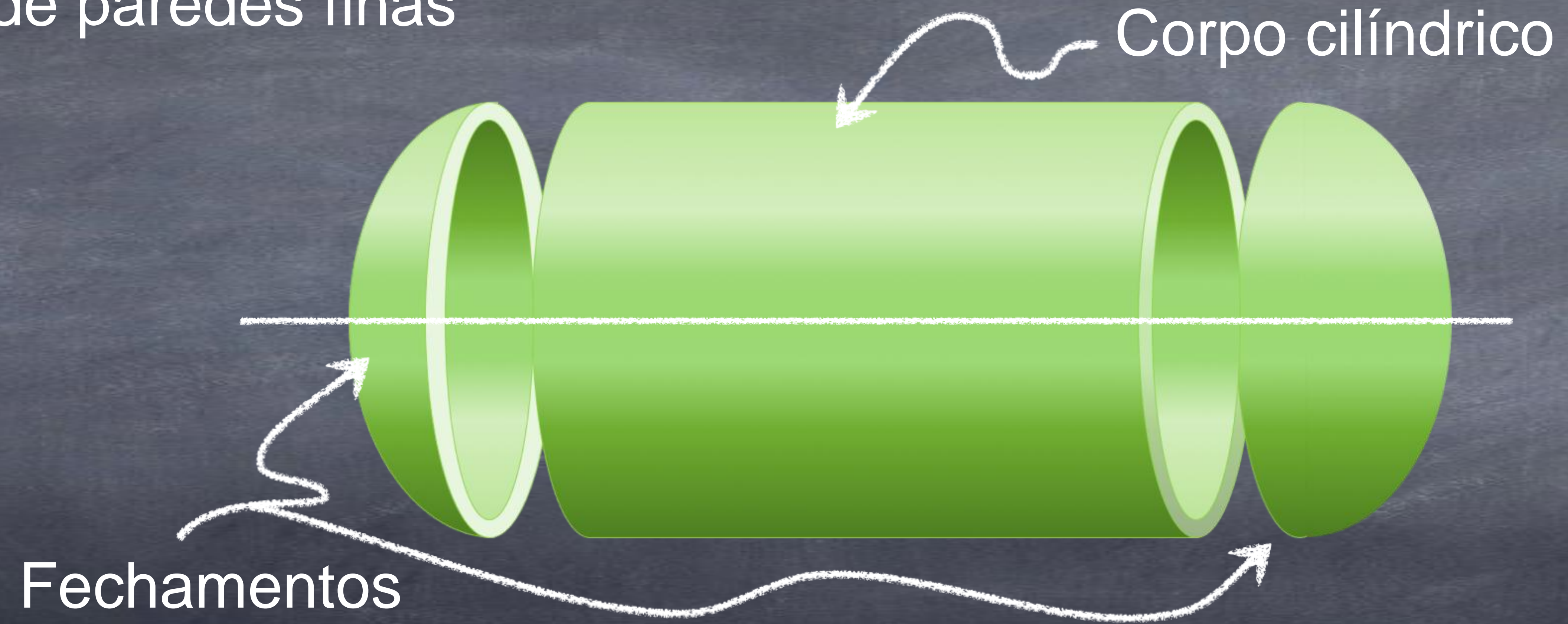
Vasos de pressão de paredes finas



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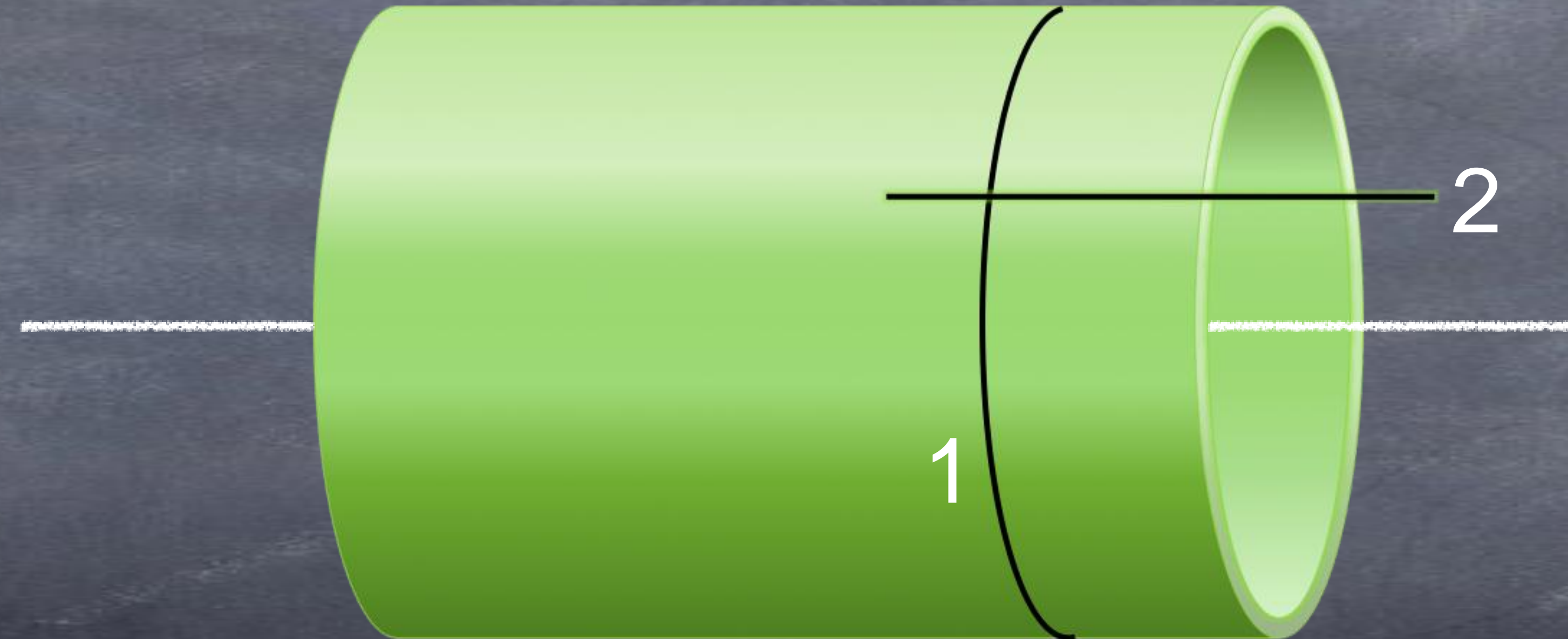


Vasos de pressão de paredes finas



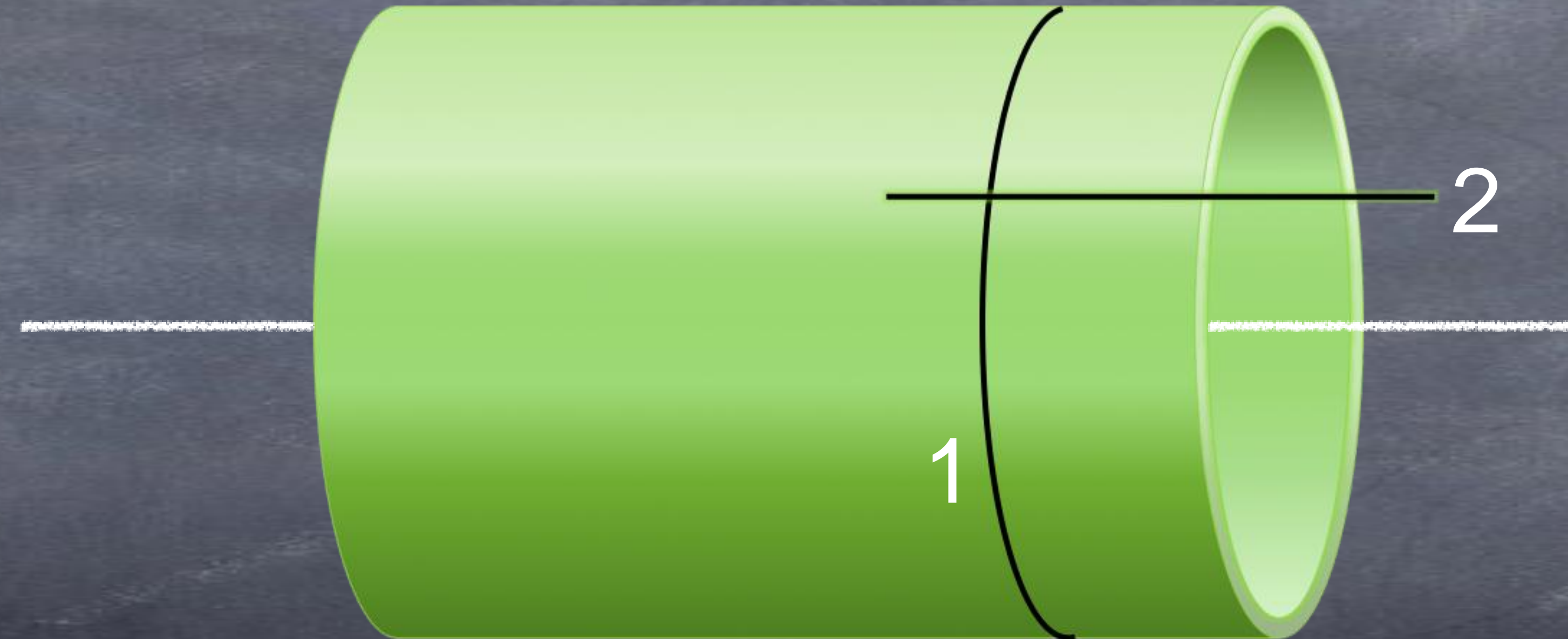
Vasos de pressão de paredes finas

Corpo cilíndrico



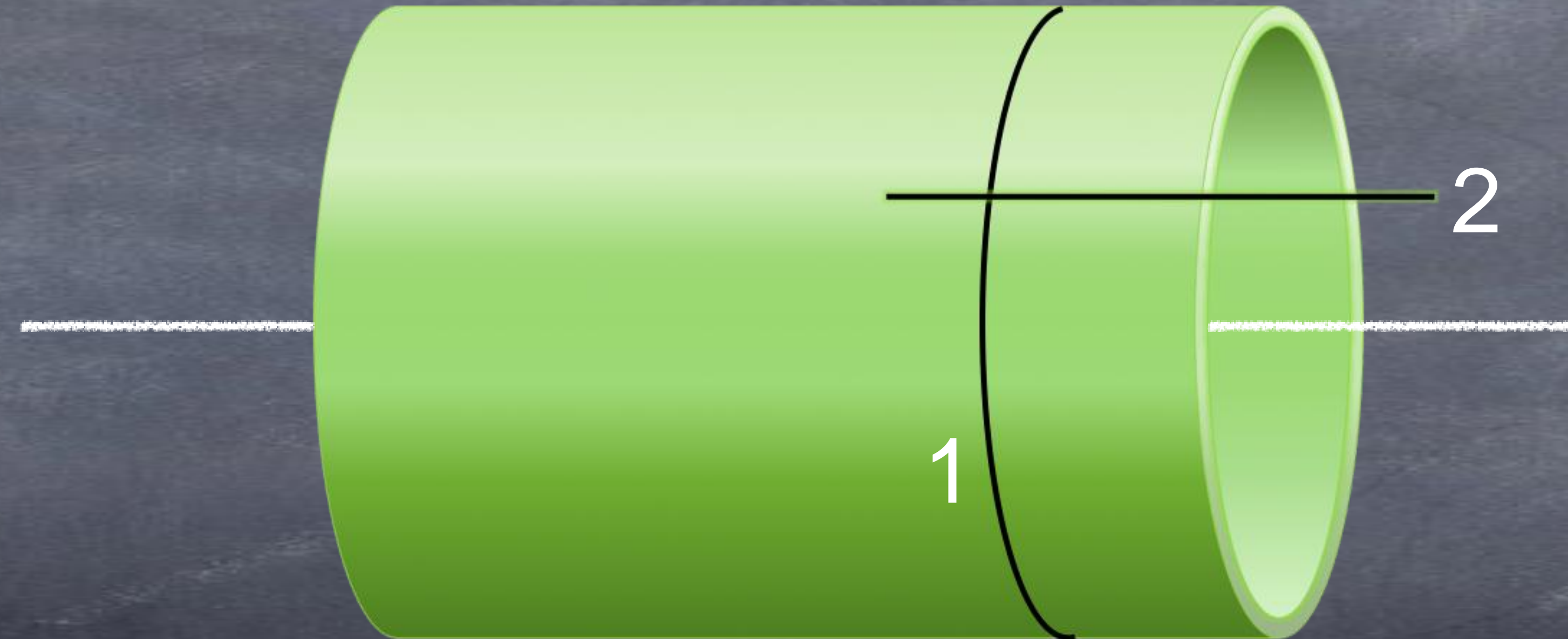
Vasos de pressão de paredes finas

Corpo cilíndrico



Vasos de pressão de paredes finas

Corpo cilíndrico

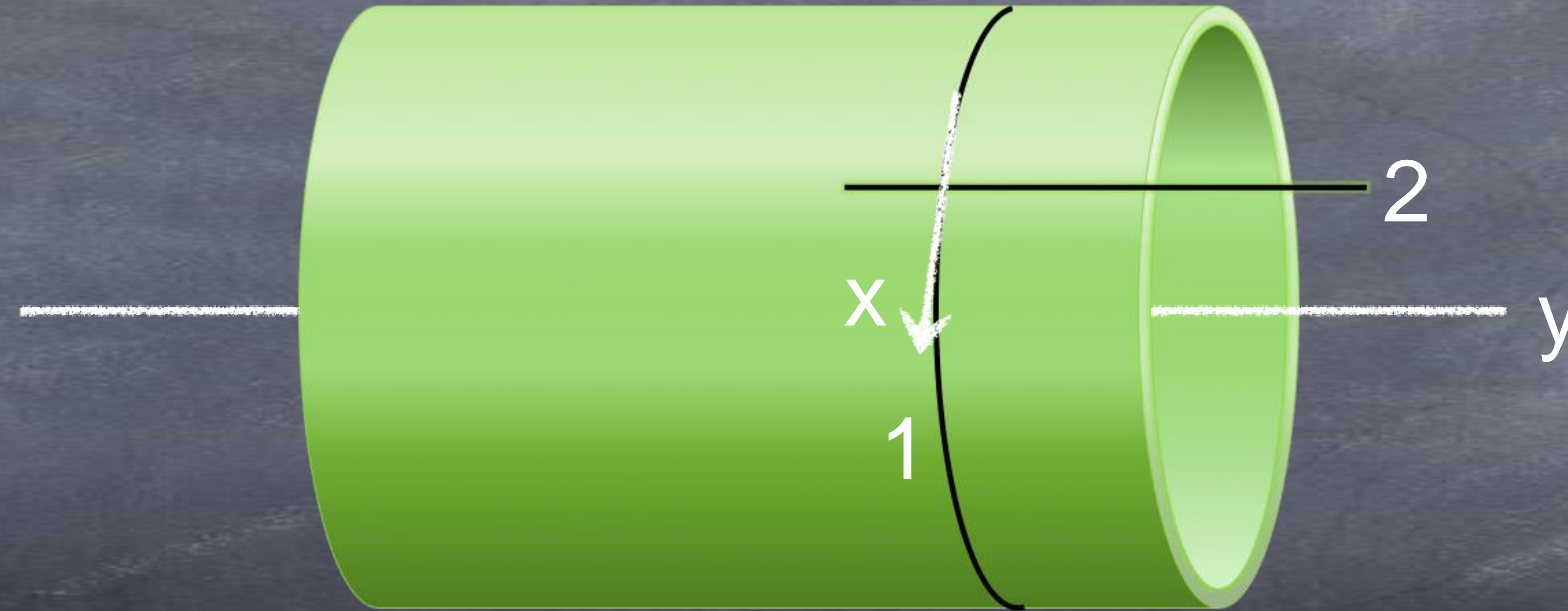


1 - direção circunferencial

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Corpo cilíndrico

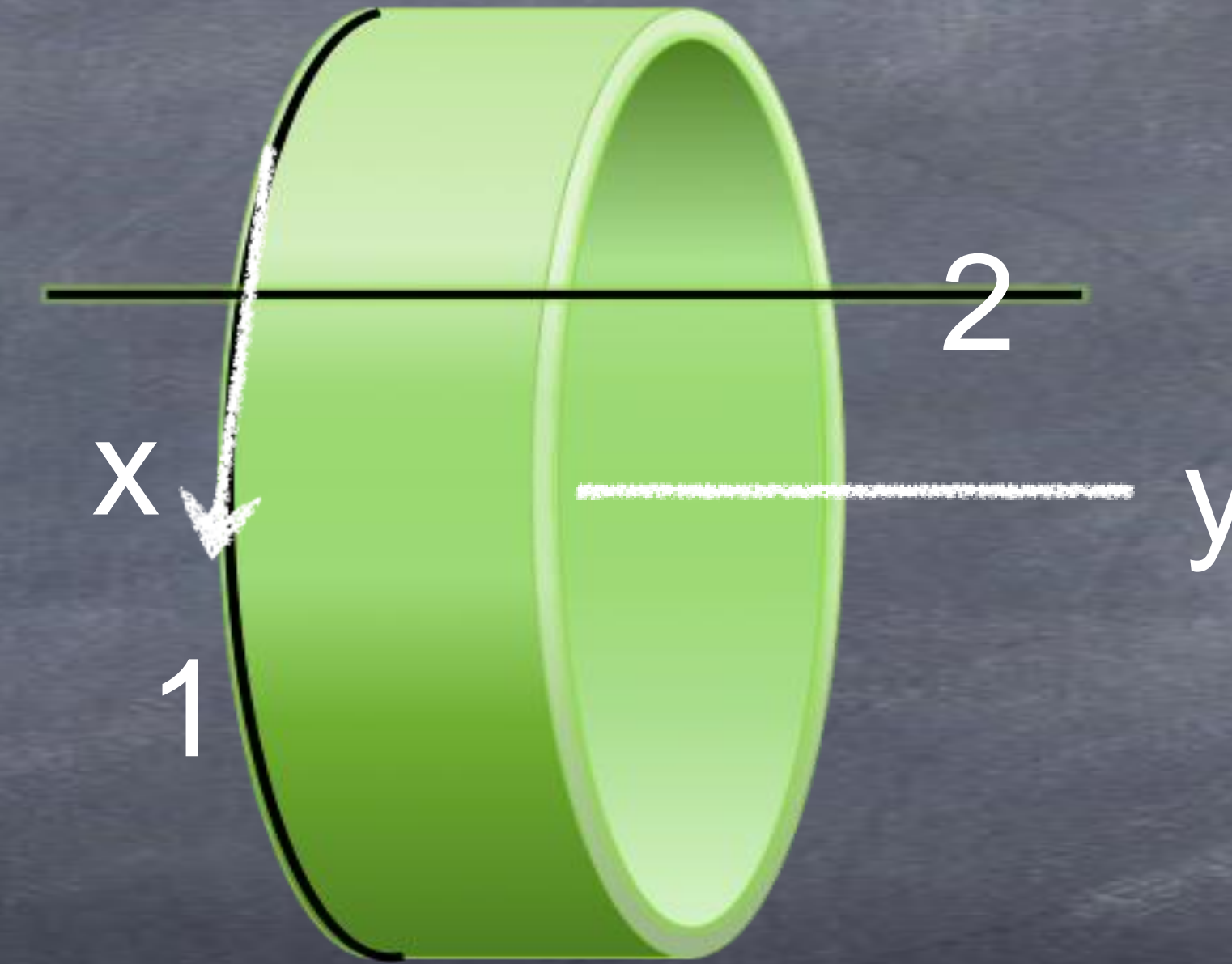


1 - direção circunferencial

2 - direção longitudinal

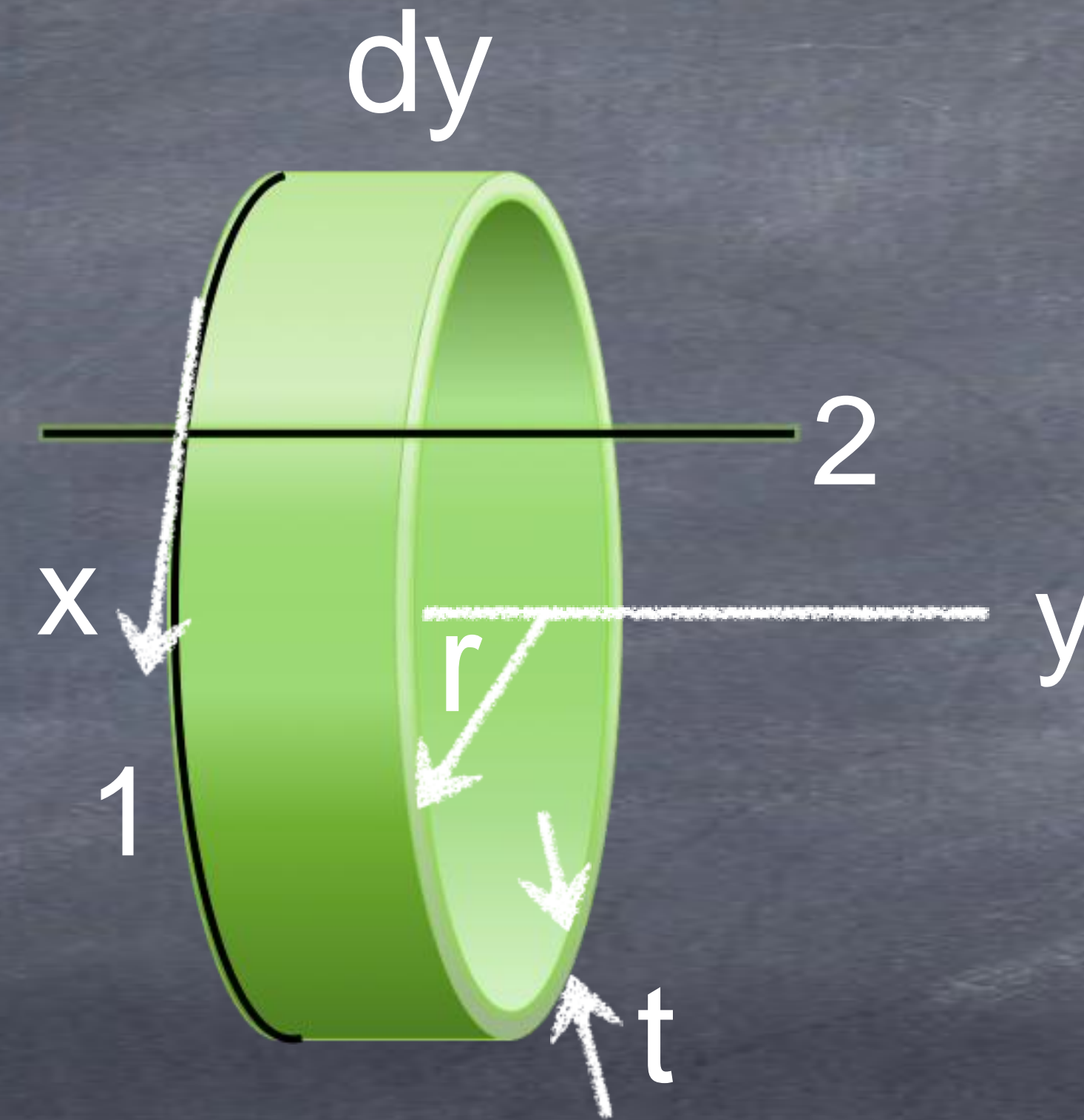
Vasos de pressão de paredes finas

Corpo cilíndrico



Vasos de pressão de paredes finas

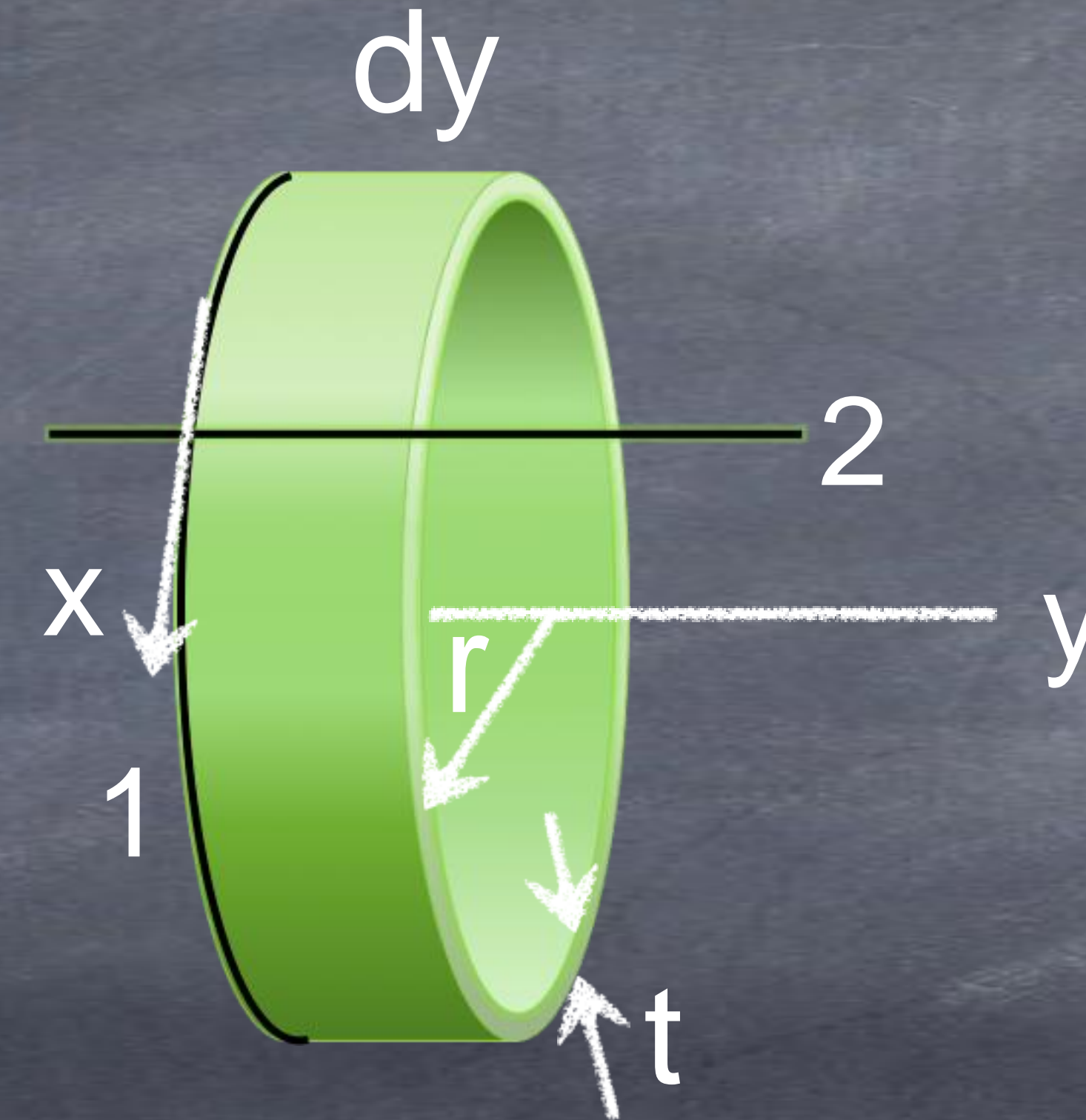
Corpo cilíndrico



Vasos de pressão de paredes finas

Corpo cilíndrico

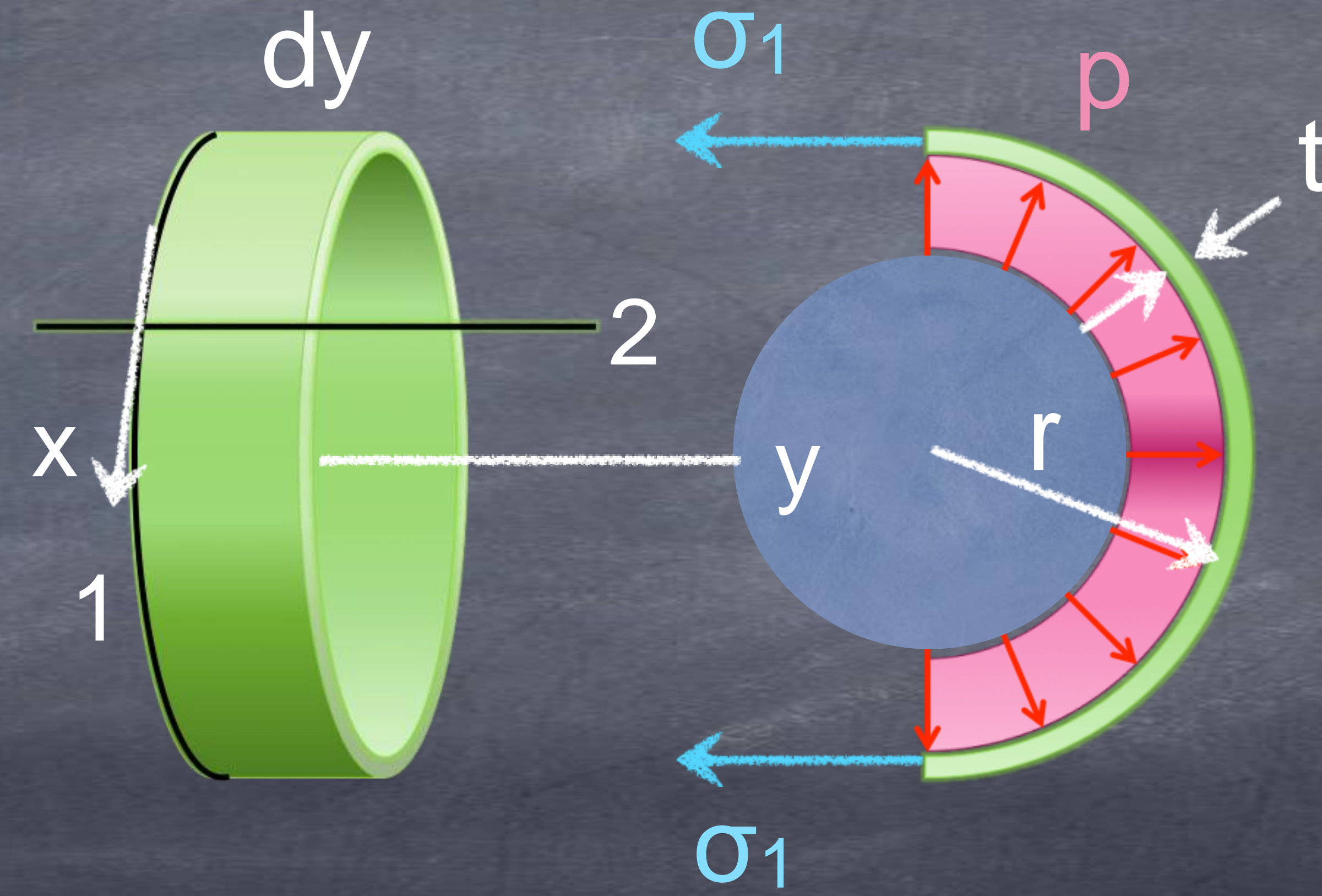
$$r/t \geq 10$$



Vasos de pressão de paredes finas

Corpo cilíndrico

$$r/t \geq 10$$



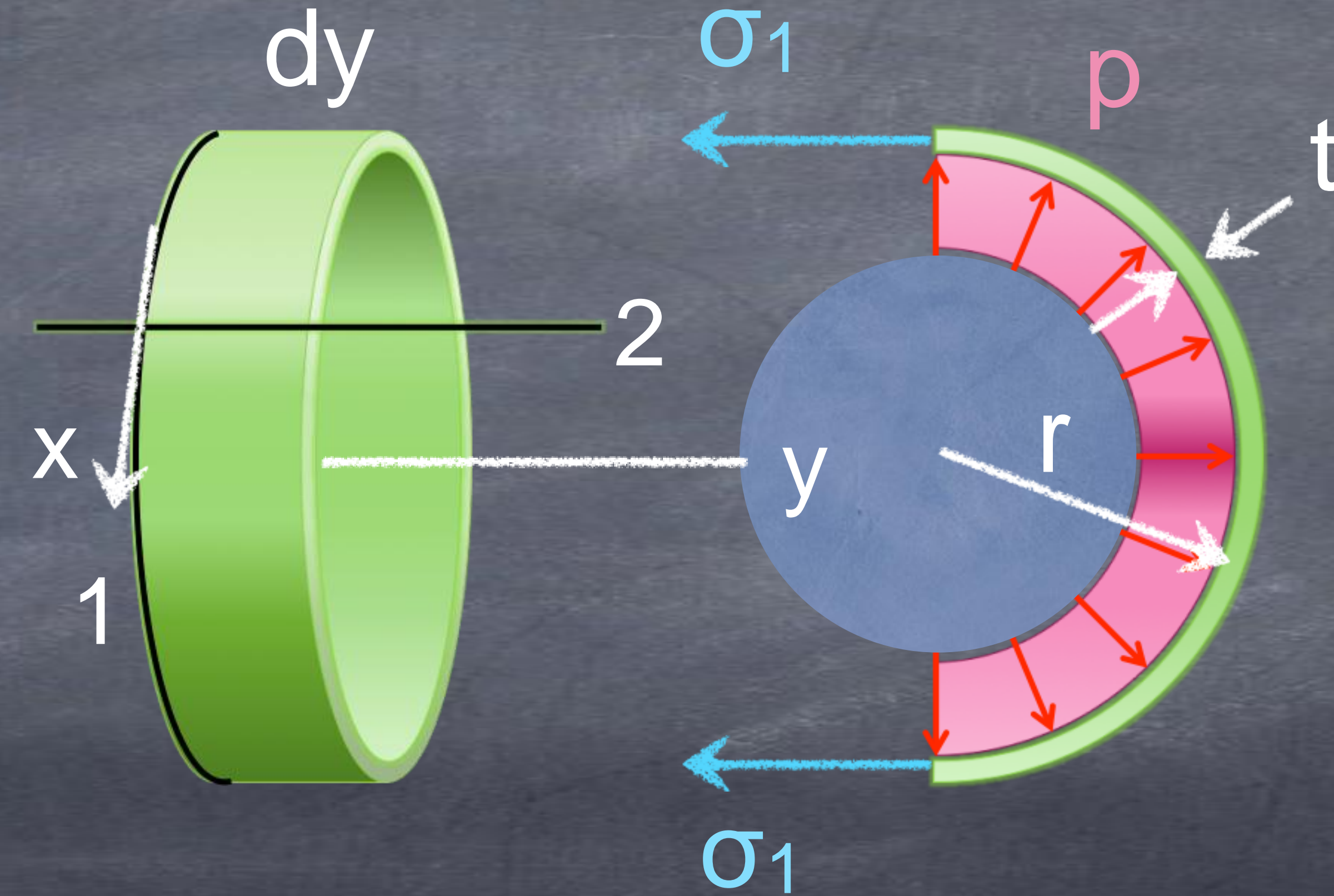
Cargas combinadas

Vasos de pressão de paredes finas

Corpo cilíndrico

$$r/t \geq 10$$

$$\Sigma F_x = 0 \Rightarrow 2 [\sigma_1 (t \cdot dy)] - p (2r \cdot dy) = 0$$



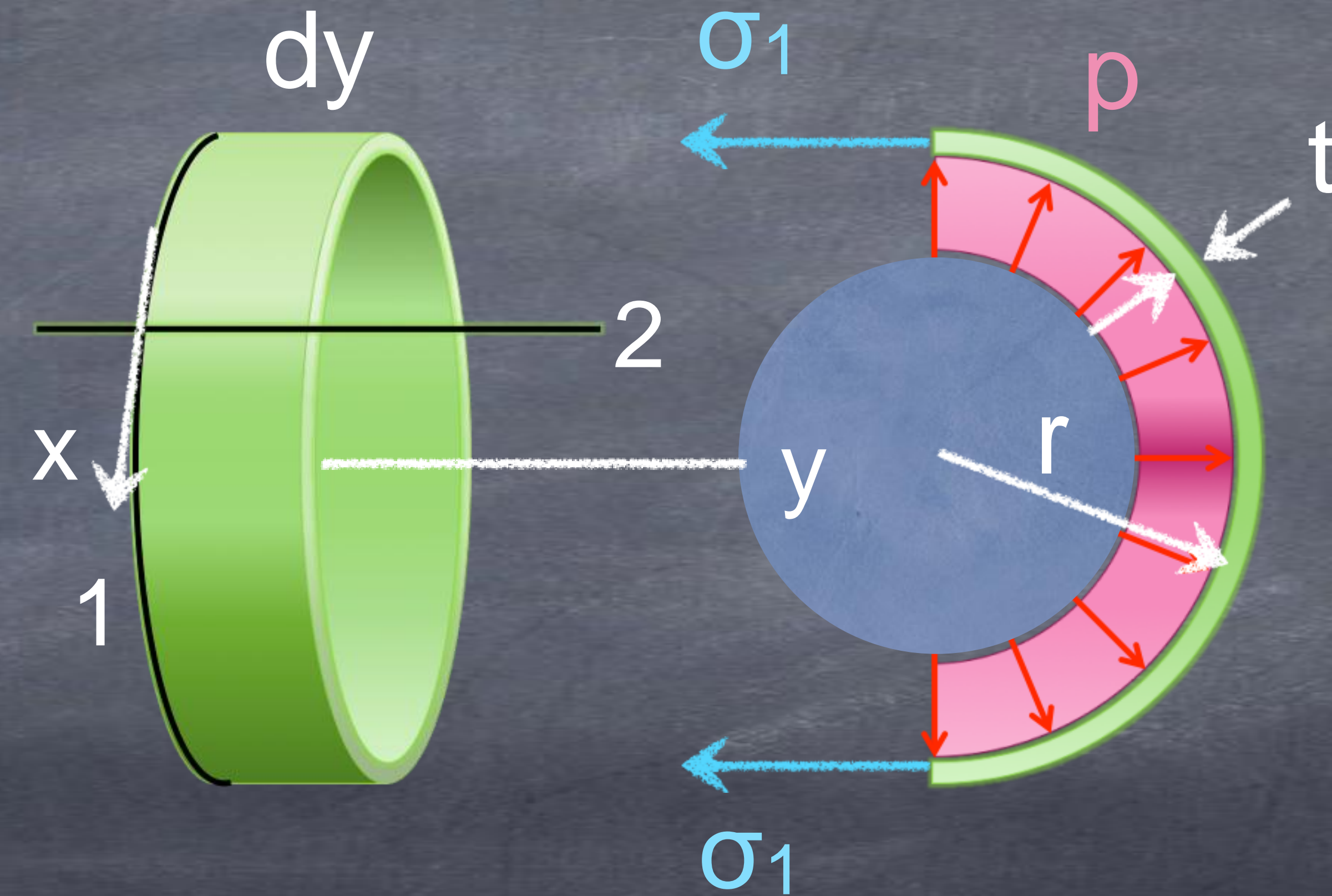
Vasos de pressão de paredes finas

Corpo cilíndrico

$$r/t \geq 10$$

$$\Sigma F_x = 0 \Rightarrow 2 [\sigma_1 (t \cdot dy)] - p (2r \cdot dy) = 0$$

$$\sigma_1 = (p \cdot r / t)$$



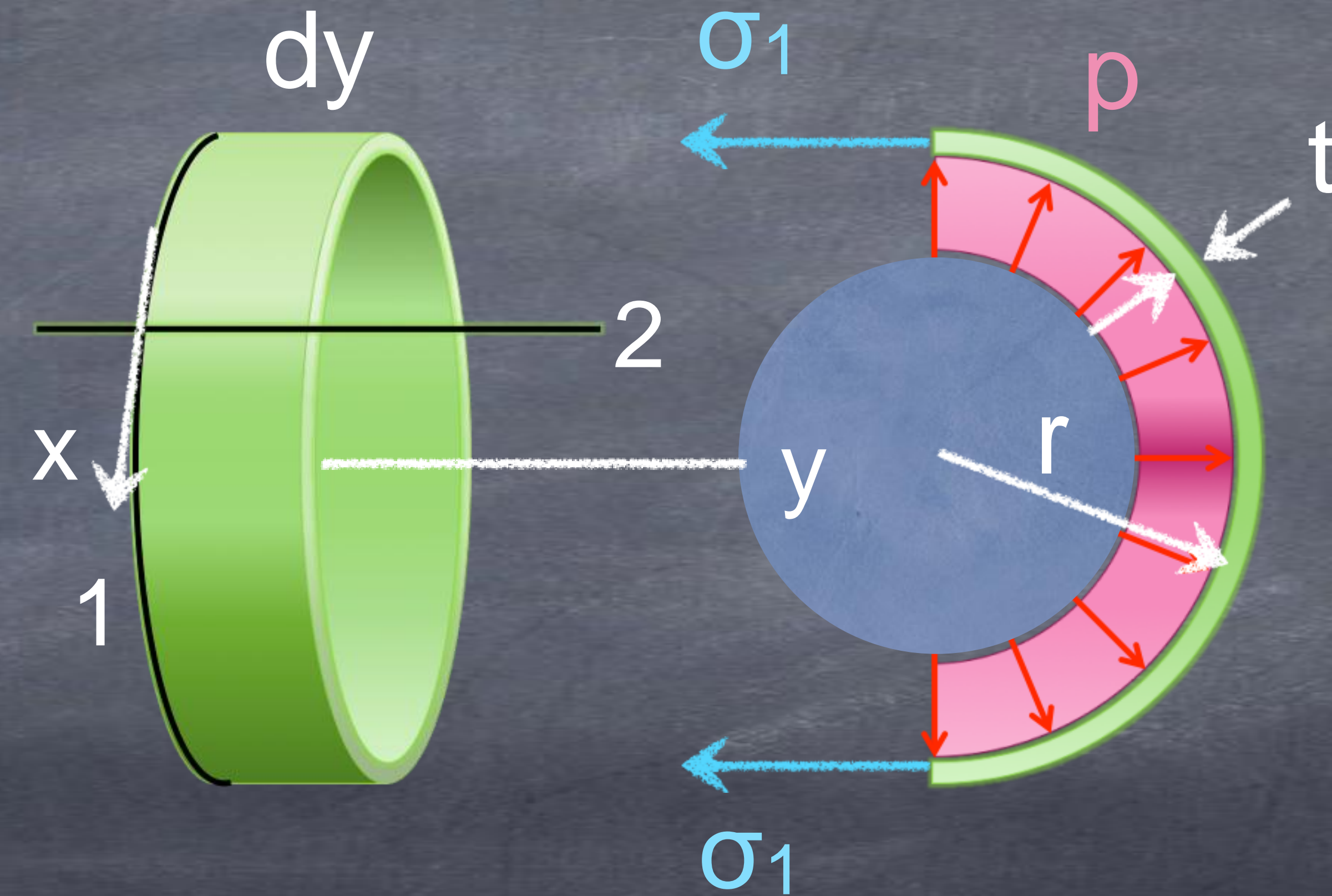
Vasos de pressão de paredes finas

Corpo cilíndrico

$$r/t \geq 10$$

$$\Sigma F_x = 0 \Rightarrow 2 [\sigma_1 (t \cdot dy)] - p (2r \cdot dy) = 0$$

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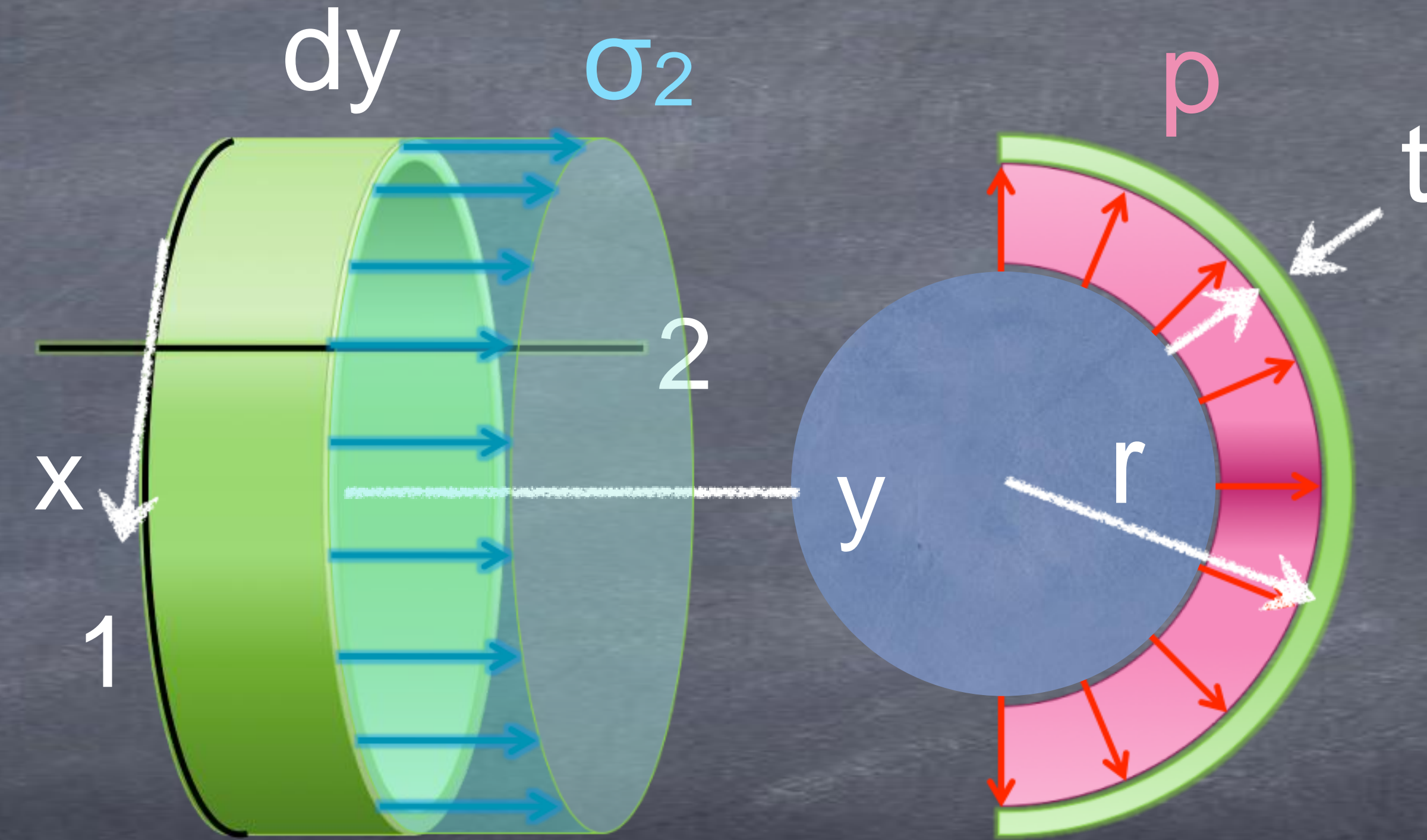
Cargas combinadas

Vasos de pressão de paredes finas

Corpo cilíndrico

$$\Sigma F_y = 0 \Rightarrow \sigma_2 (2\pi r \cdot t) - p (\pi r^2) = 0$$

$$r/t \geq 10$$



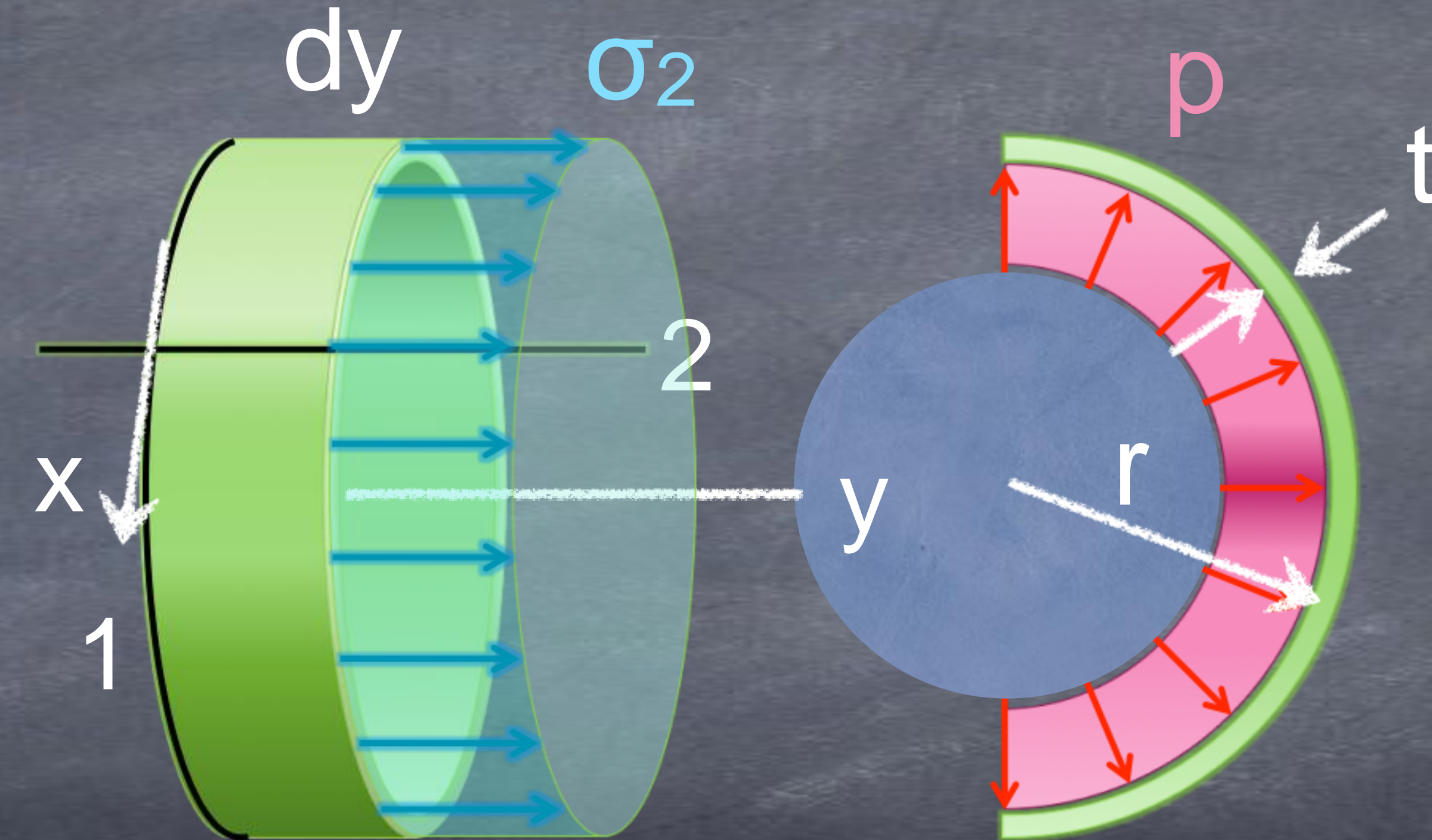
Vasos de pressão de paredes finas

Corpo cilíndrico

$$\Sigma F_y = 0 \Rightarrow \sigma_2 (2\pi r \cdot t) - p (\pi r^2) = 0$$

$$\sigma_2 = (p \cdot r / 2t)$$

$$r/t \geq 10$$



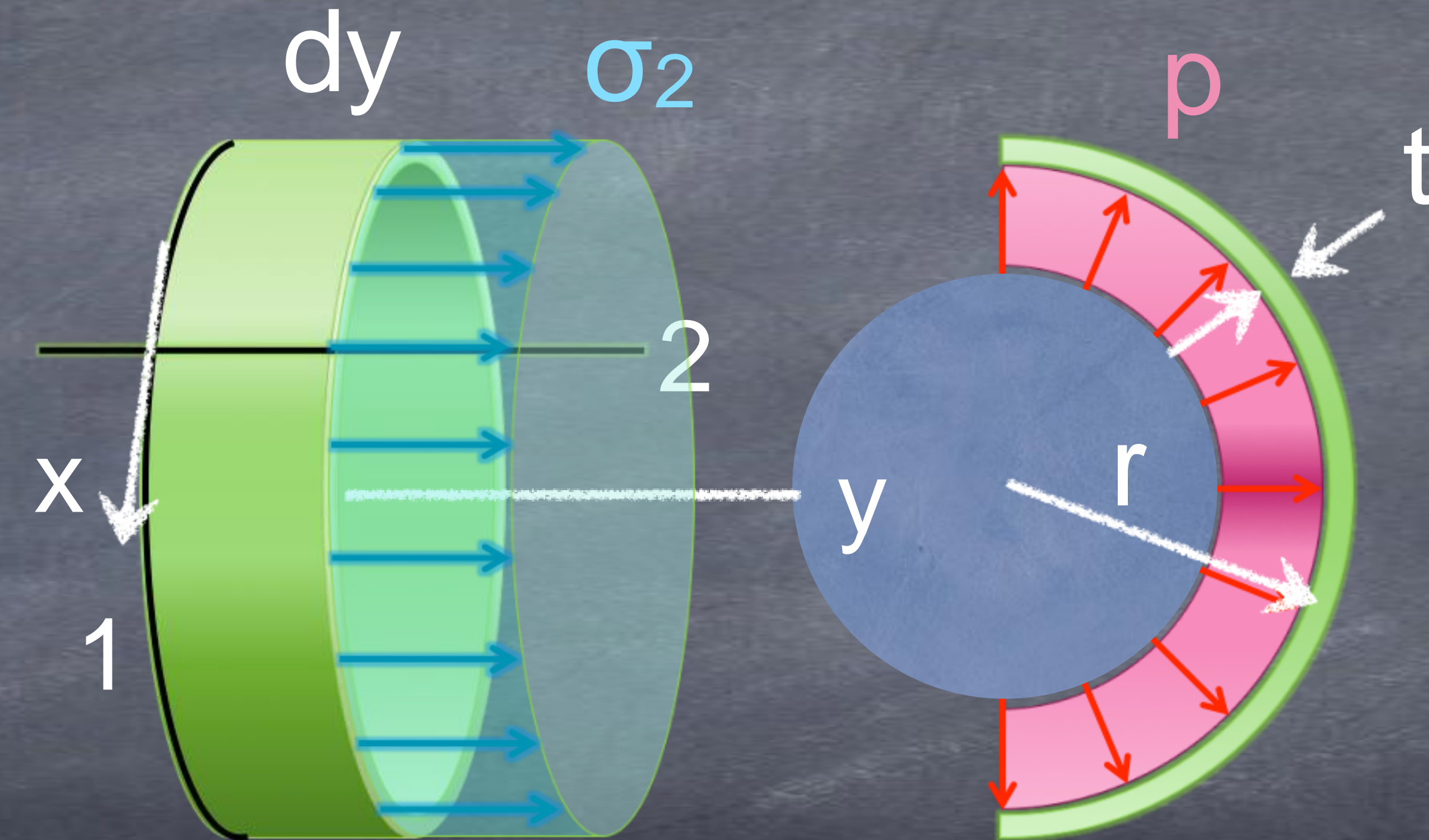
Vasos de pressão de paredes finas

Corpo cilíndrico

$$\Sigma F_y = 0 \Rightarrow \sigma_2 (2\pi r \cdot t) - p (\pi r^2) = 0$$

$$\sigma_2 = (p \cdot r / 2t)$$

$$r/t \geq 10$$



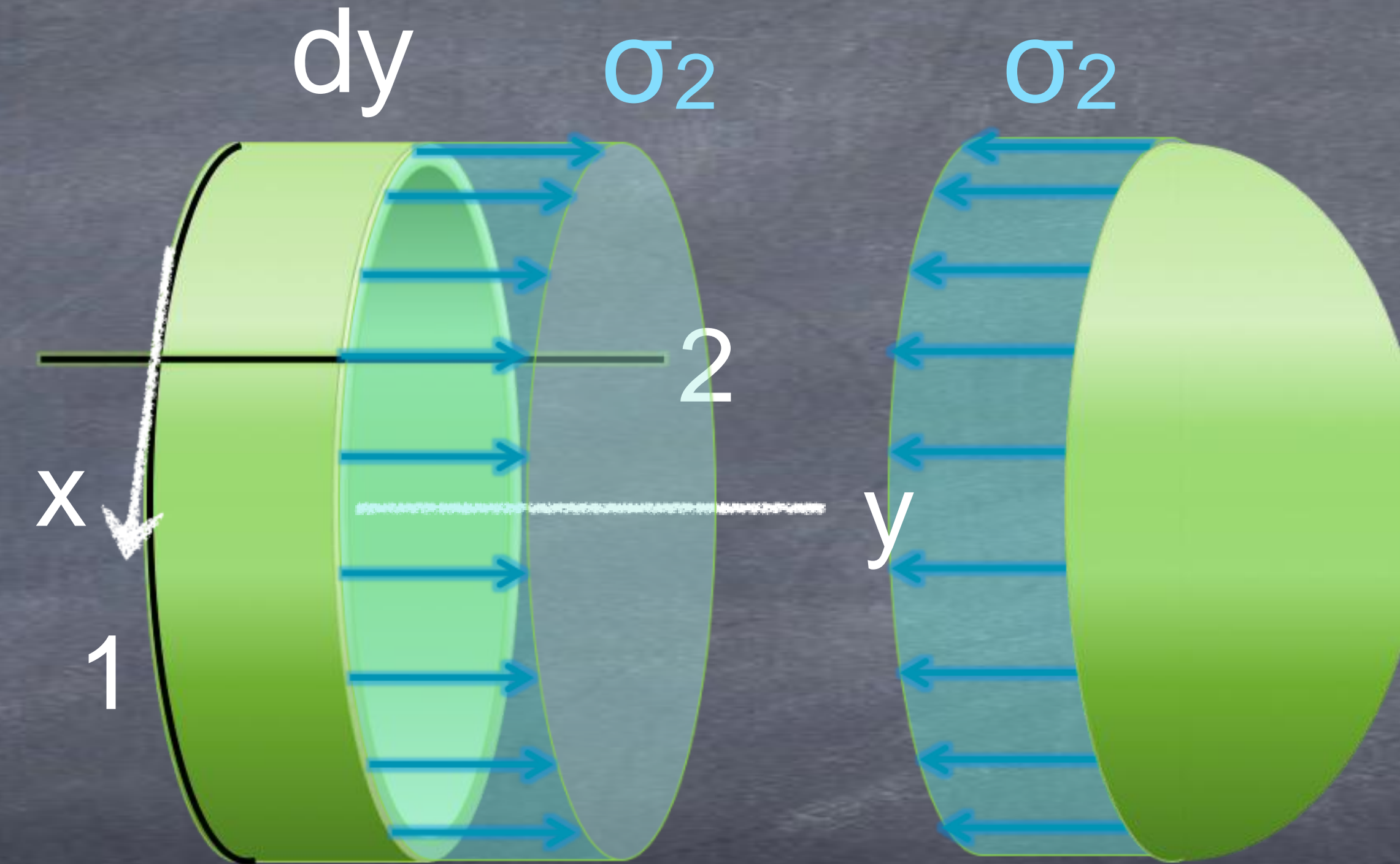
Vasos de pressão de paredes finas

Fechamento

$$\Sigma F_y = 0 \Rightarrow \sigma_2 (2\pi r \cdot t) - p (\pi r^2) = 0$$

$$\sigma_2 = (p \cdot r / 2t)$$

$$r/t \geq 10$$

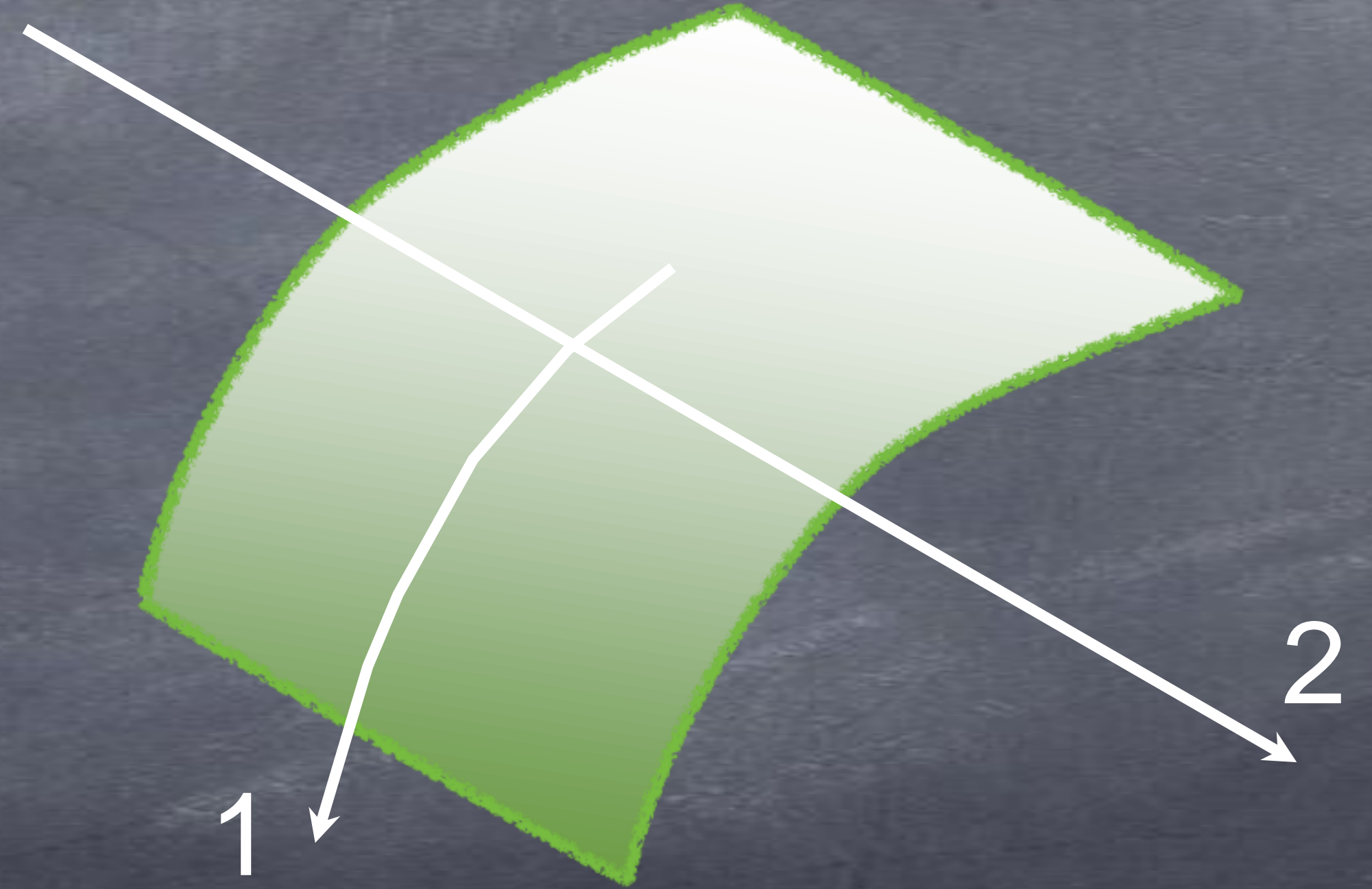


Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

Vasos de pressão de paredes finas

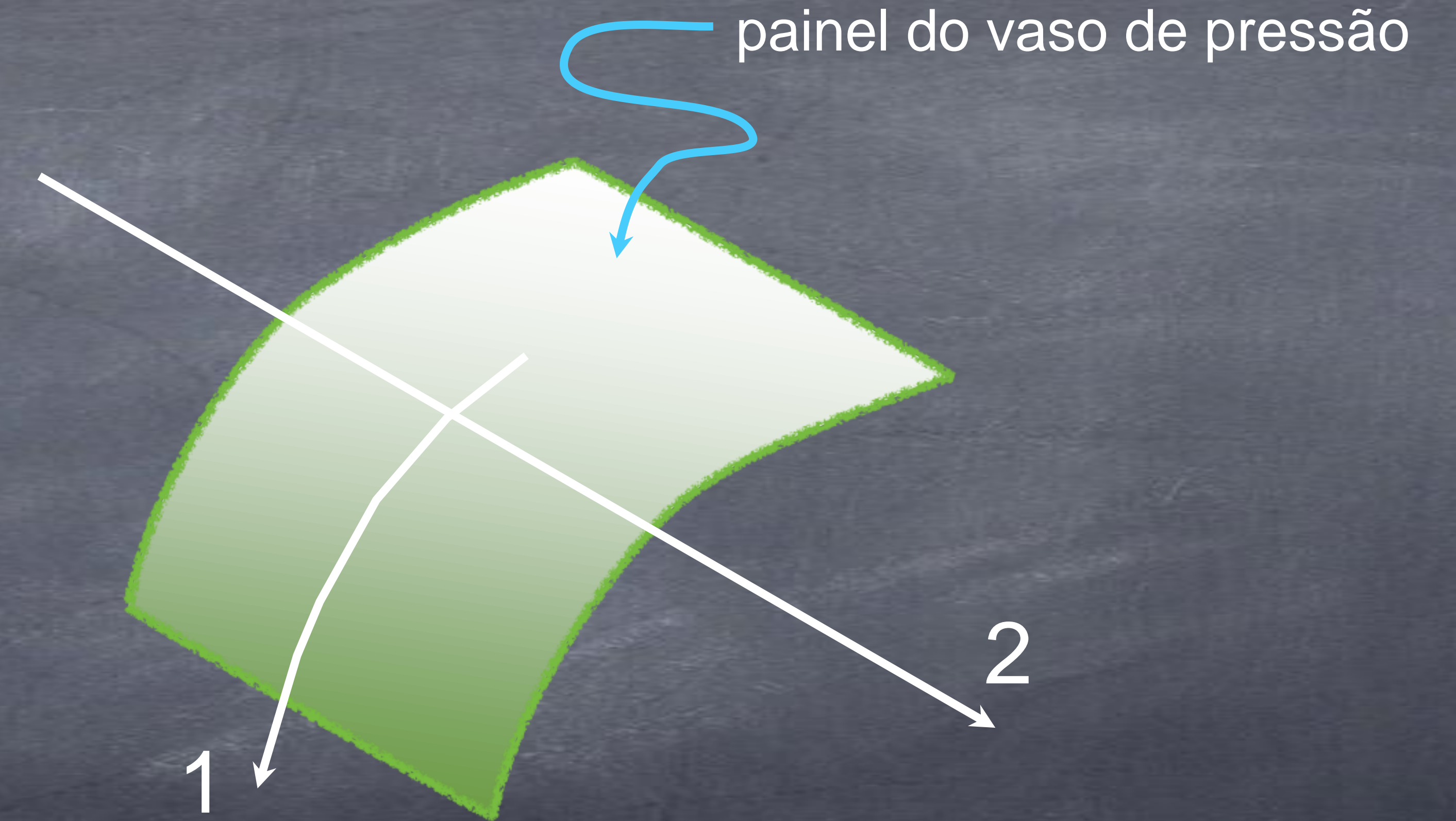
Estado de tensão causado por cargas combinadas



Cargas combinadas

Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

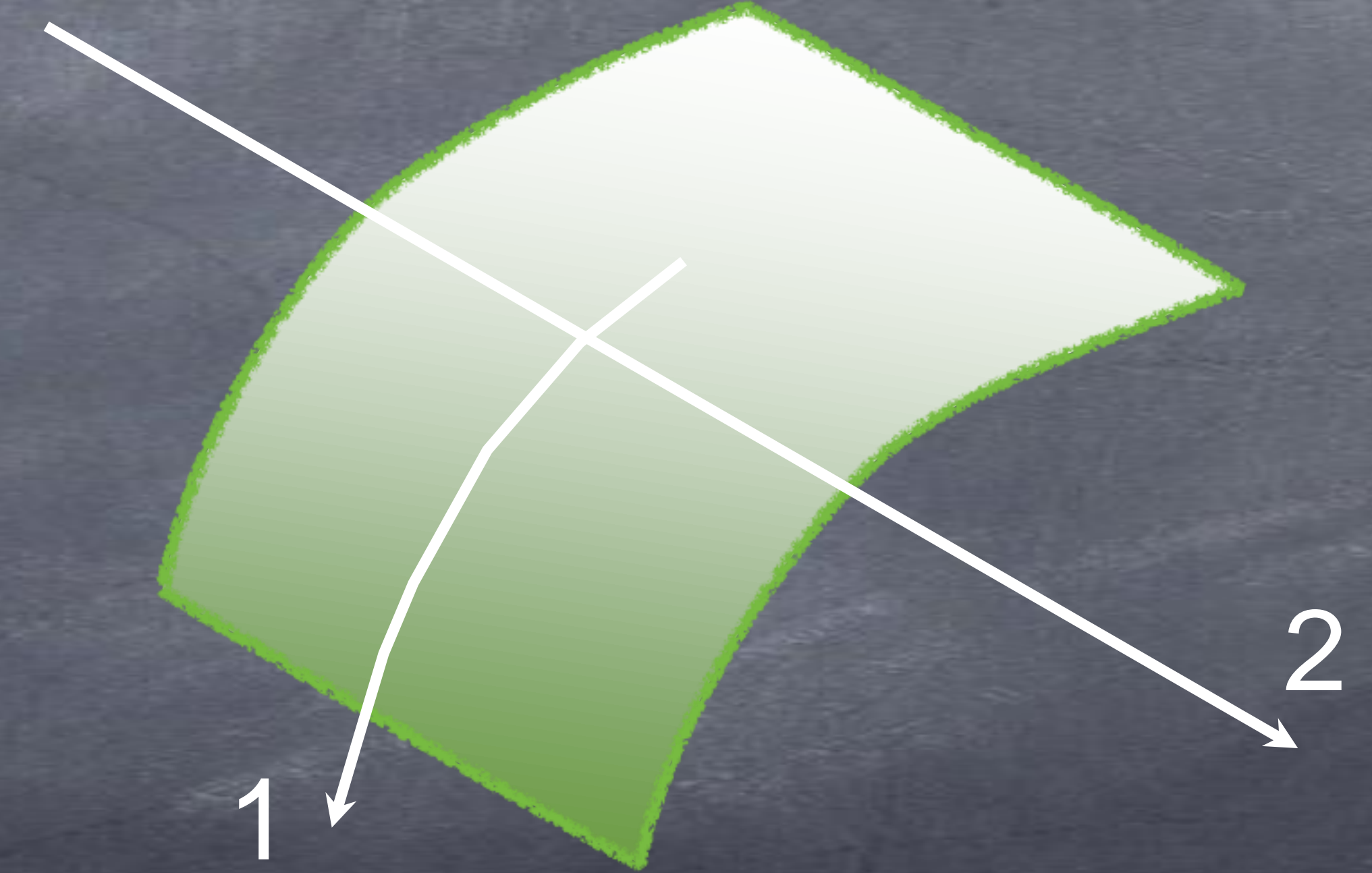


Cargas combinadas

Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

Na dir. 1

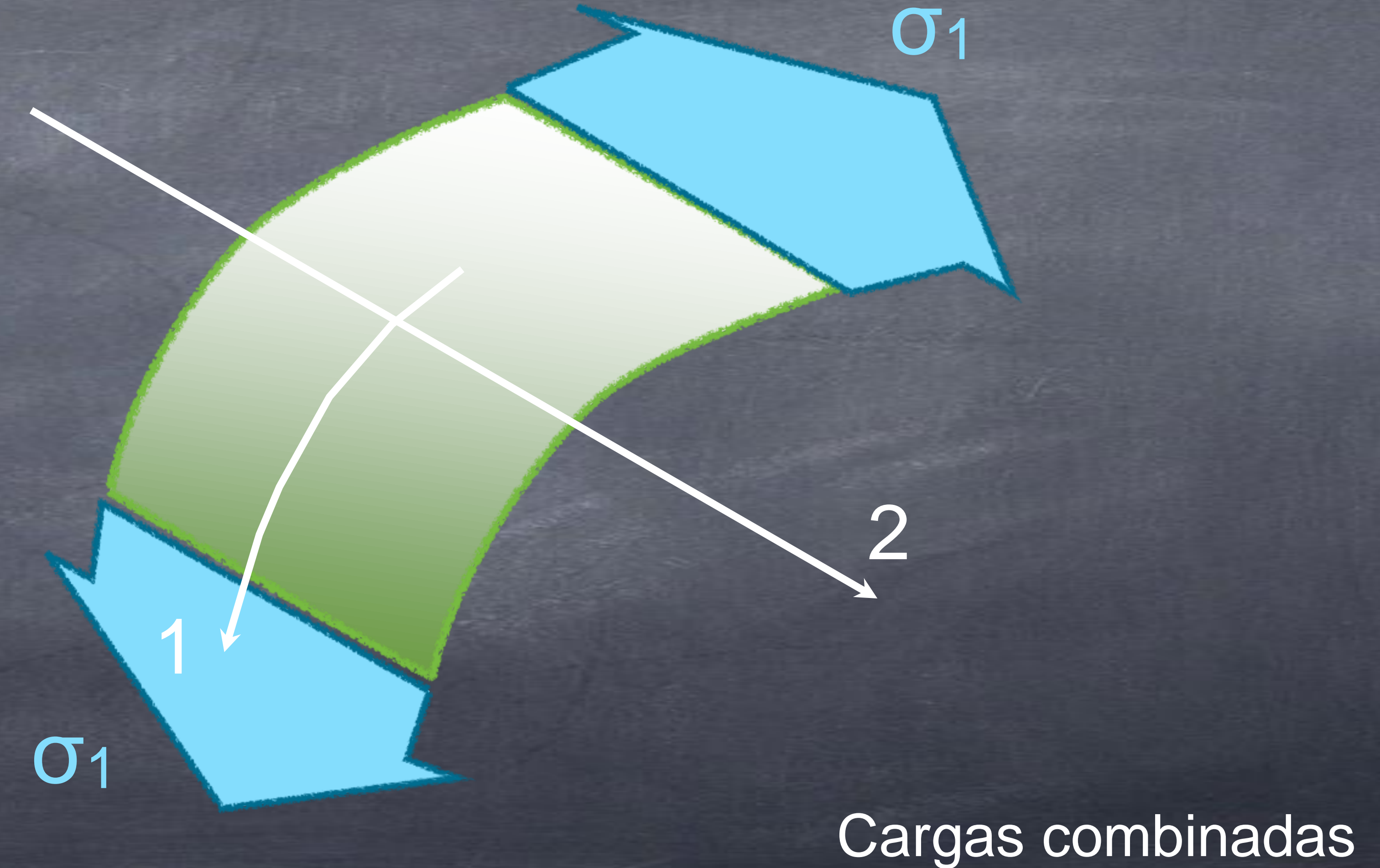


Cargas combinadas

Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

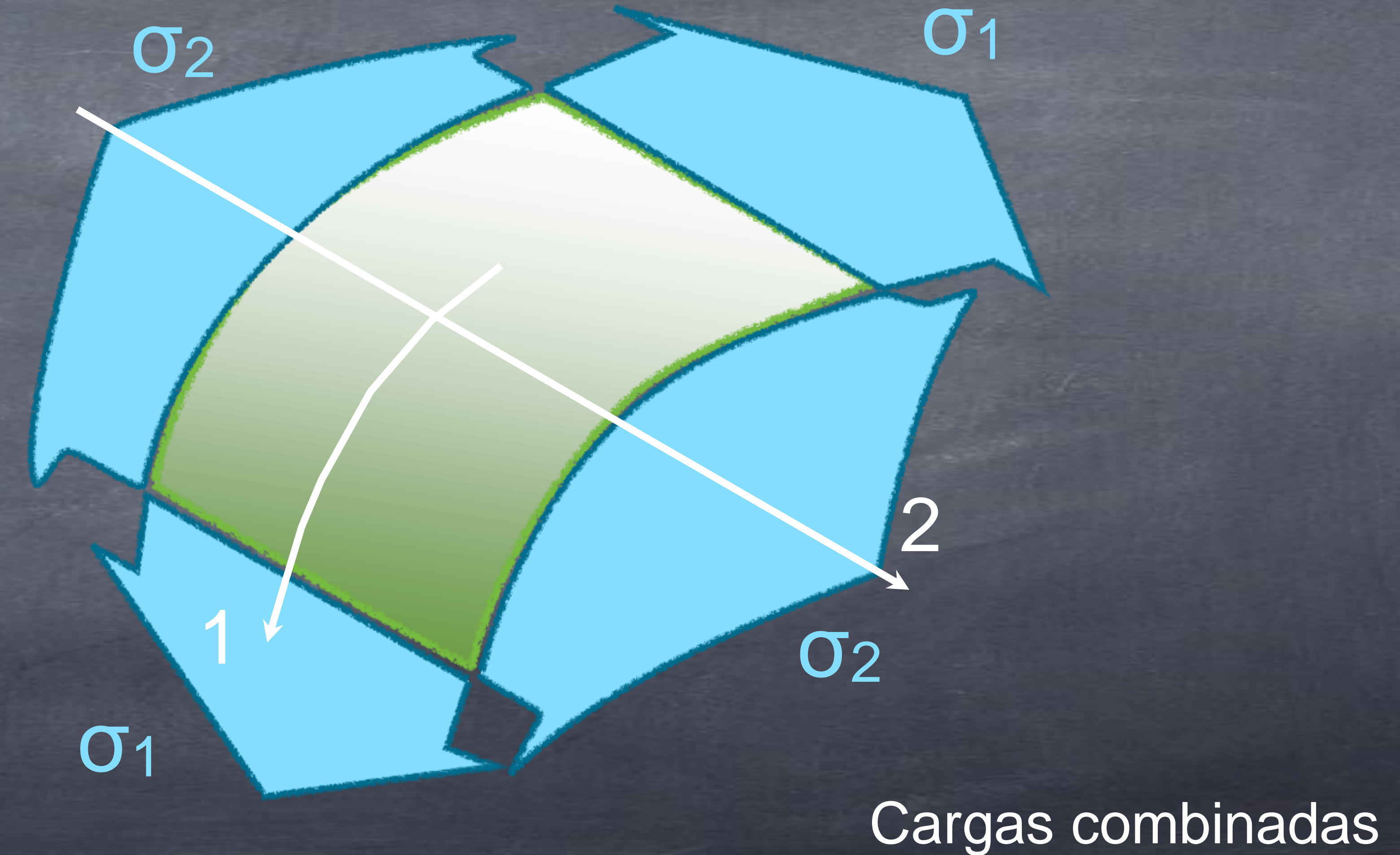
Na dir. 1



Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

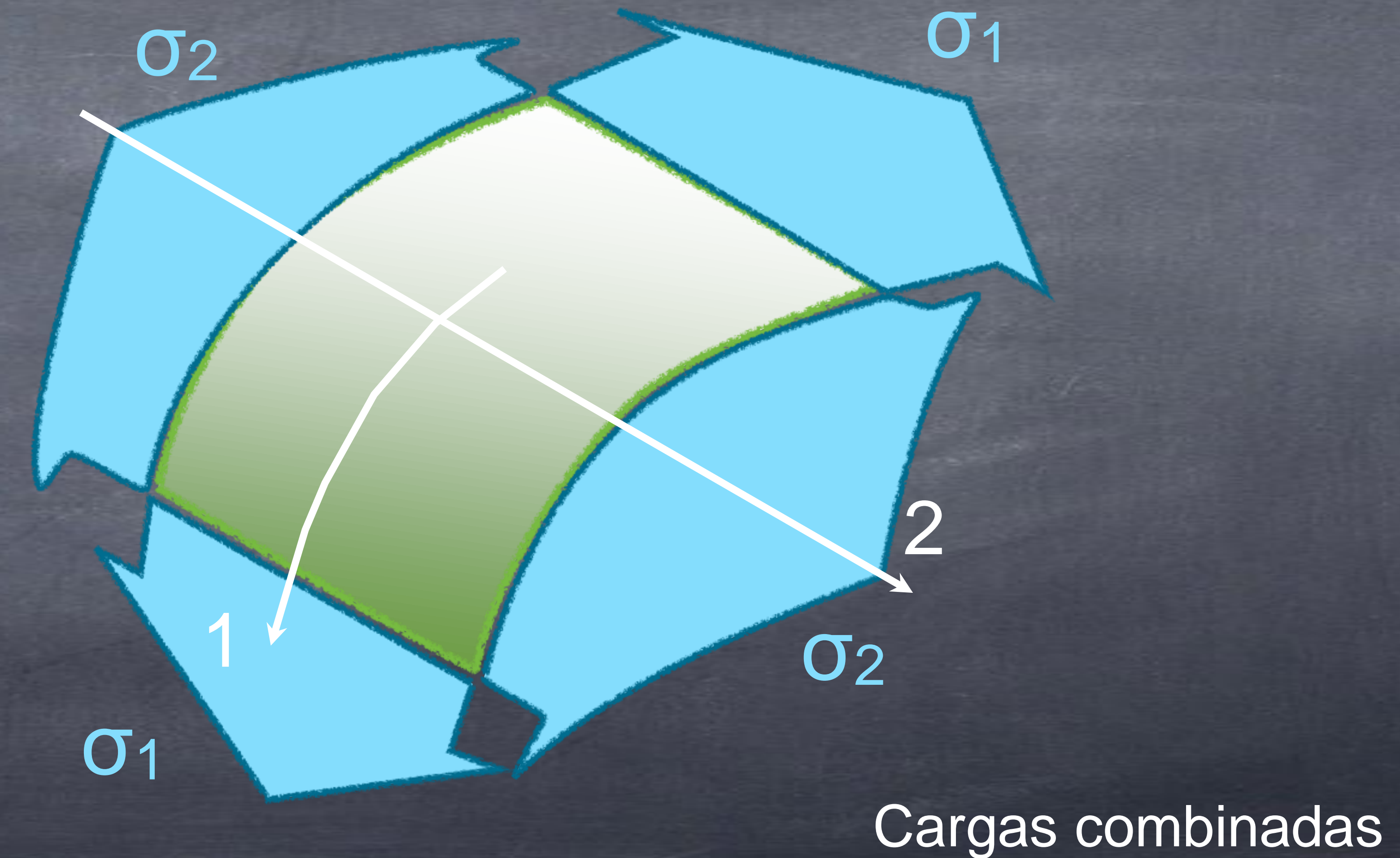
Na dir. 1 e na dir. 2



Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

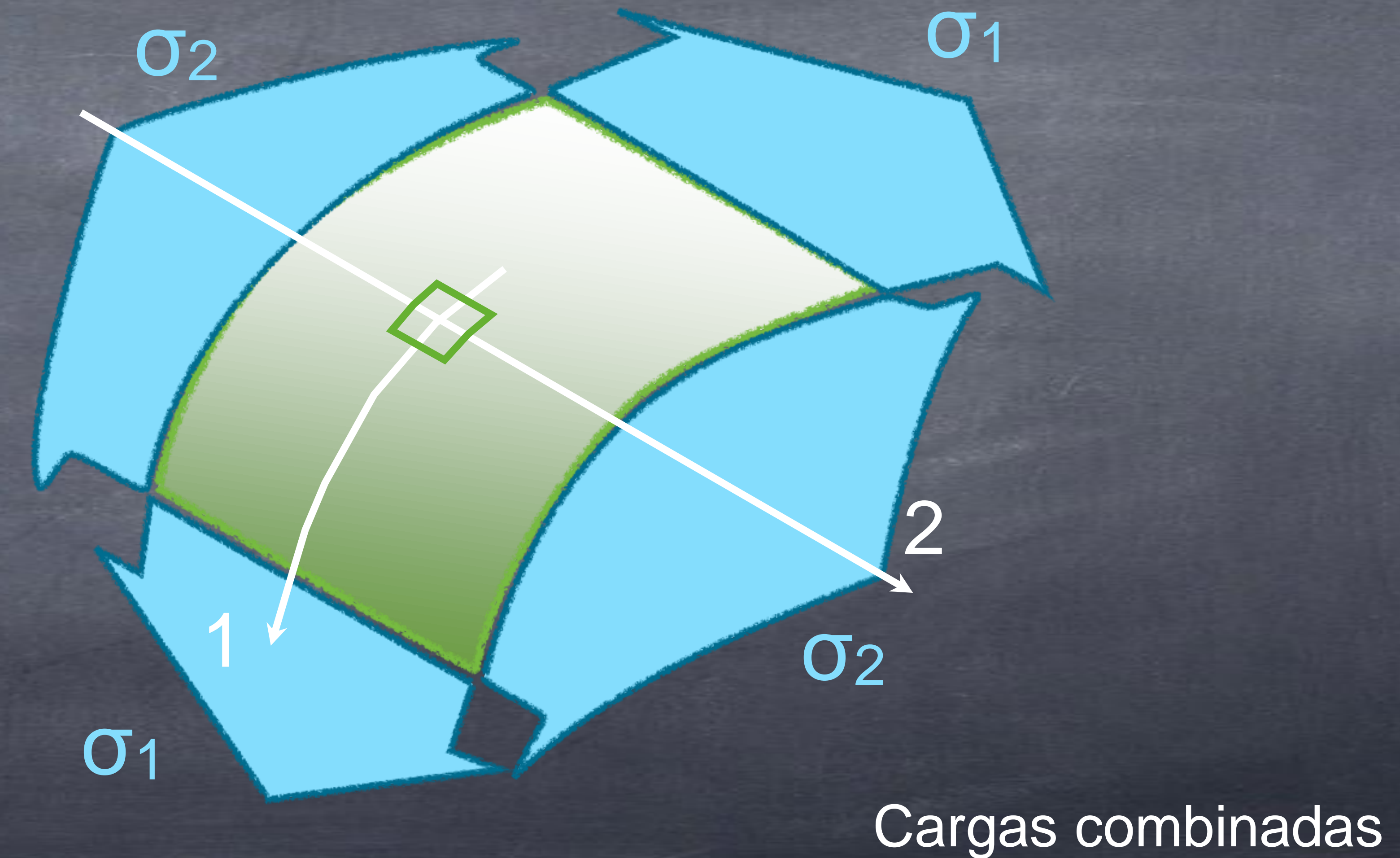
Na dir. 1 e na dir. 2 → tensões combinadas



Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

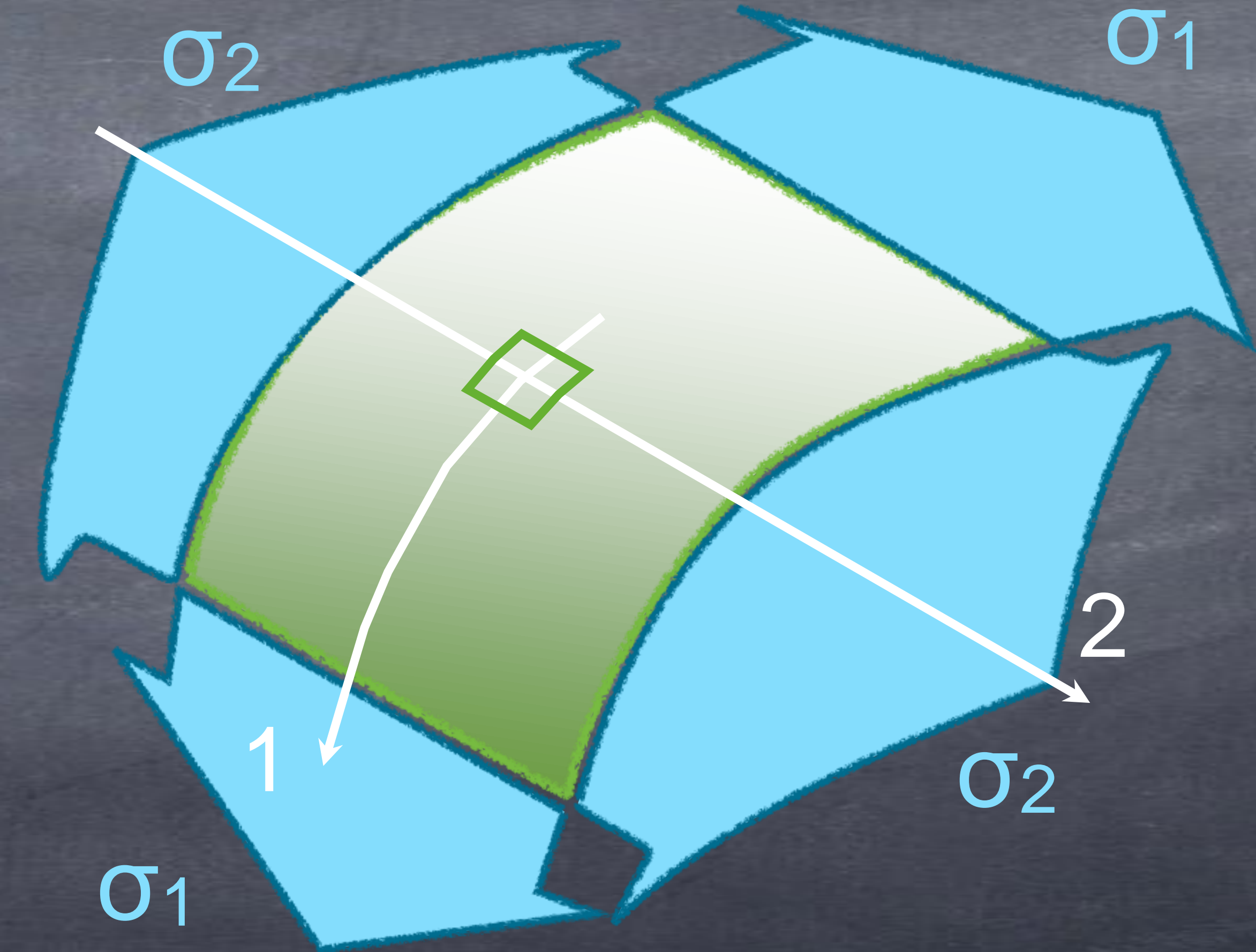
Na dir. 1 e na dir. 2 → tensões combinadas



Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

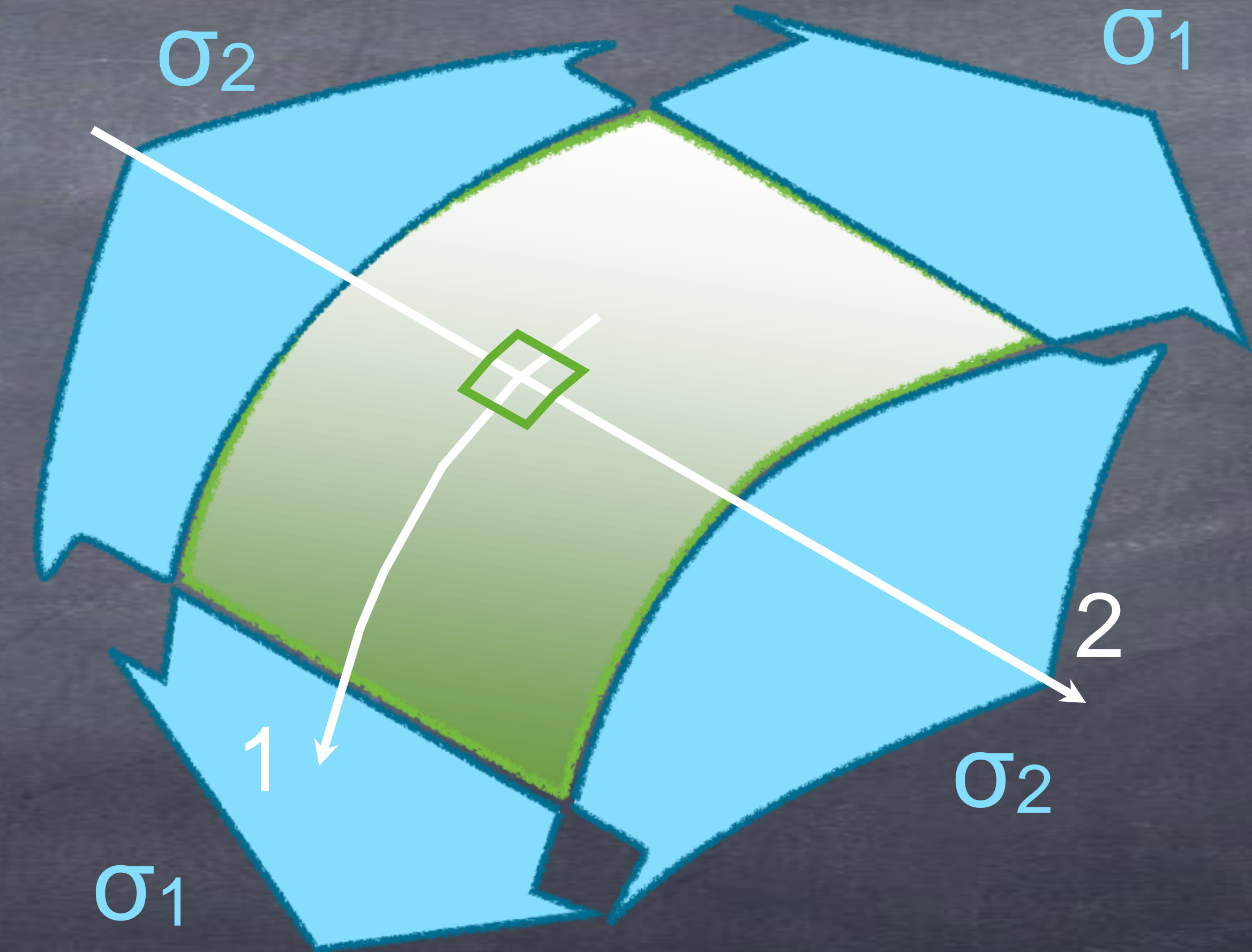
Representação



Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

Representação

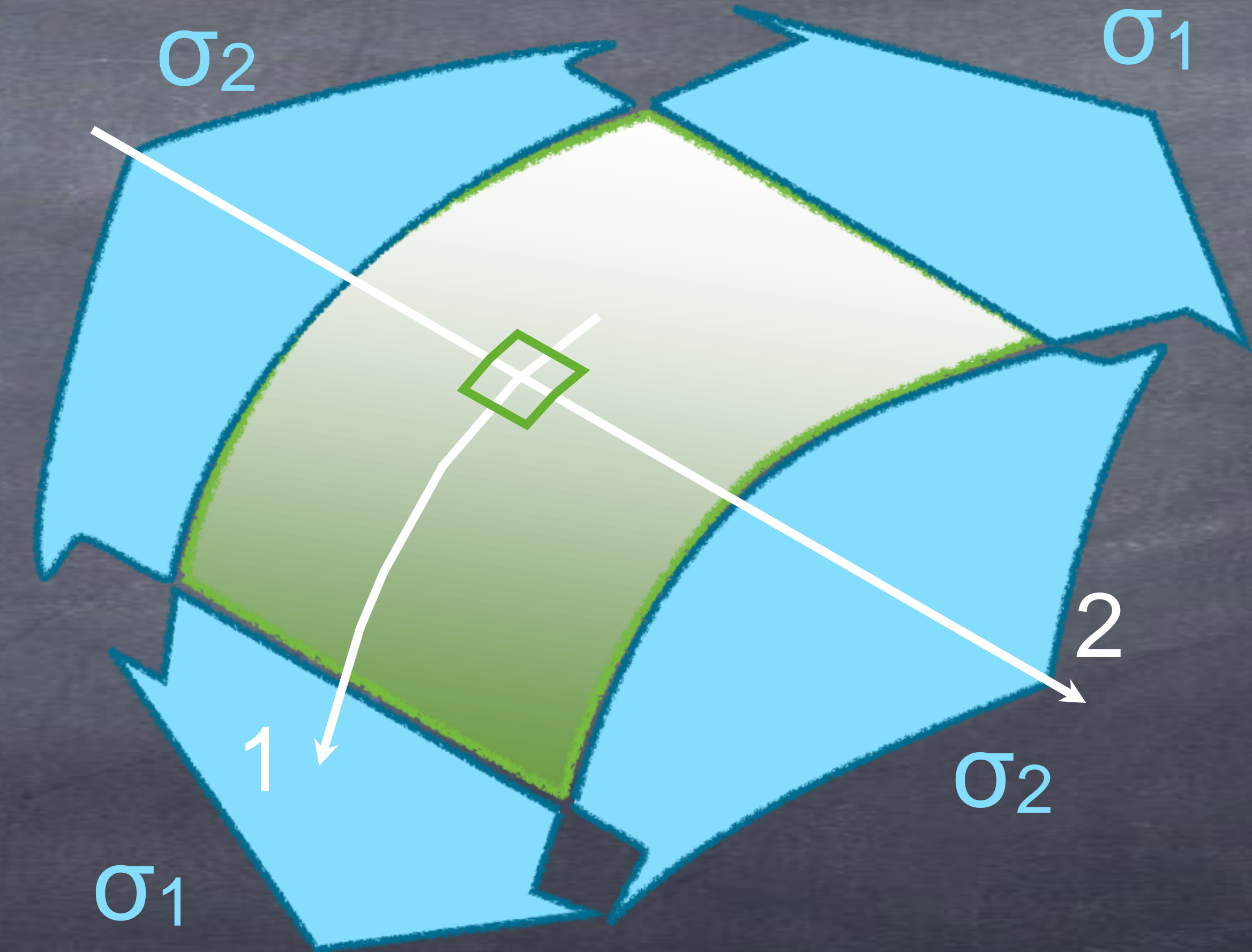
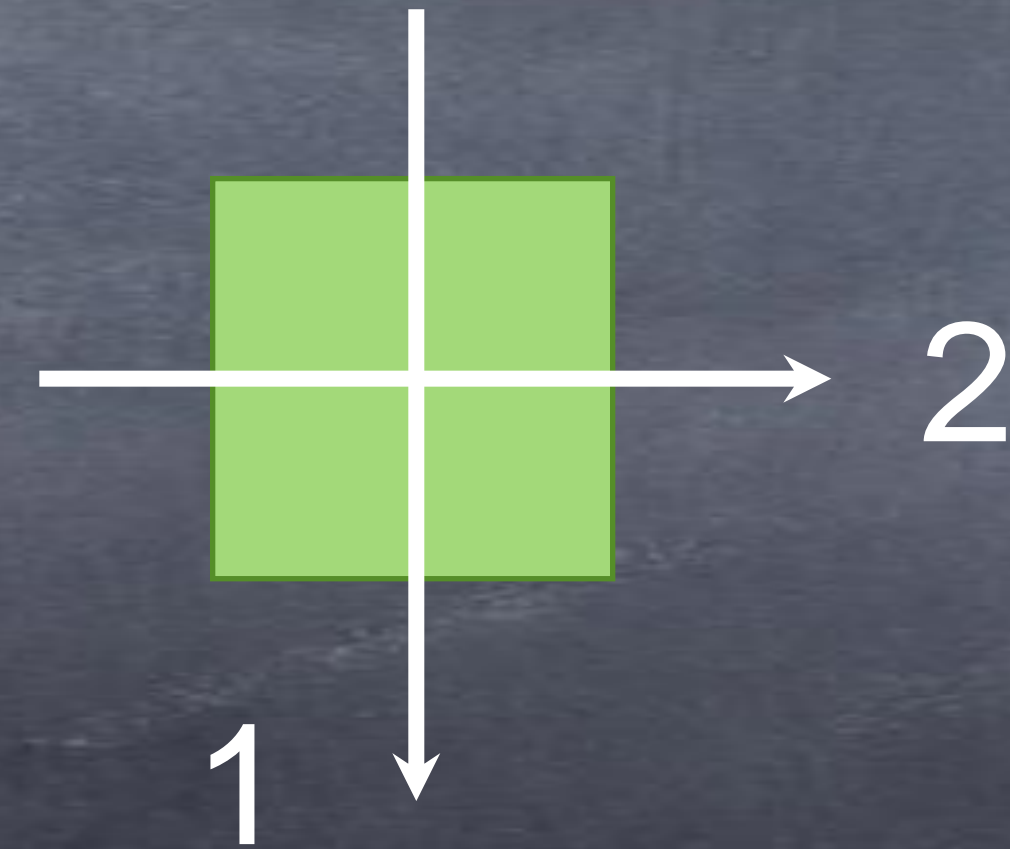


Cargas combinadas

Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

Representação

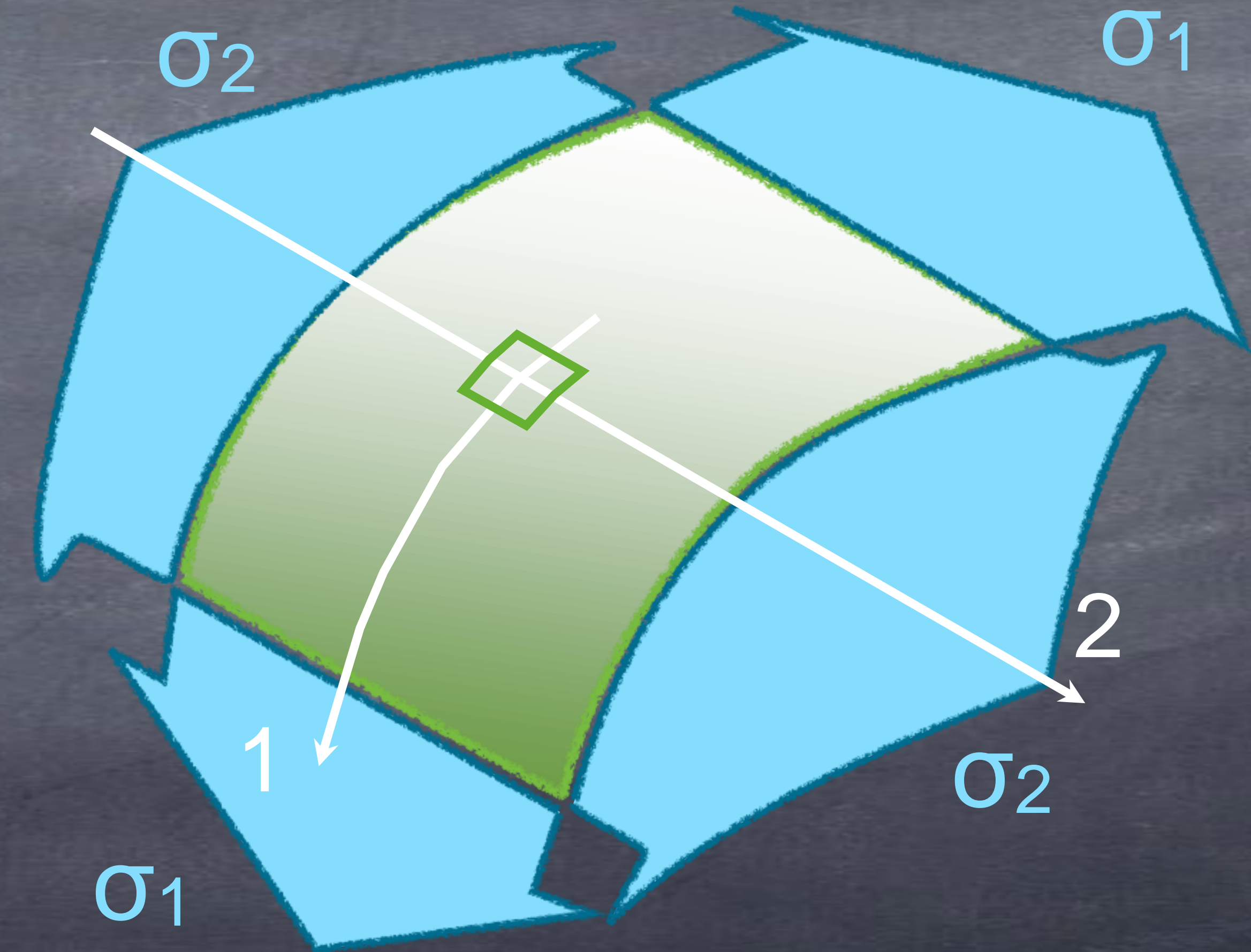
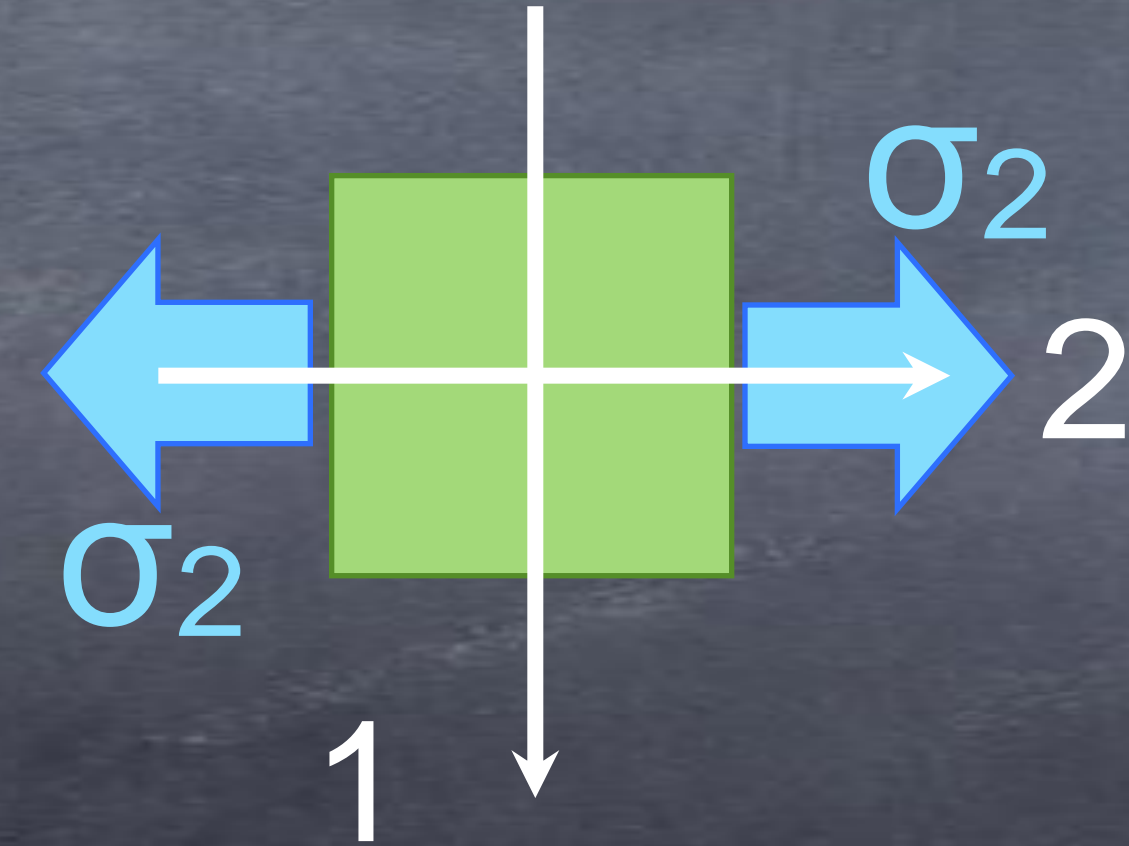


Cargas combinadas

Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

Representação

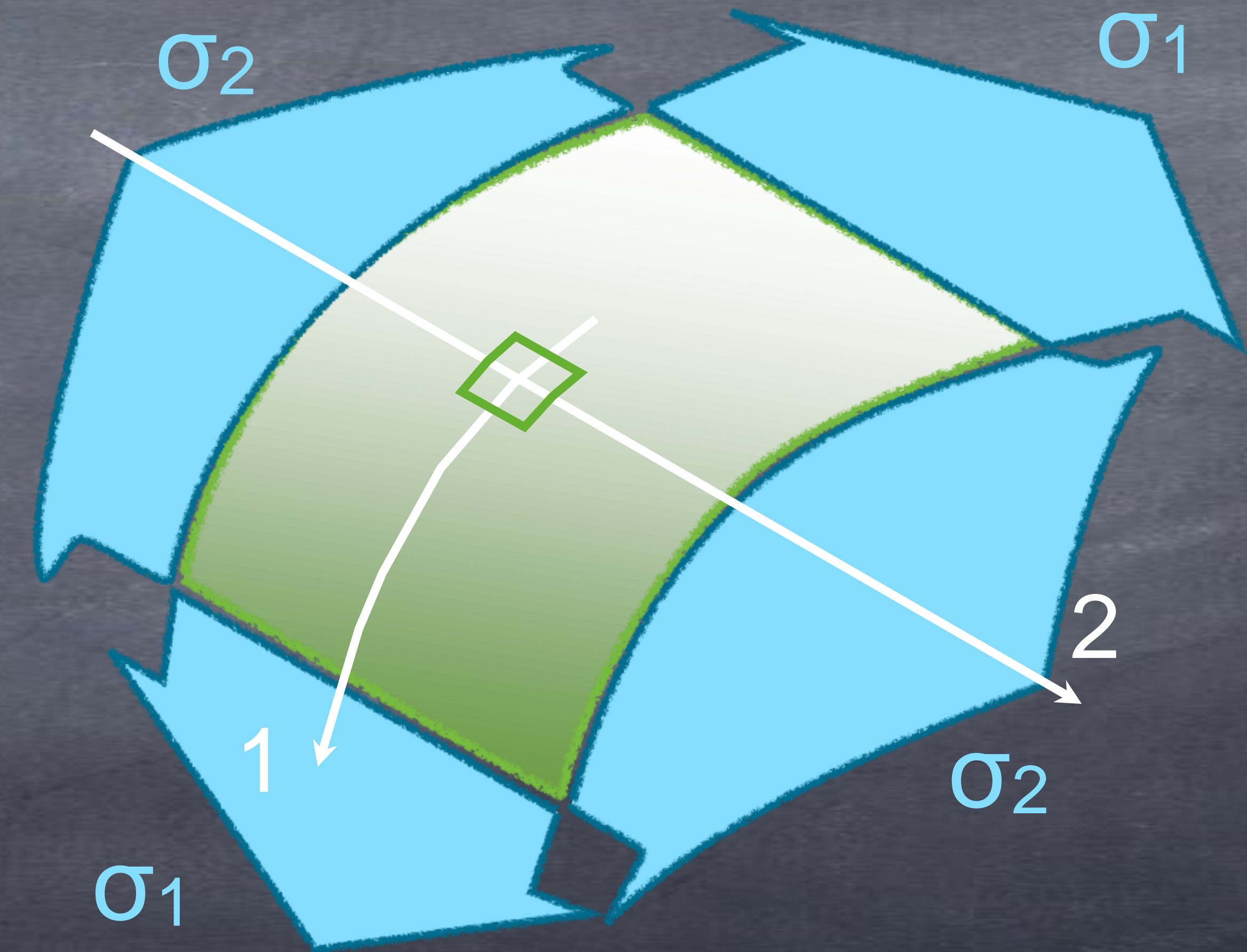
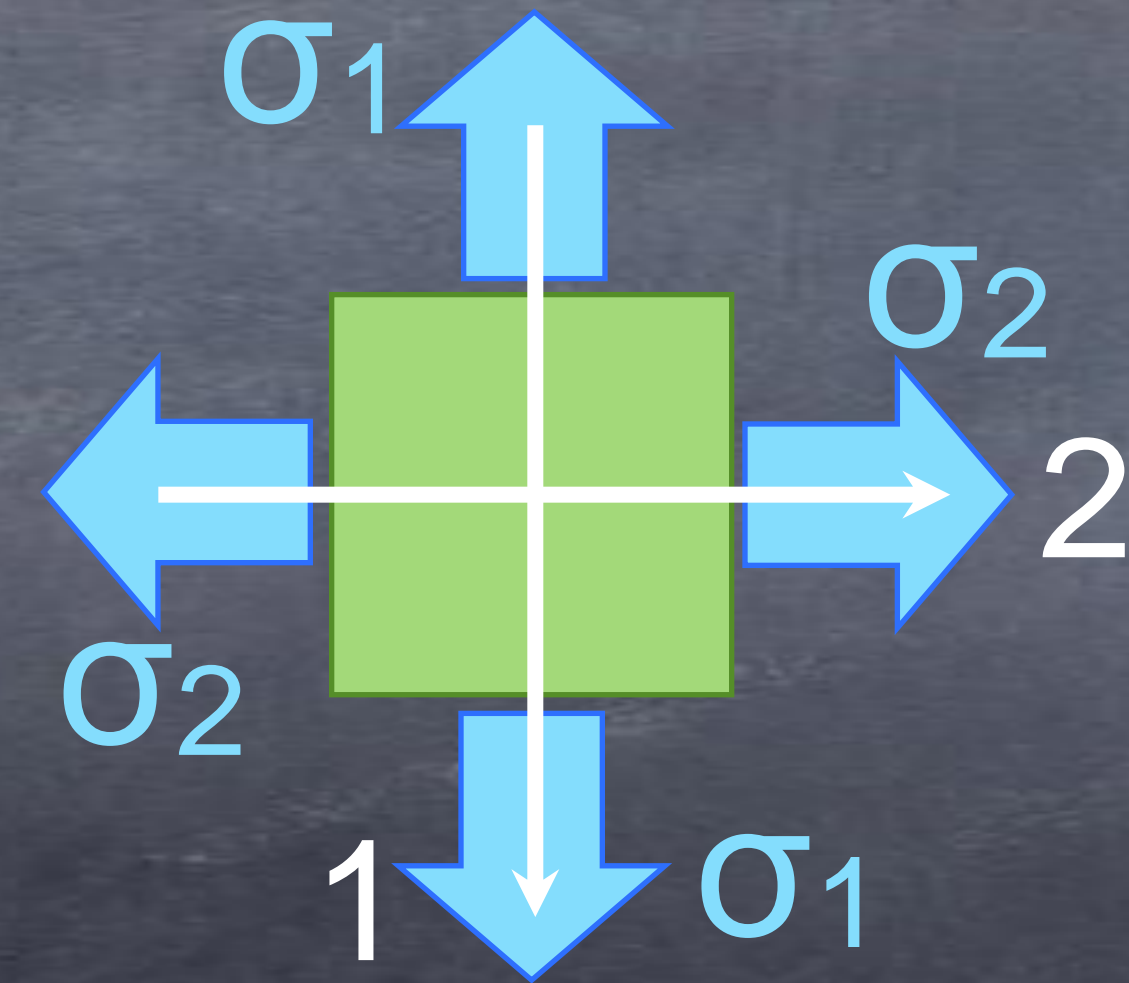


Cargas combinadas

Vasos de pressão de paredes finas

Estado de tensão causado por cargas combinadas

Representação

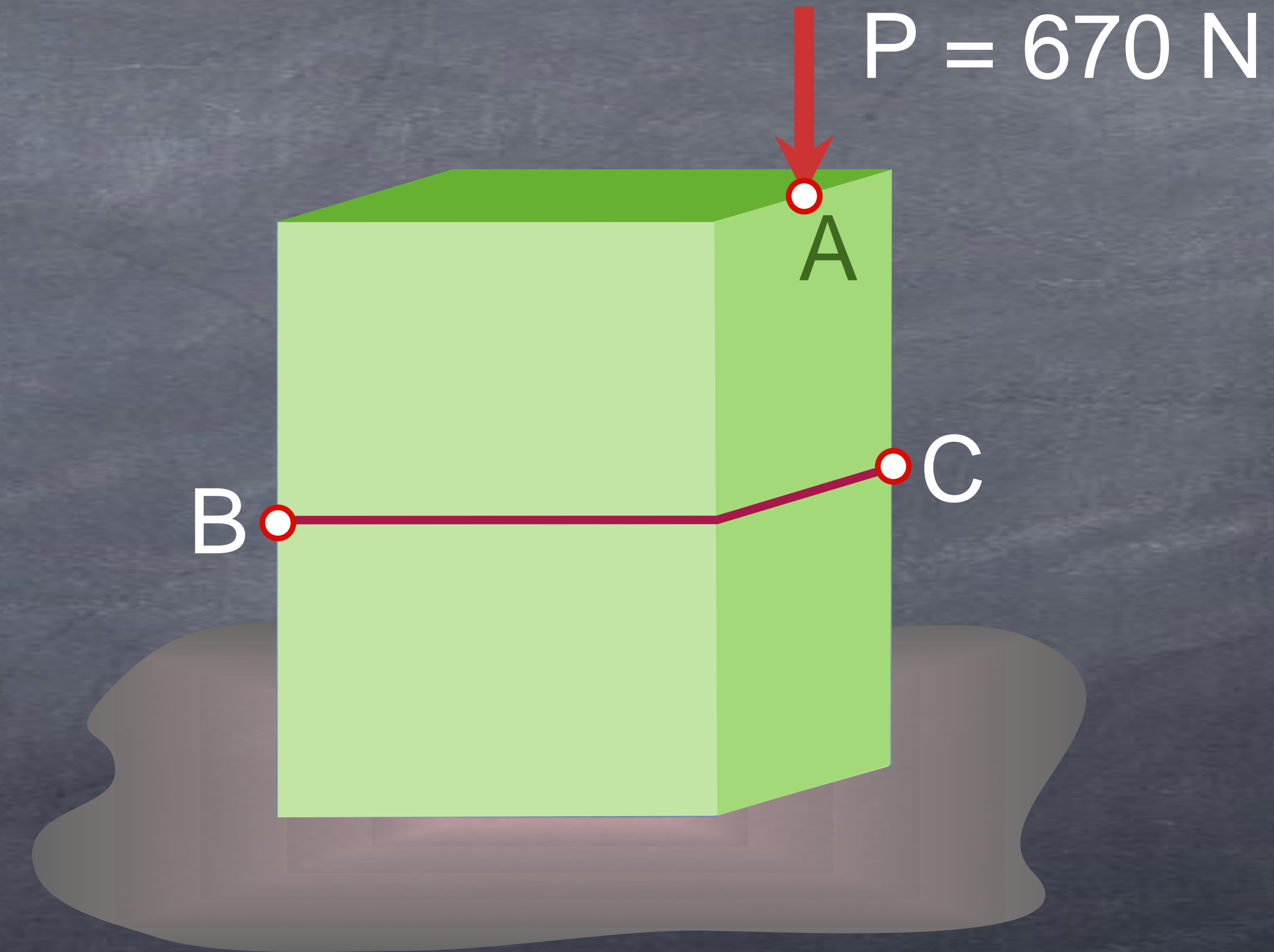
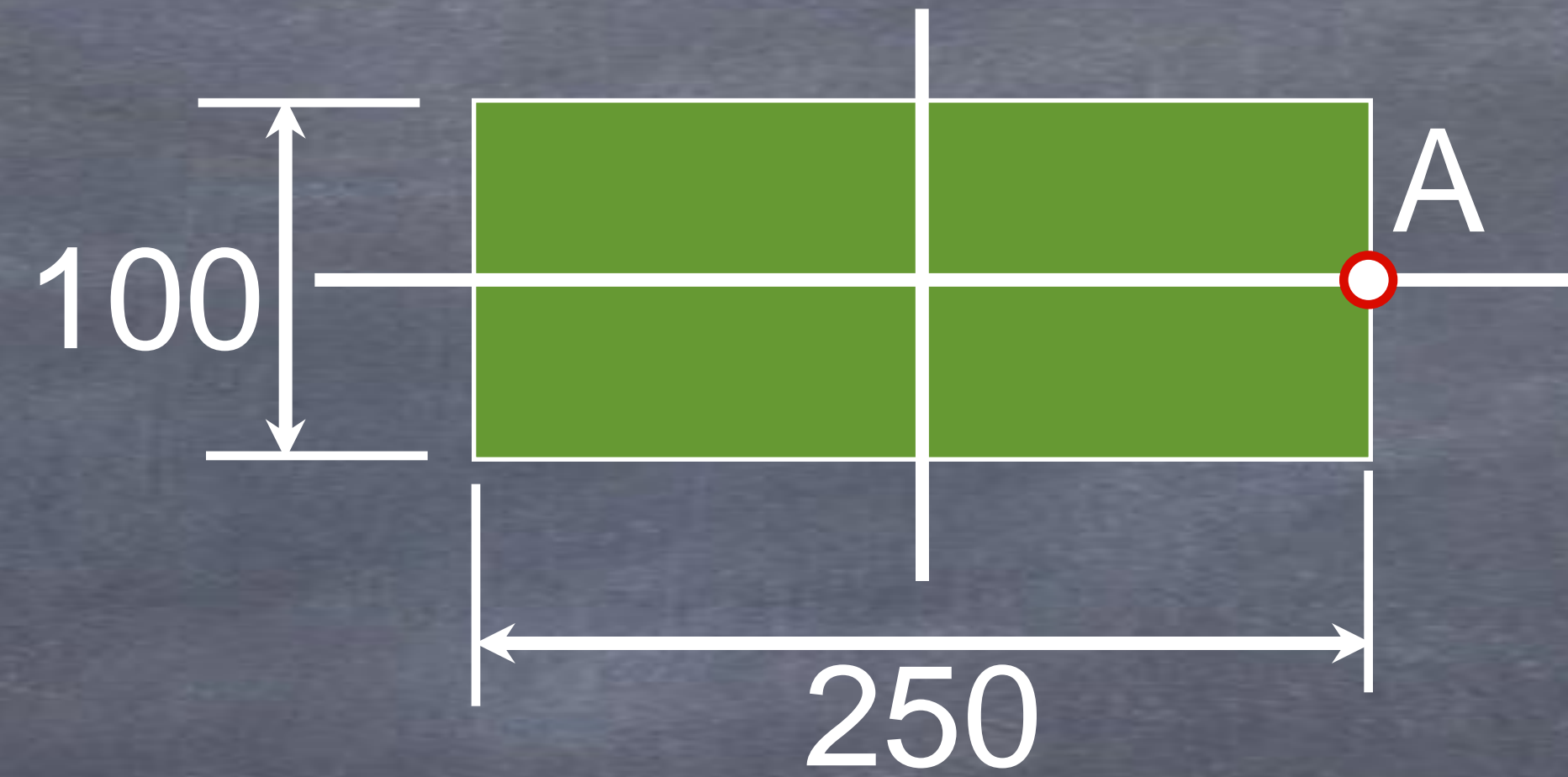


Cargas combinadas

Outros exemplos

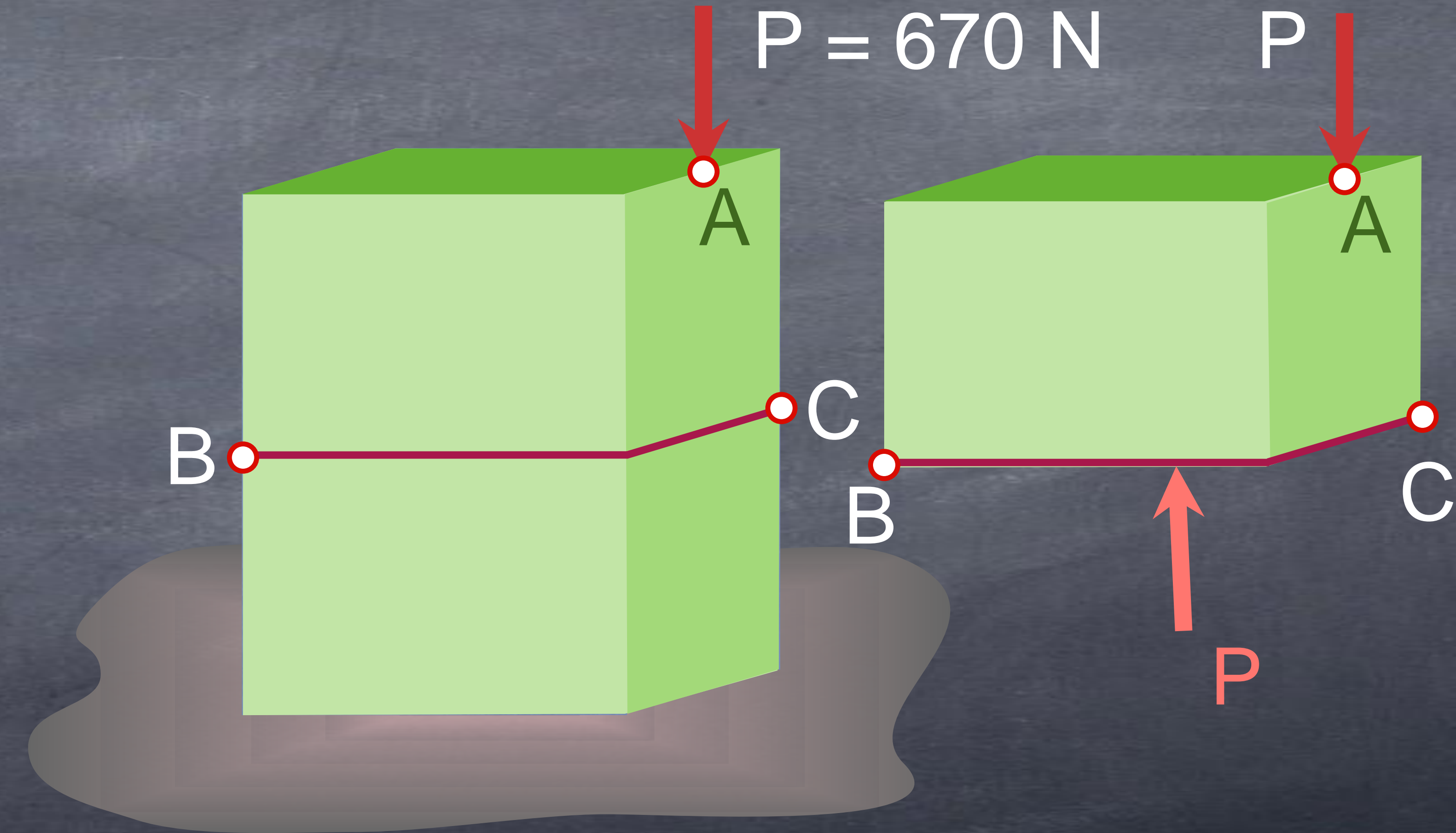
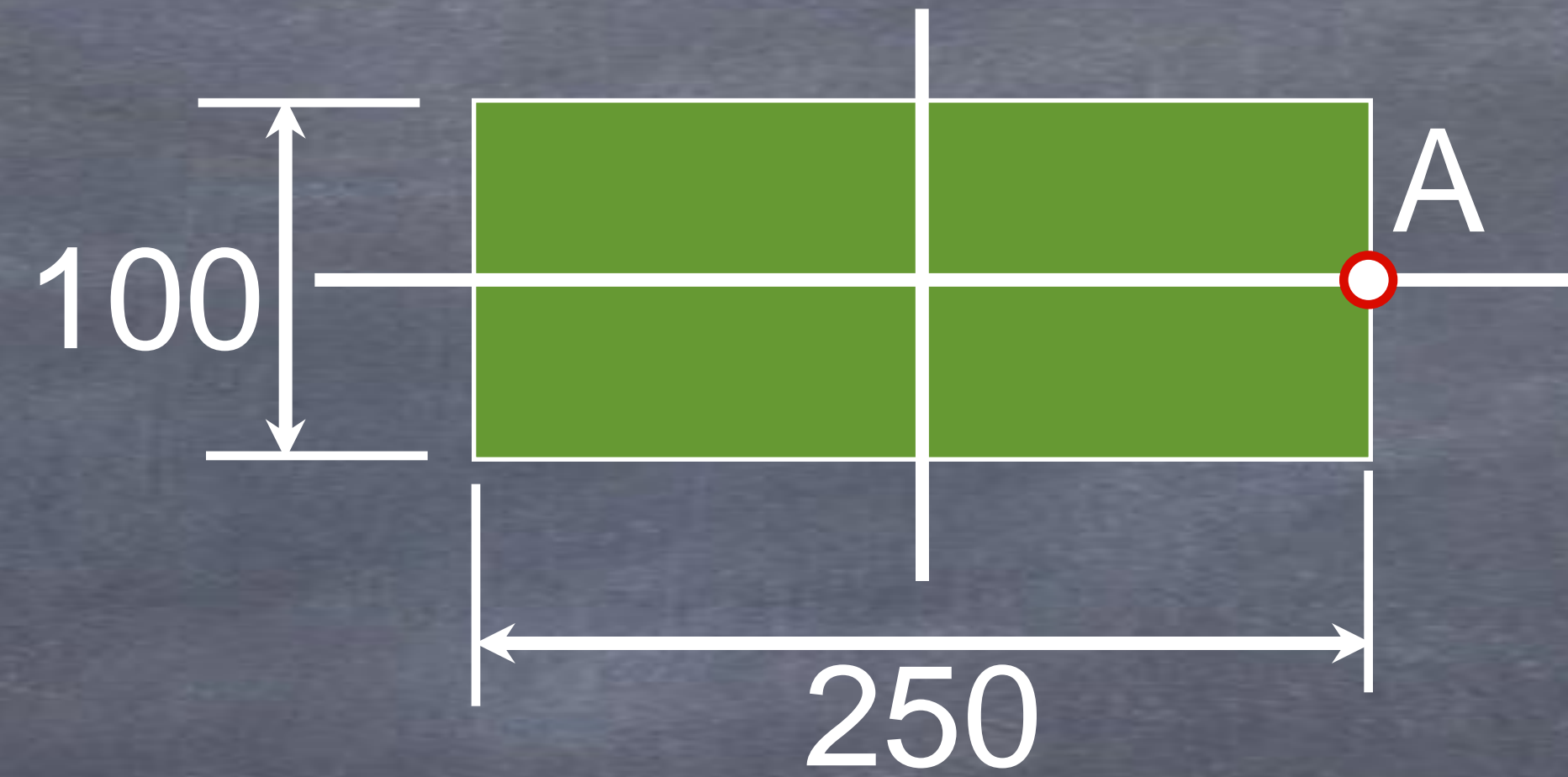
Outros exemplos

Determinar o estado de tensões nos pontos B e C da barra da figura.



Outros exemplos

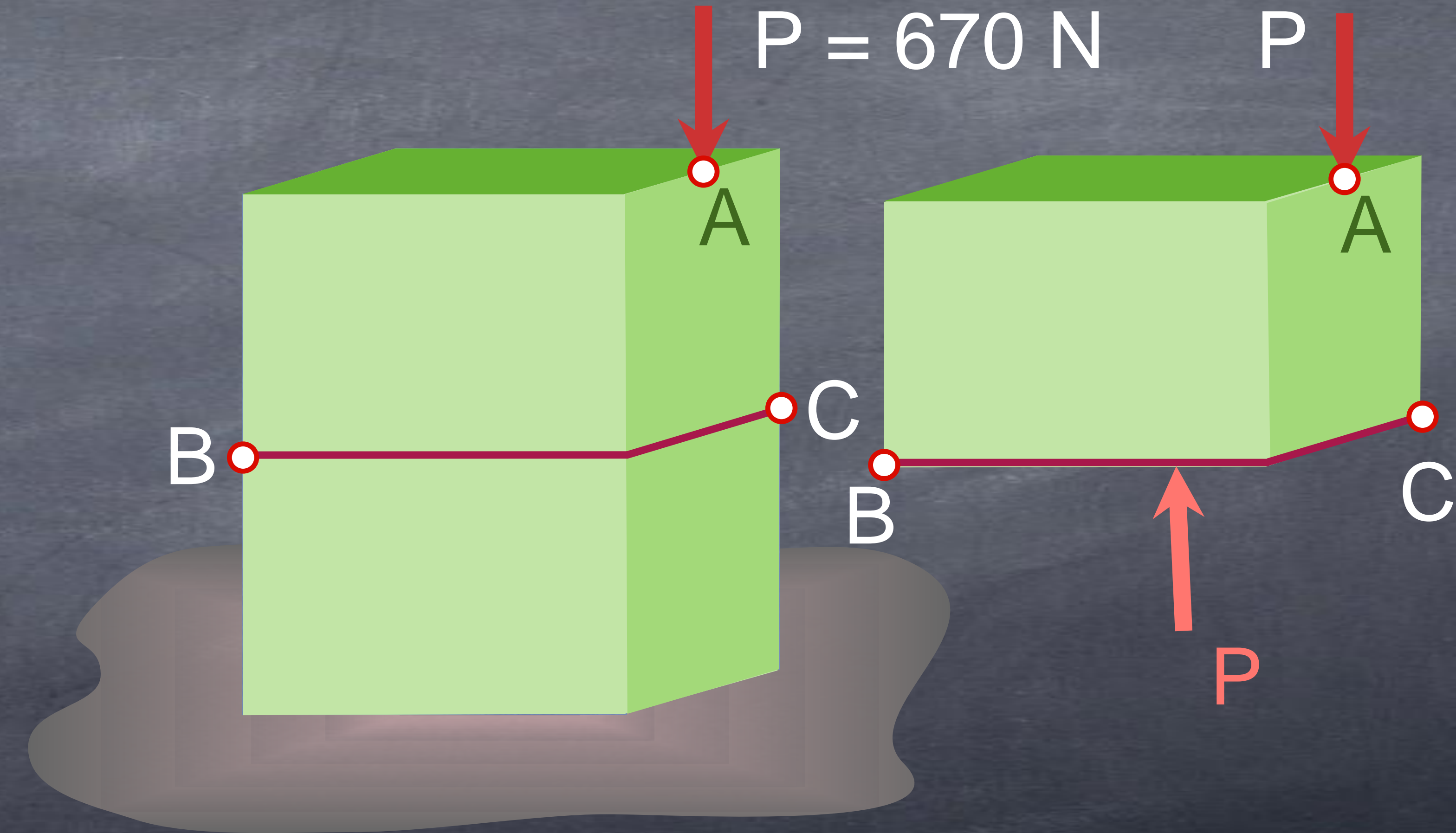
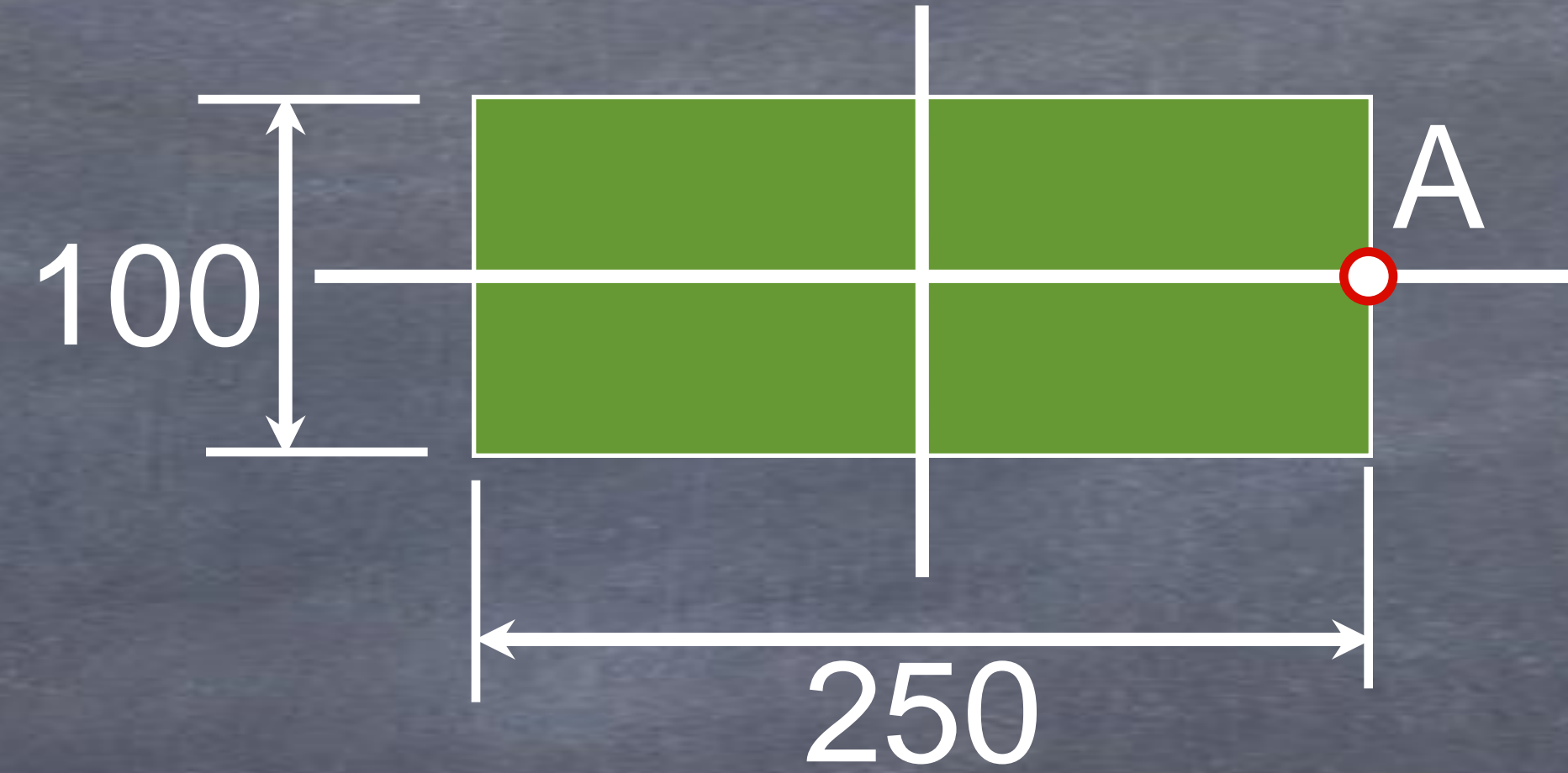
a) Tensão causada pela
força normal



Outros exemplos

a) Tensão causada pela
força normal

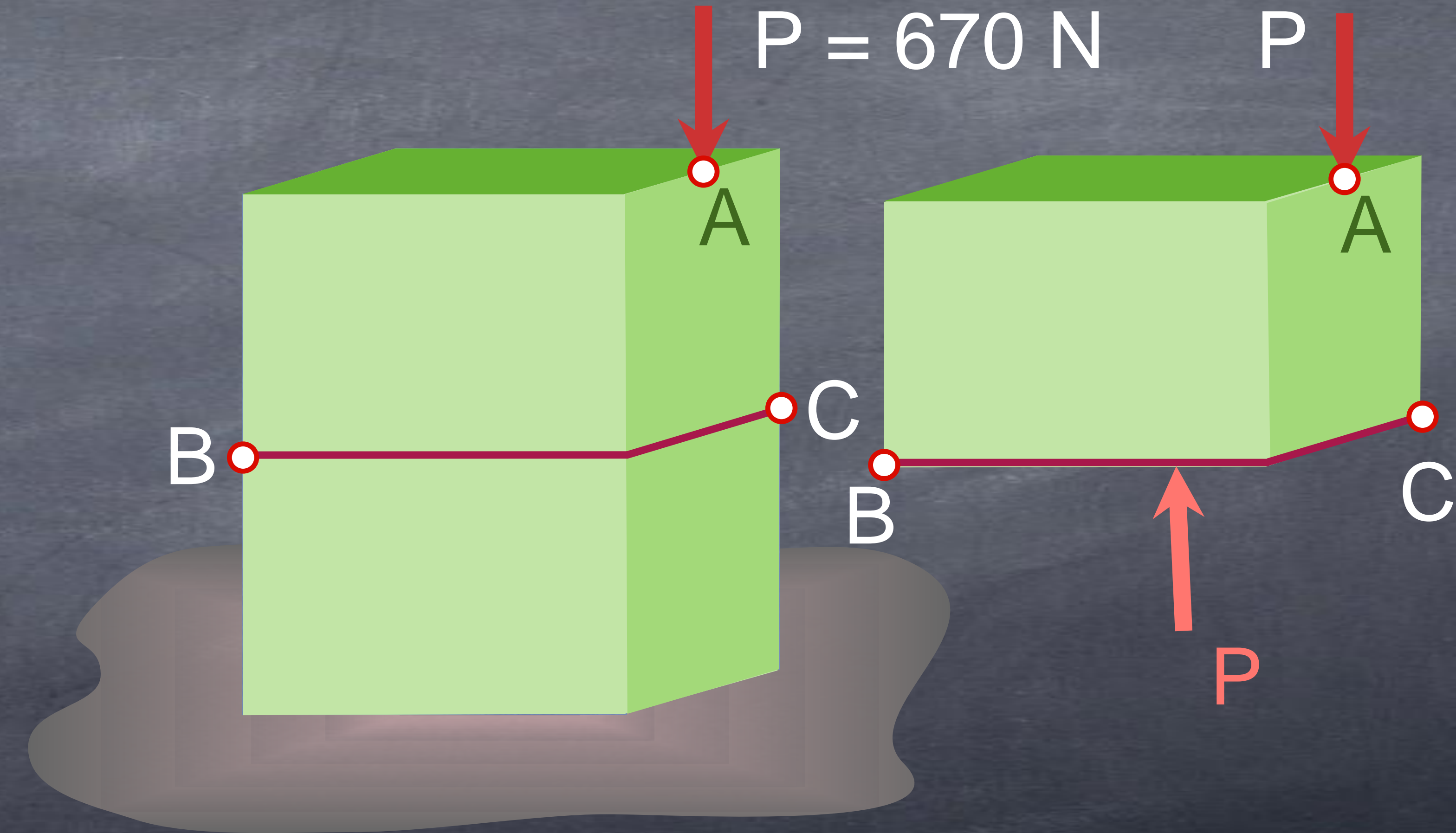
$$\sigma = P / A$$



Outros exemplos

a) Tensão causada pela força normal

$$\sigma = P / A = -670 / (0,10 \times 0,25)$$

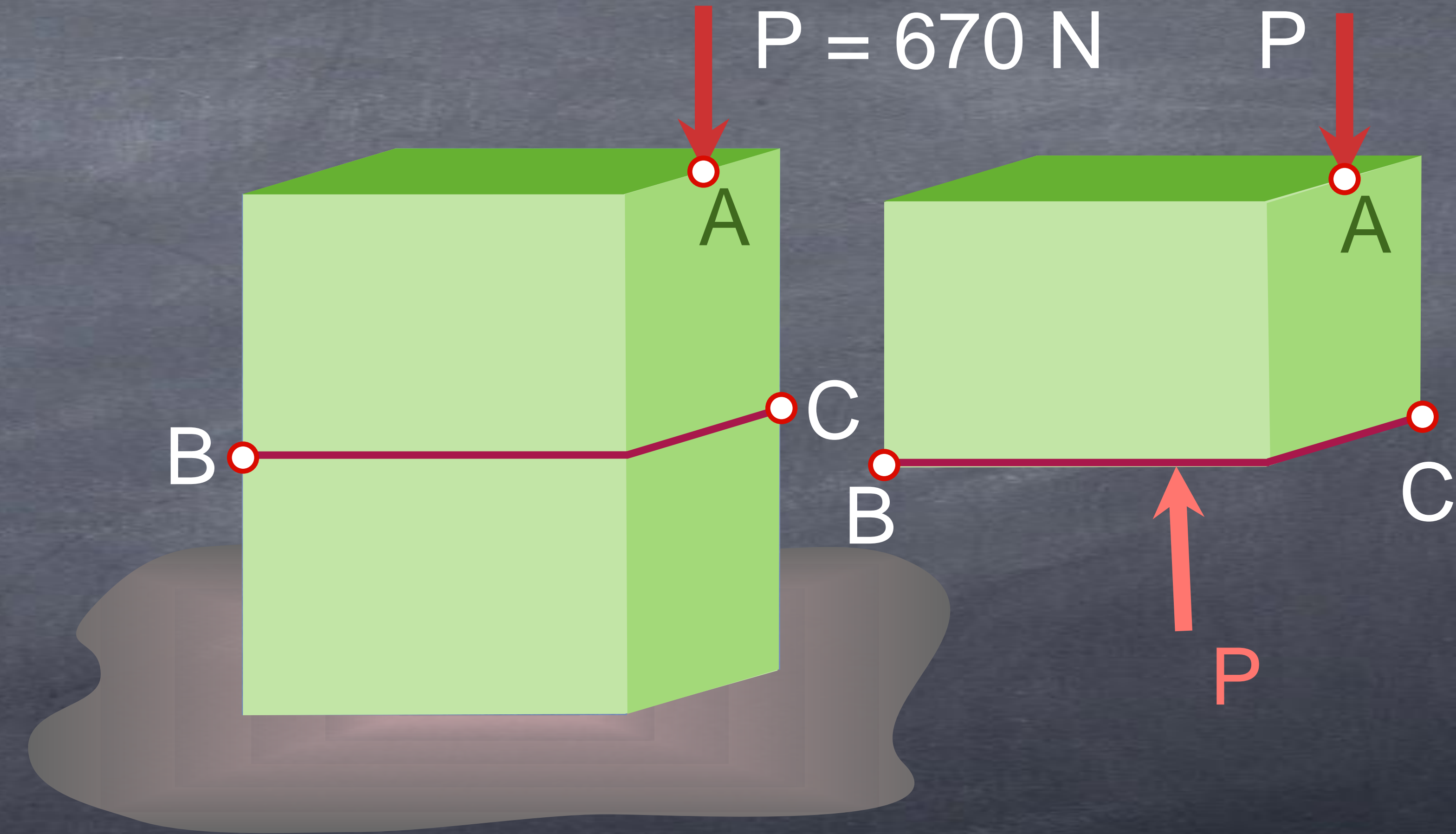


Outros exemplos

a) Tensão causada pela força normal

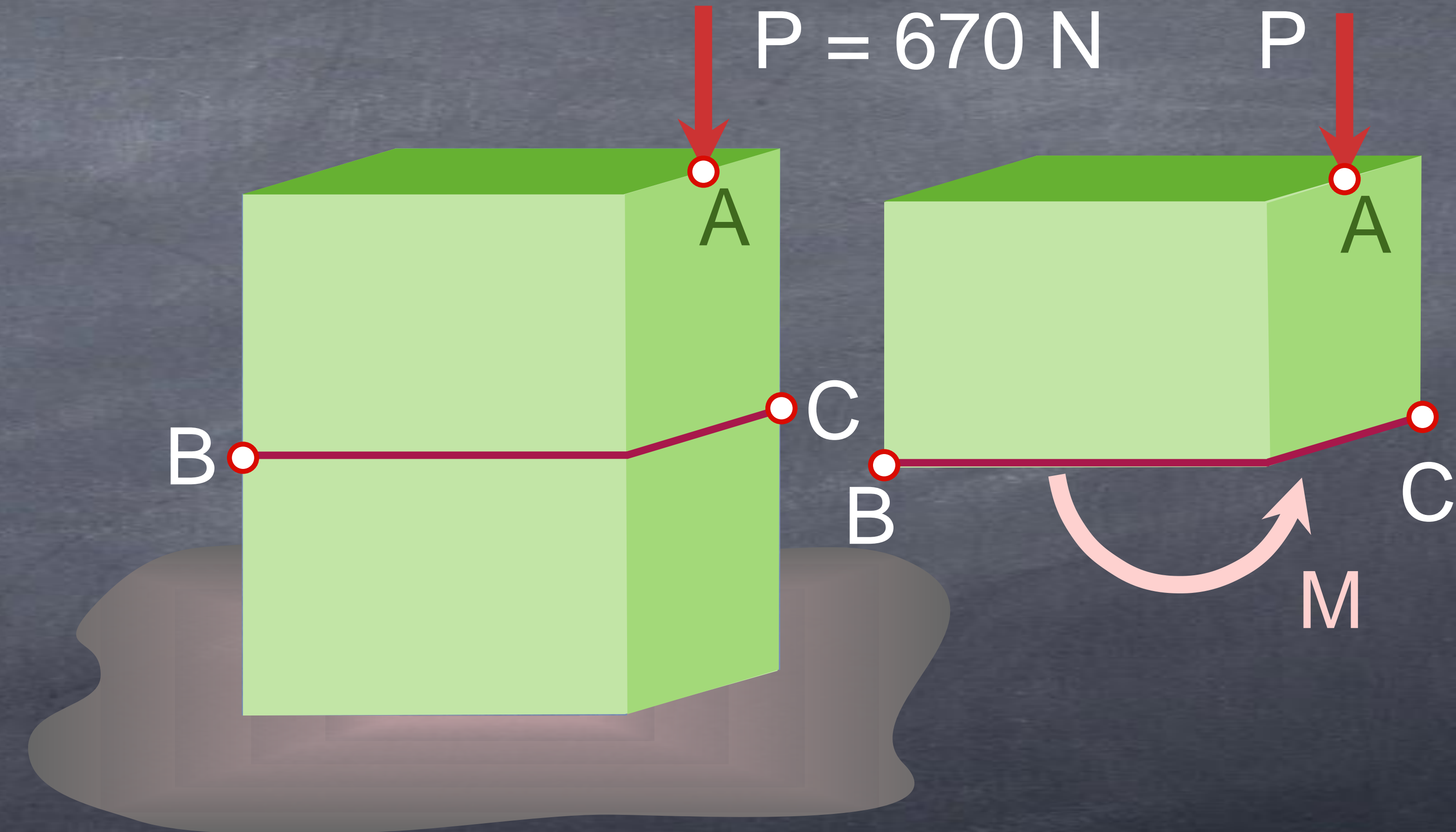
$$\sigma = P / A = -670 / (0,10 \times 0,25)$$

$$\sigma = -26.800 \text{ N/m}^2$$



Outros exemplos

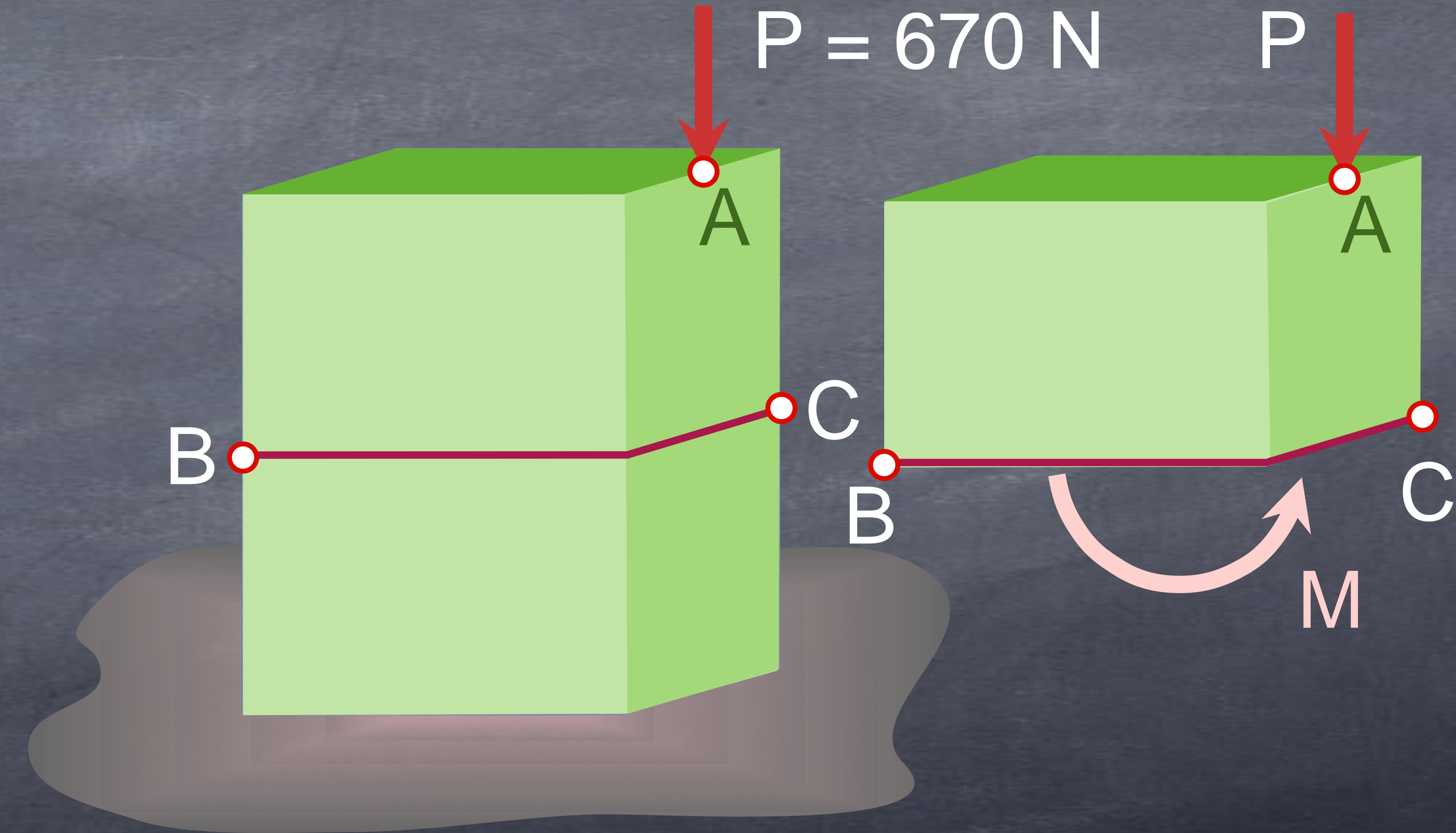
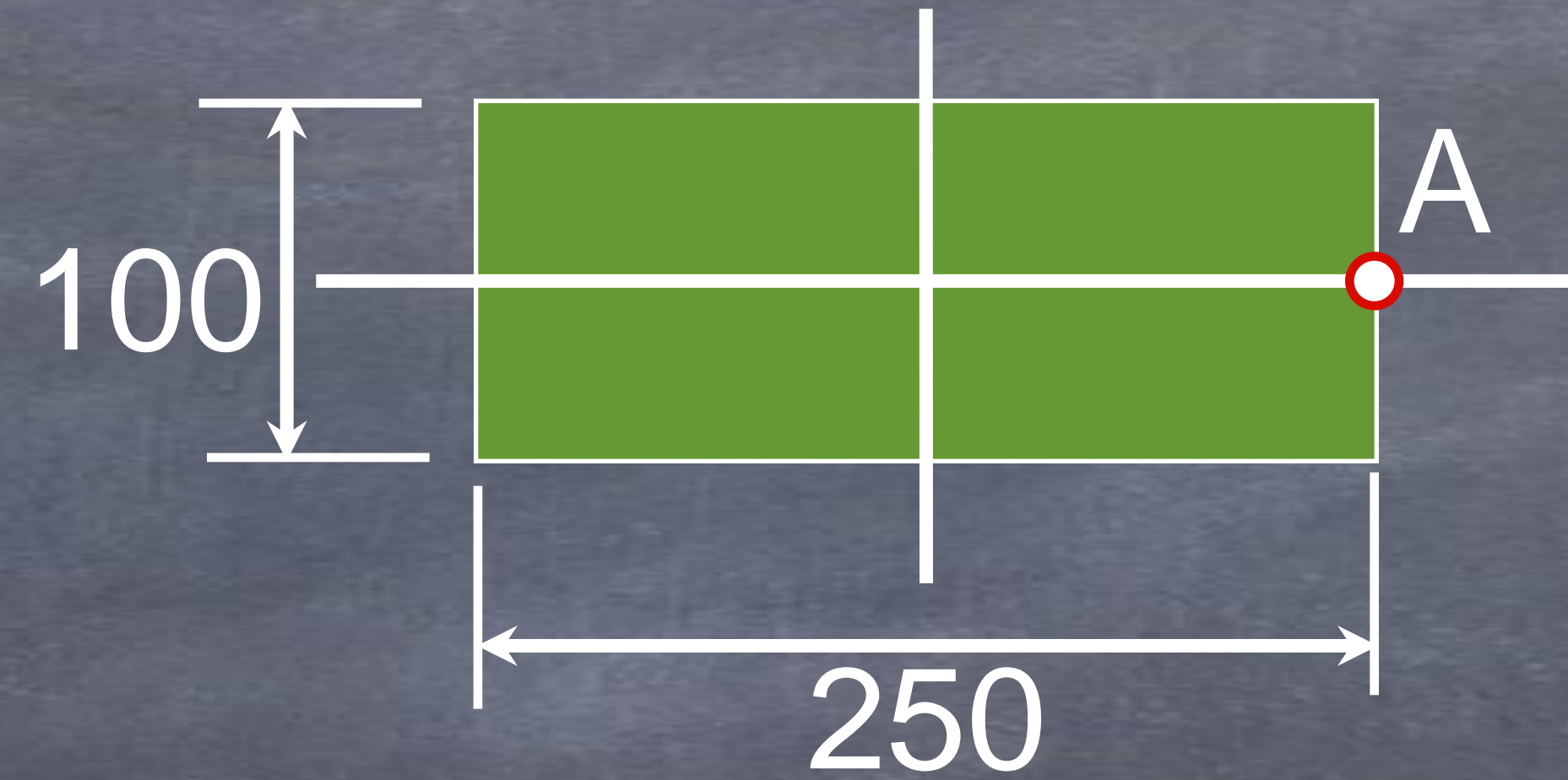
b) Tensão causada pelo momento fletor



Outros exemplos

b) Tensão causada pelo momento fletor

$$\sigma_{\max} = \pm M c / I$$

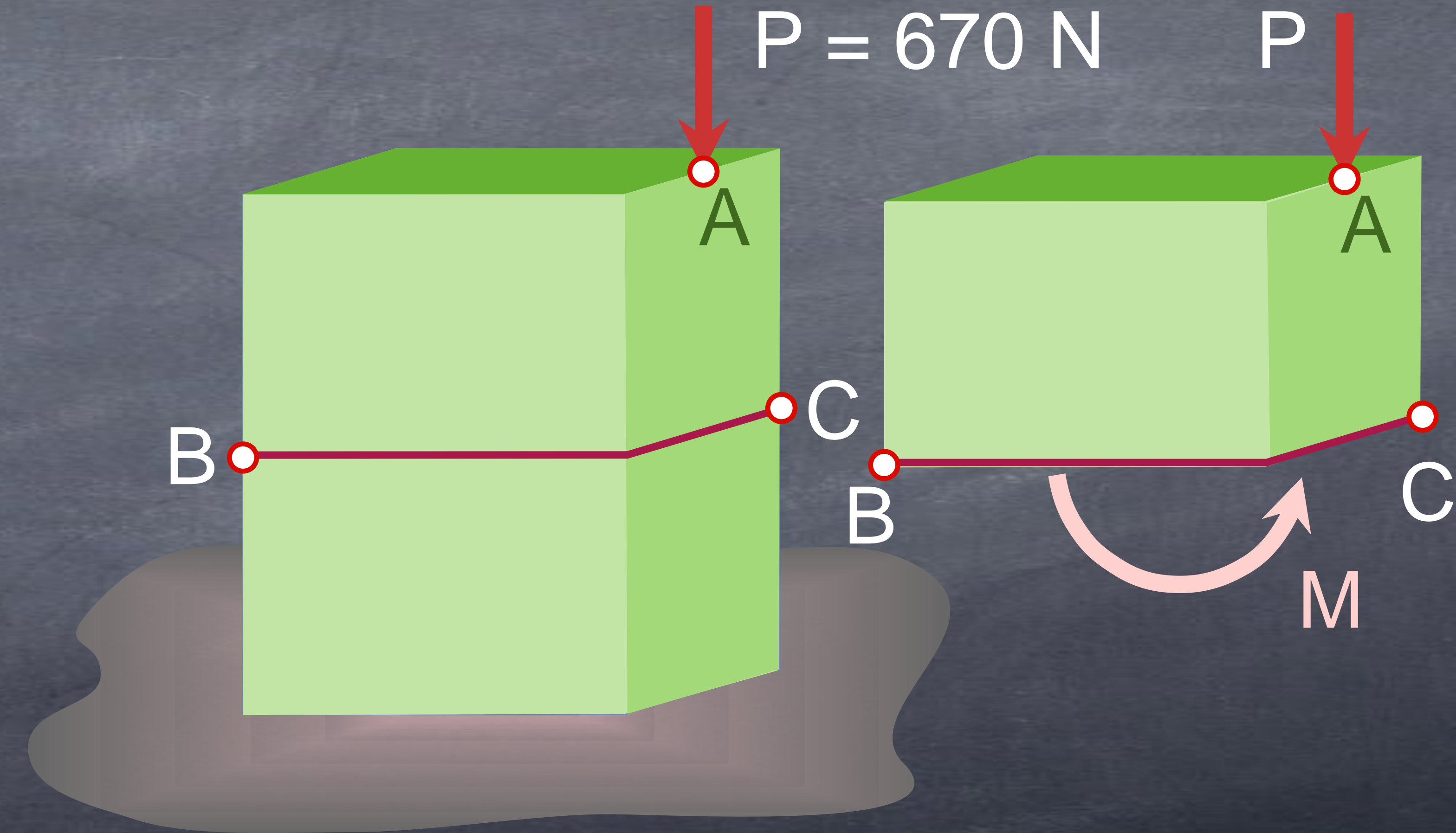
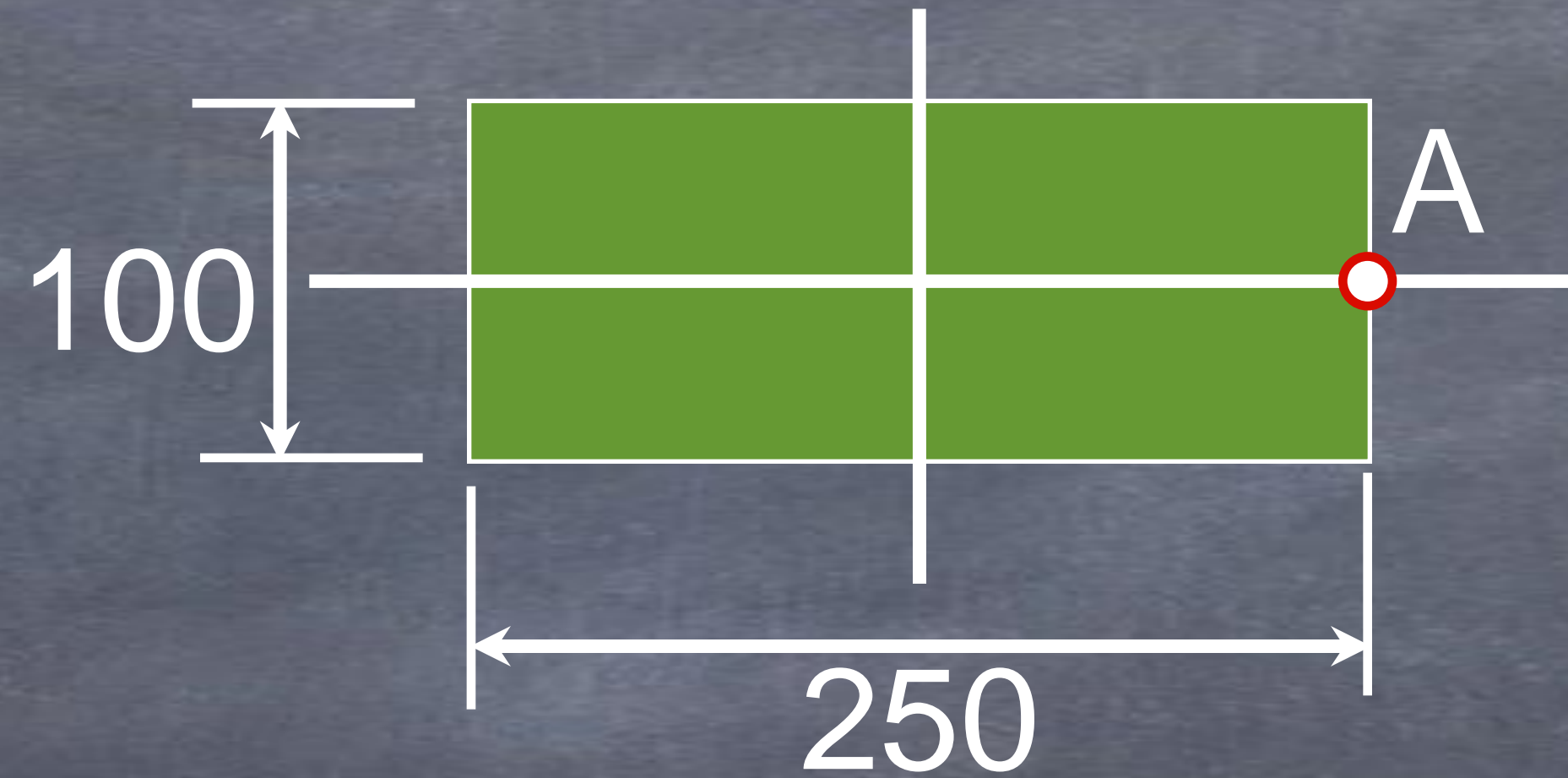


Outros exemplos

b) Tensão causada pelo momento fletor

$$\sigma_{\max} = \pm M c / I$$

$$\sigma_{\max} = \pm 670 \times (0,25/2) \times (0,25/2) / [(0,10 \times 0,25^3) / 12]$$



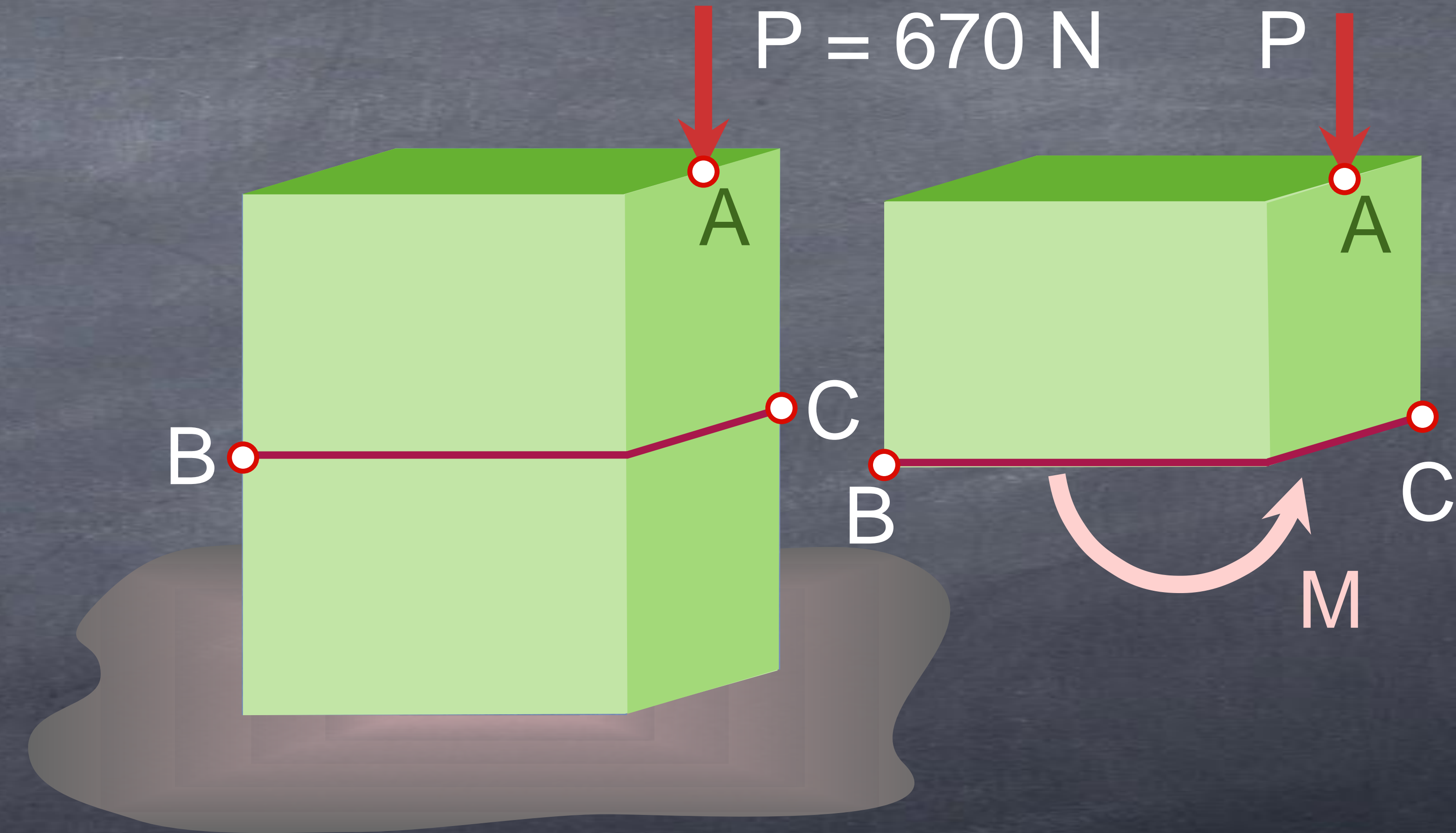
Outros exemplos

b) Tensão causada pelo momento fletor

$$\sigma_{\max} = \pm M c / I$$

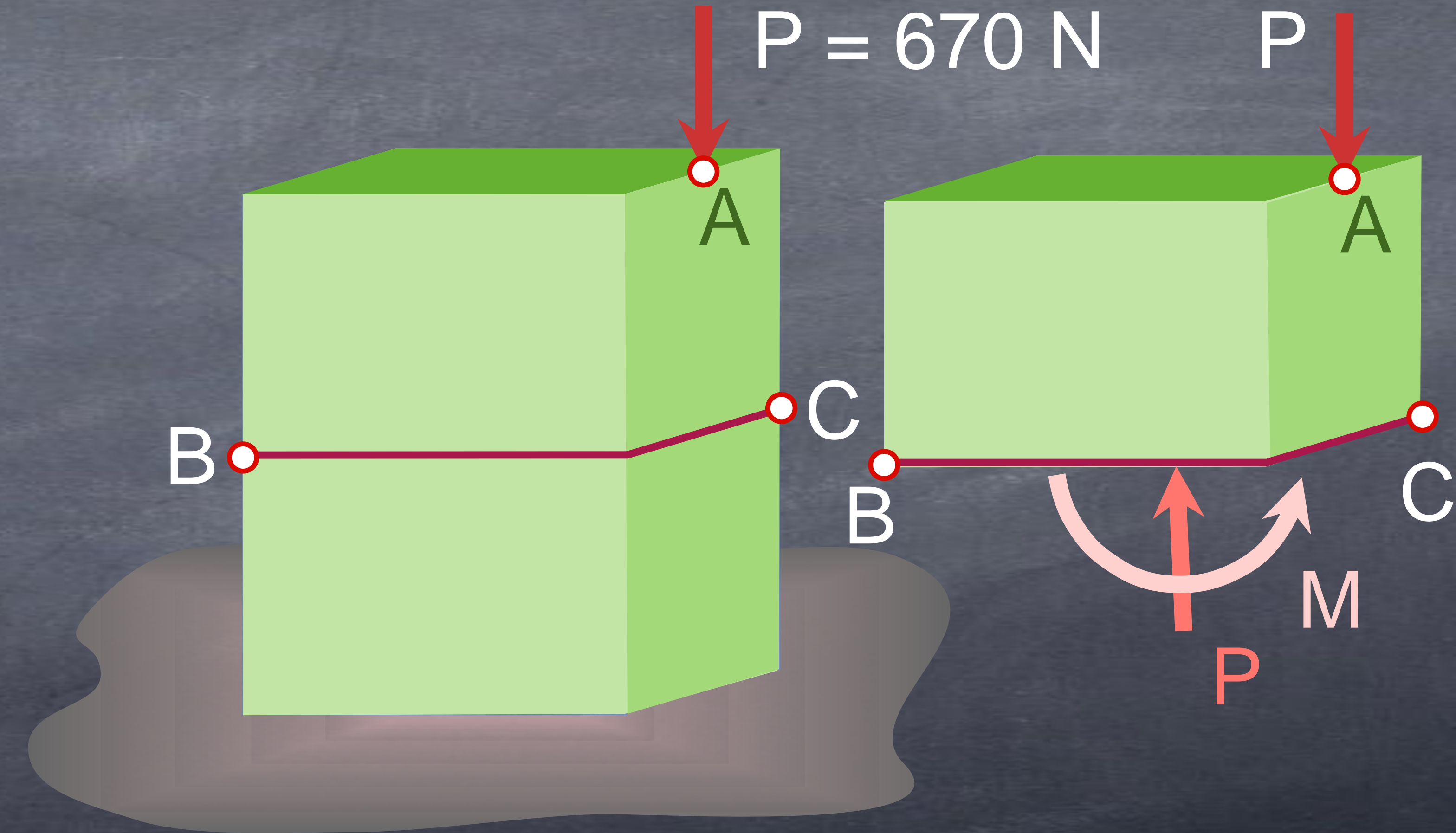
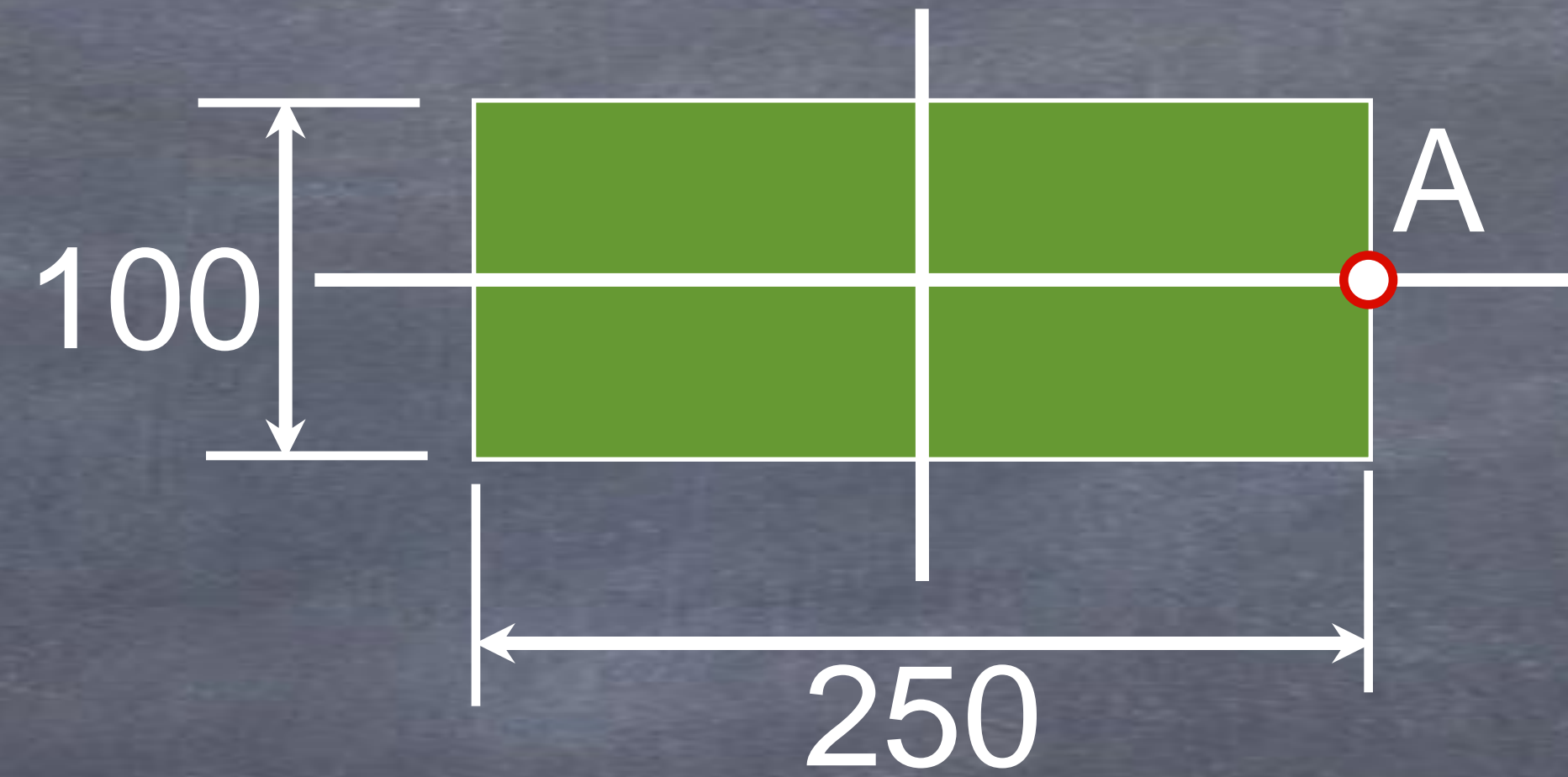
$$\sigma_{\max} = \pm 670 \times (0,25/2) \times (0,25/2) / [(0,10 \times 0,25^3) / 12]$$

$$\sigma_{\max} = \pm 80.400 \text{ N/m}^2$$



Outros exemplos

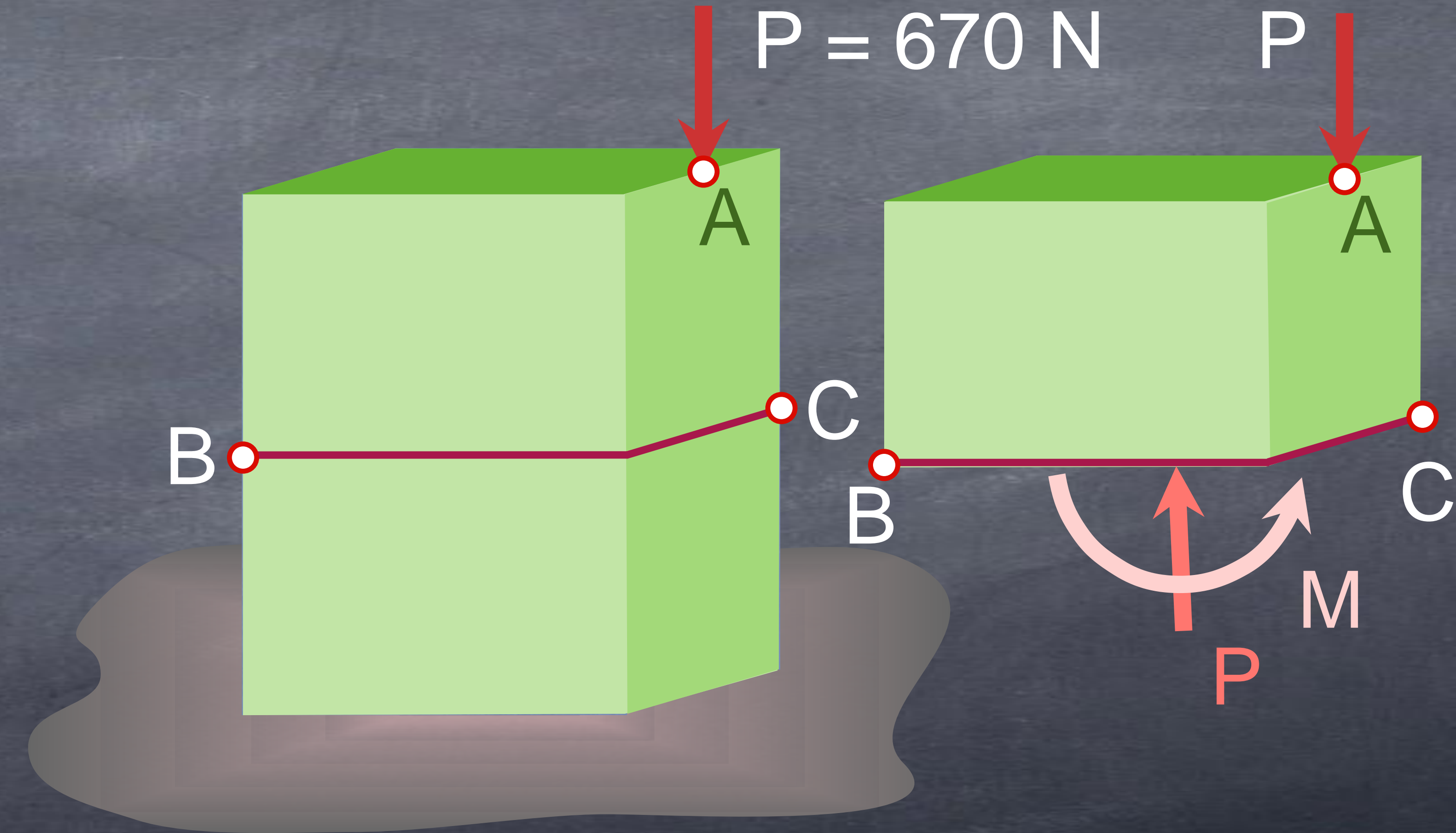
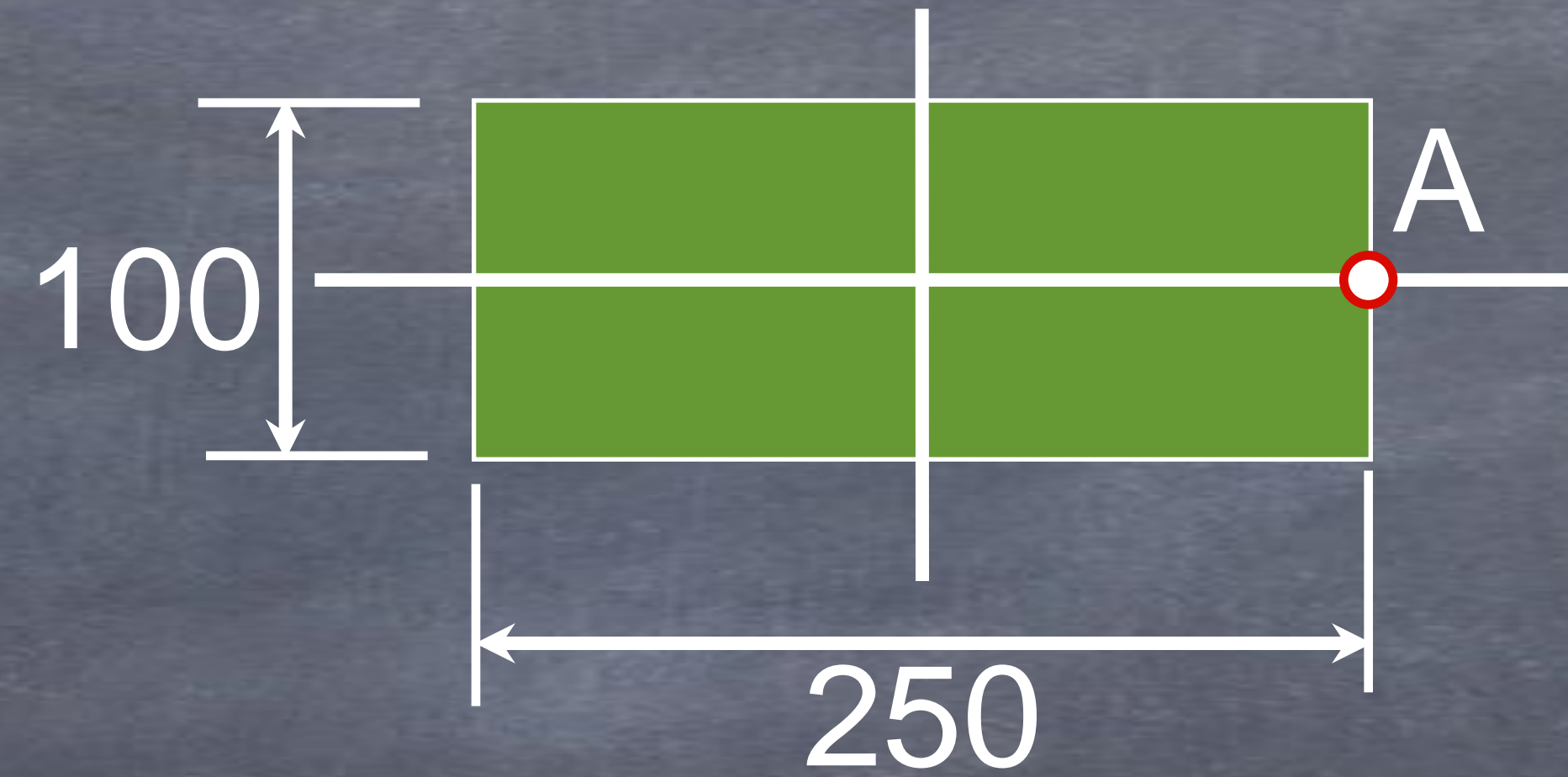
c) Superposição das tensões



Outros exemplos

c) Superposição das tensões

$$\sigma_B = \sigma + \sigma_{\max}$$

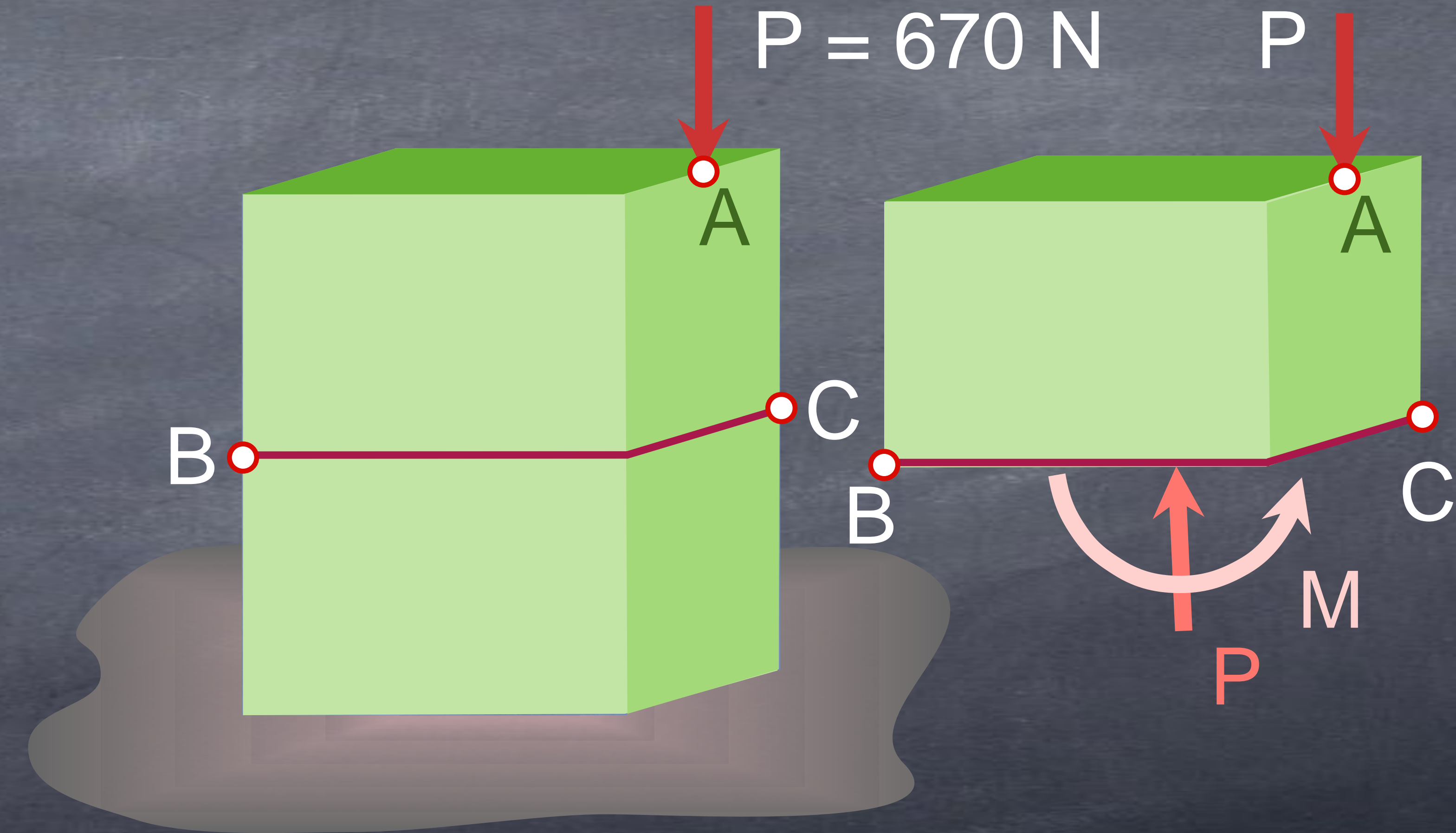


Outros exemplos

c) Superposição das tensões

$$\sigma_B = \sigma + \sigma_{\max}$$

$$\sigma_C = \sigma - \sigma_{\max}$$

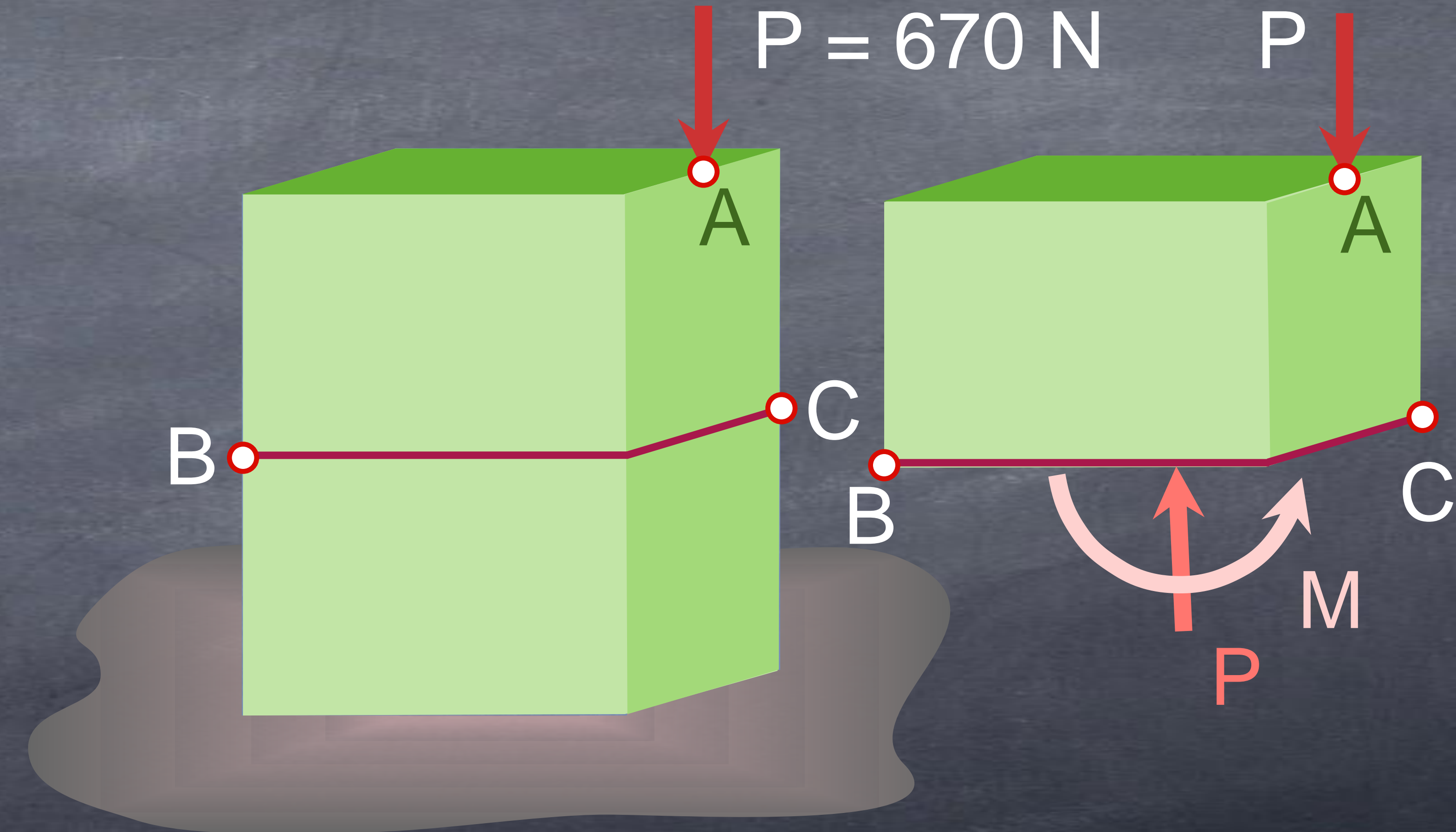


Outros exemplos

c) Superposição das tensões

$$\sigma_B = \sigma + \sigma_{\max}$$

$$\sigma_C = \sigma - \sigma_{\max}$$

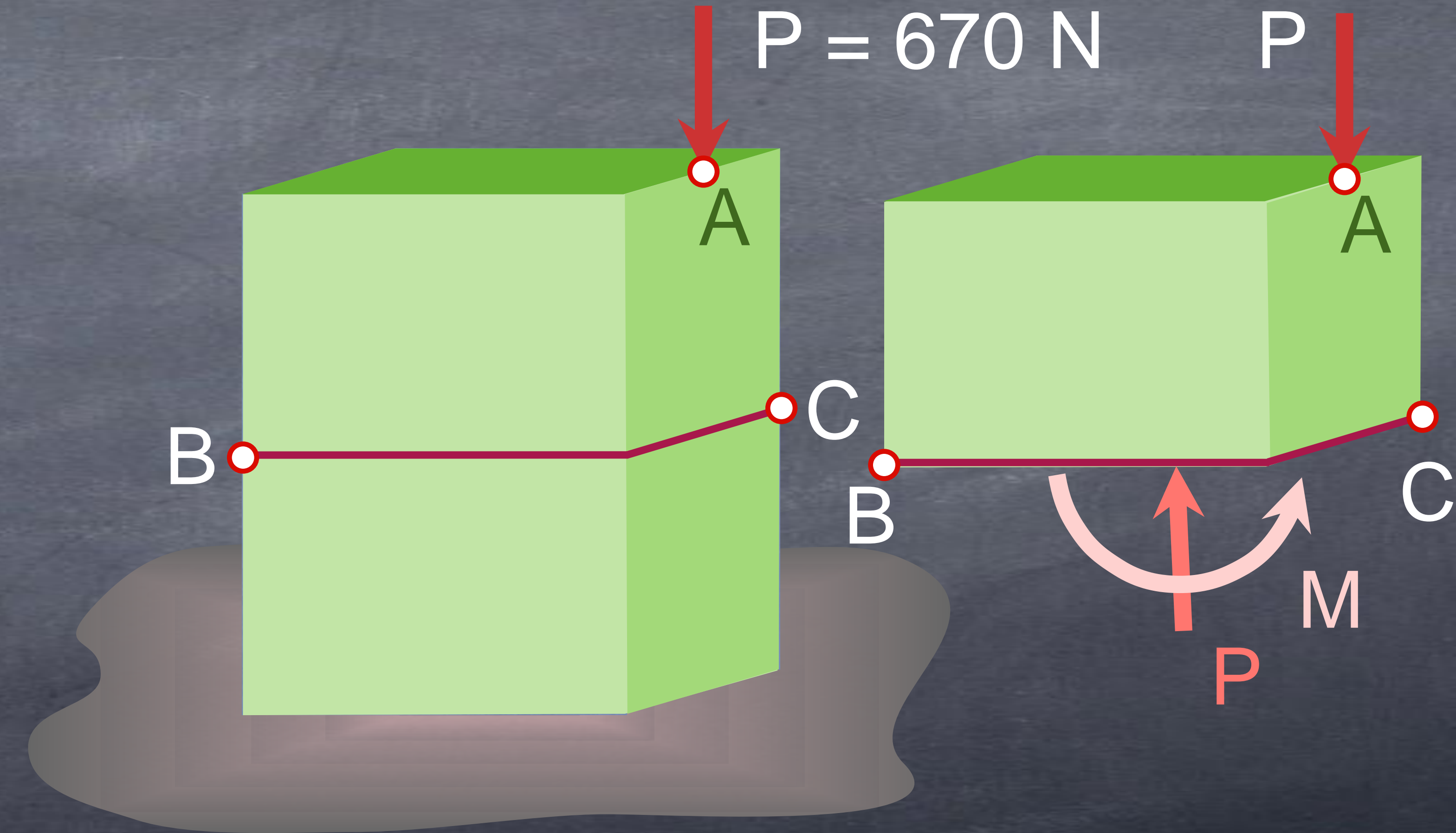


Outros exemplos

c) Superposição das tensões

$$\sigma_B = \sigma + \sigma_{\max} = -26.800 + 80.400$$

$$\sigma_C = \sigma - \sigma_{\max}$$

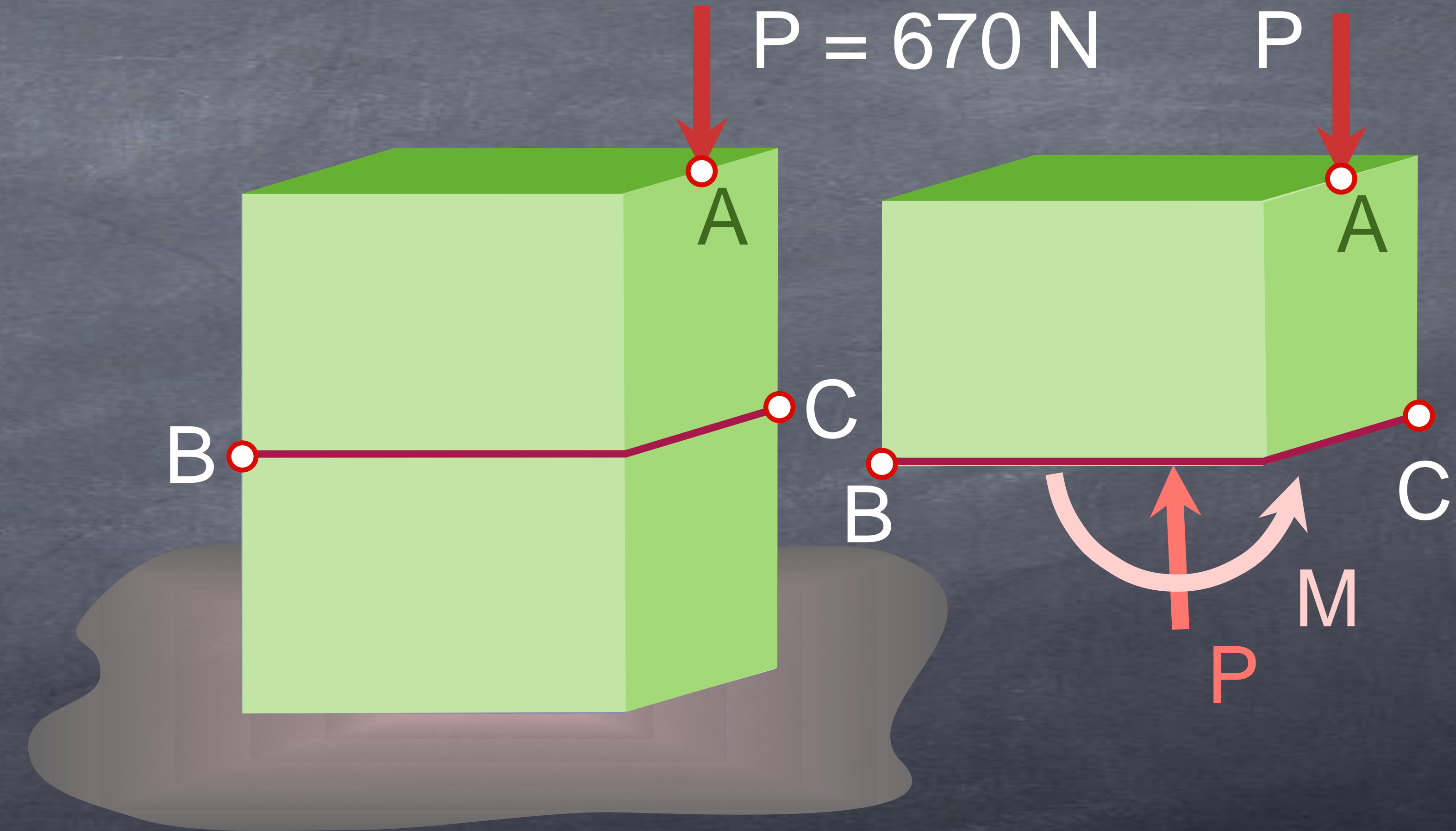


Outros exemplos

c) Superposição das tensões

$$\sigma_B = \sigma + \sigma_{\max} = -26.800 + 80.400$$

$$\sigma_C = \sigma - \sigma_{\max} = -26.800 - 80.400$$

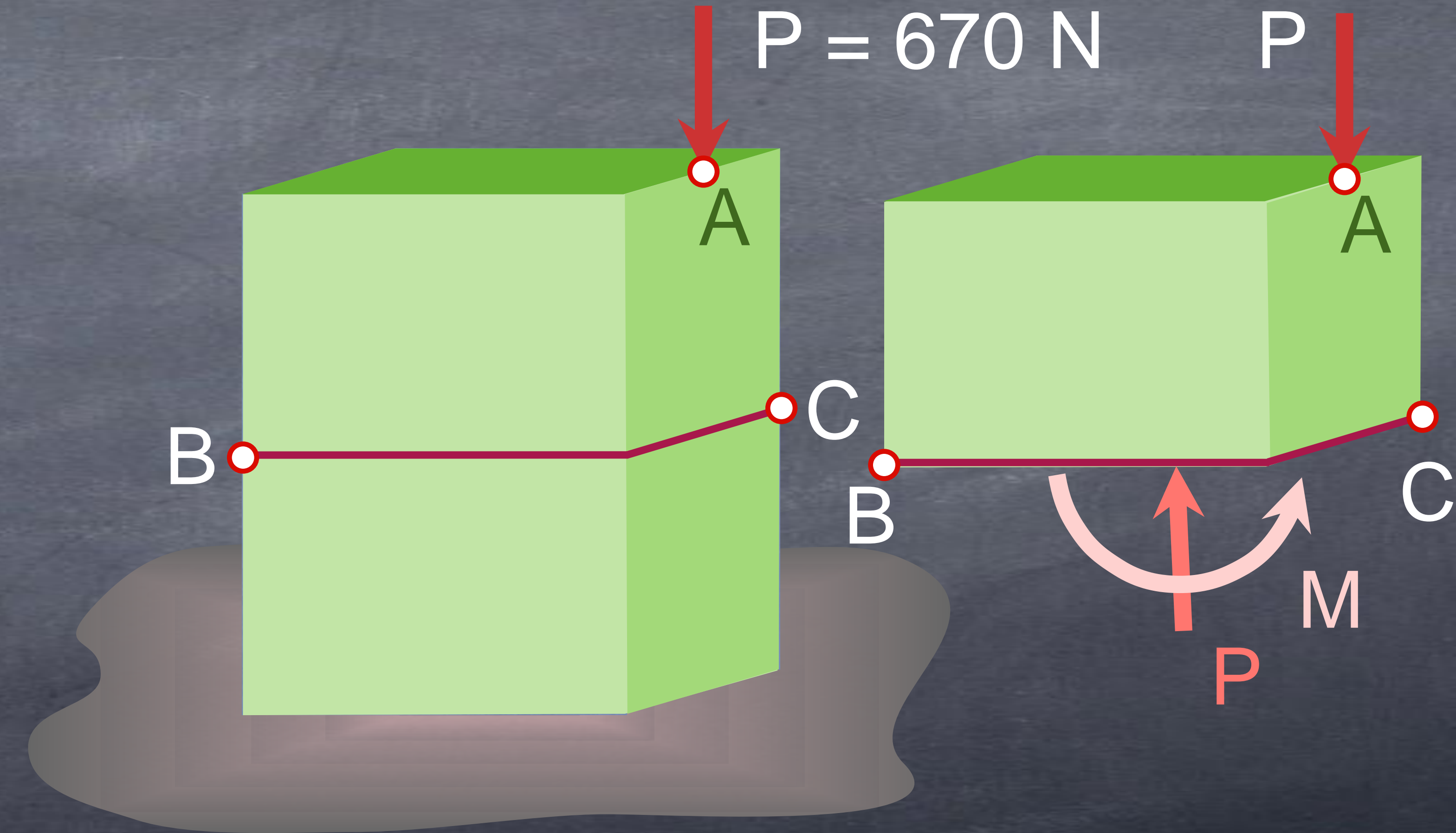


Outros exemplos

c) Superposição das tensões

$$\sigma_B = \sigma + \sigma_{\max} = 53.600 \text{ N/m}^2$$

$$\sigma_C = \sigma - \sigma_{\max} = -107.200 \text{ N/m}^2$$

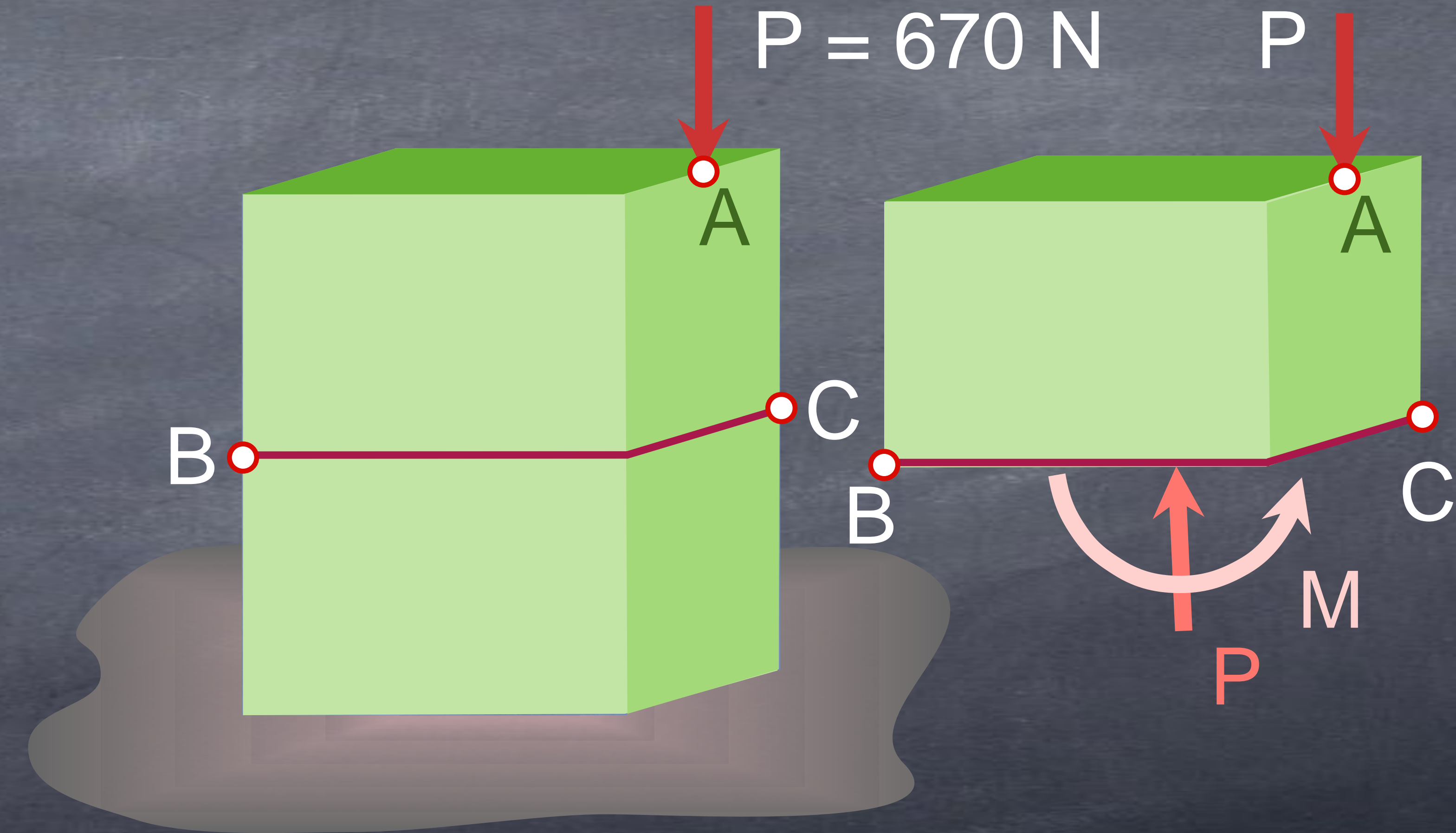
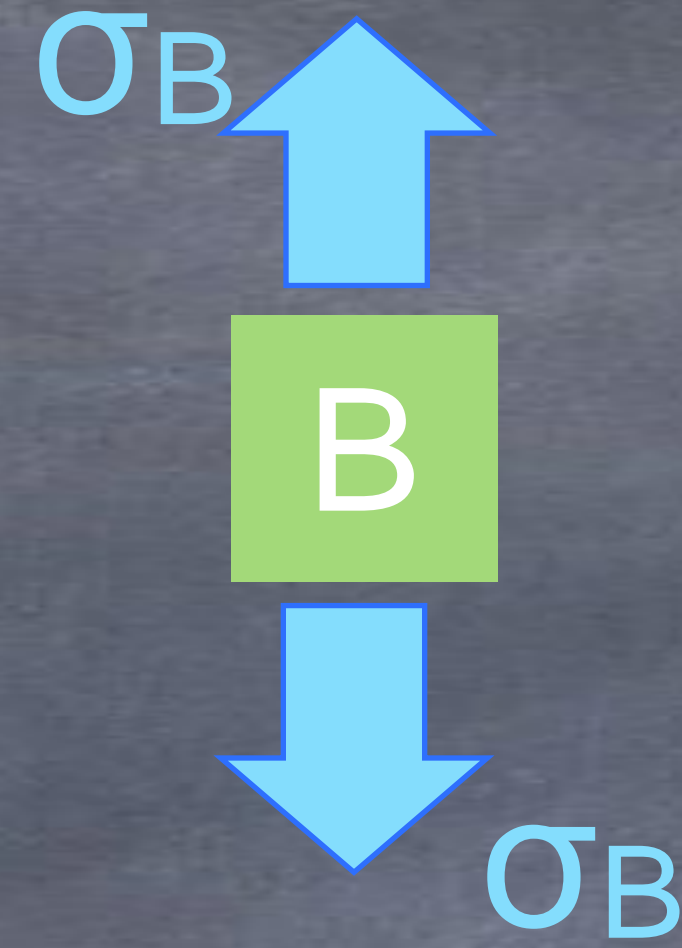


Outros exemplos

c) Superposição das tensões

$$\sigma_B = \sigma + \sigma_{\max} = 53.600 \text{ N/m}^2$$

$$\sigma_C = \sigma - \sigma_{\max} = -107.200 \text{ N/m}^2$$

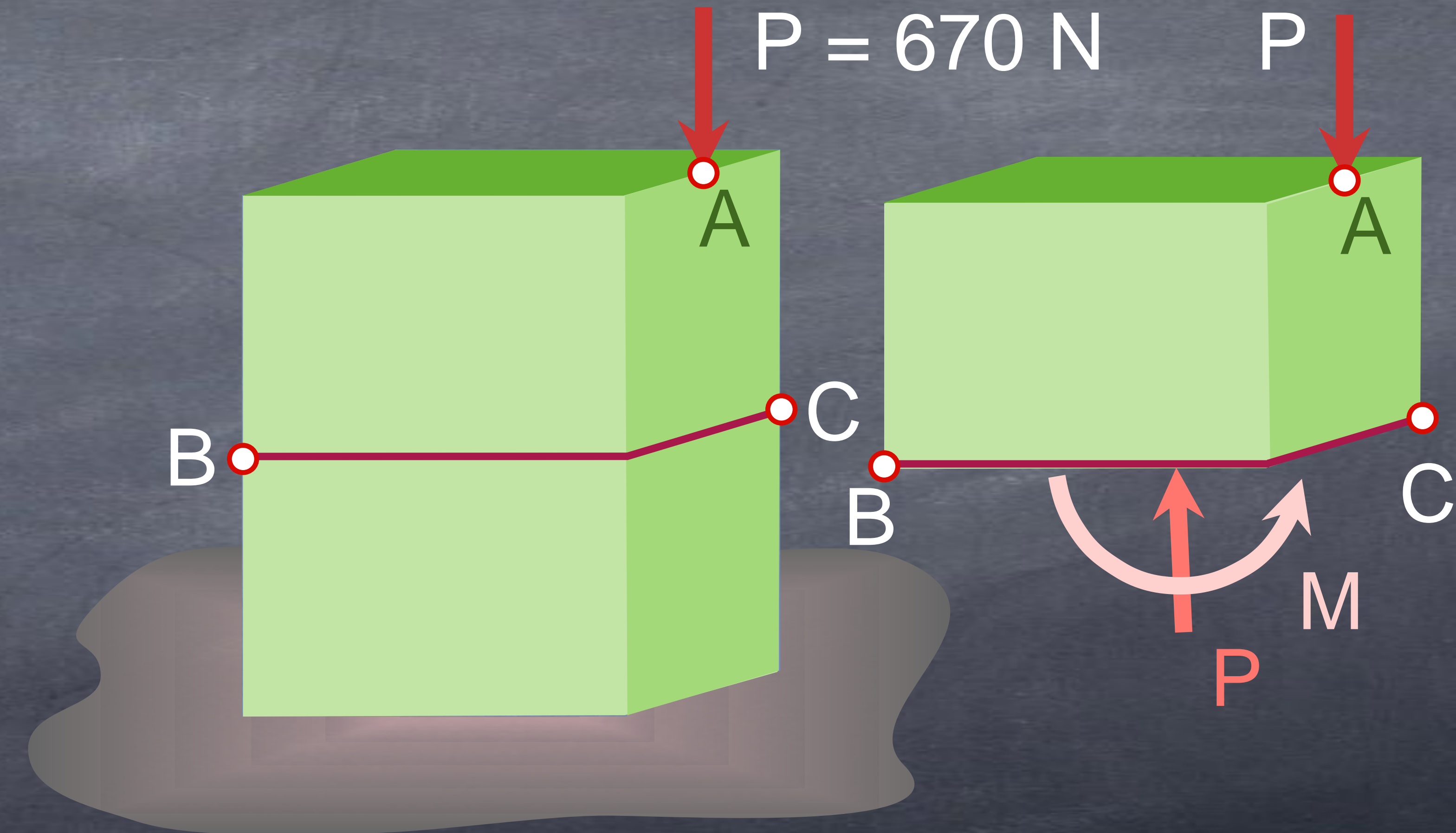
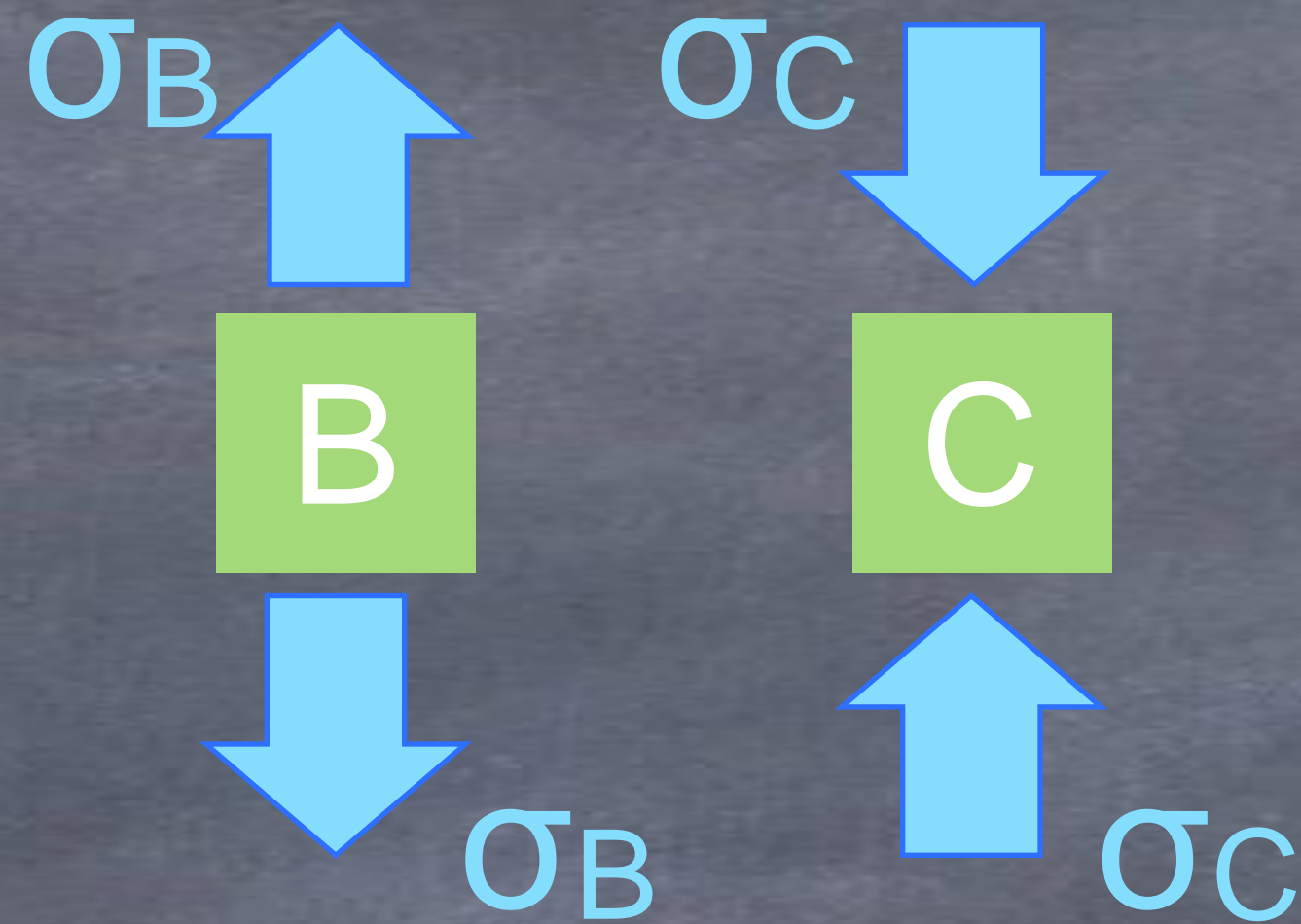


Outros exemplos

c) Superposição das tensões

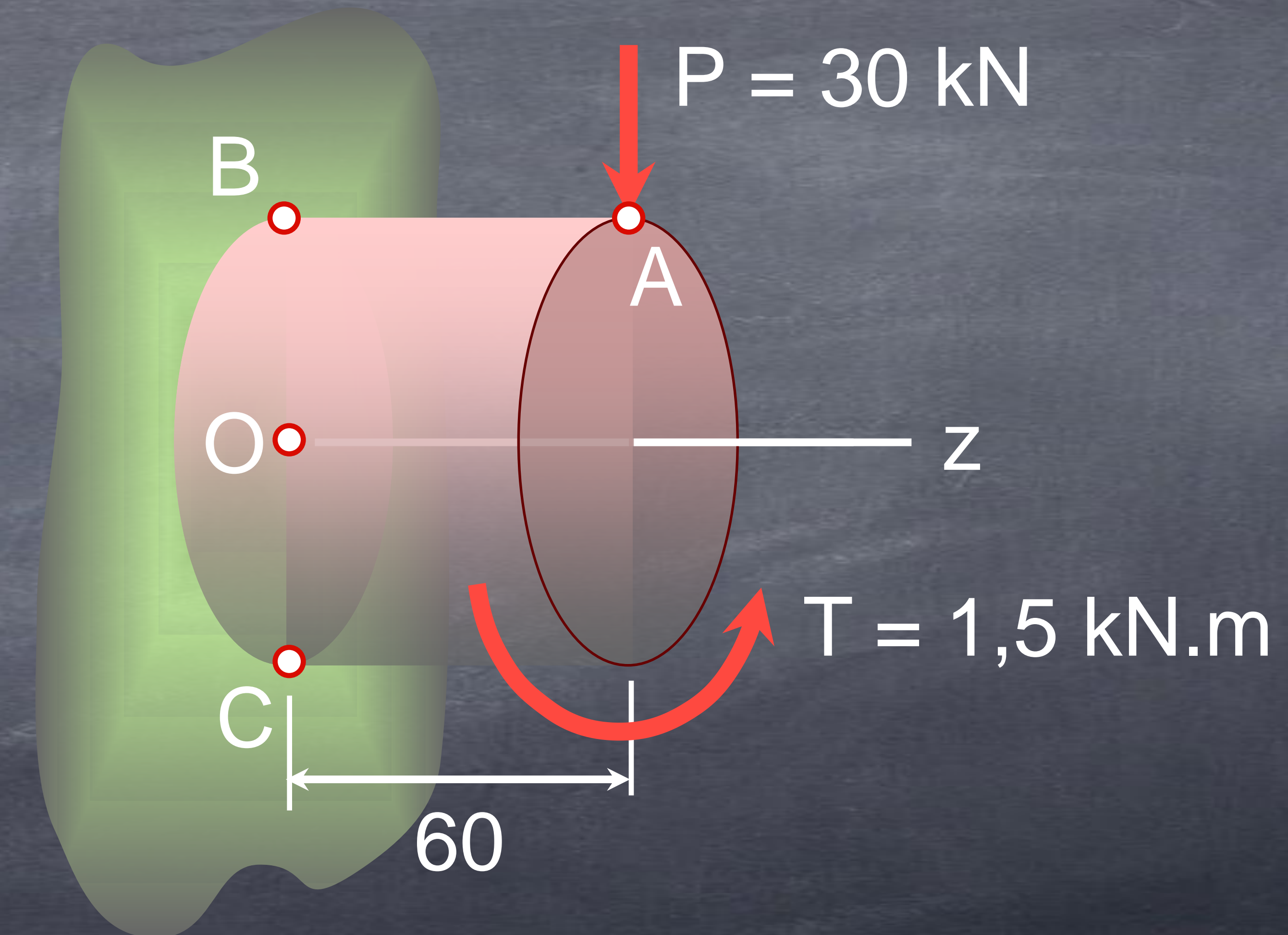
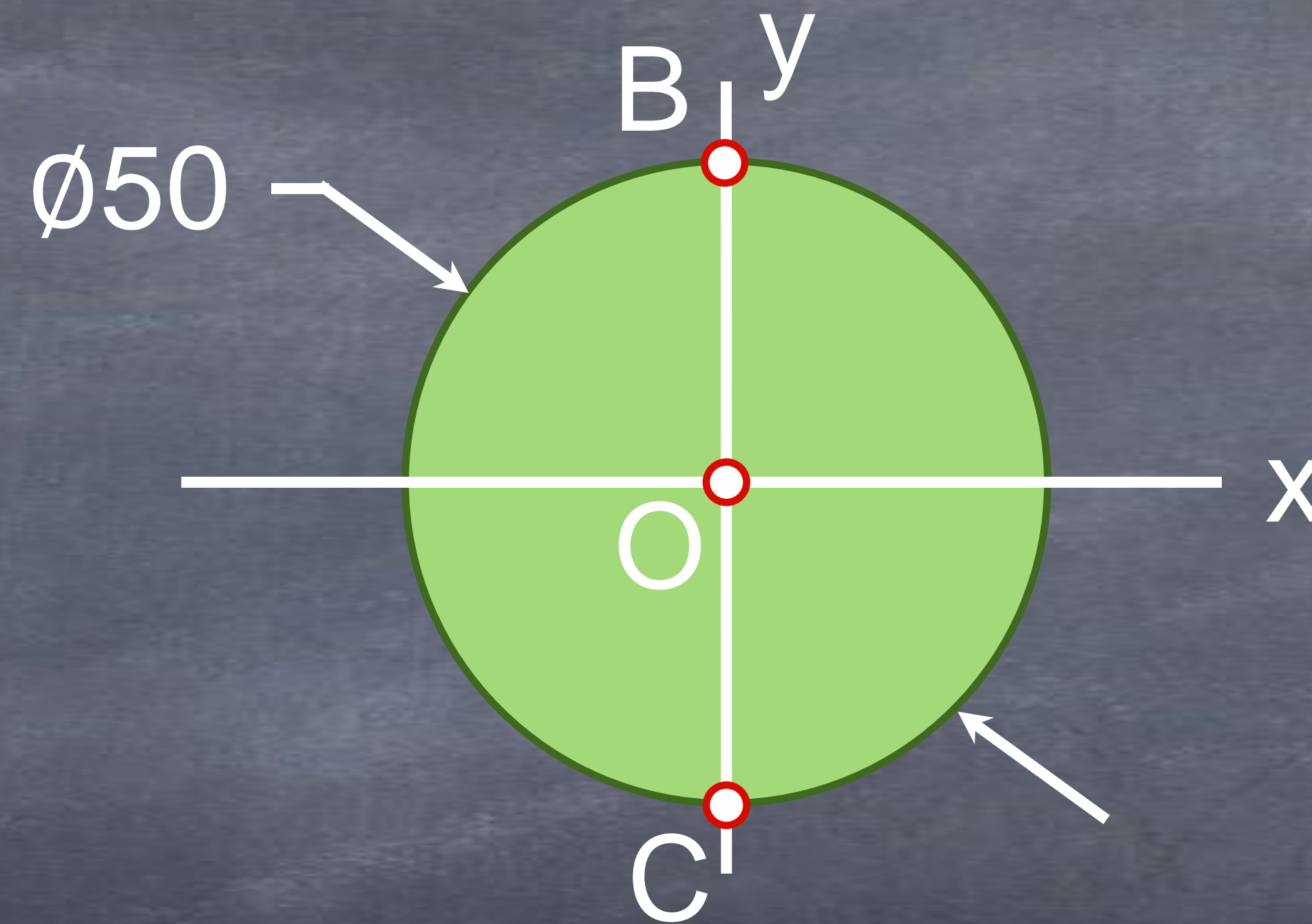
$$\sigma_B = \sigma + \sigma_{\max} = 53.600 \text{ N/m}^2$$

$$\sigma_C = \sigma - \sigma_{\max} = -107.200 \text{ N/m}^2$$



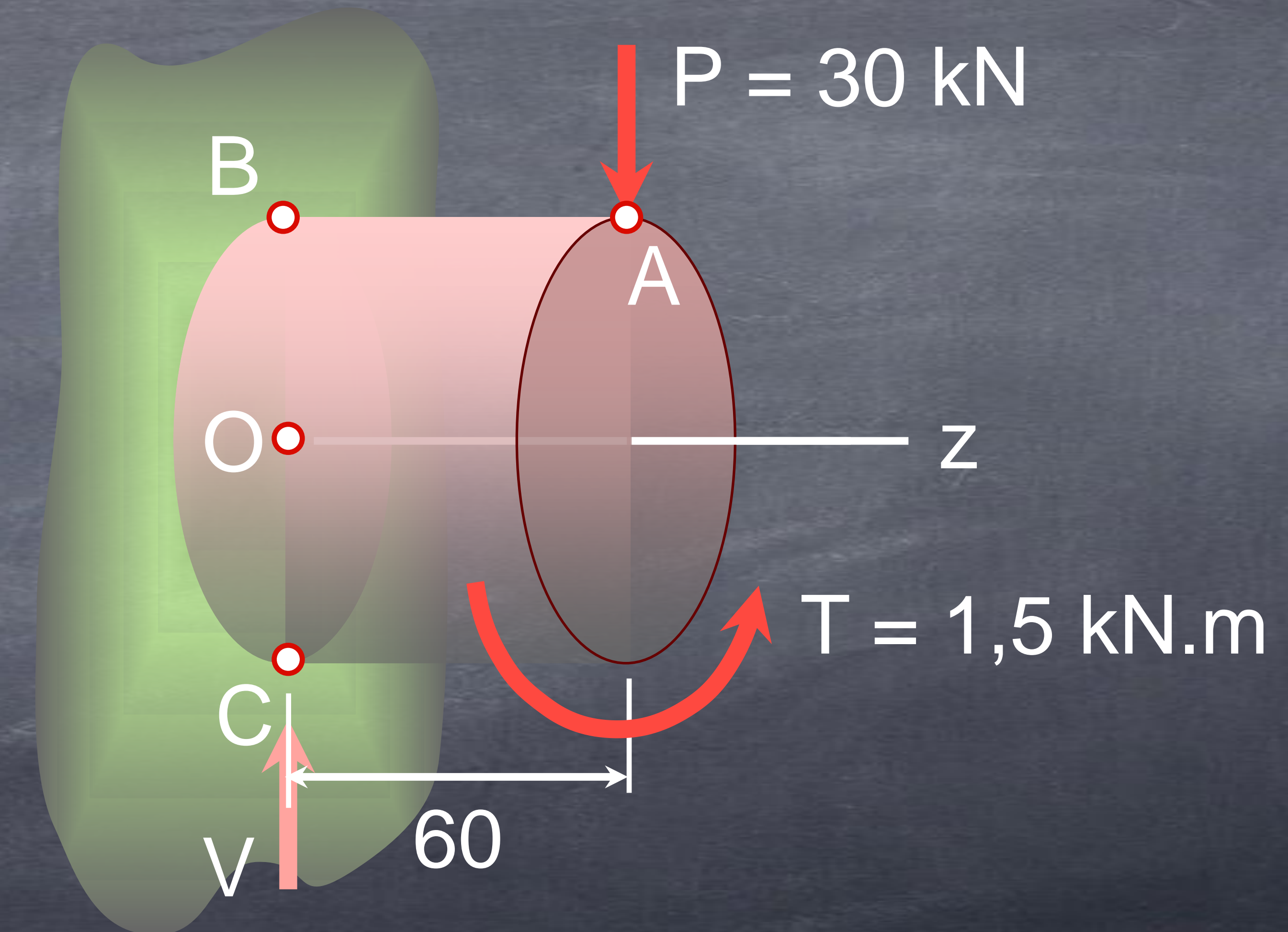
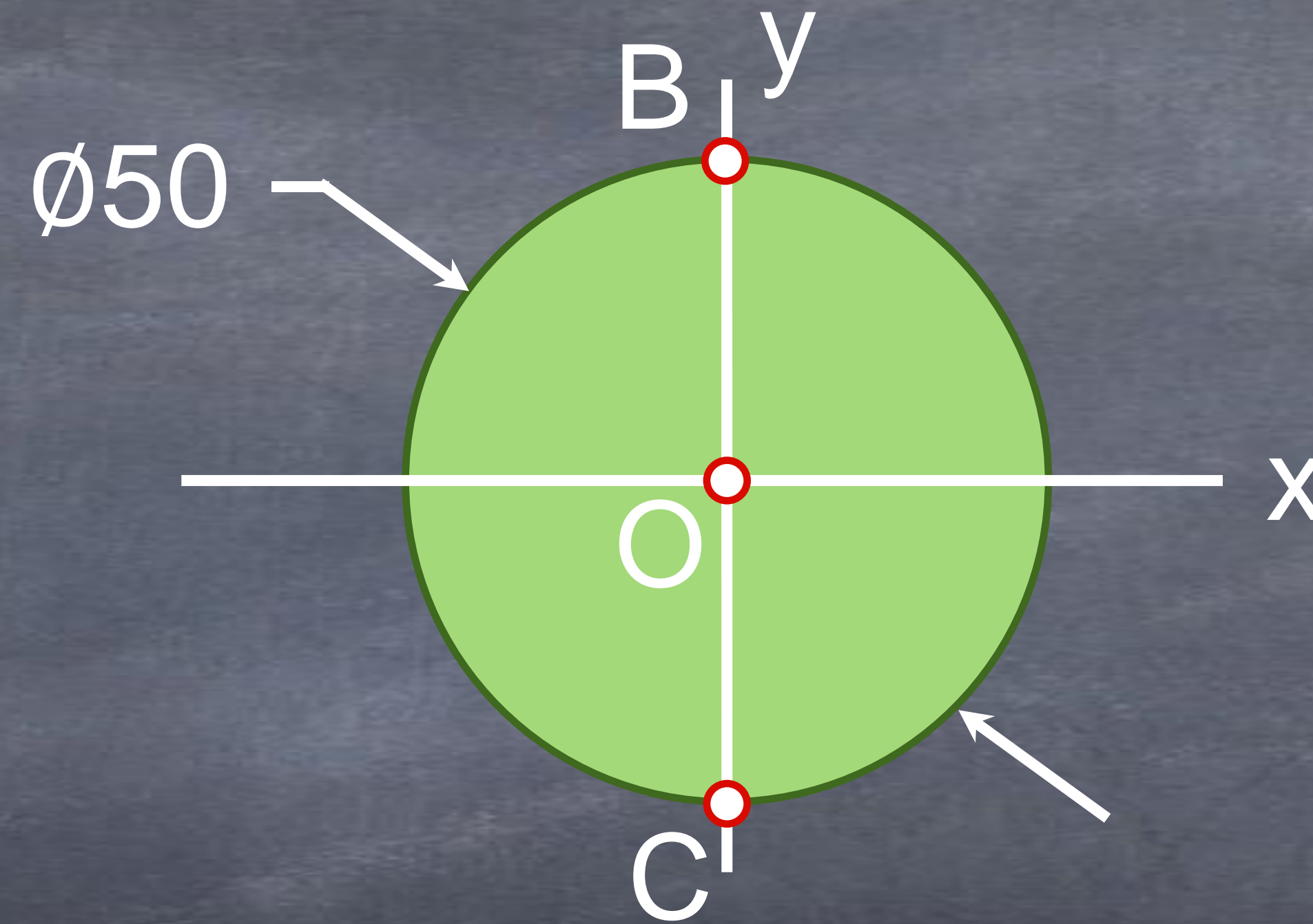
Outros exemplos

Determinar o estado de tensões nos pontos B, C e O da barra da figura.



Outros exemplos

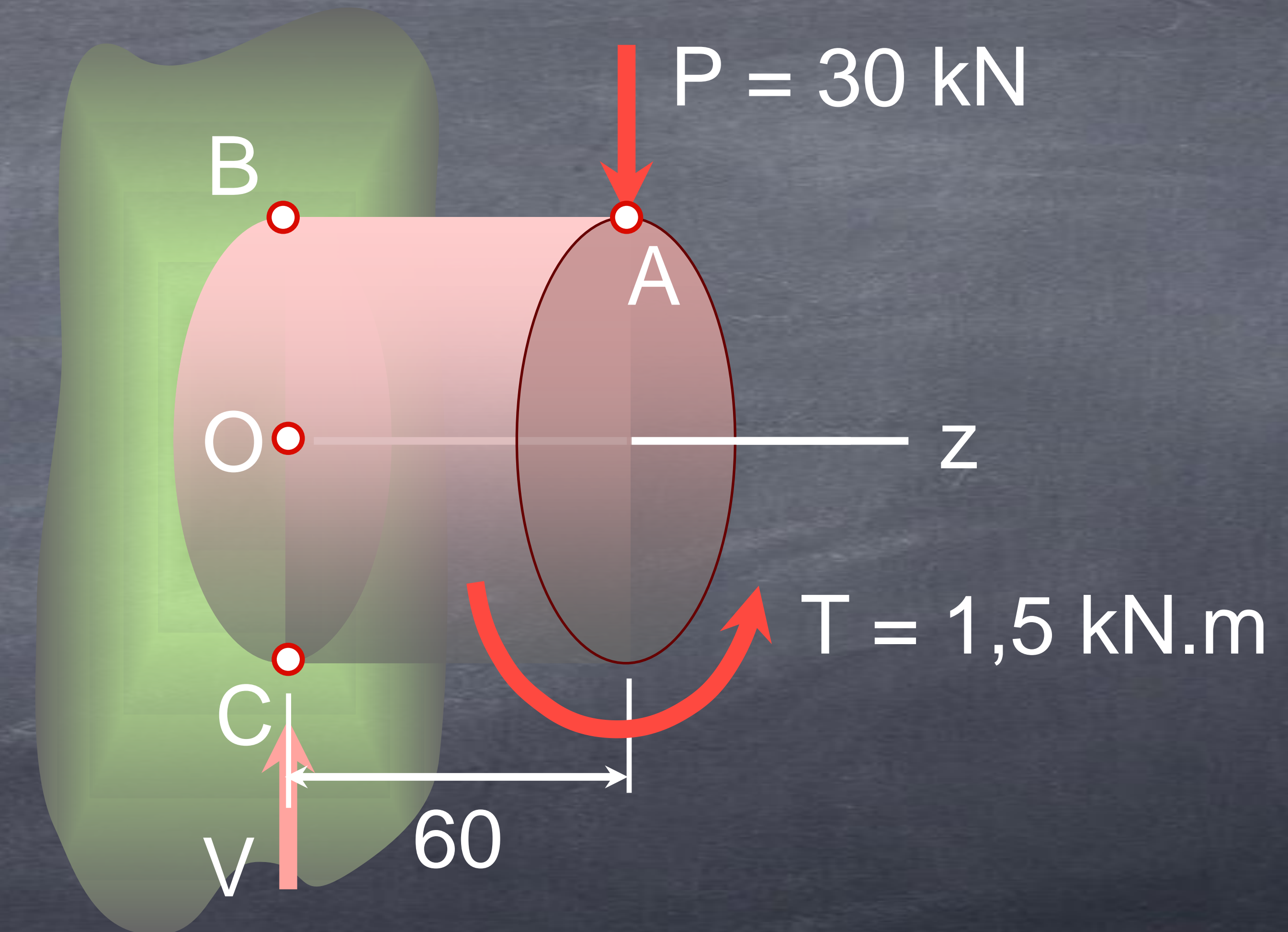
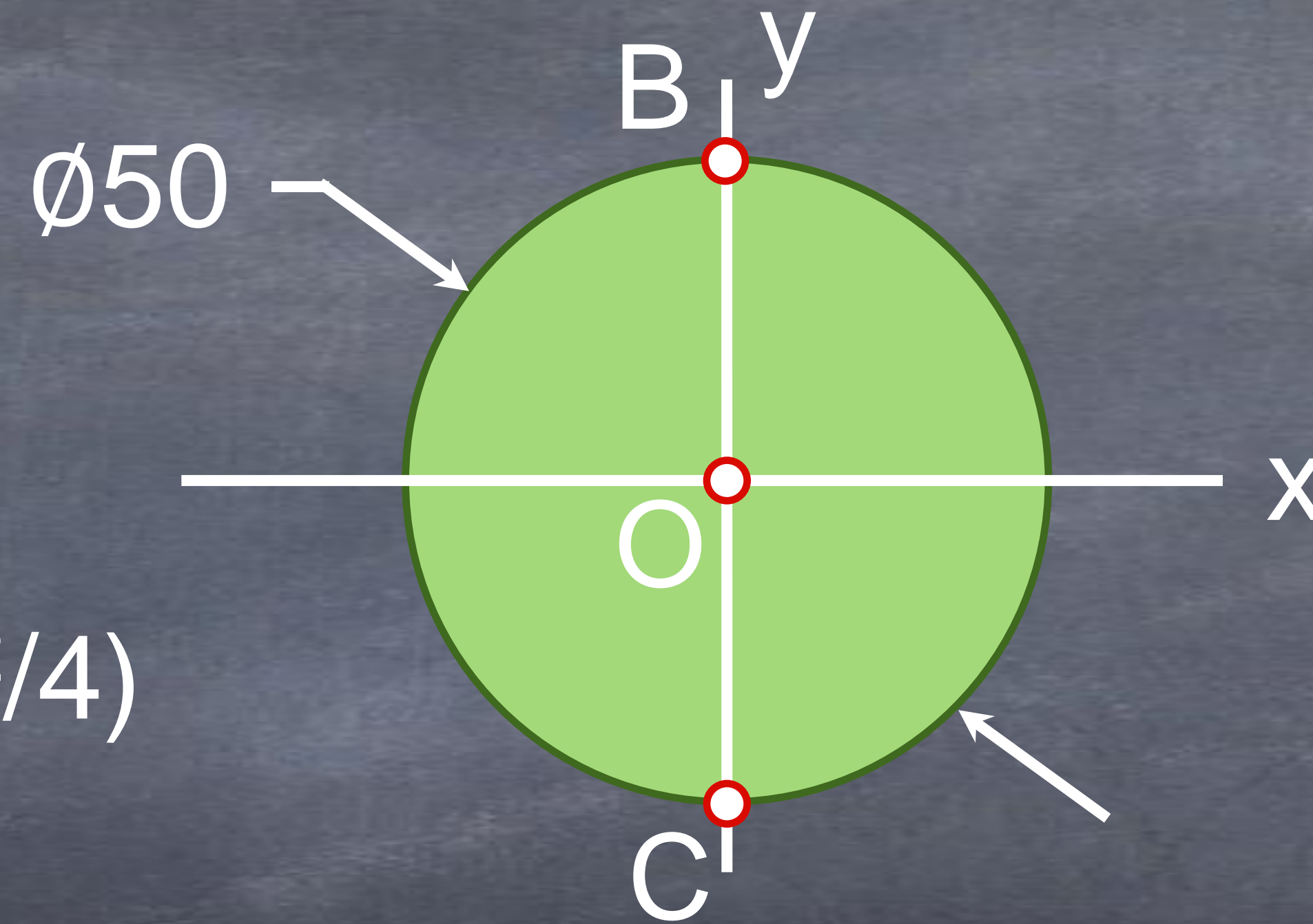
a) Tensão cisalhante causada pela força transversal



Outros exemplos

a) Tensão cisalhante causada pela força transversal

$$\tau = V / A = 30 \times 10^3 / (\pi \times 0,05^2 / 4)$$

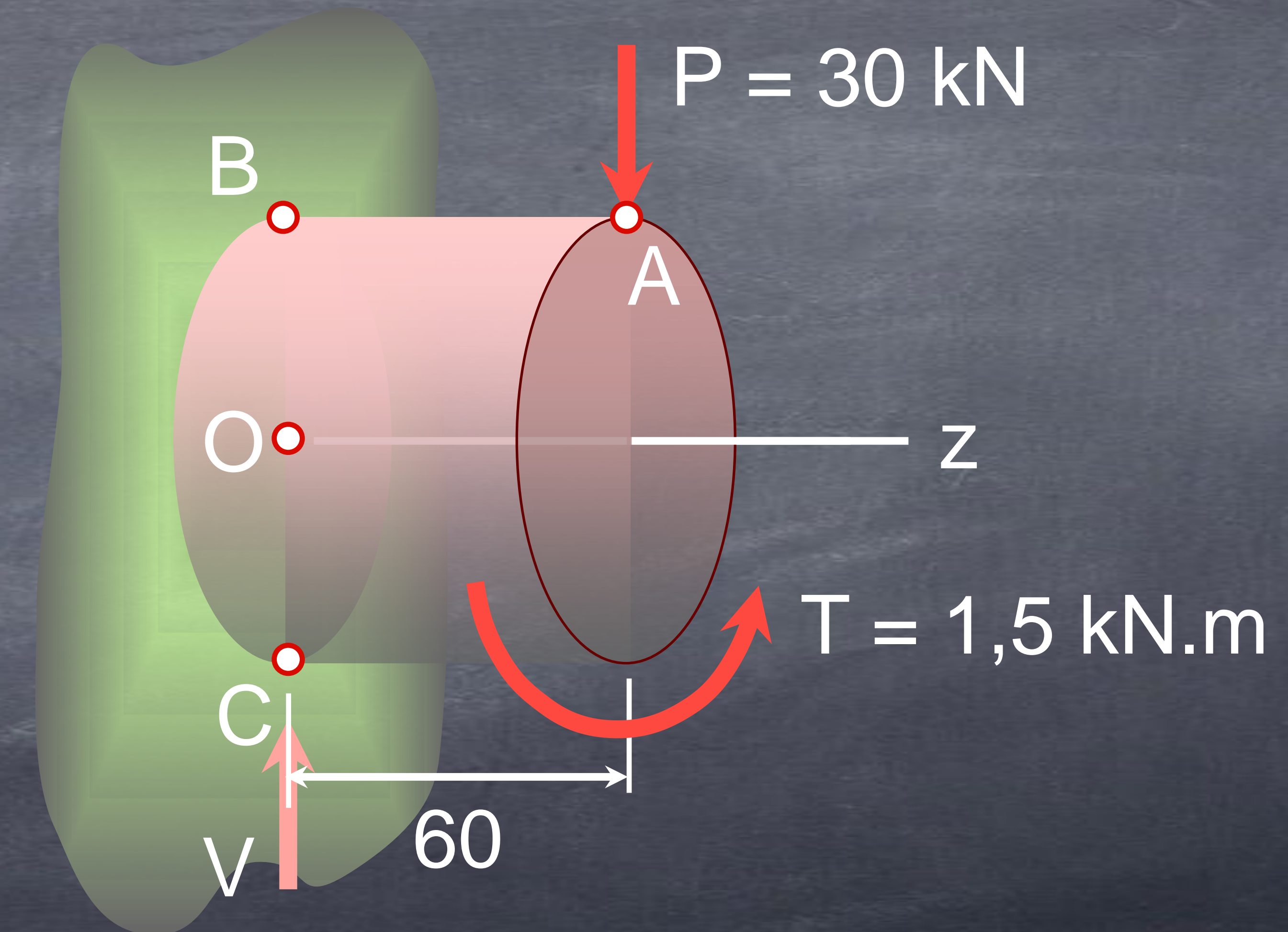
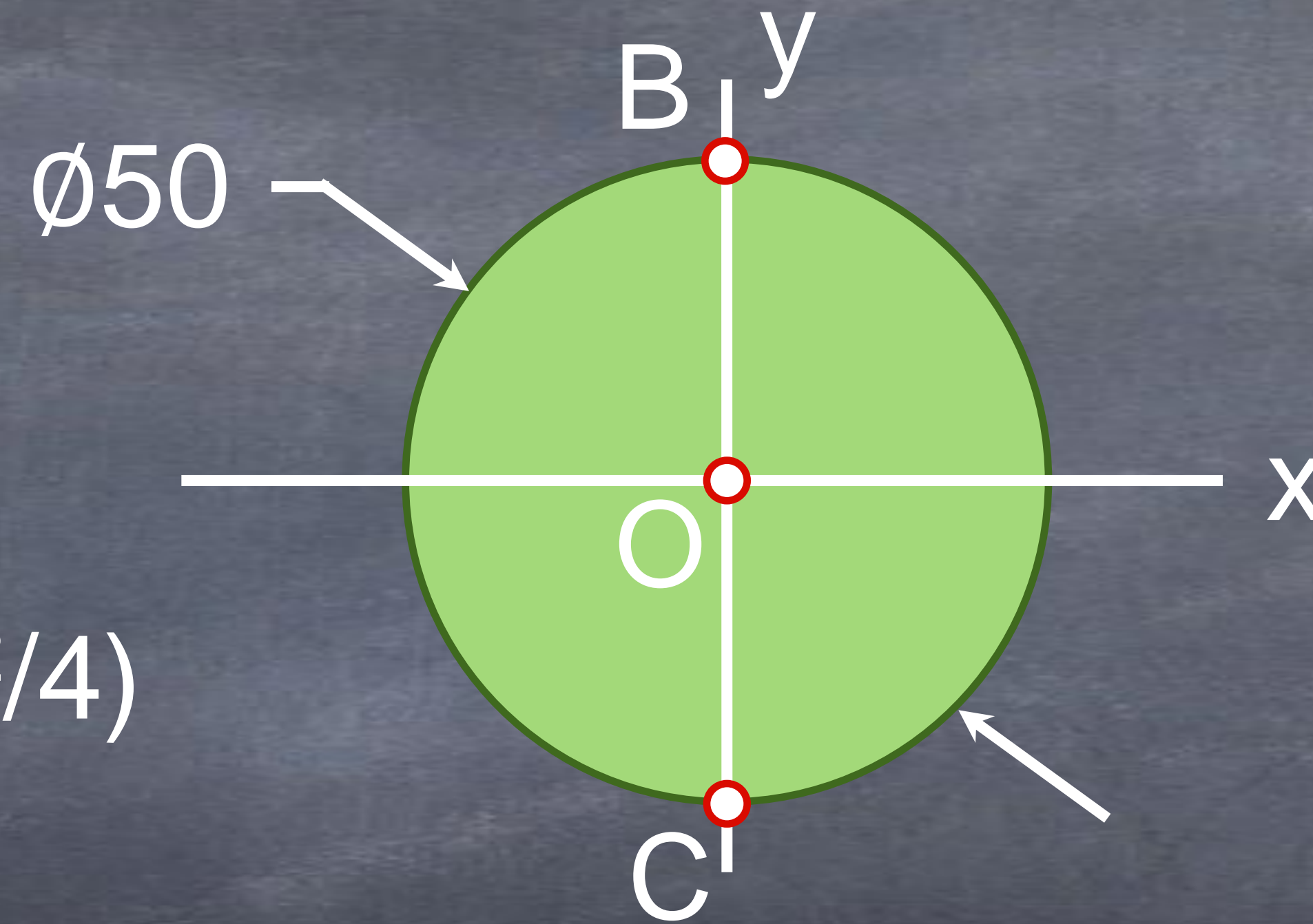


Outros exemplos

a) Tensão cisalhante causada pela força transversal

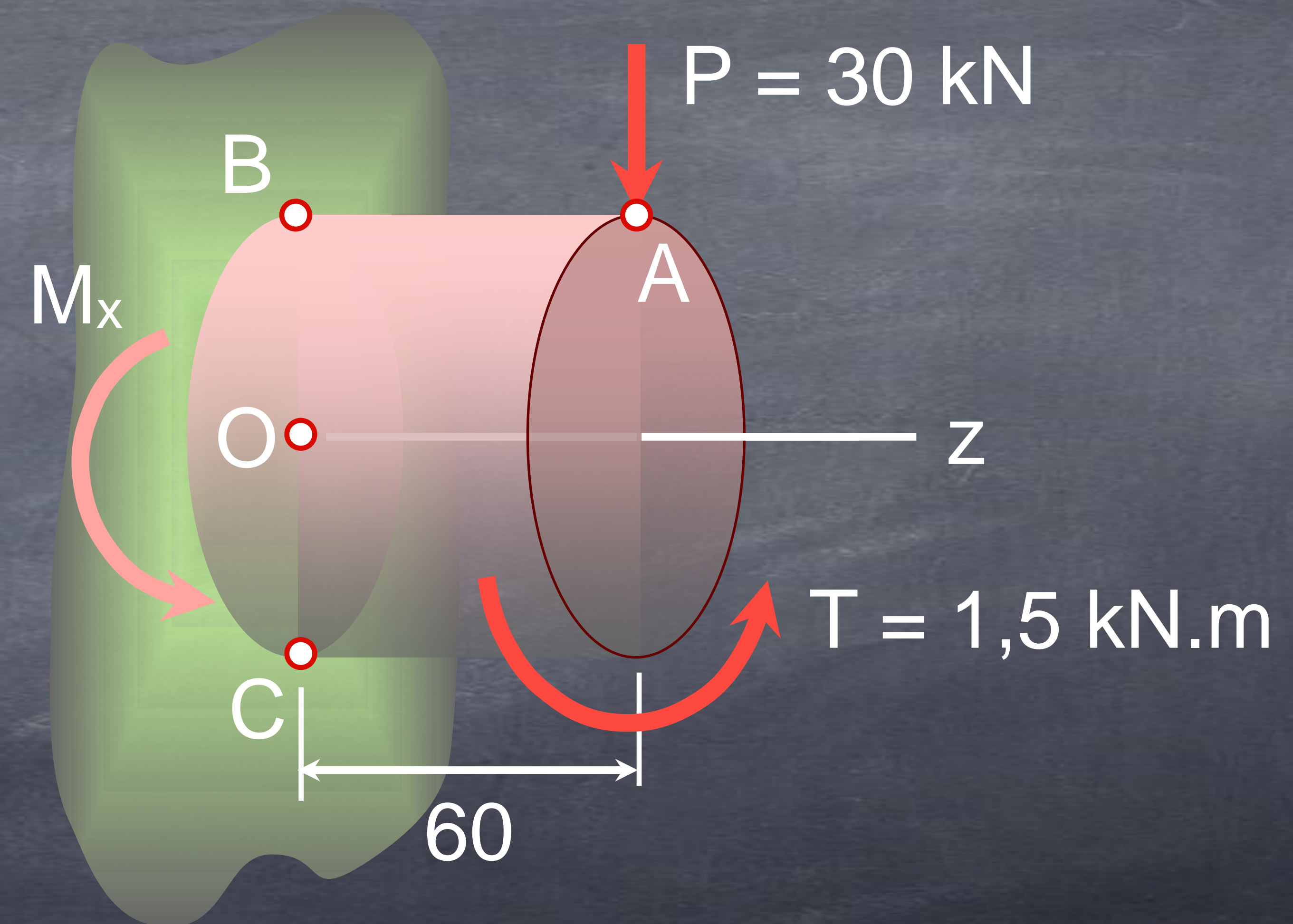
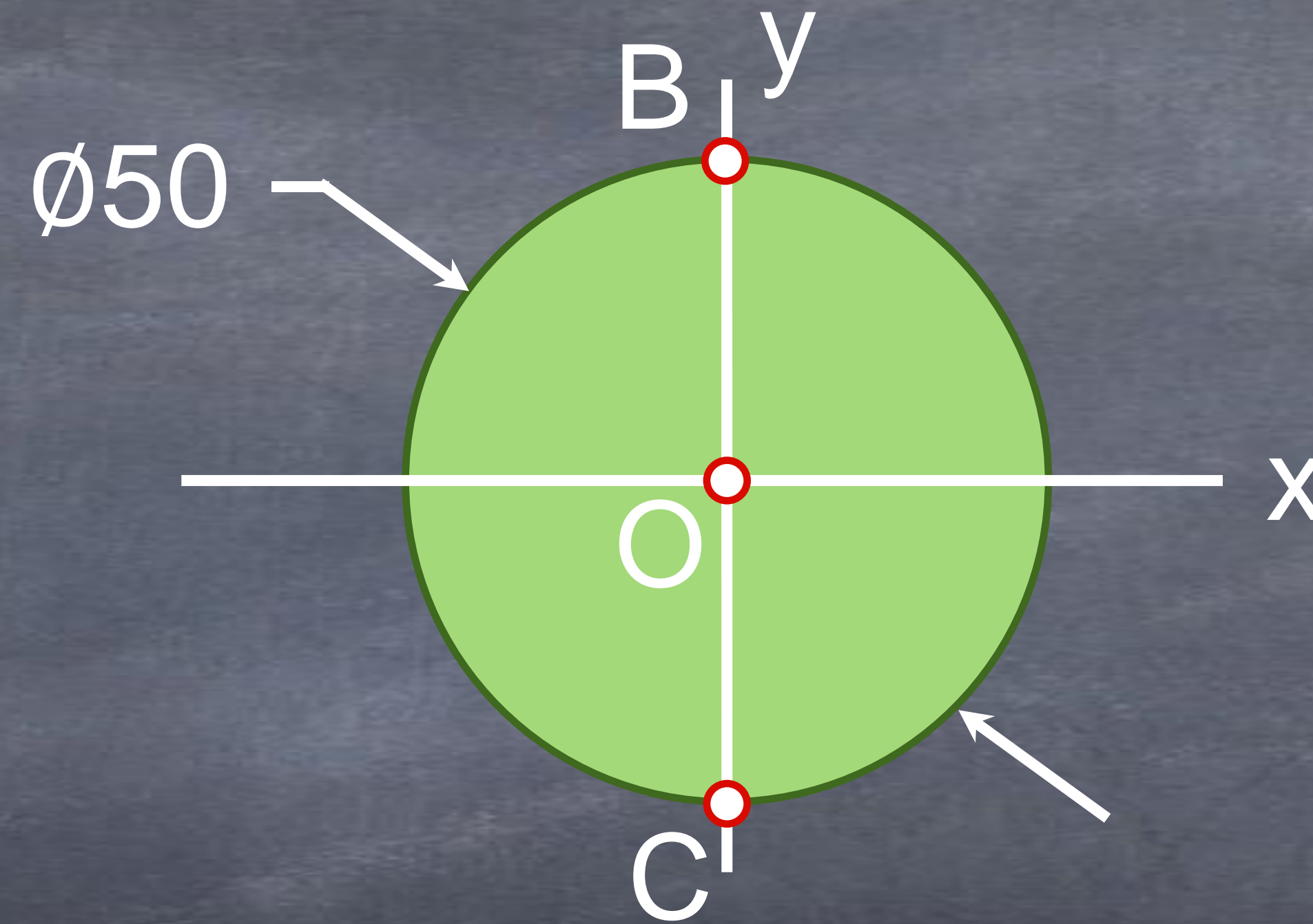
$$\tau = V / A = 30 \times 10^3 / (\pi \times 0,05^2 / 4)$$

$$\tau = 15,28 \text{ MPa}$$



Outros exemplos

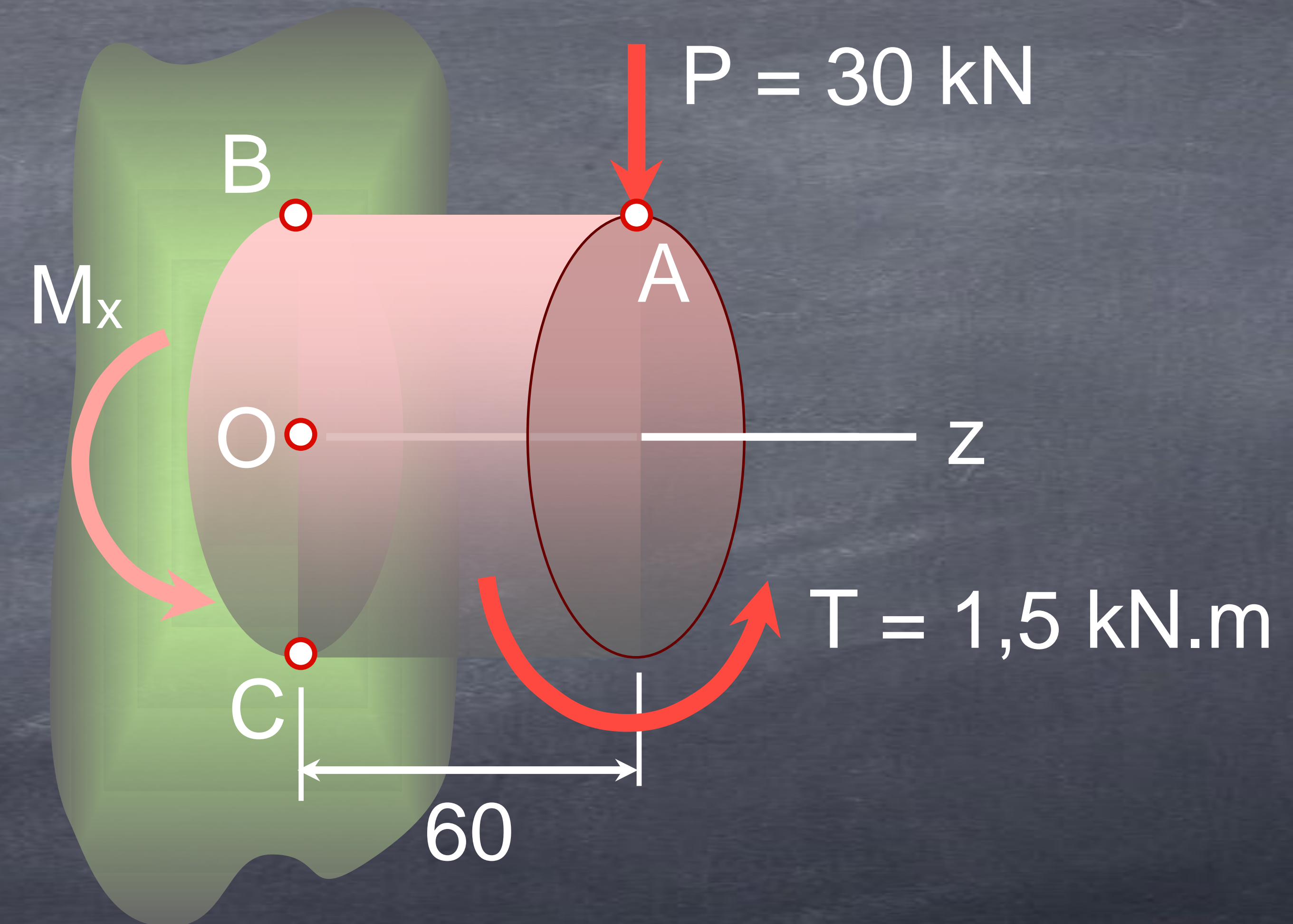
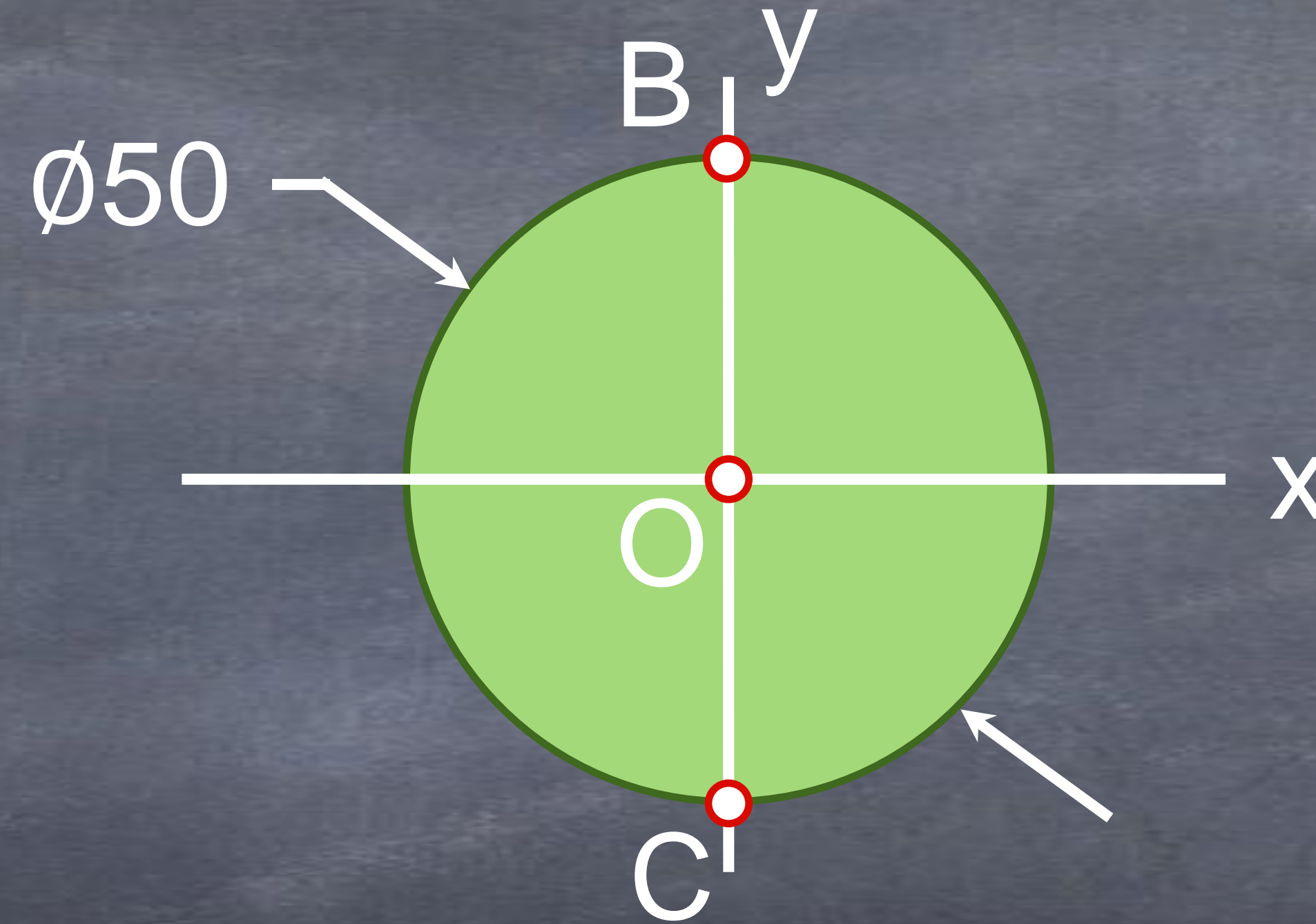
b) Tensão normal causada pelo momento fletor



Outros exemplos

b) Tensão normal causada pelo momento fletor

$$\sigma_{\max} = \pm M_x r / I_{xx}$$

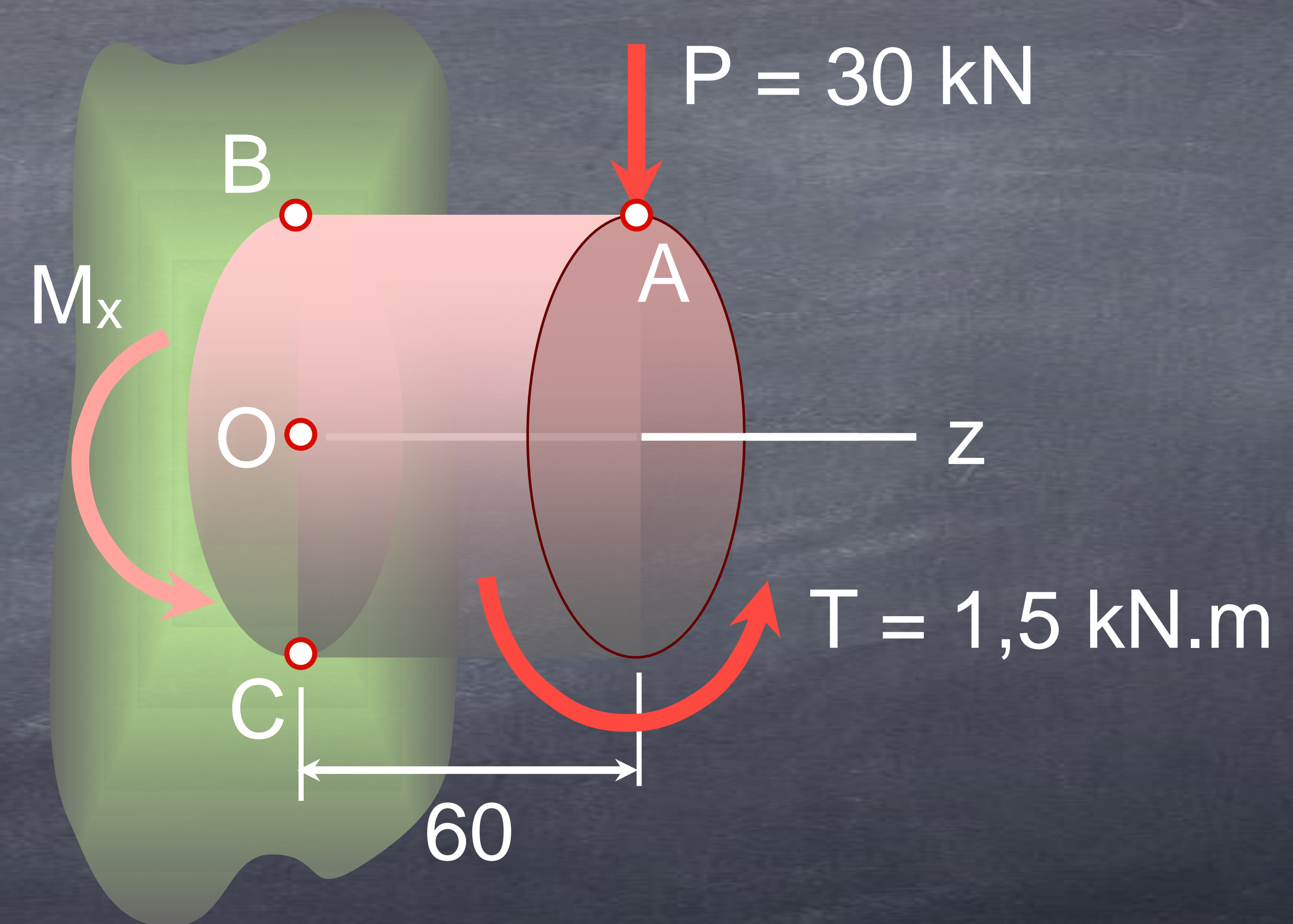
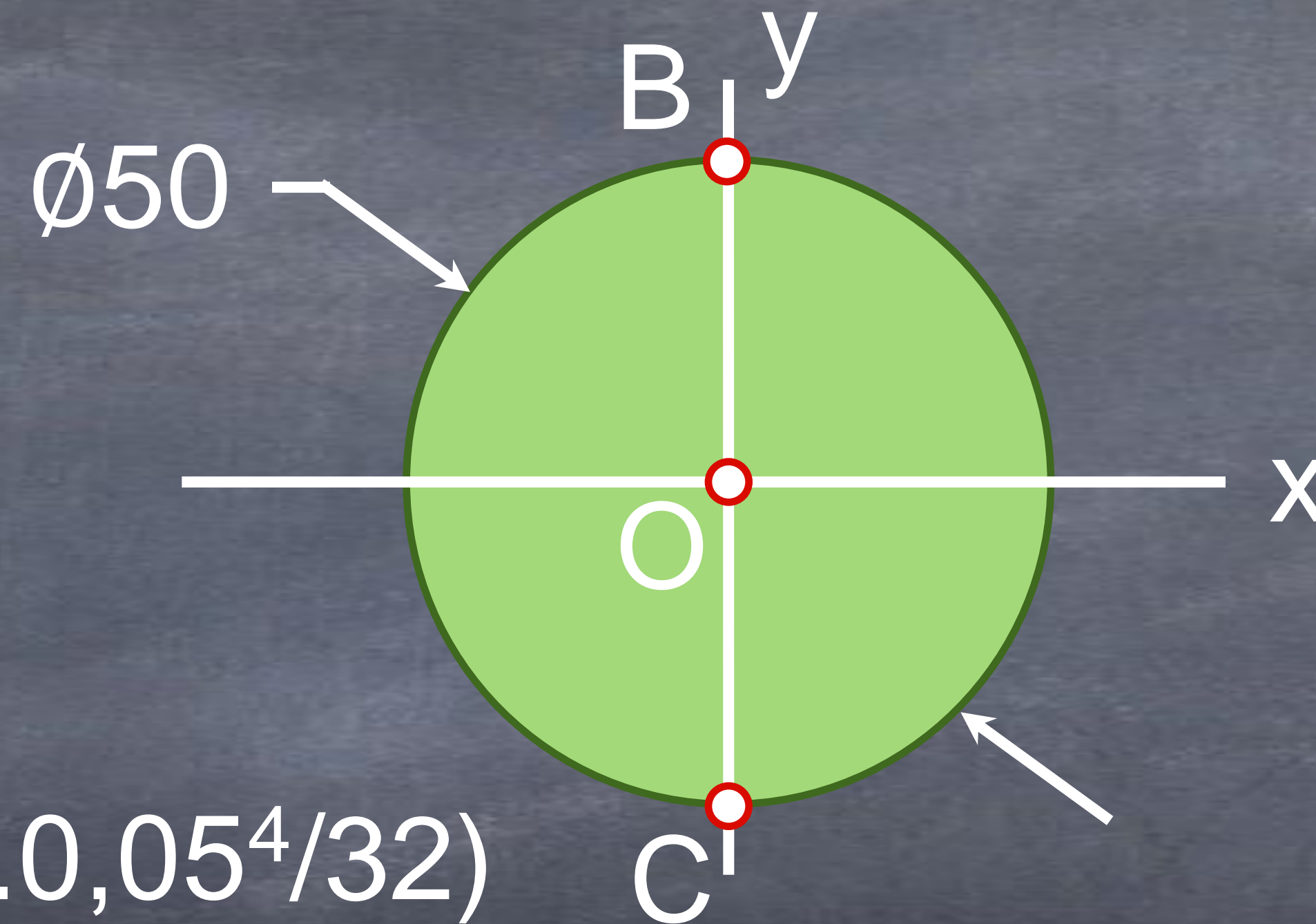


Outros exemplos

b) Tensão normal causada pelo momento fletor

$$\sigma_{\max} = \pm M_x r / I_{xx}$$

$$\sigma_{\max} = \pm 30 \cdot 10^3 \cdot (0,06) \cdot (0,025) / (\pi \cdot 0,05^4 / 32)$$



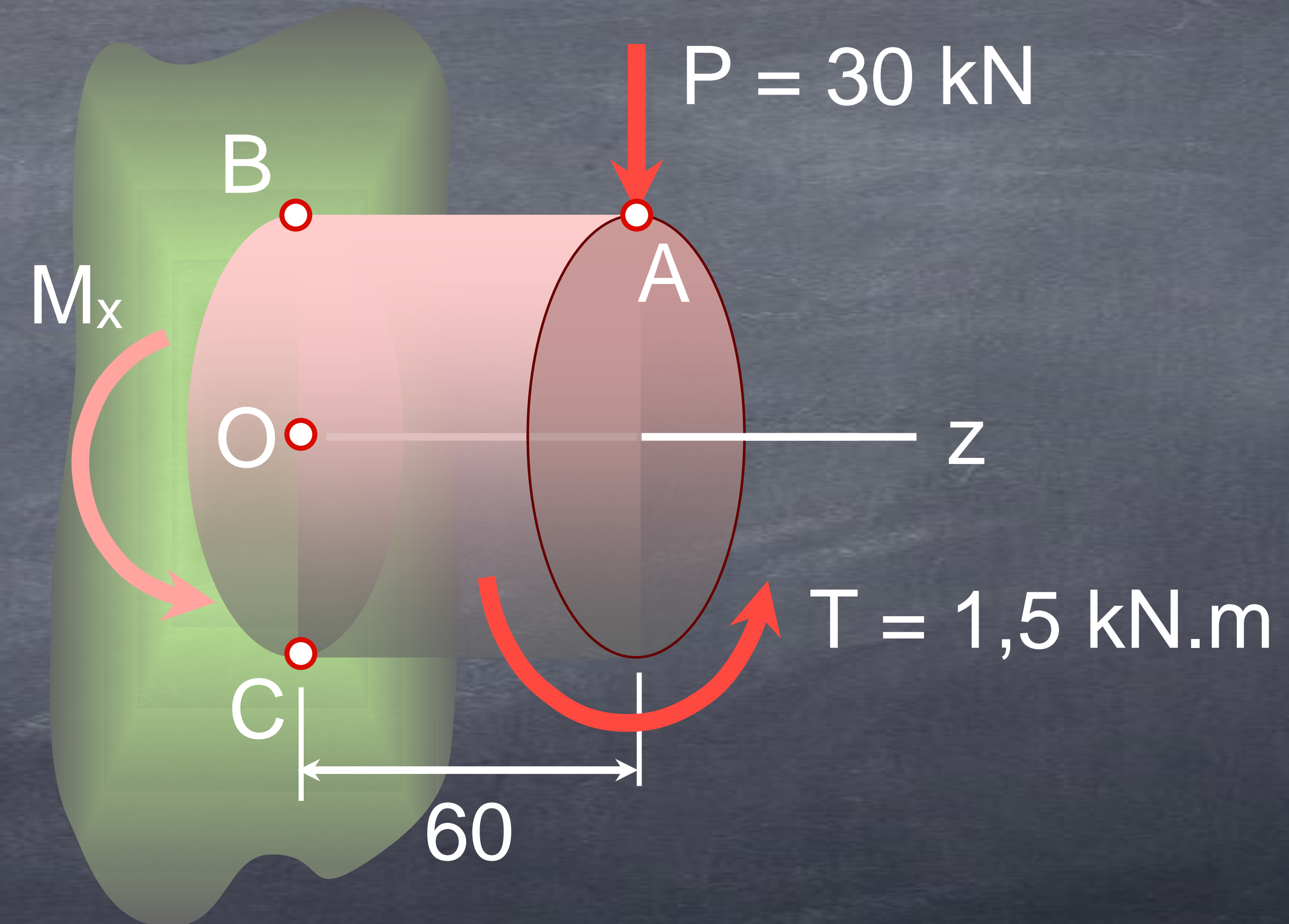
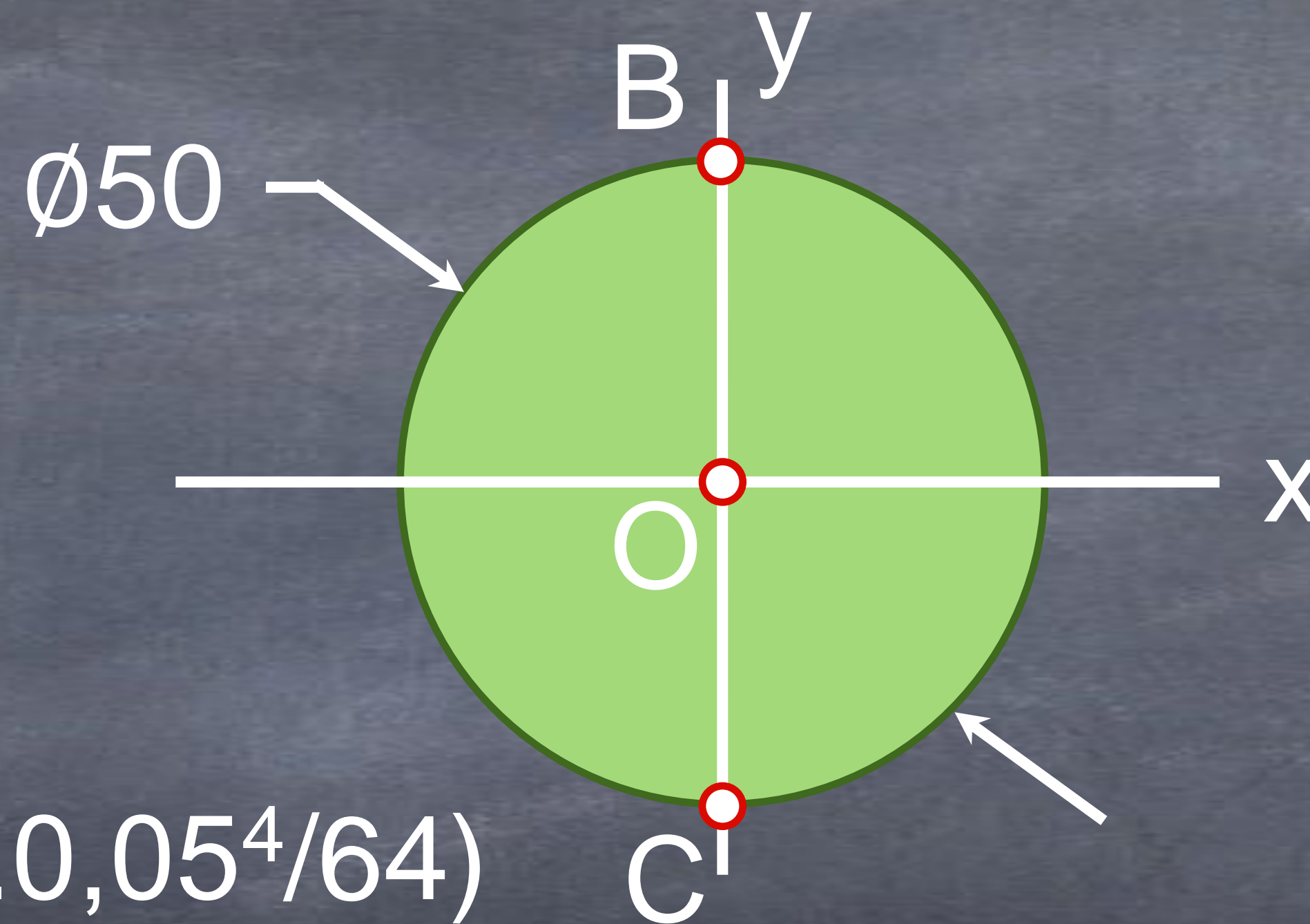
Outros exemplos

b) Tensão normal causada pelo momento fletor

$$\sigma_{\max} = \pm M_x r / I_{xx}$$

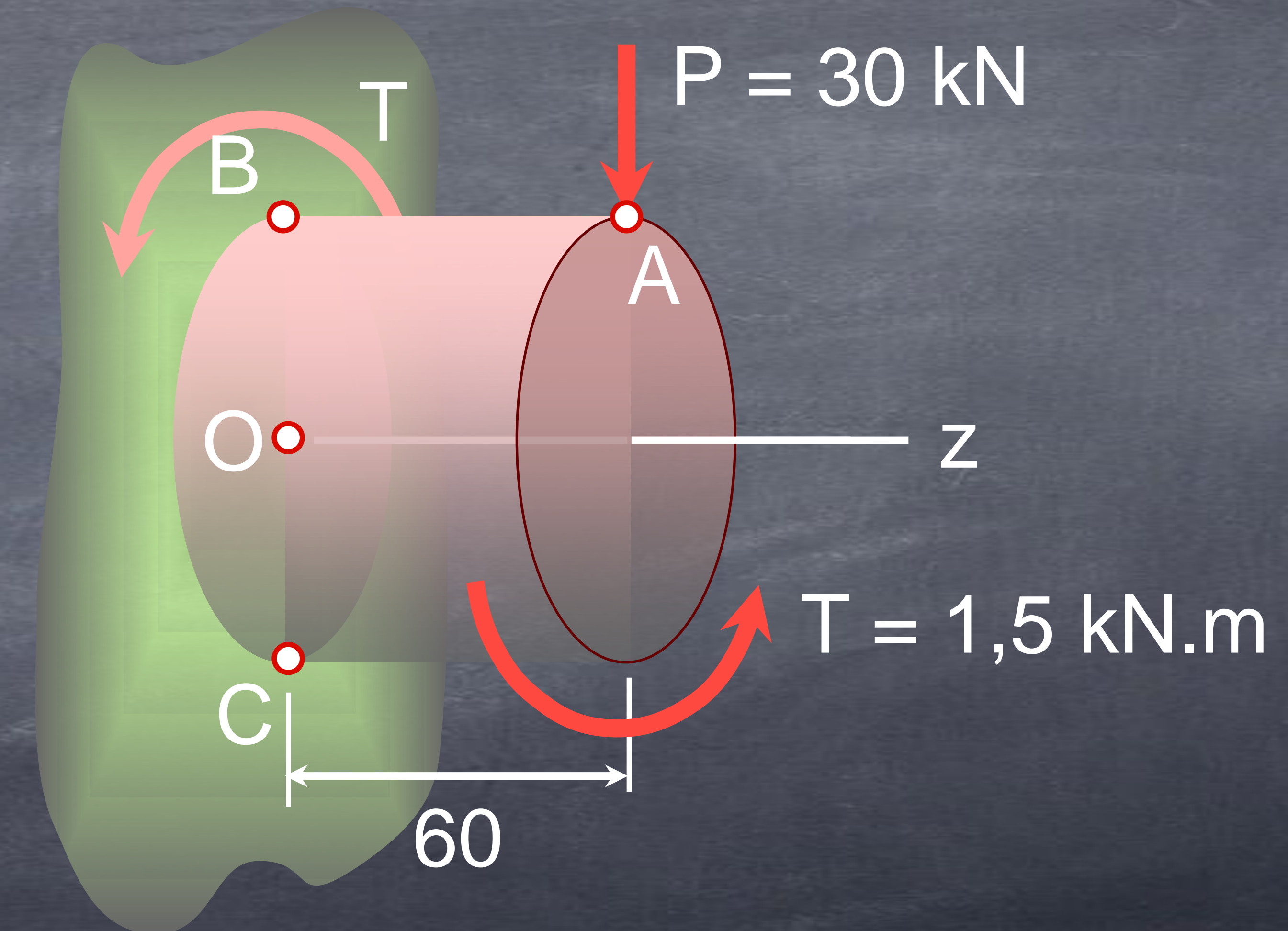
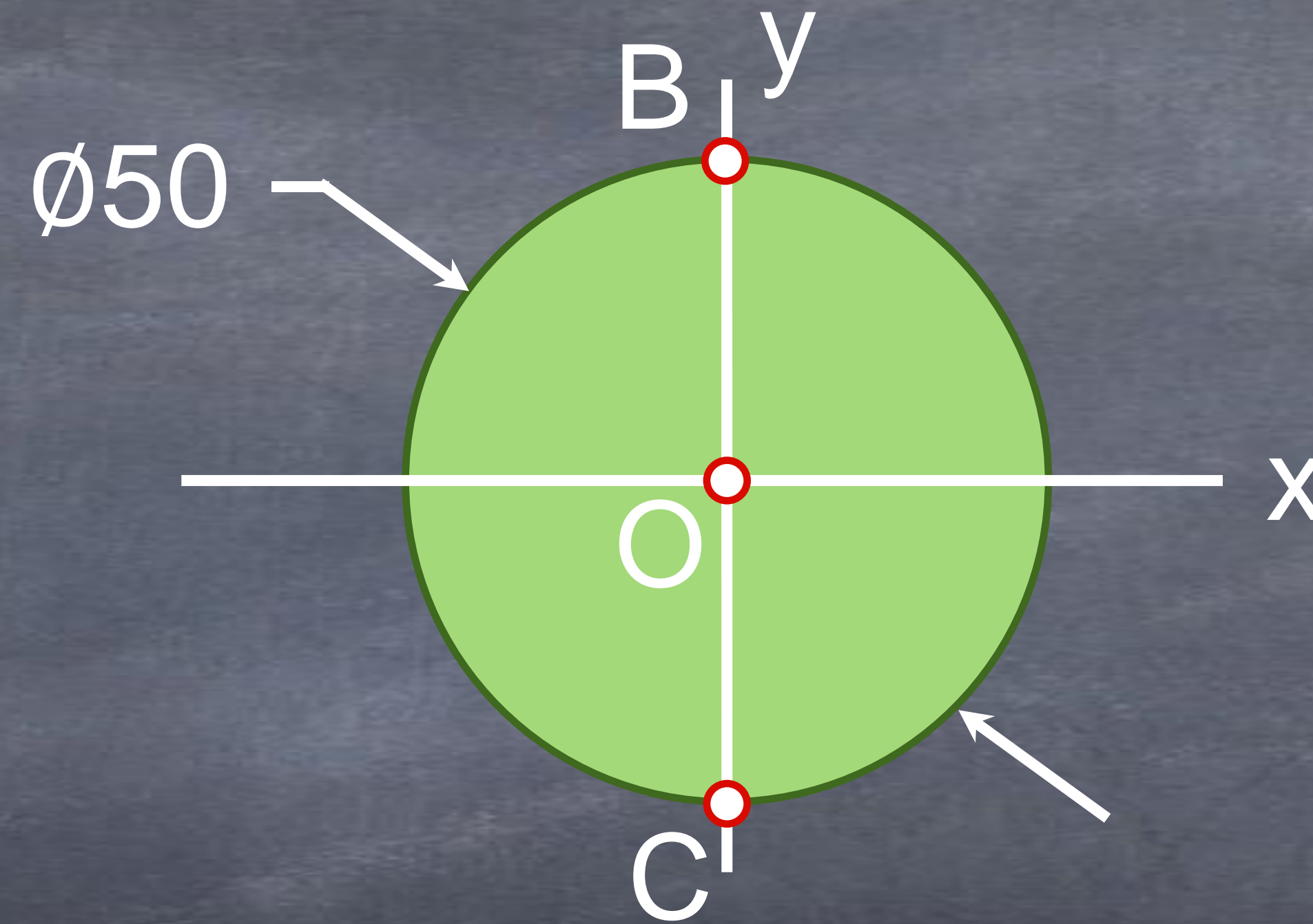
$$\sigma_{\max} = \pm 30 \cdot 10^3 \cdot (0,06) \cdot (0,025) / (\pi \cdot 0,05^4 / 64)$$

$$\sigma_{\max} = \pm 146,7 \text{ MPa}$$



Outros exemplos

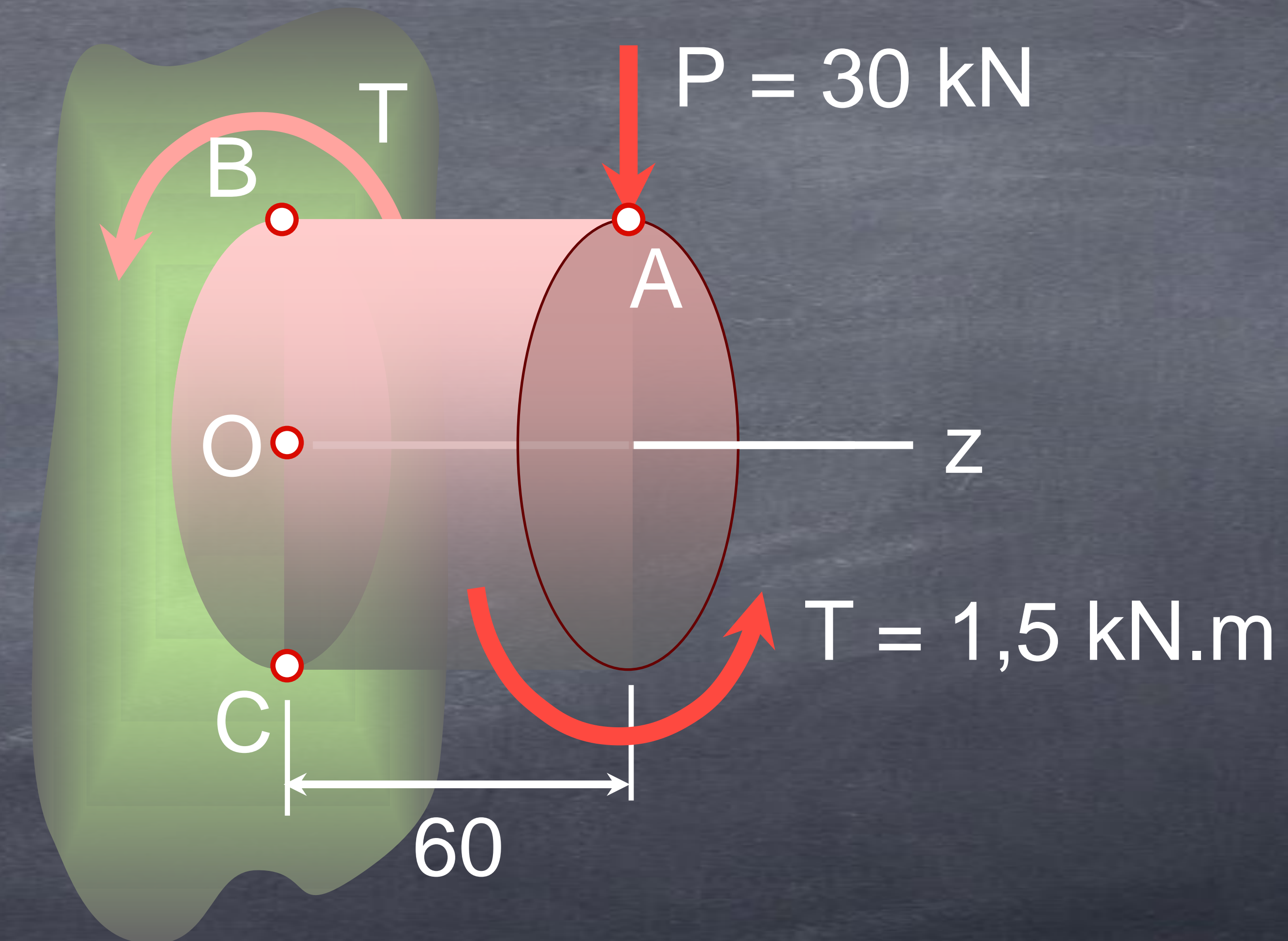
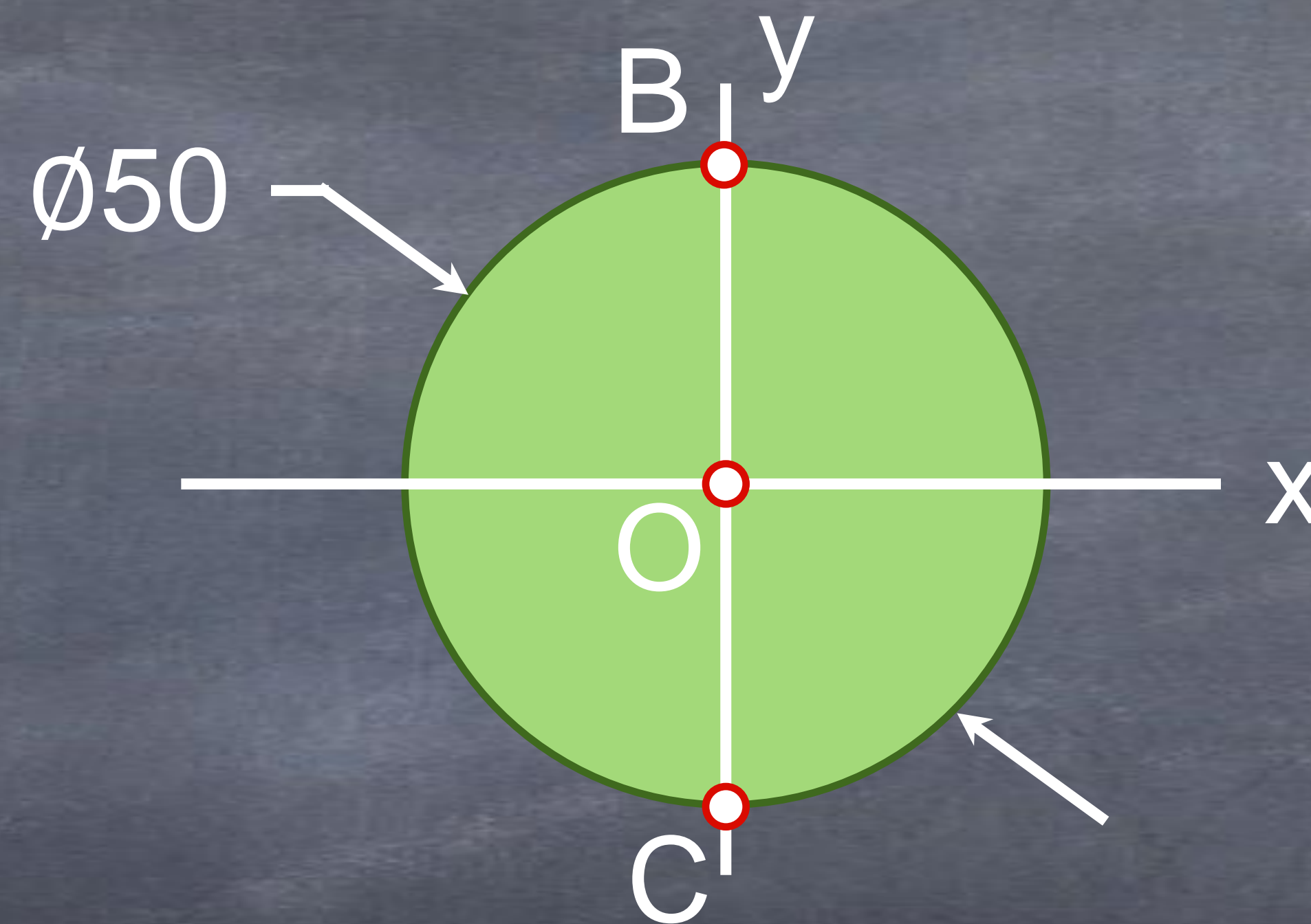
c) Tensão normal causada pelo momento torsor



Outros exemplos

c) Tensão normal causada
pelo momento torsor

$$\tau_{\max} = T \cdot r / J_{zz}$$

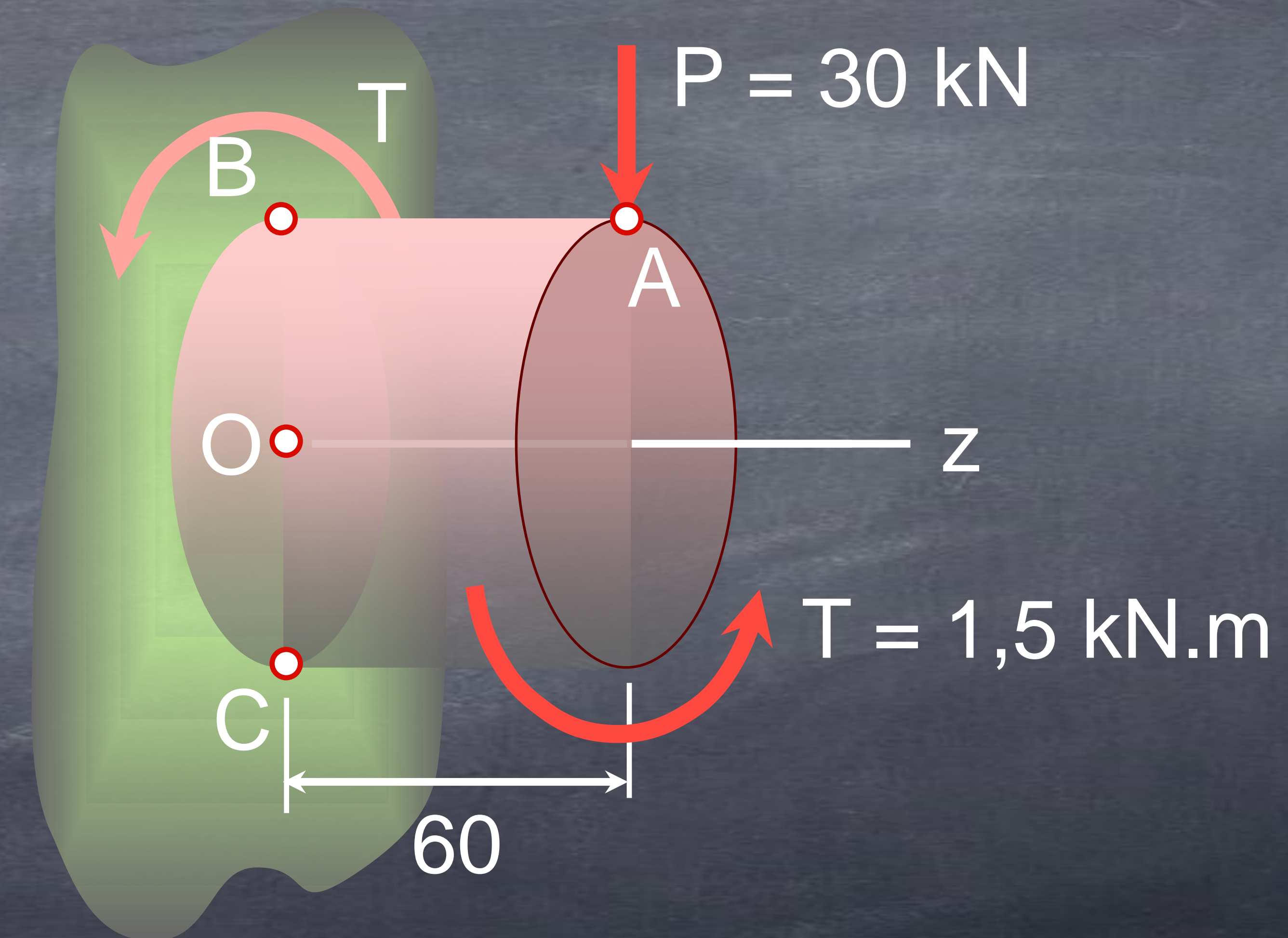
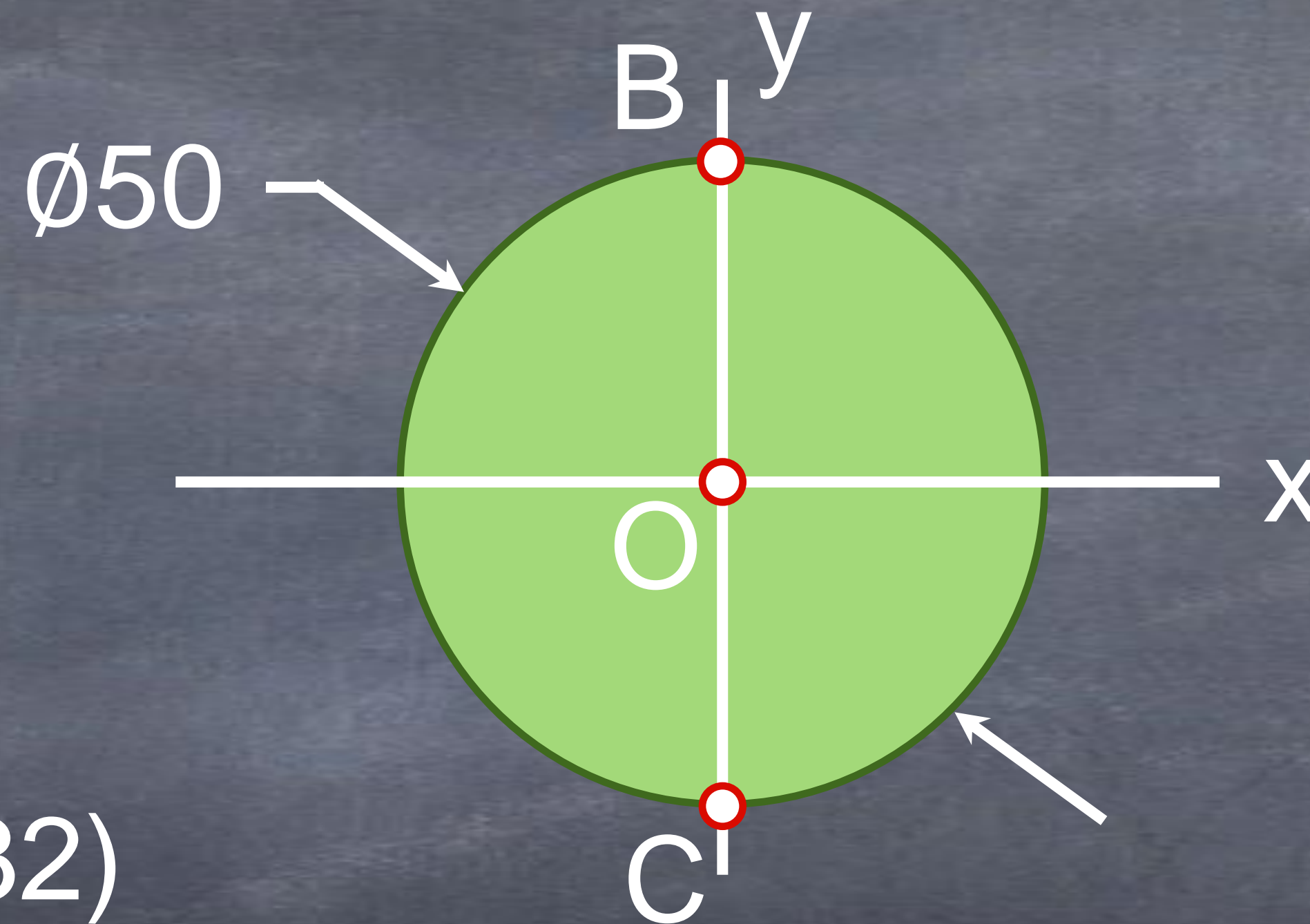


Outros exemplos

c) Tensão normal causada pelo momento torsor

$$\tau_{\max} = T \cdot r / J_{zz}$$

$$\tau_{\max} = 1,5 \cdot 10^3 \cdot (0,025) / (\pi \cdot 0,05^4 / 32)$$



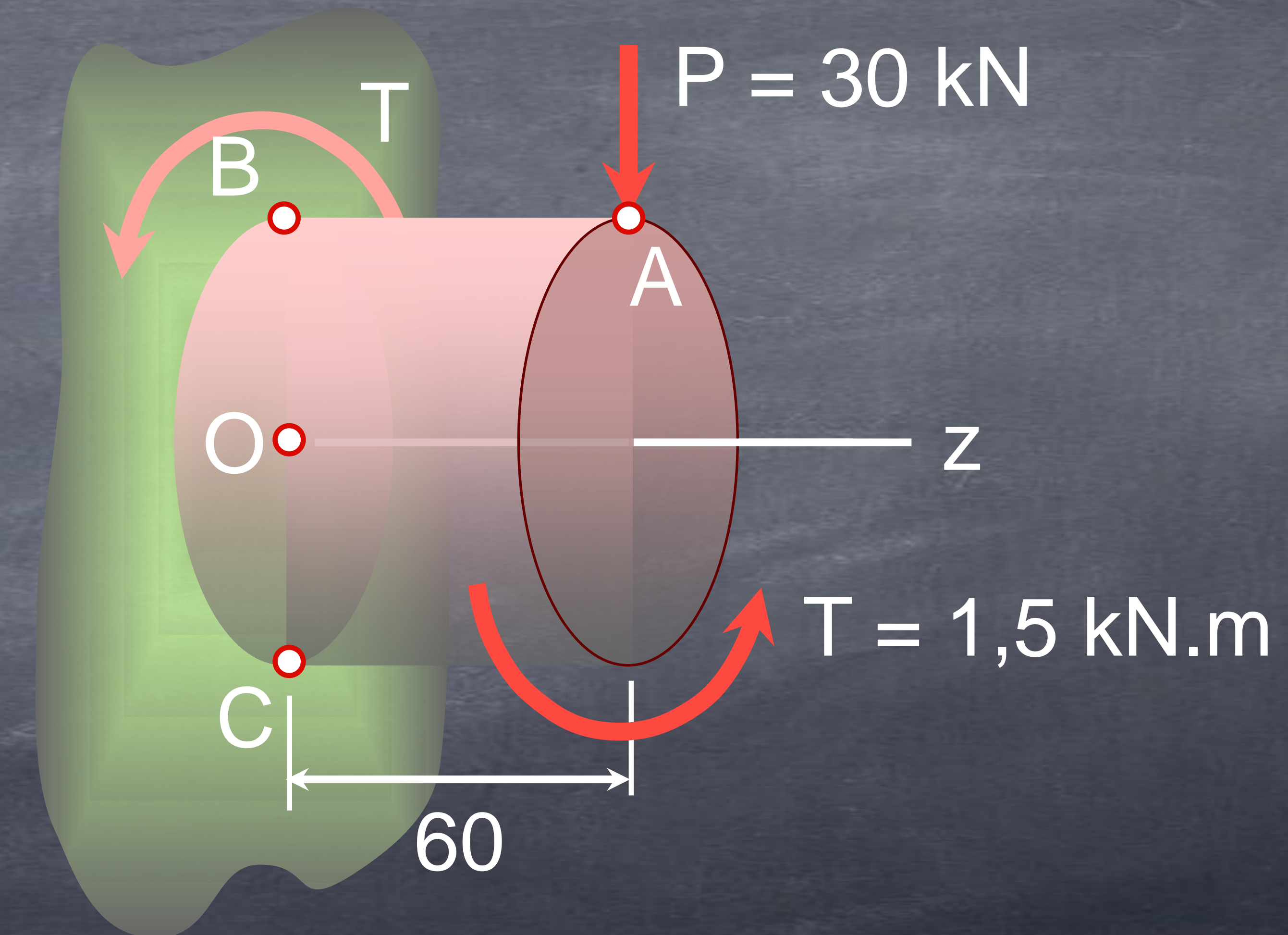
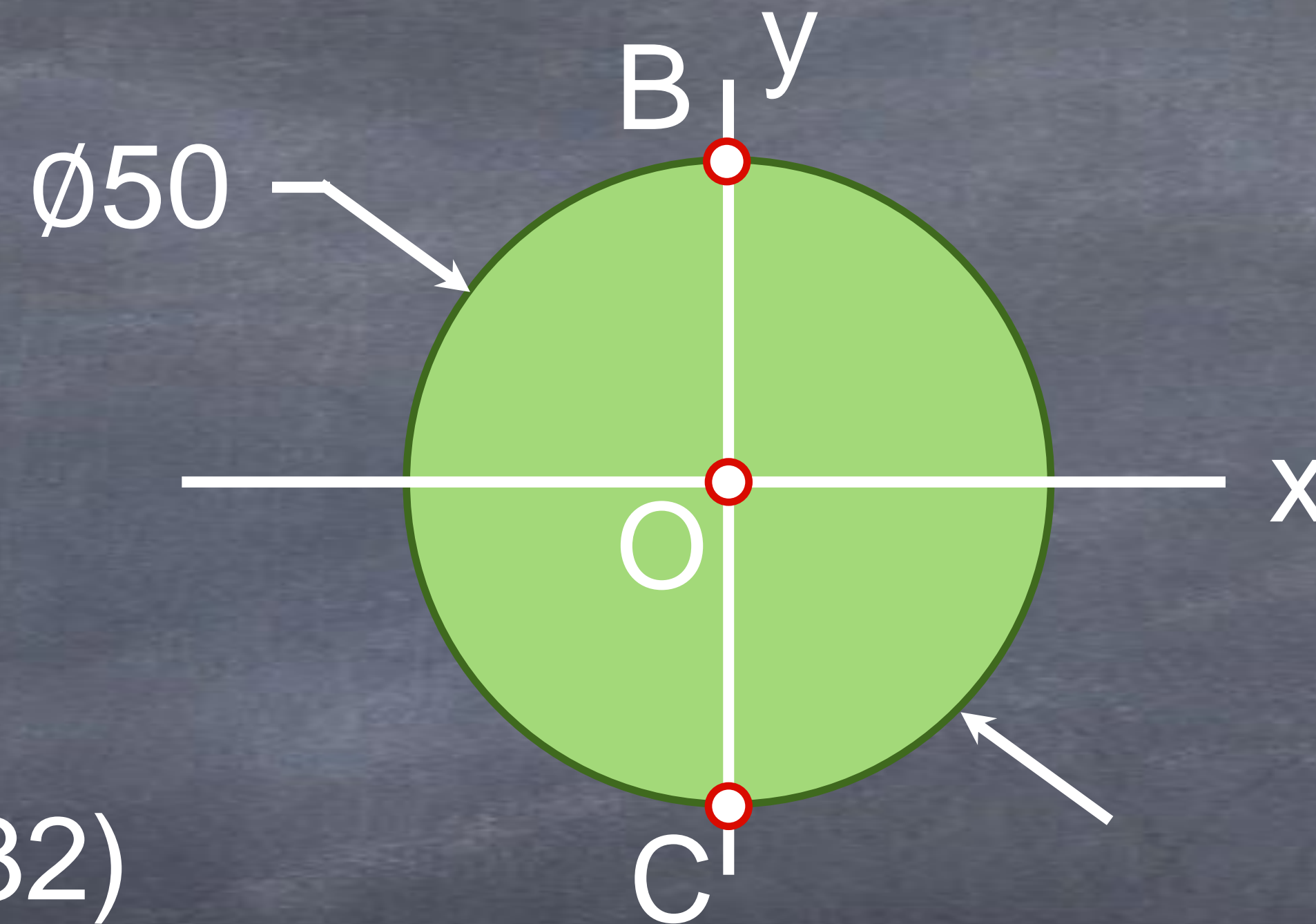
Outros exemplos

c) Tensão normal causada pelo momento torsor

$$\tau_{\max} = T r / J_{zz}$$

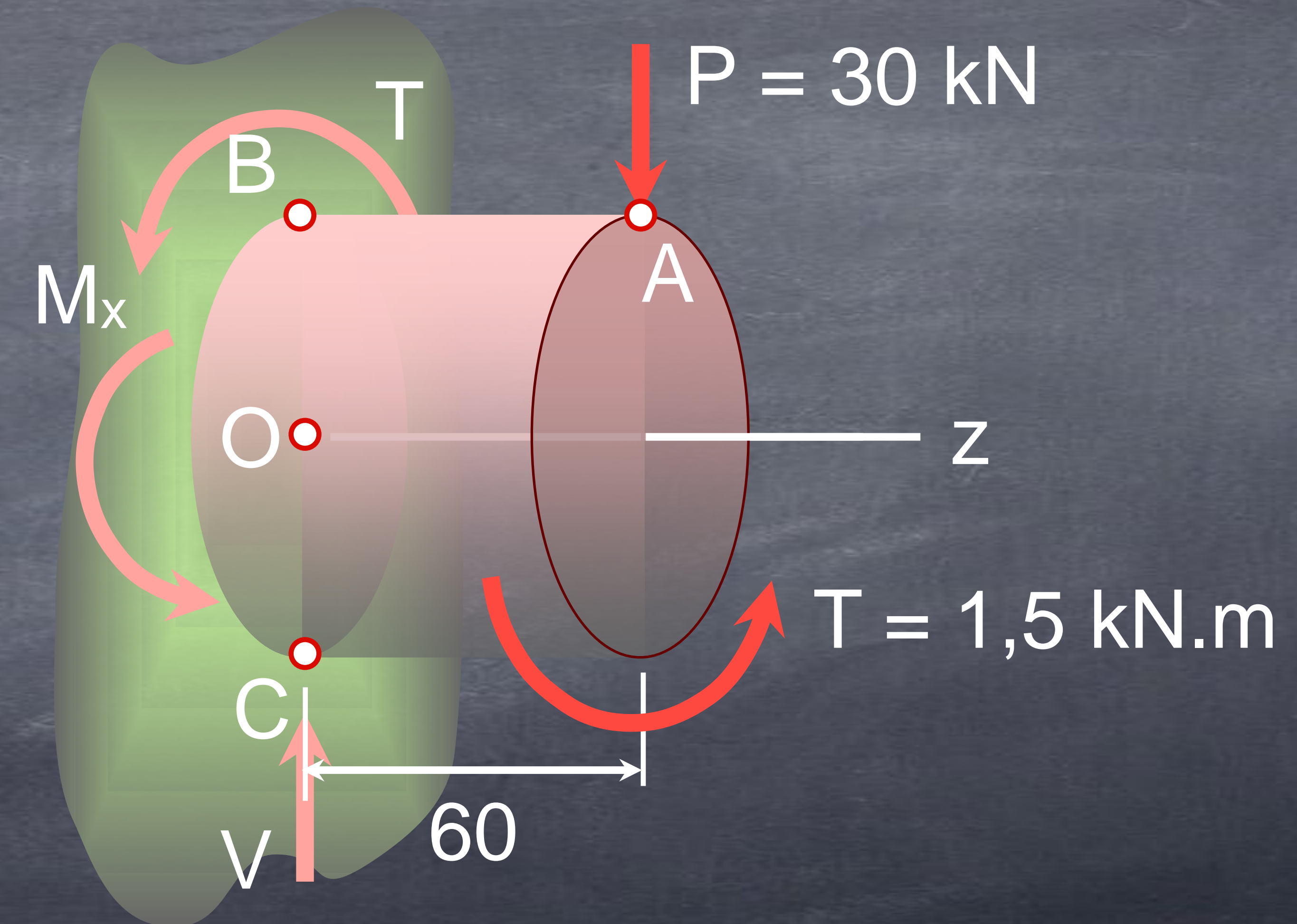
$$\tau_{\max} = 1,5 \cdot 10^3 \cdot (0,025) / (\pi \cdot 0,05^4 / 32)$$

$$\tau_{\max} = 61,12 \text{ MPa}$$



Outros exemplos

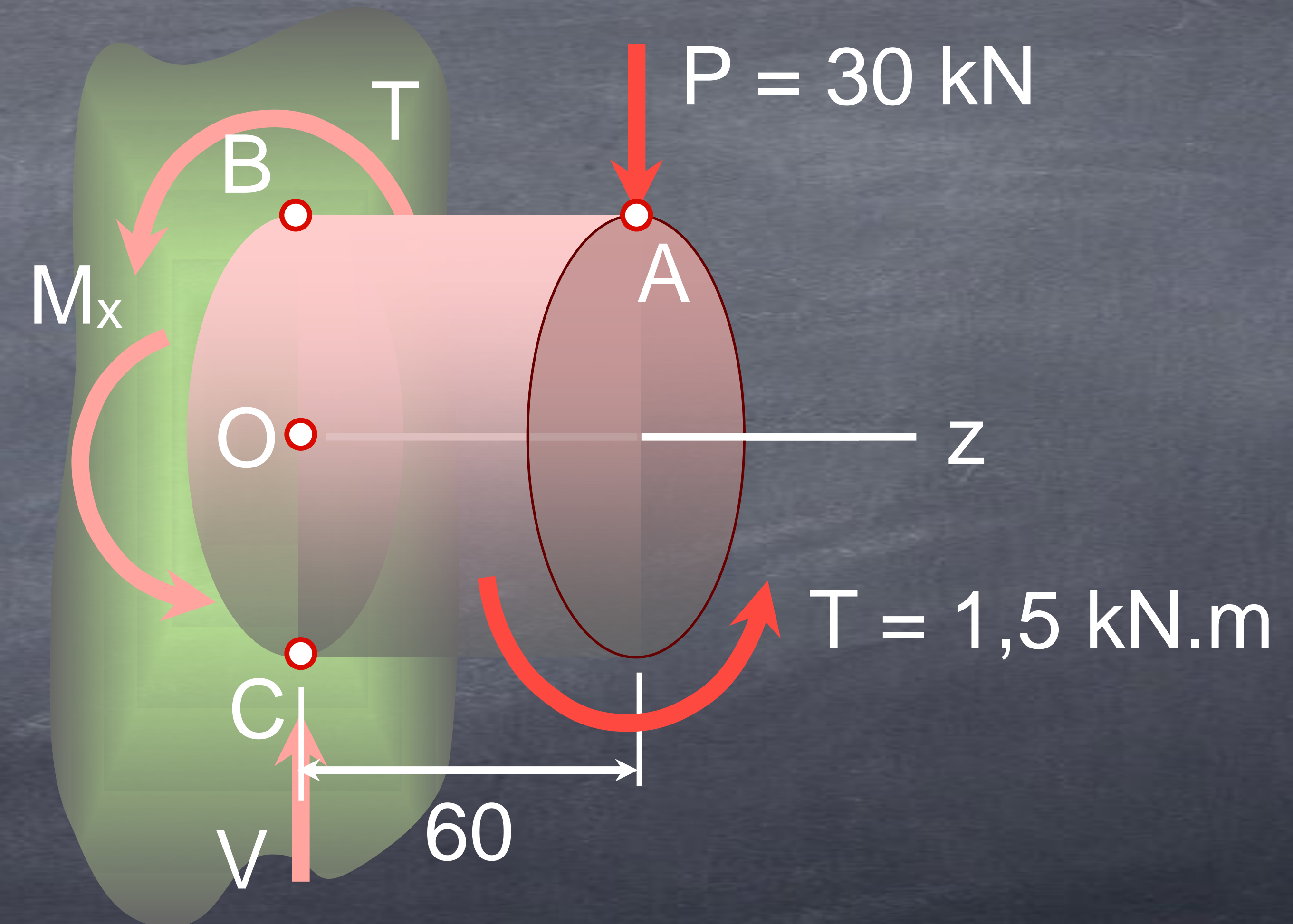
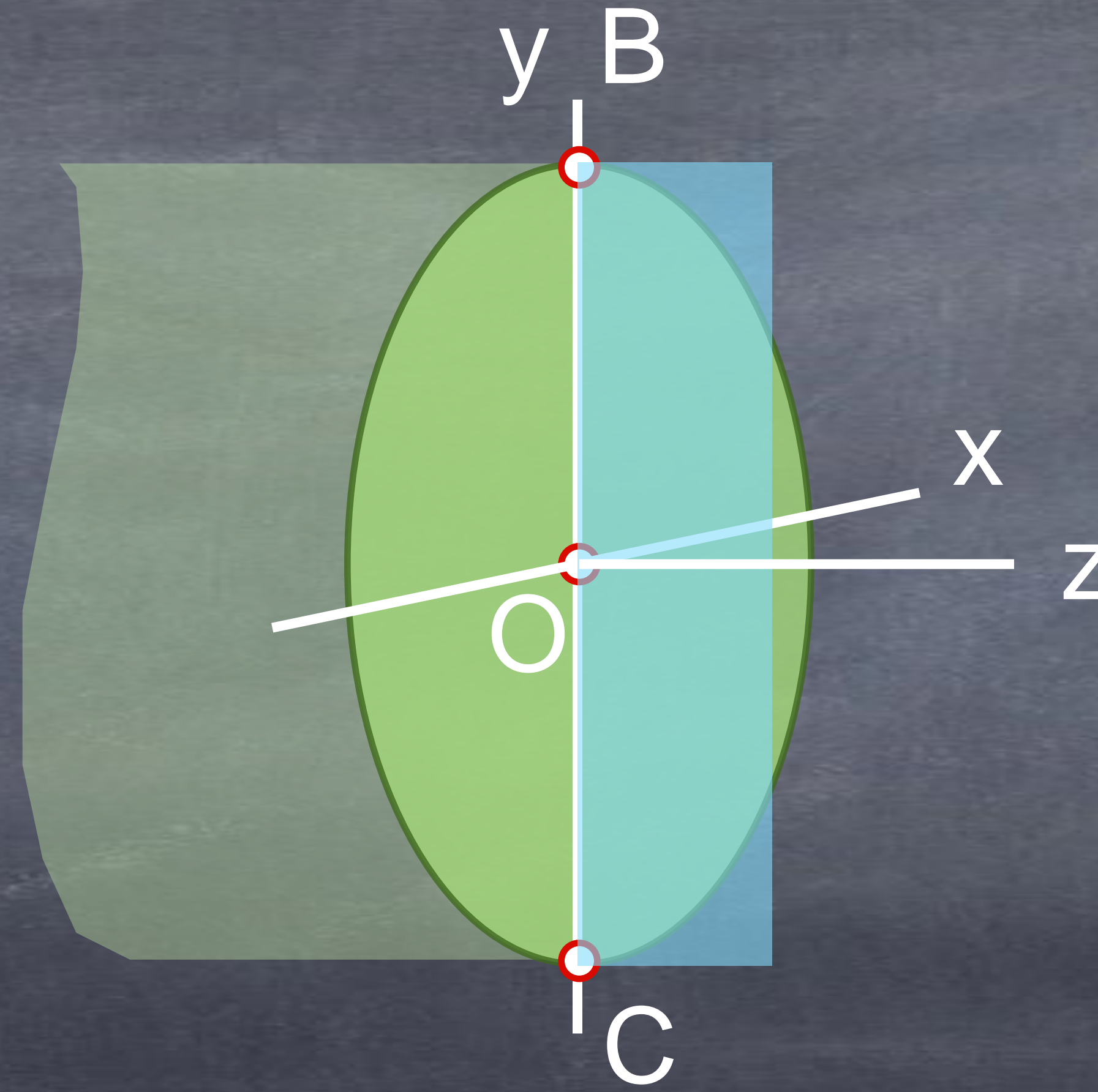
d) Superposição das tensões



Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

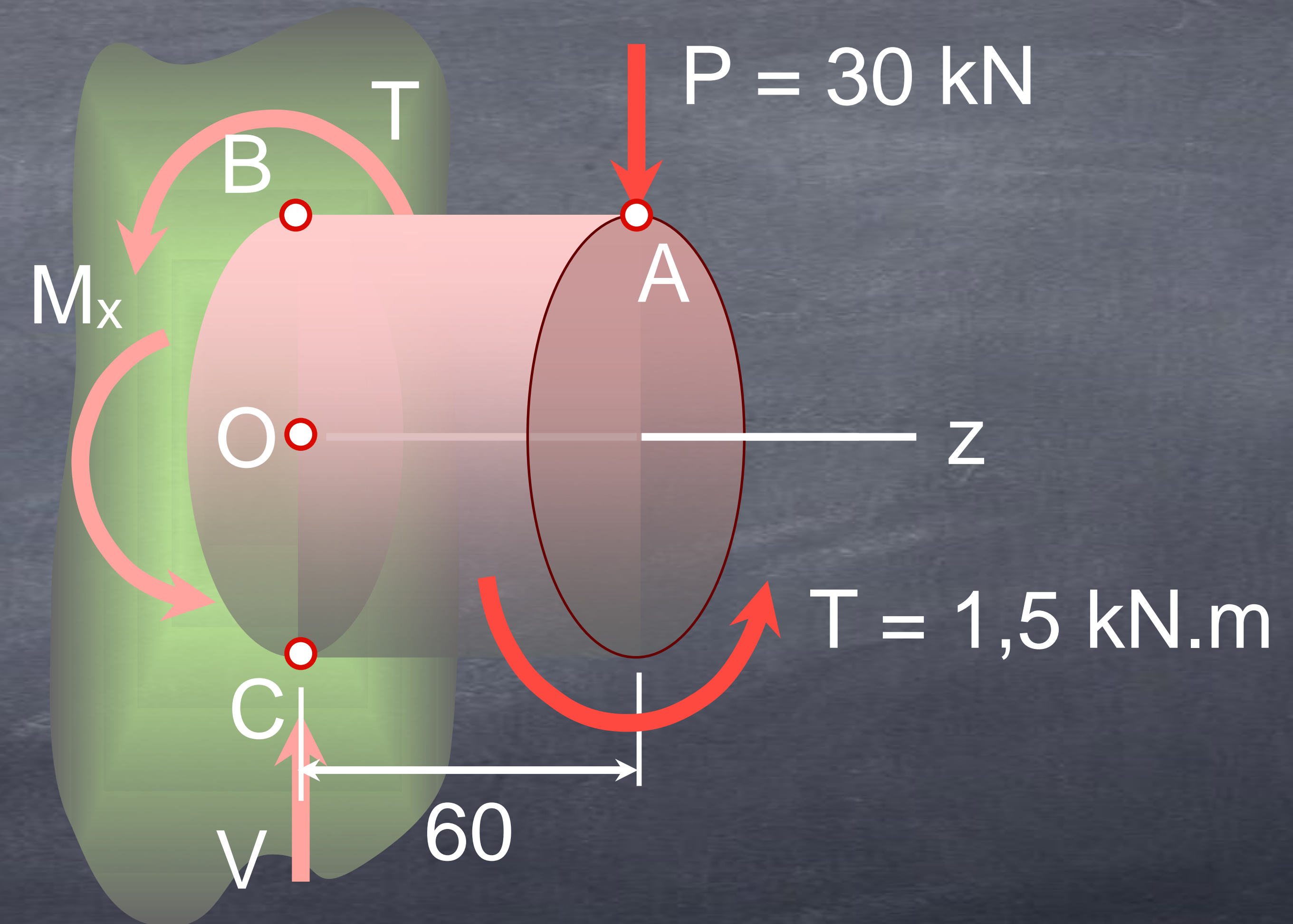
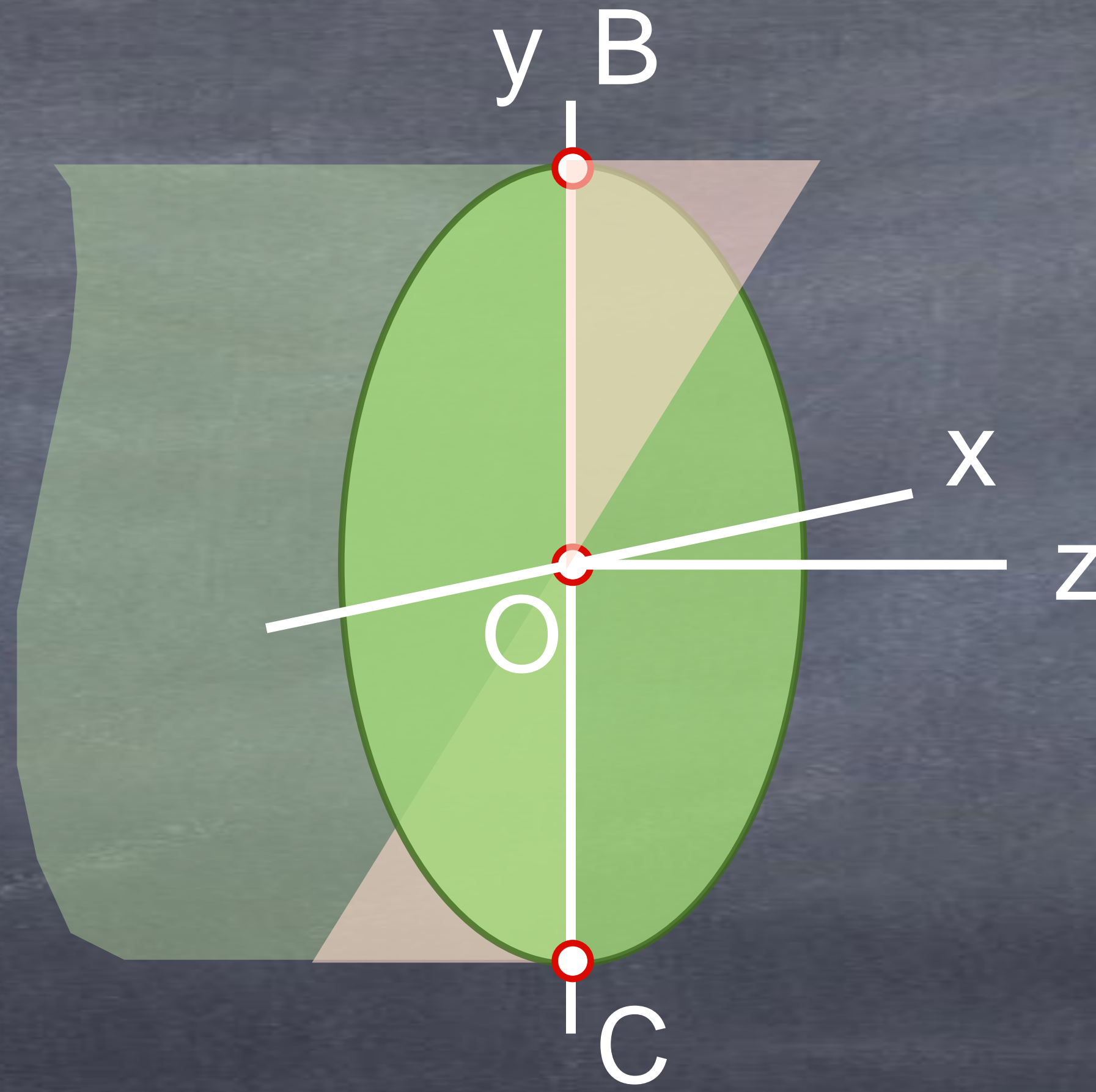


Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$



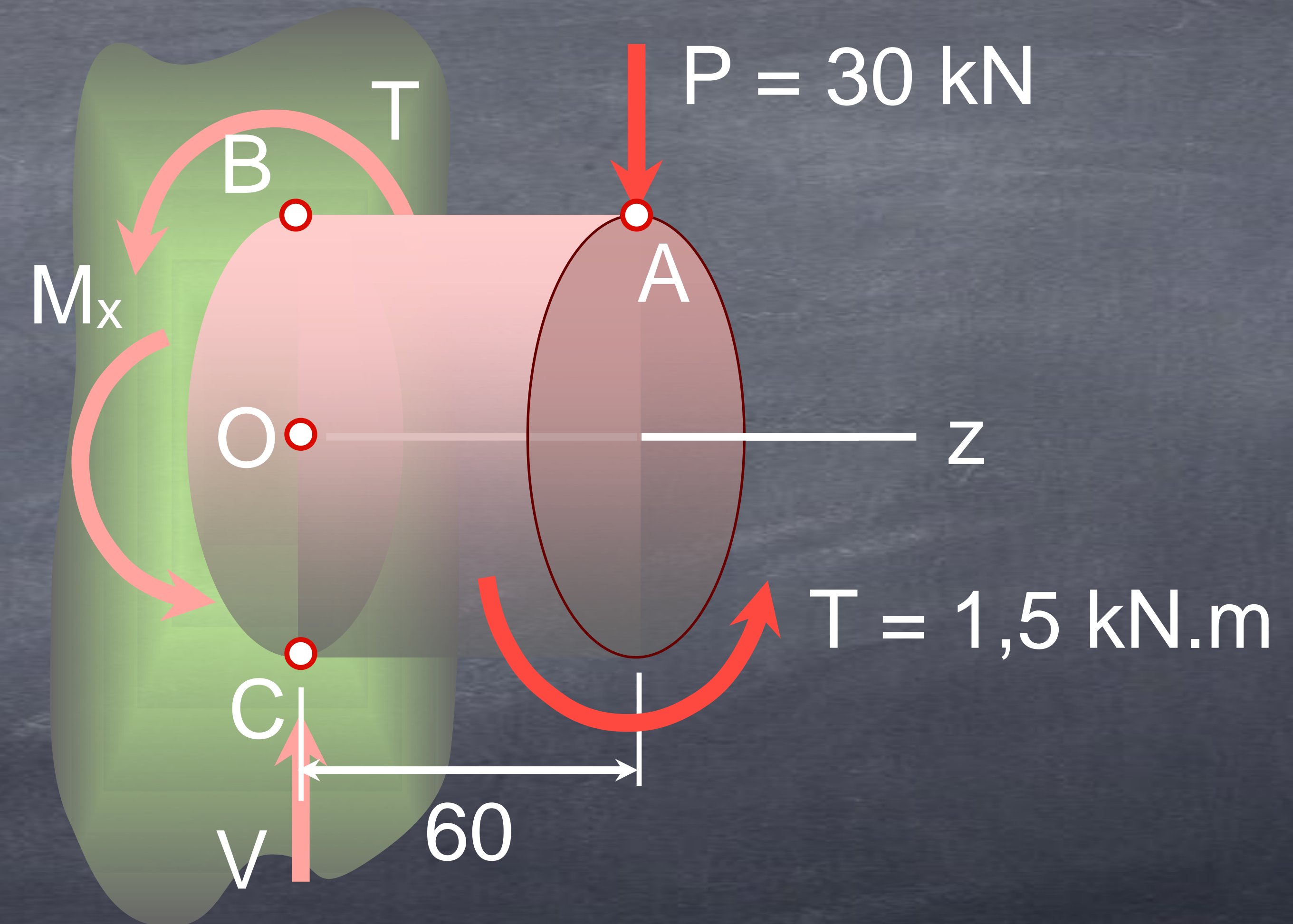
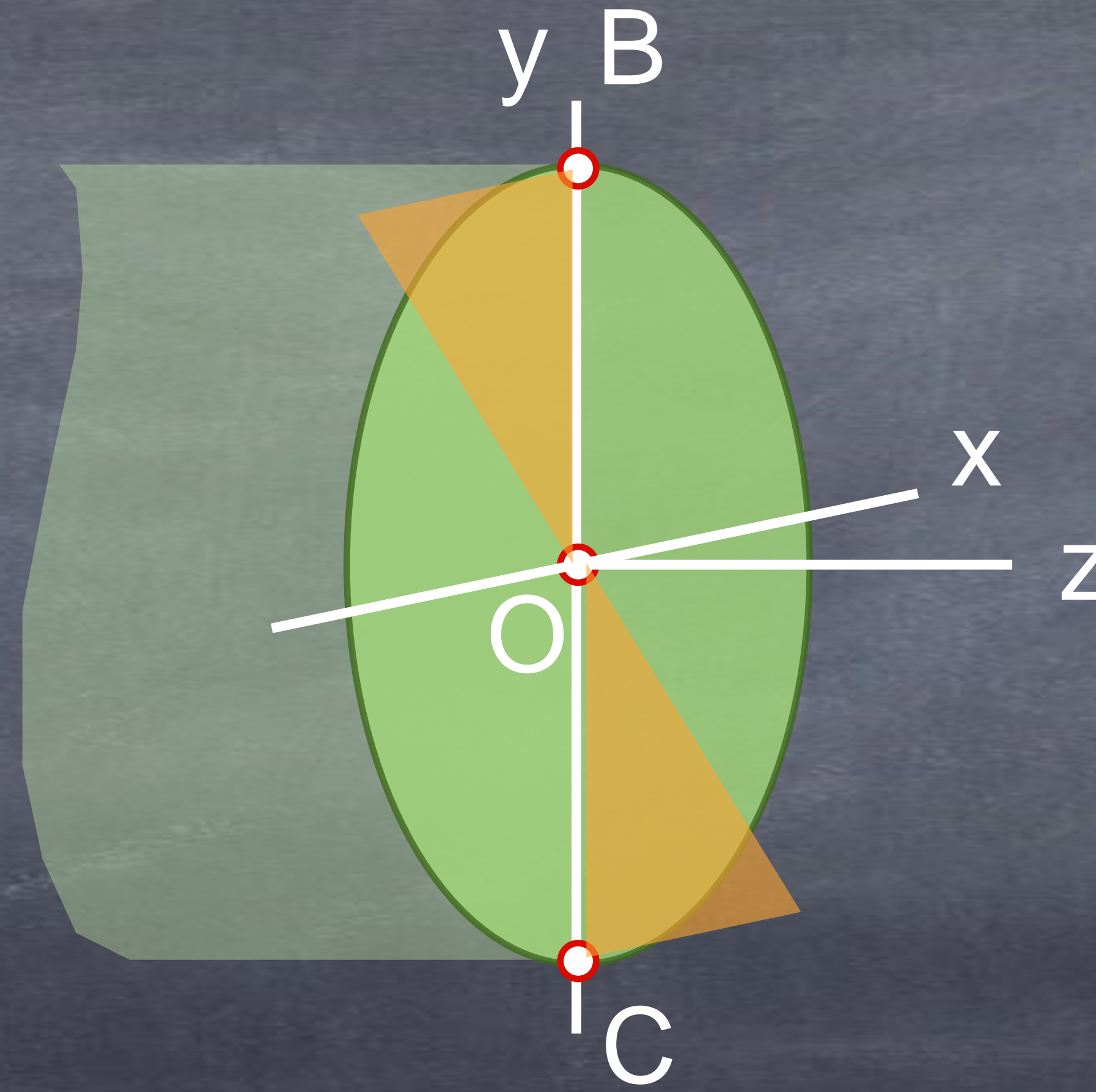
Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$

d.3) $\tau_{\max} = T \cdot r / J$



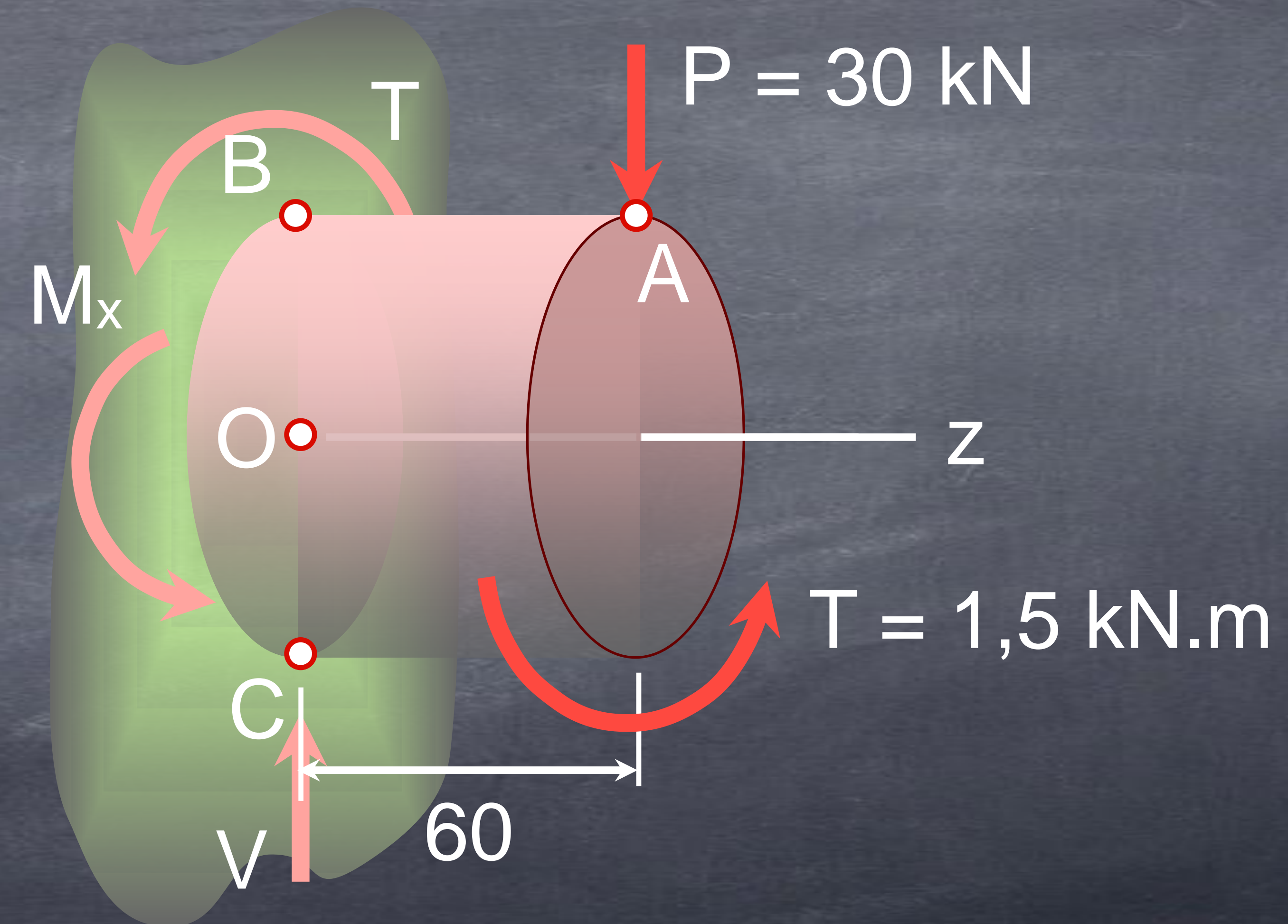
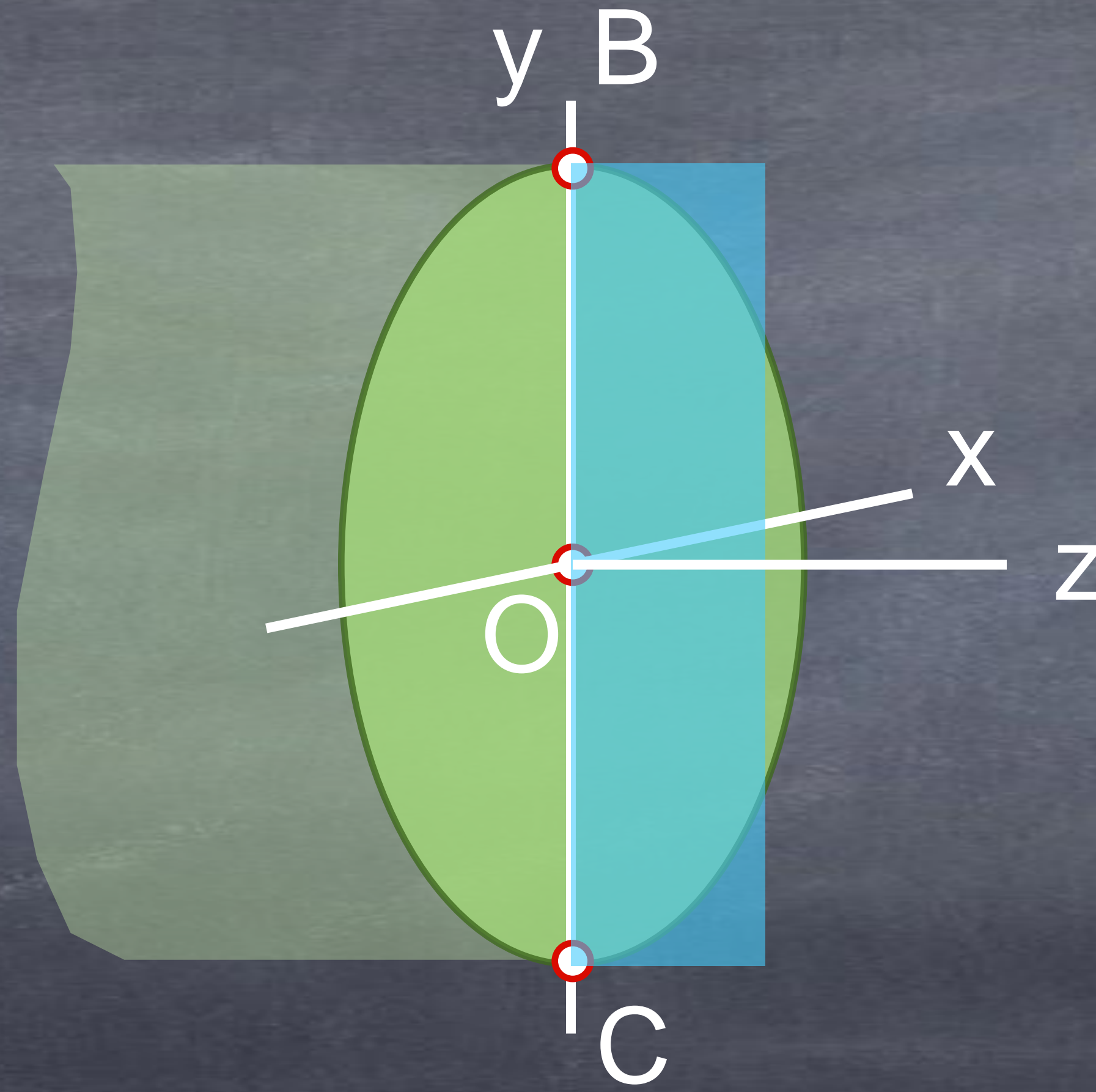
Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$

d.3) $\tau_{\max} = T \cdot r / J$



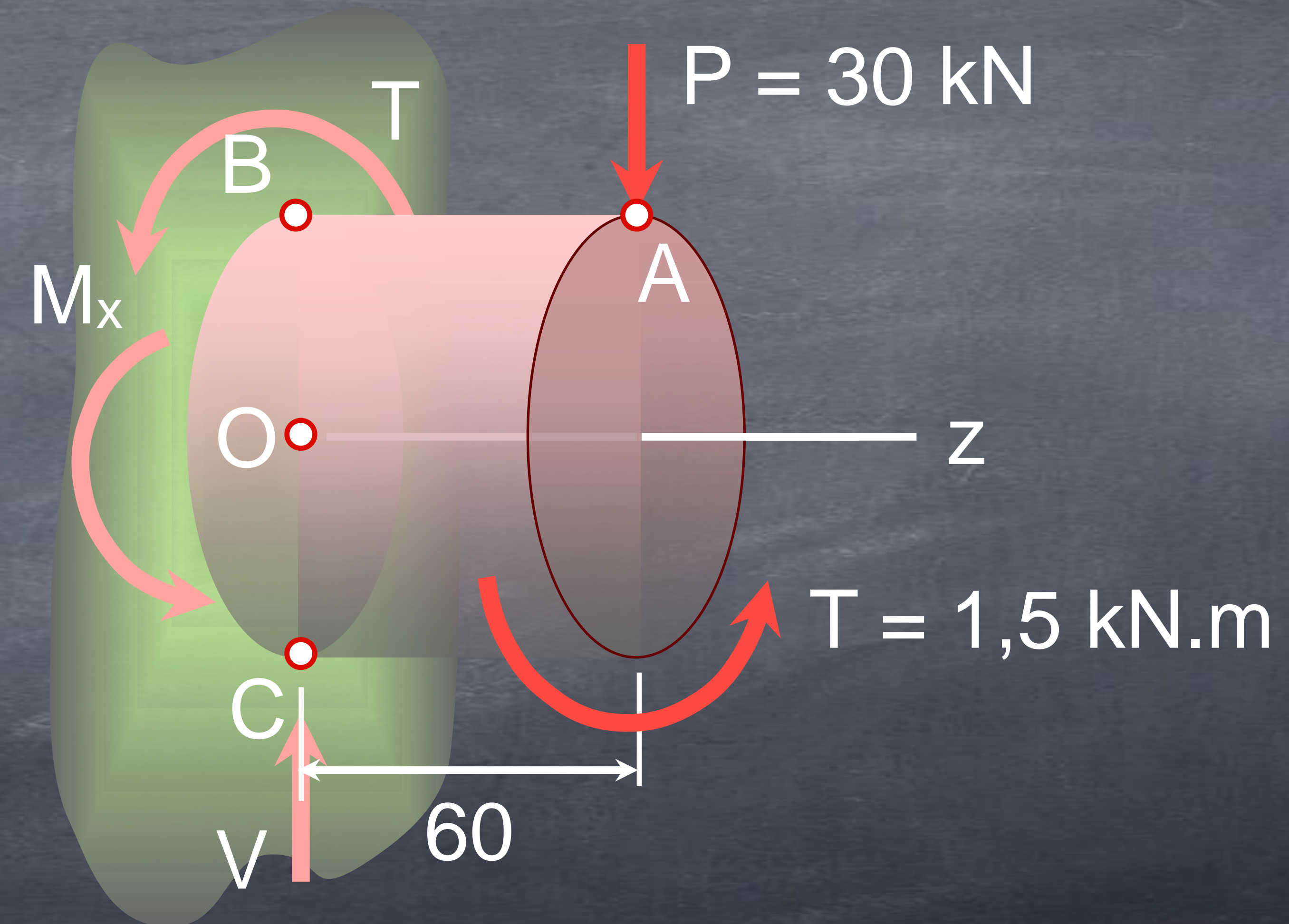
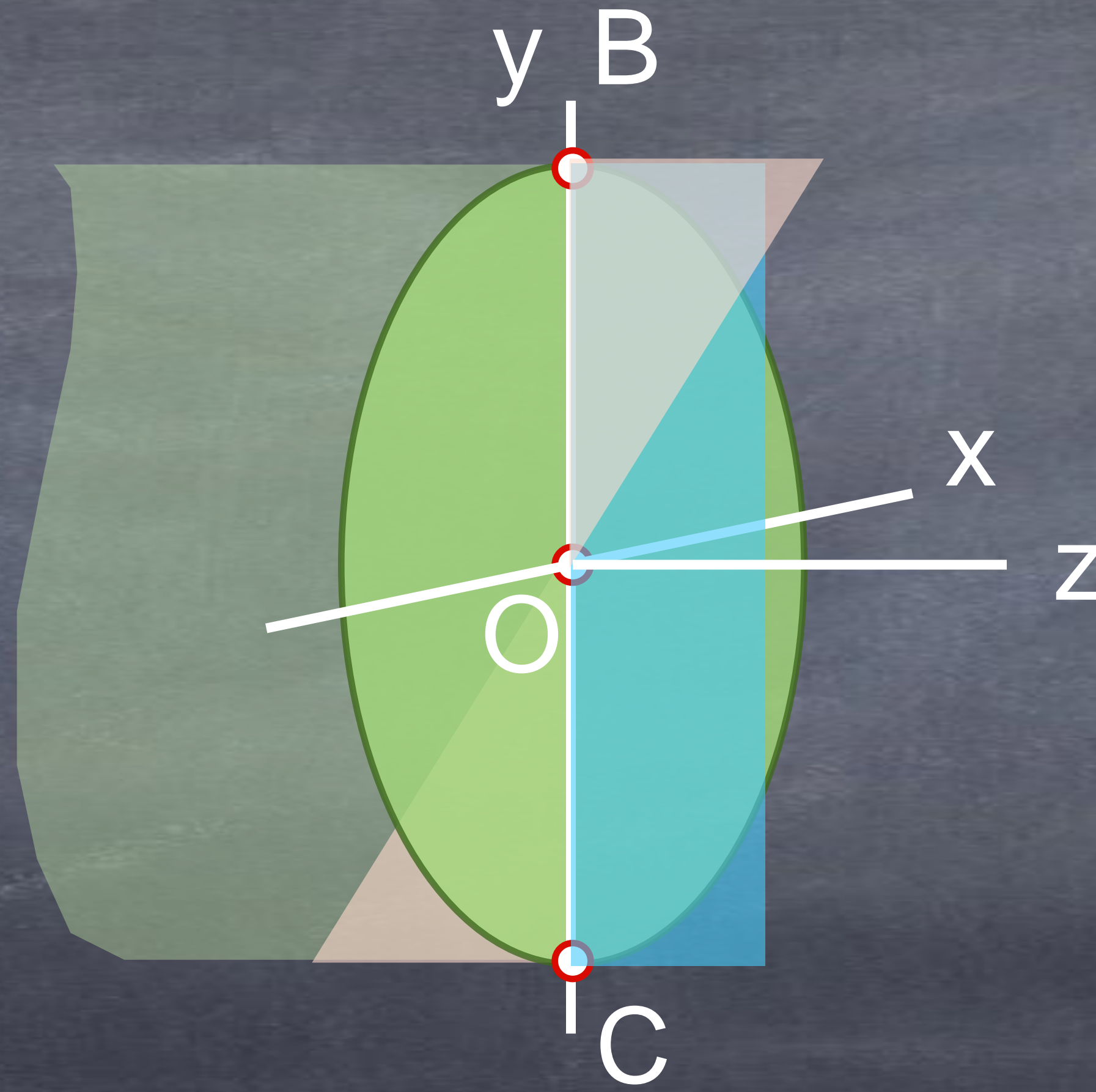
Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$

d.3) $\tau_{\max} = T \cdot r / J$



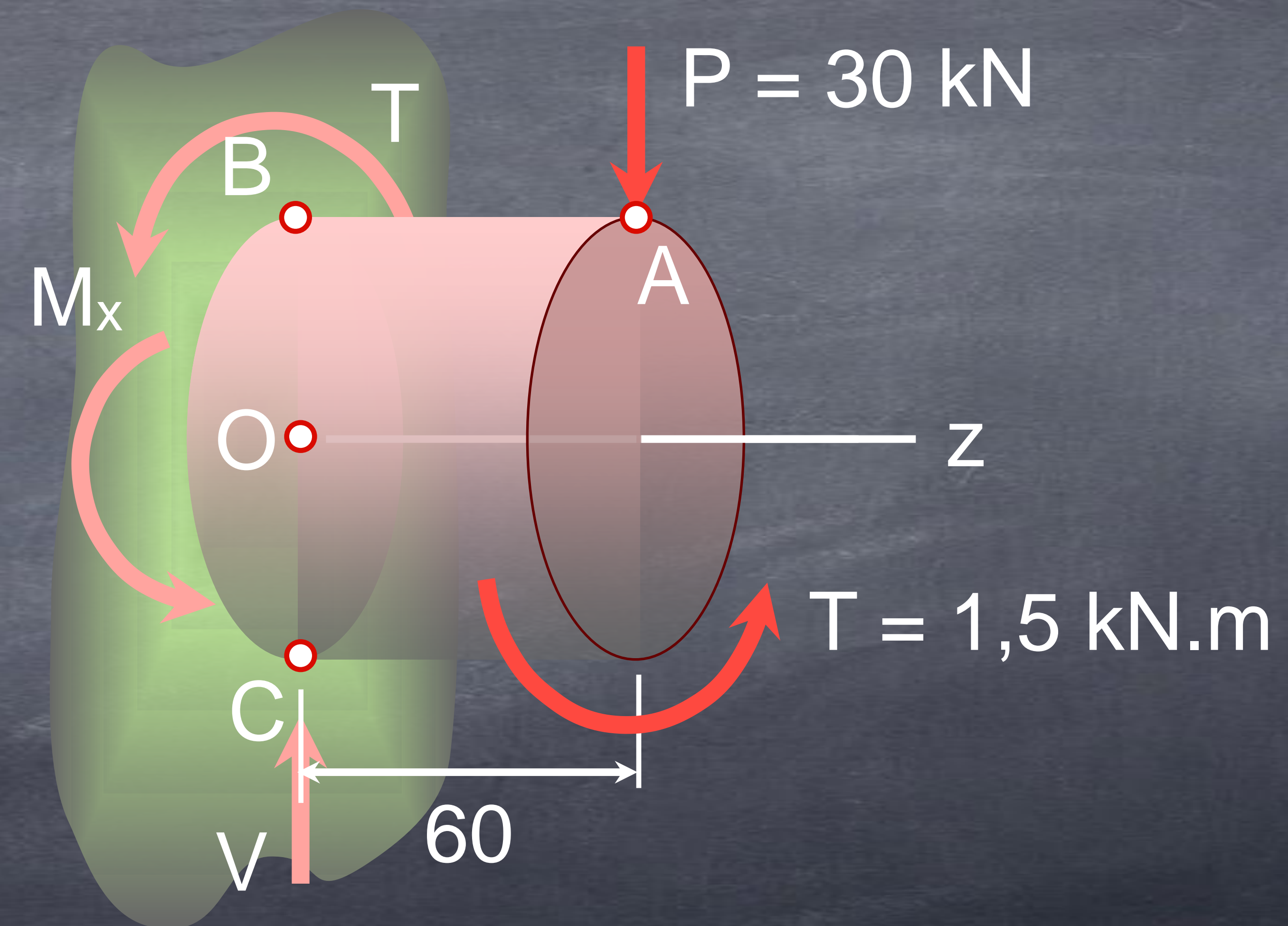
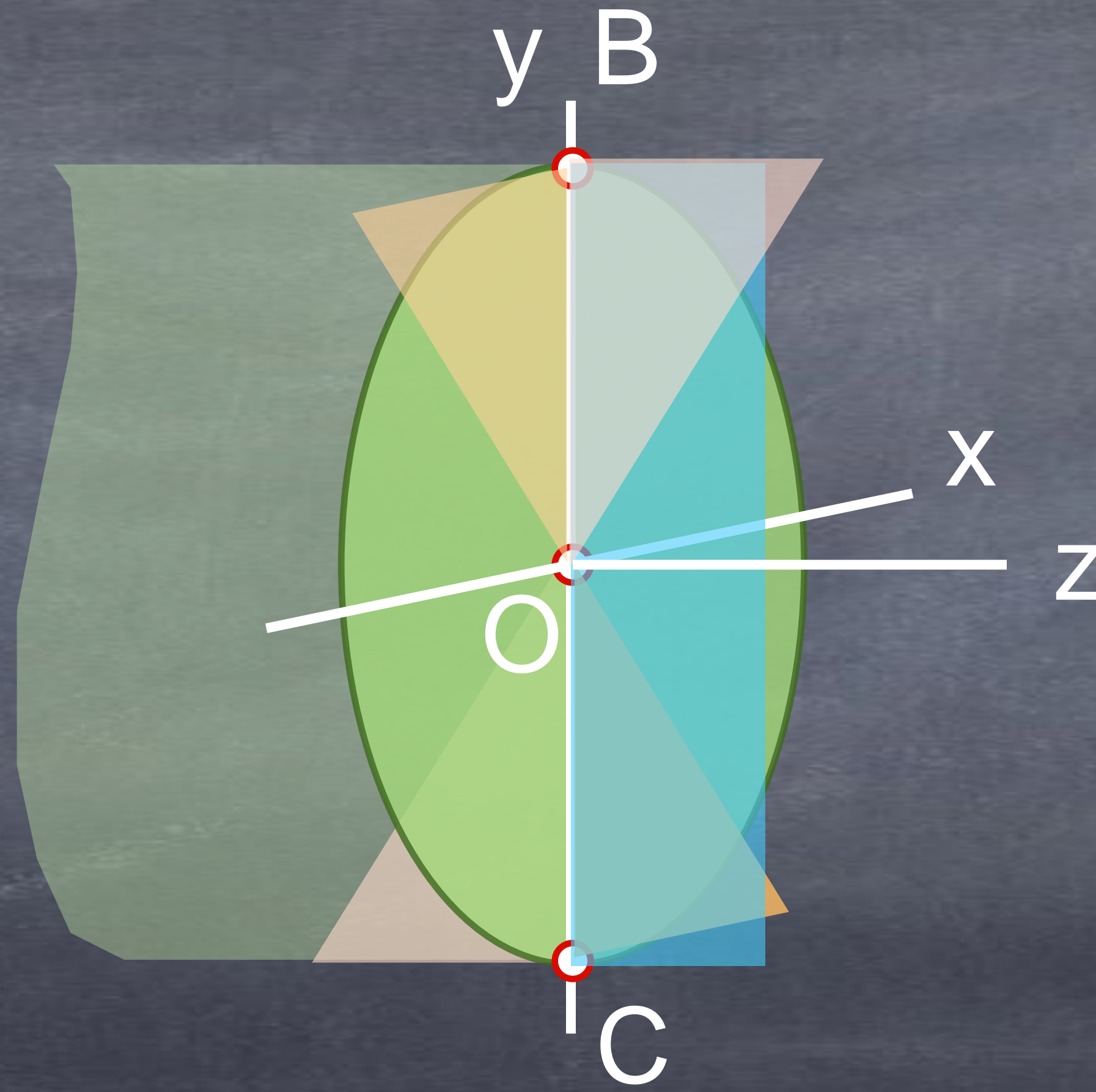
Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$

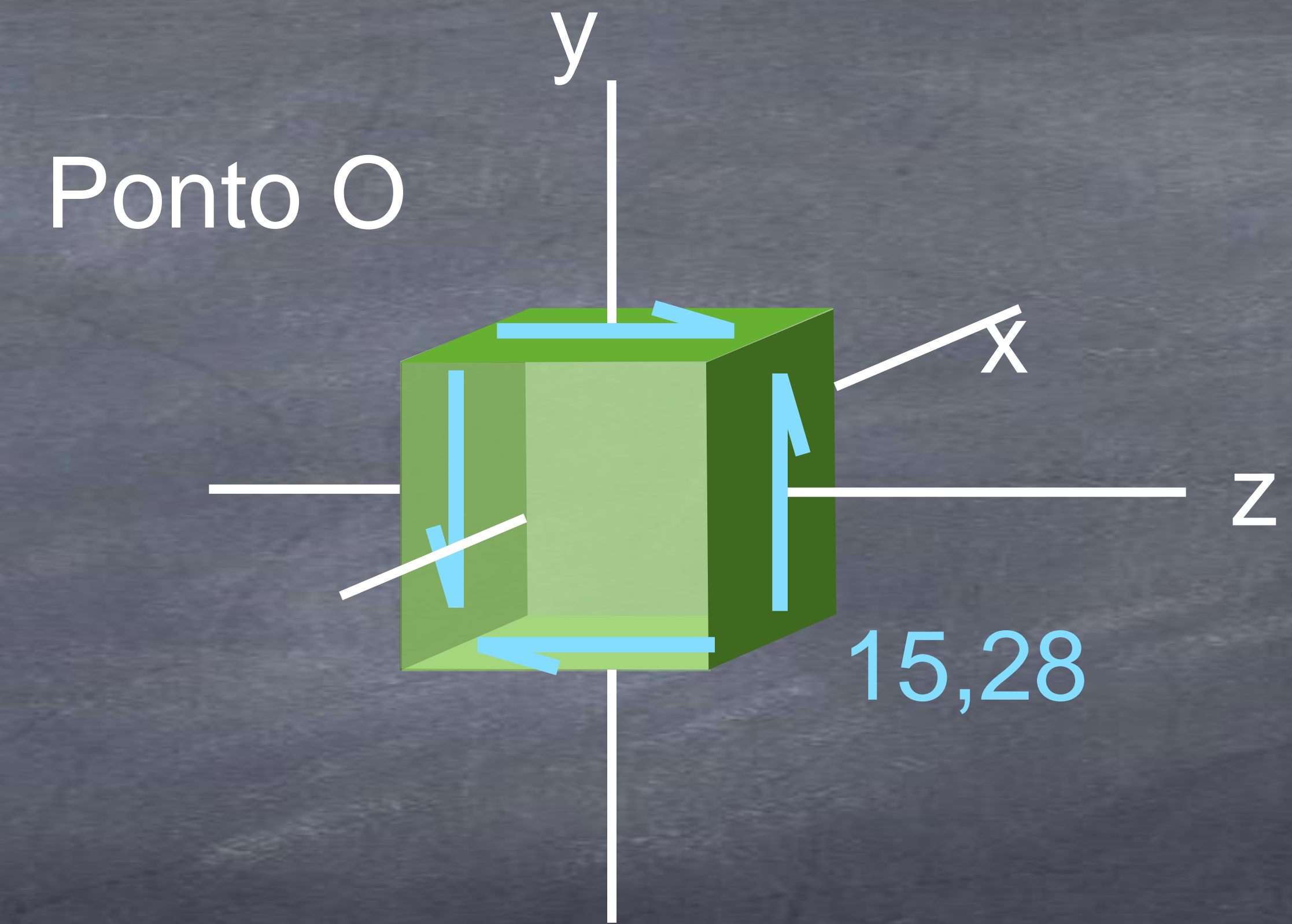
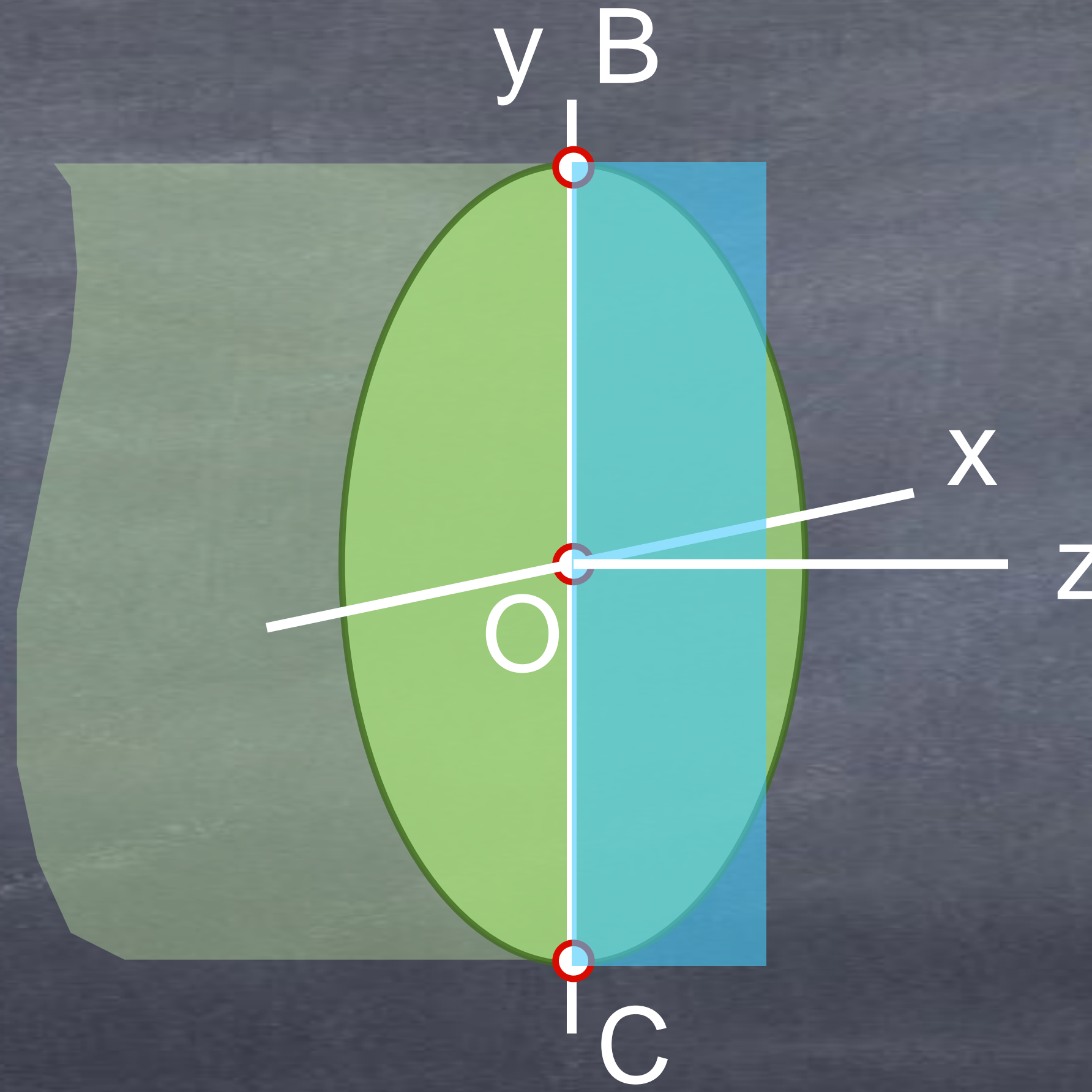
d.3) $\tau_{\max} = T \cdot r / J$



Outros exemplos

d) Superposição das tensões

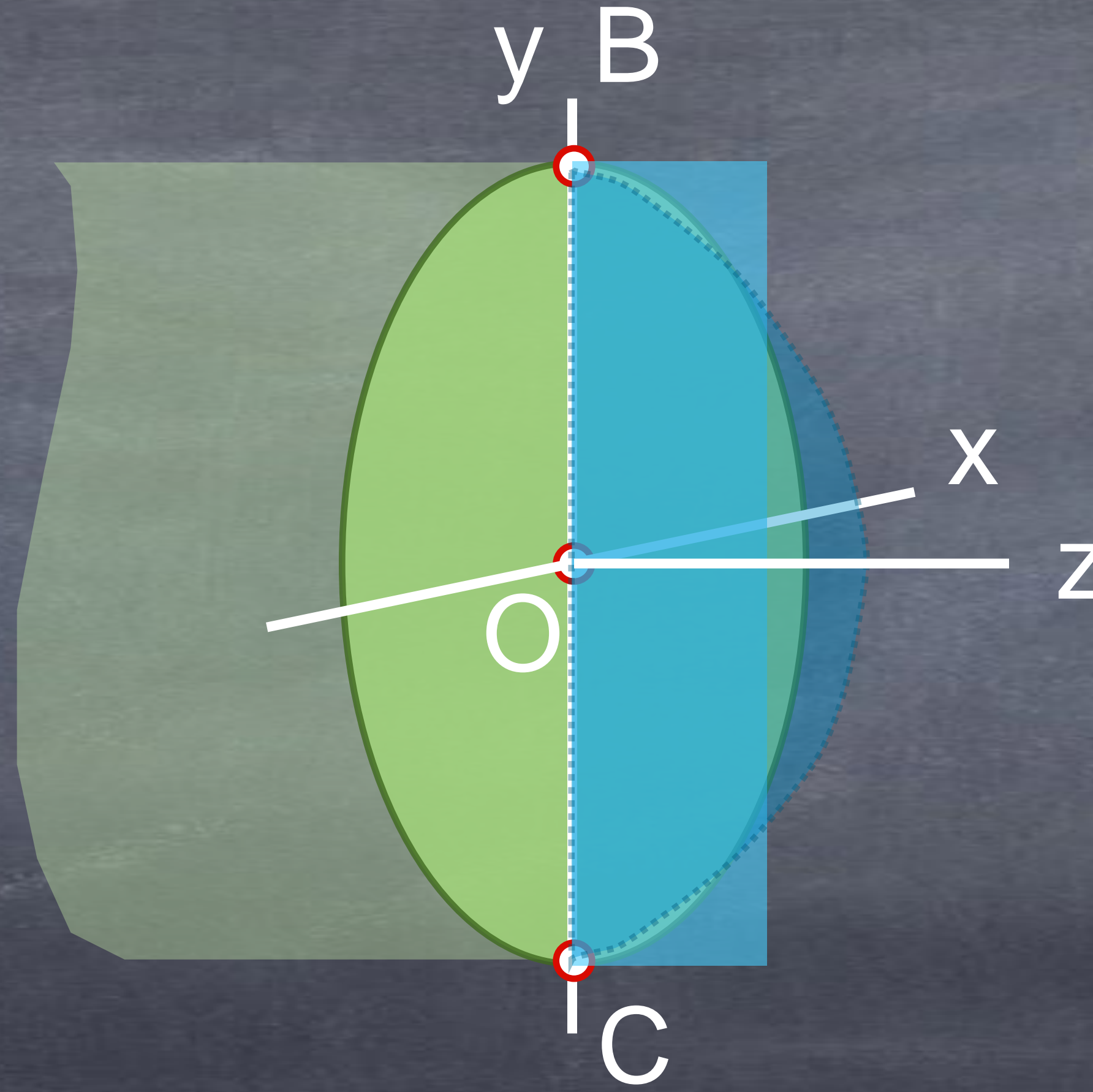
d.1) $\tau = V / A$



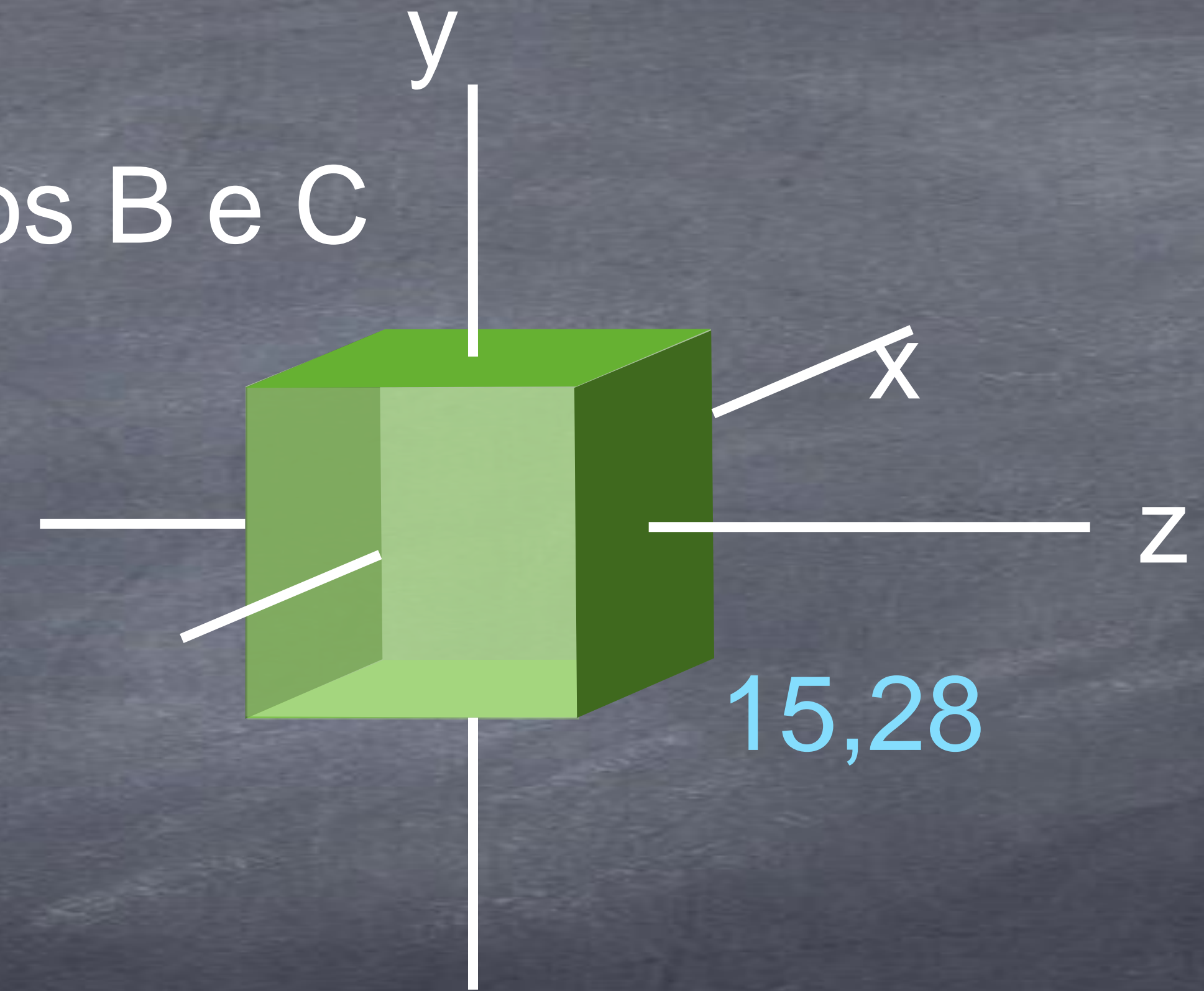
Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$



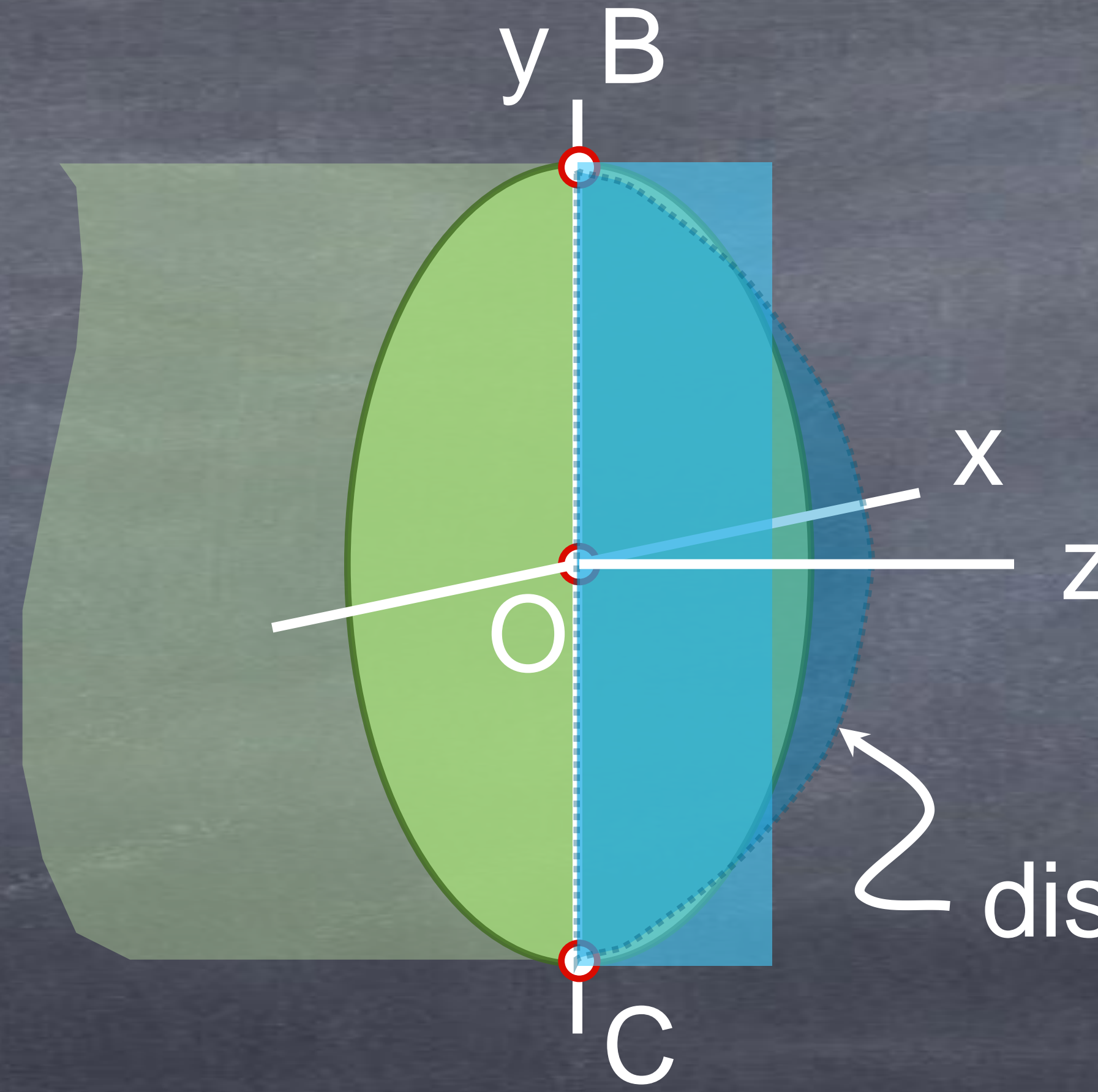
Pontos B e C



Outros exemplos

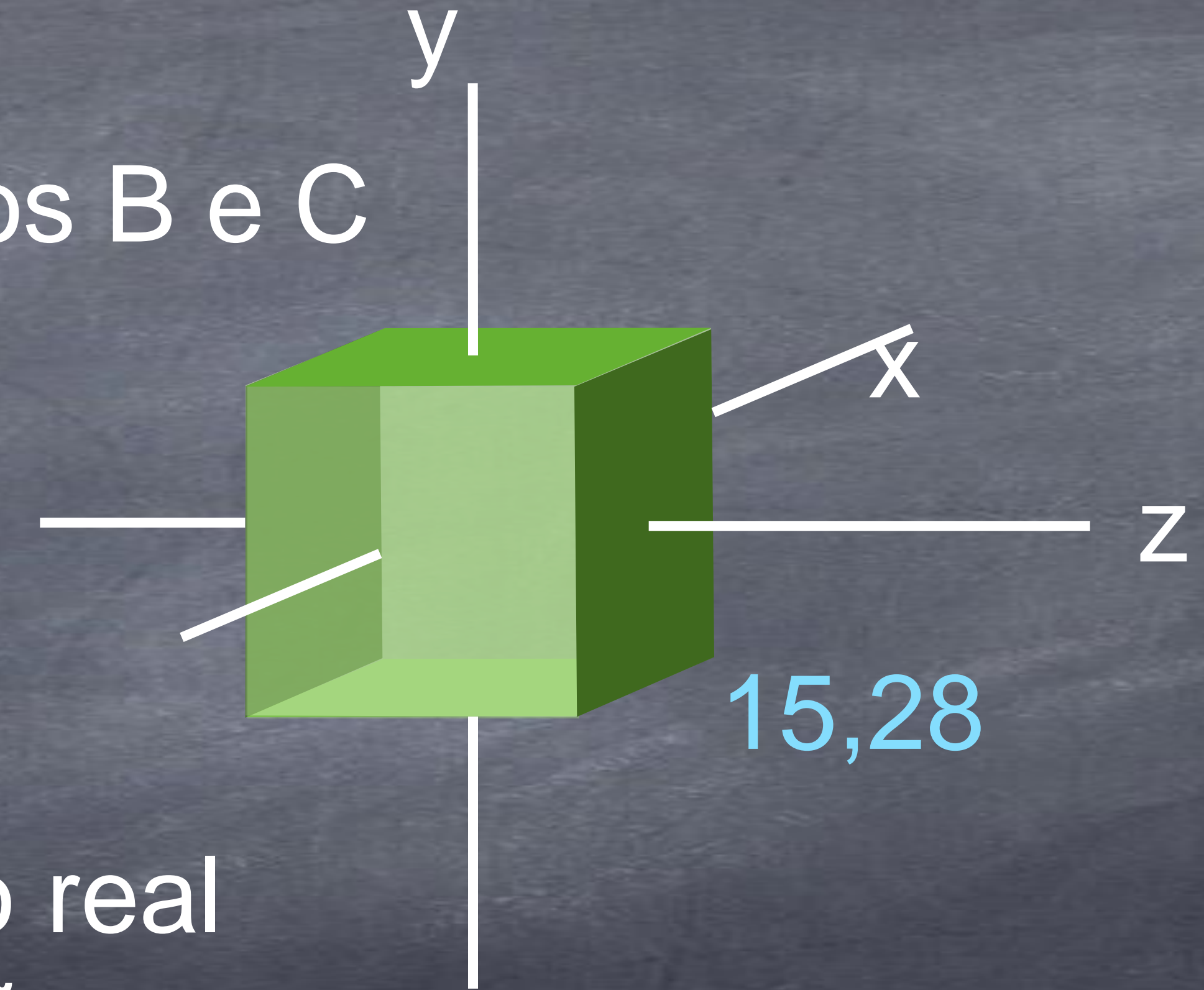
d) Superposição das tensões

d.1) $\tau = V / A$



distribuição real
da tensão

Pontos B e C

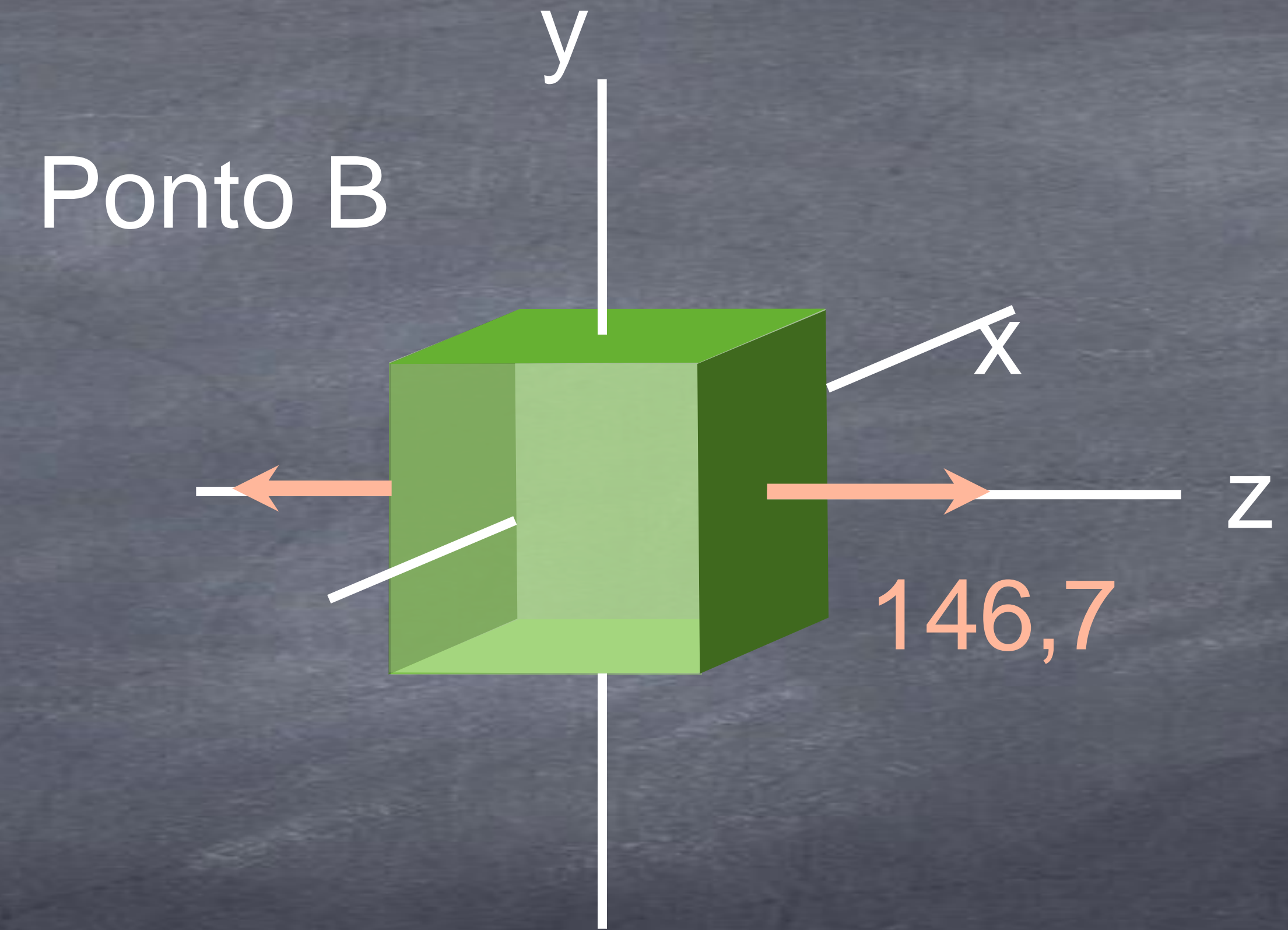
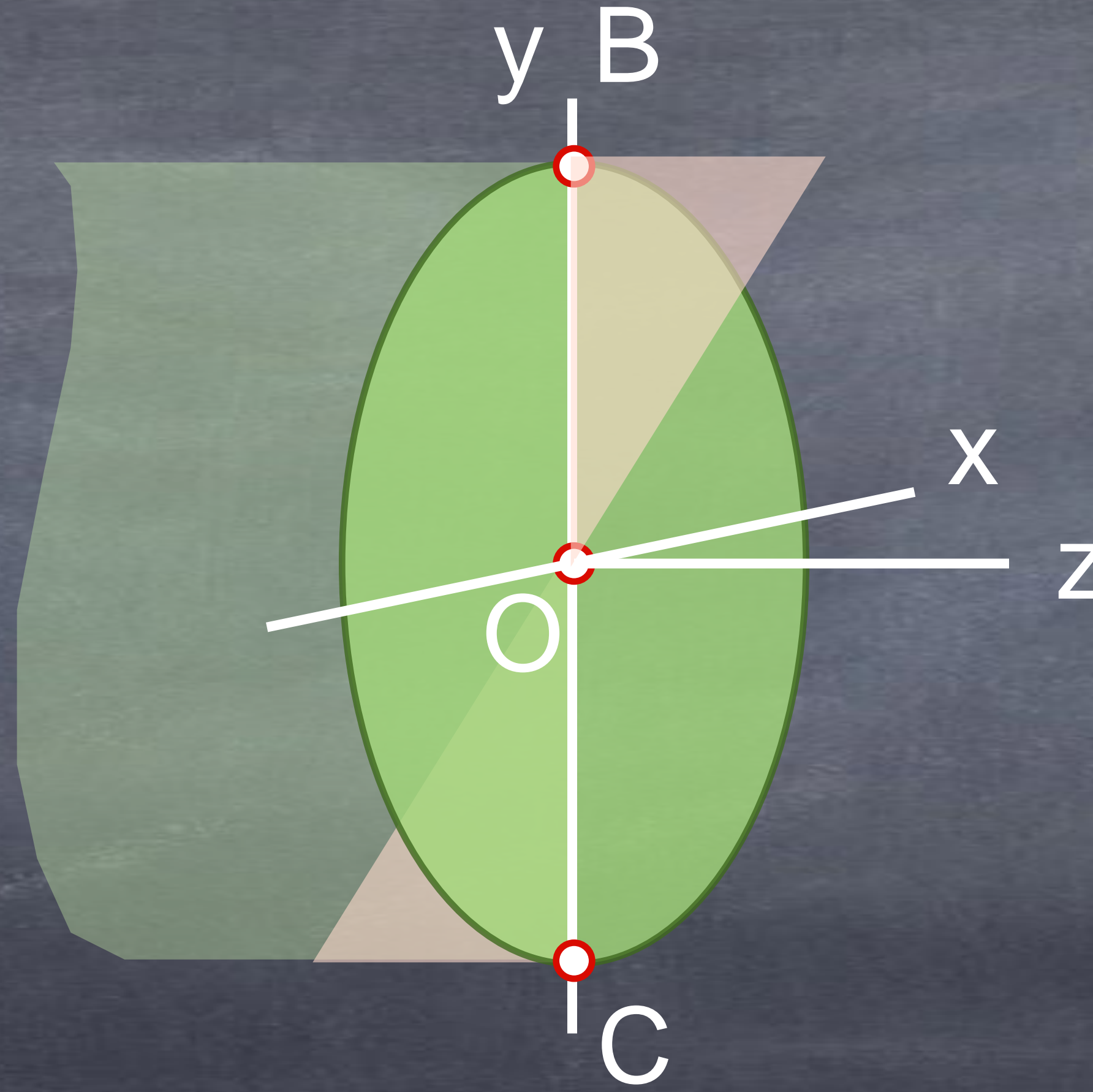


Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$

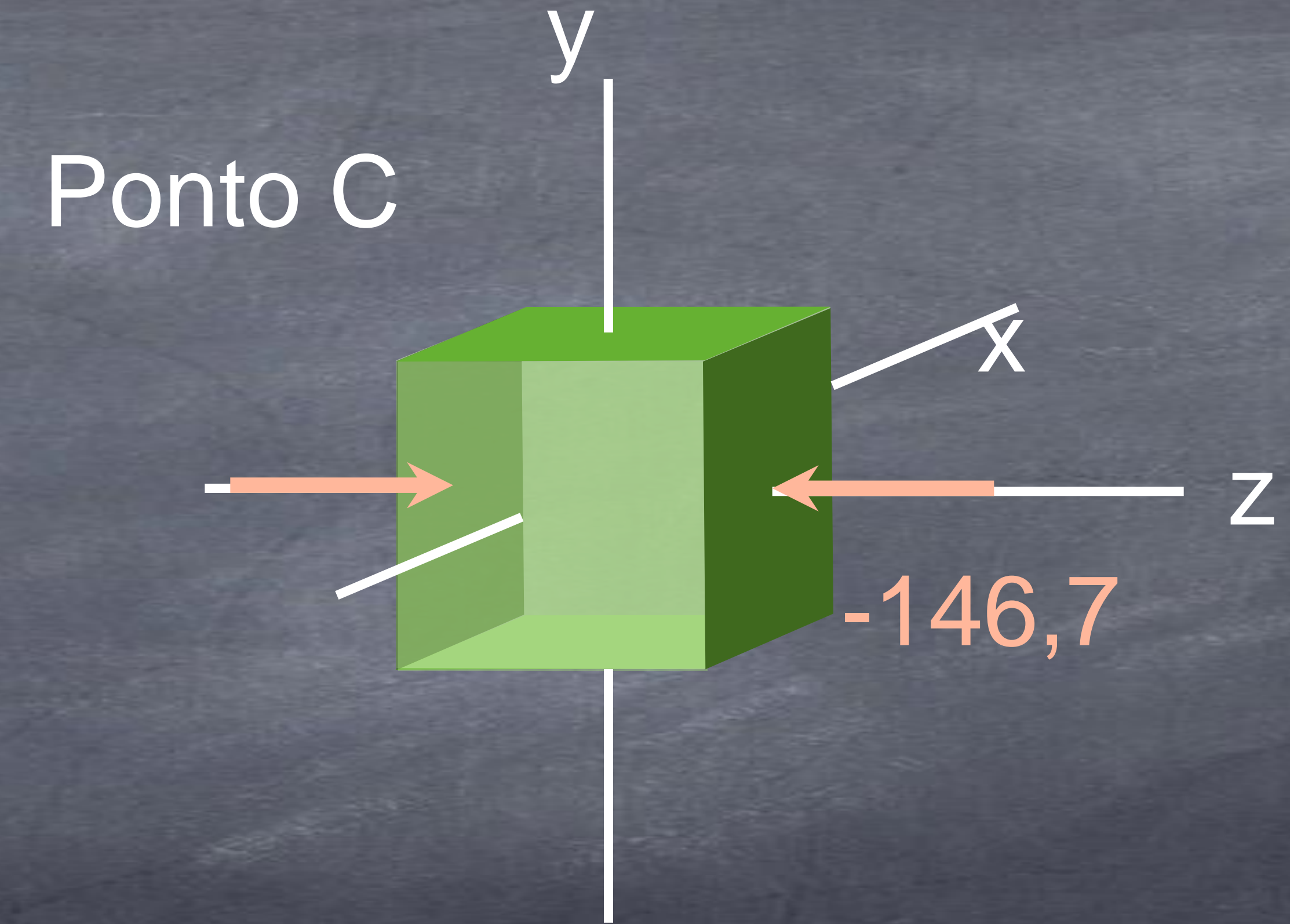
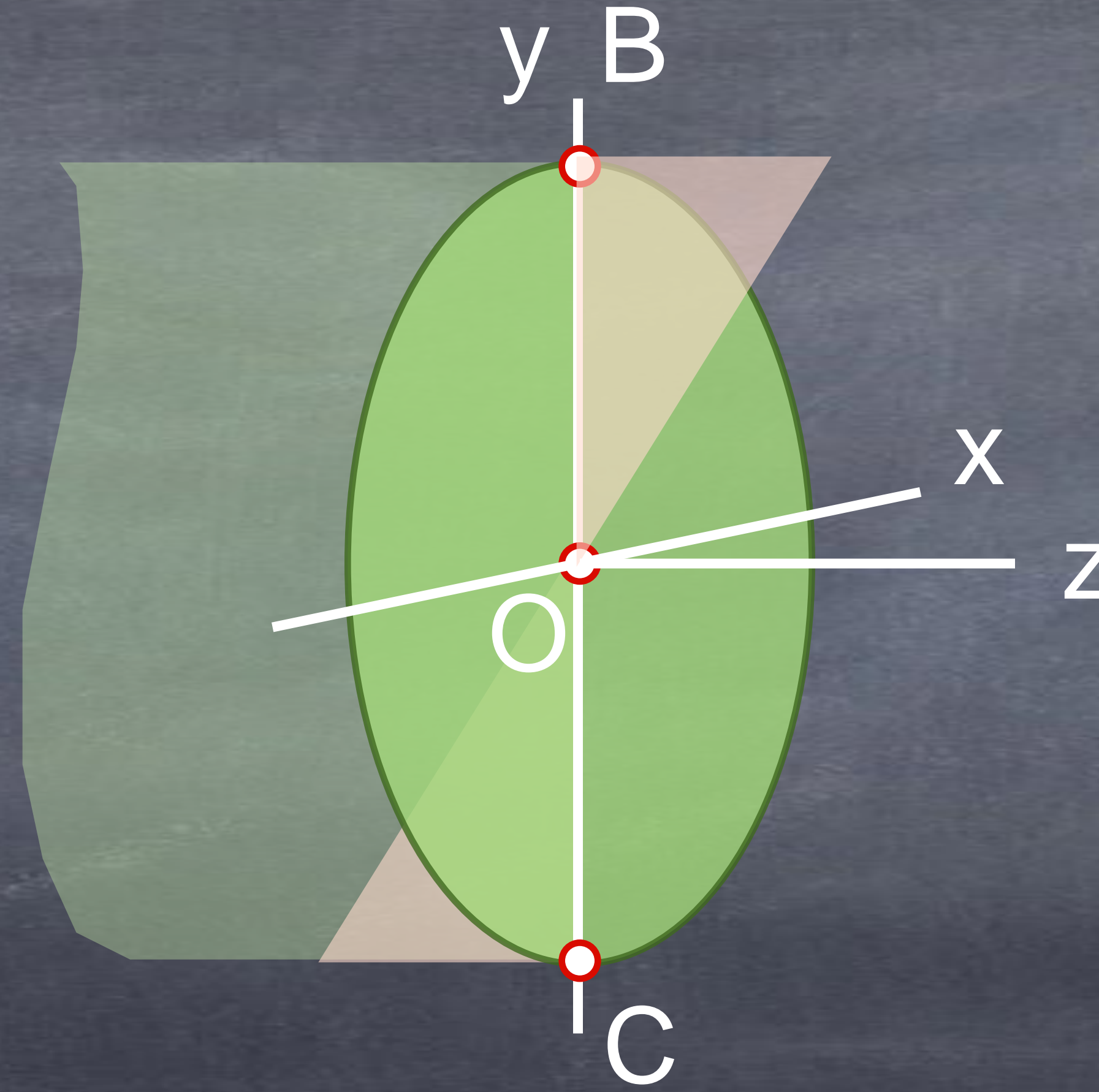


Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$

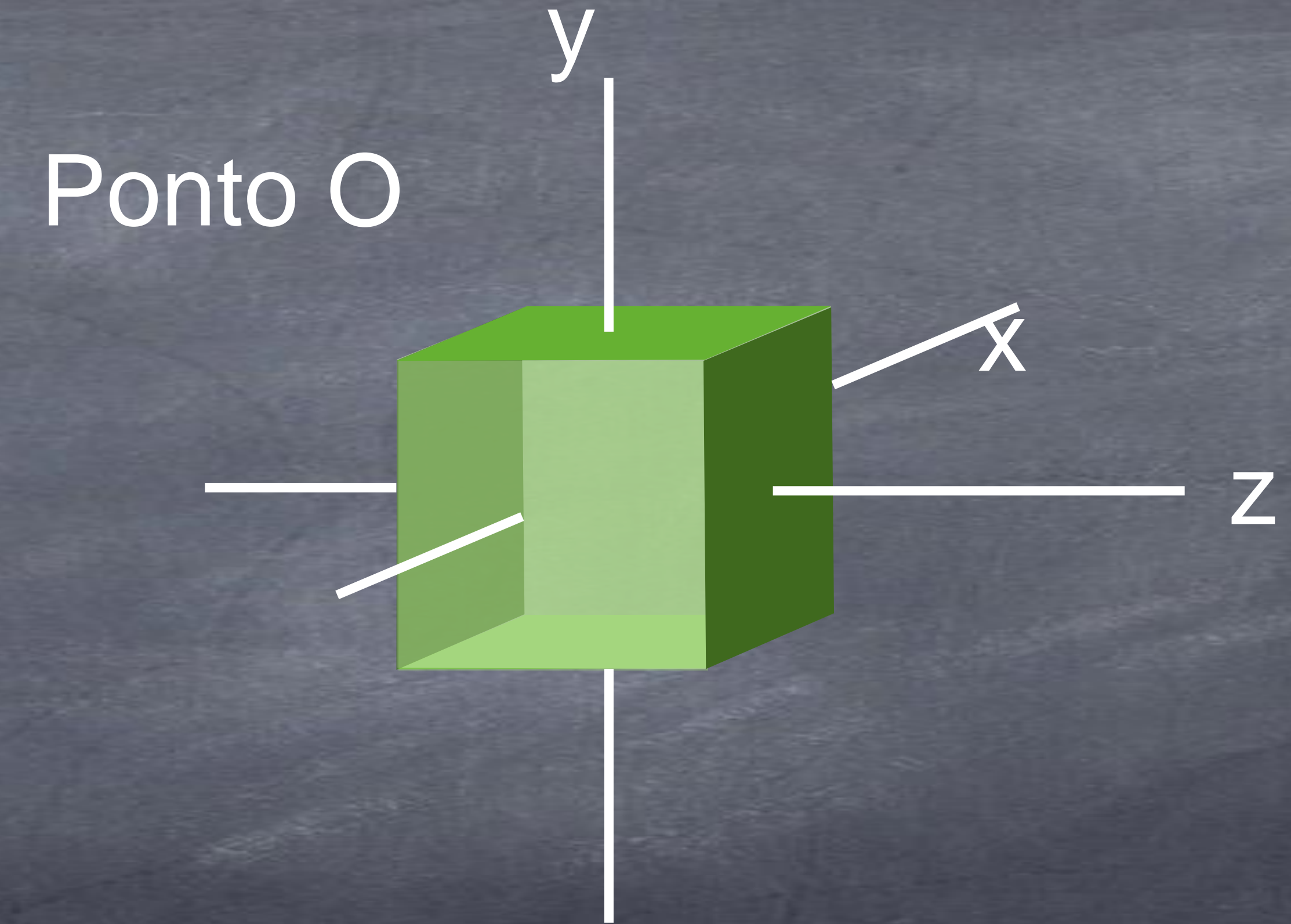
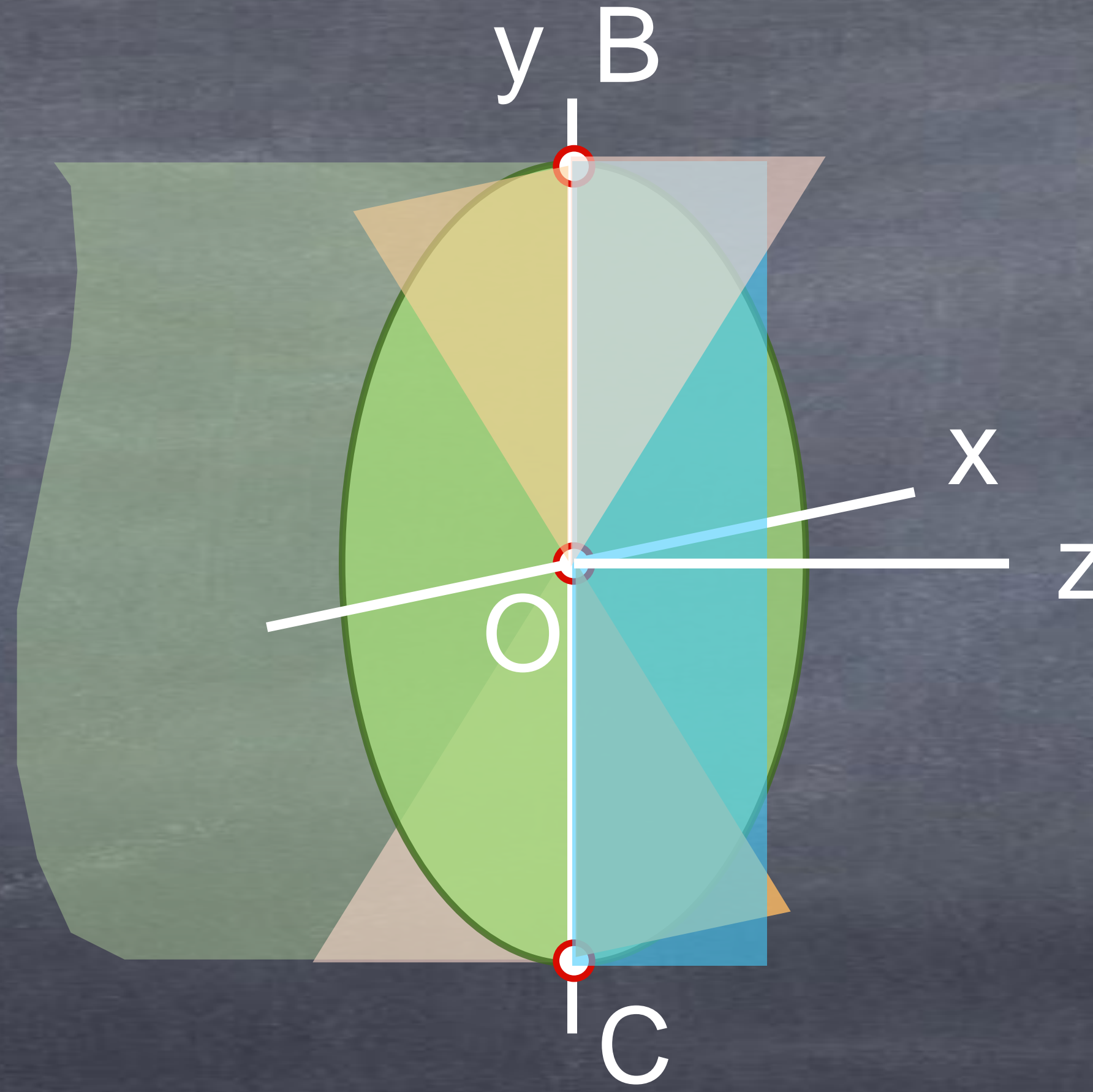


Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$



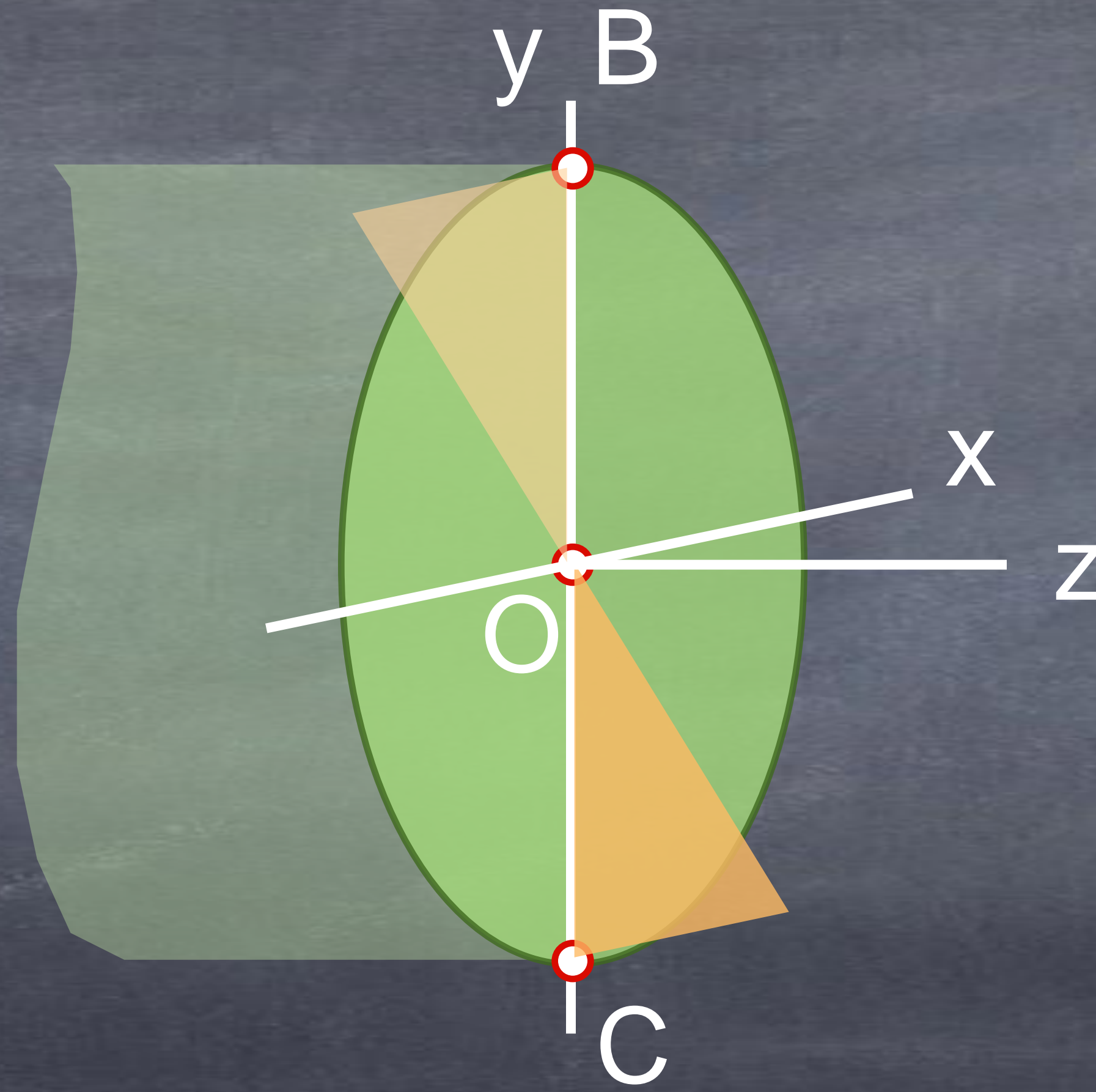
Outros exemplos

d) Superposição das tensões

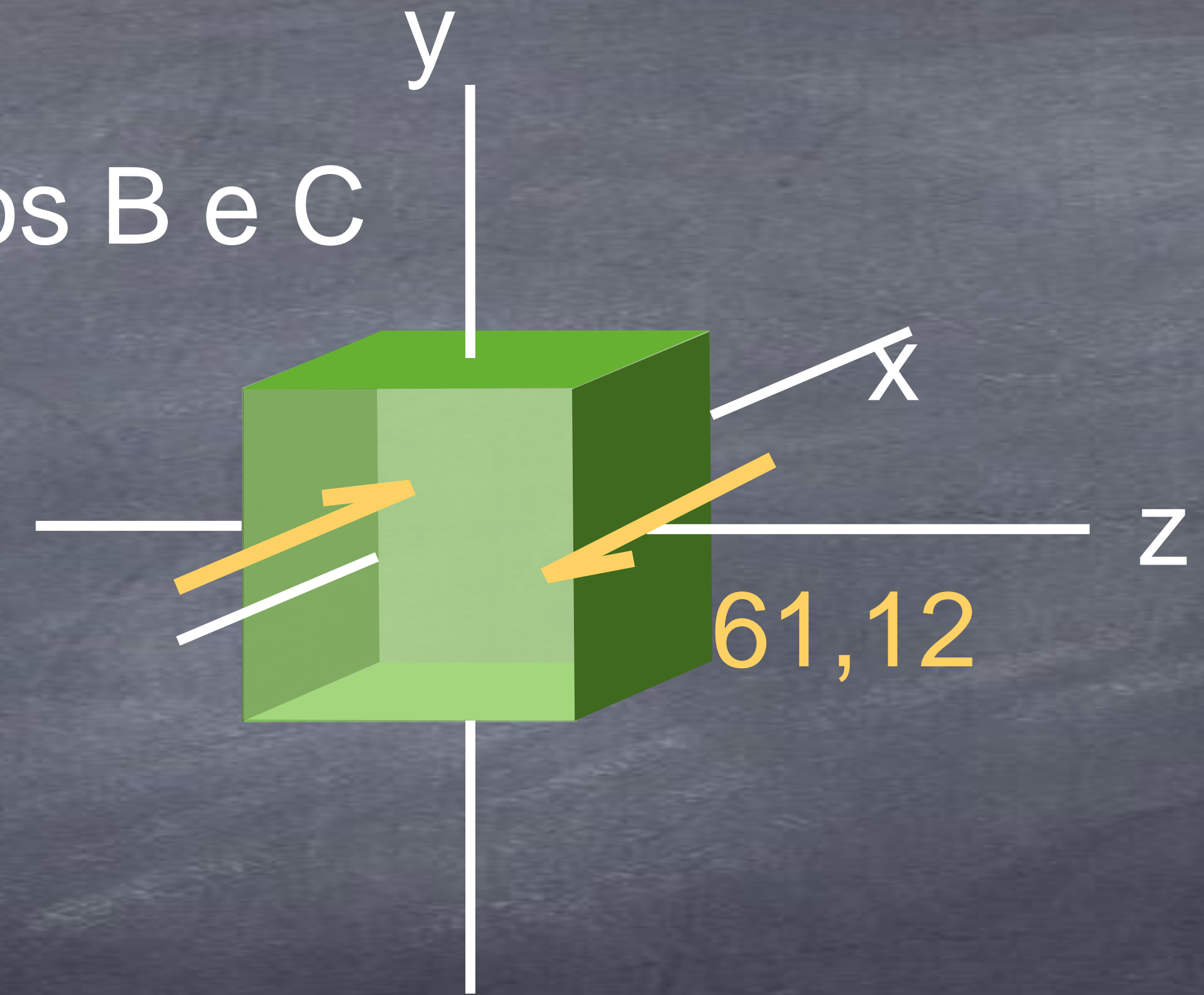
d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$

d.3) $\tau_{\max} = T \cdot r / J$



Pontos B e C



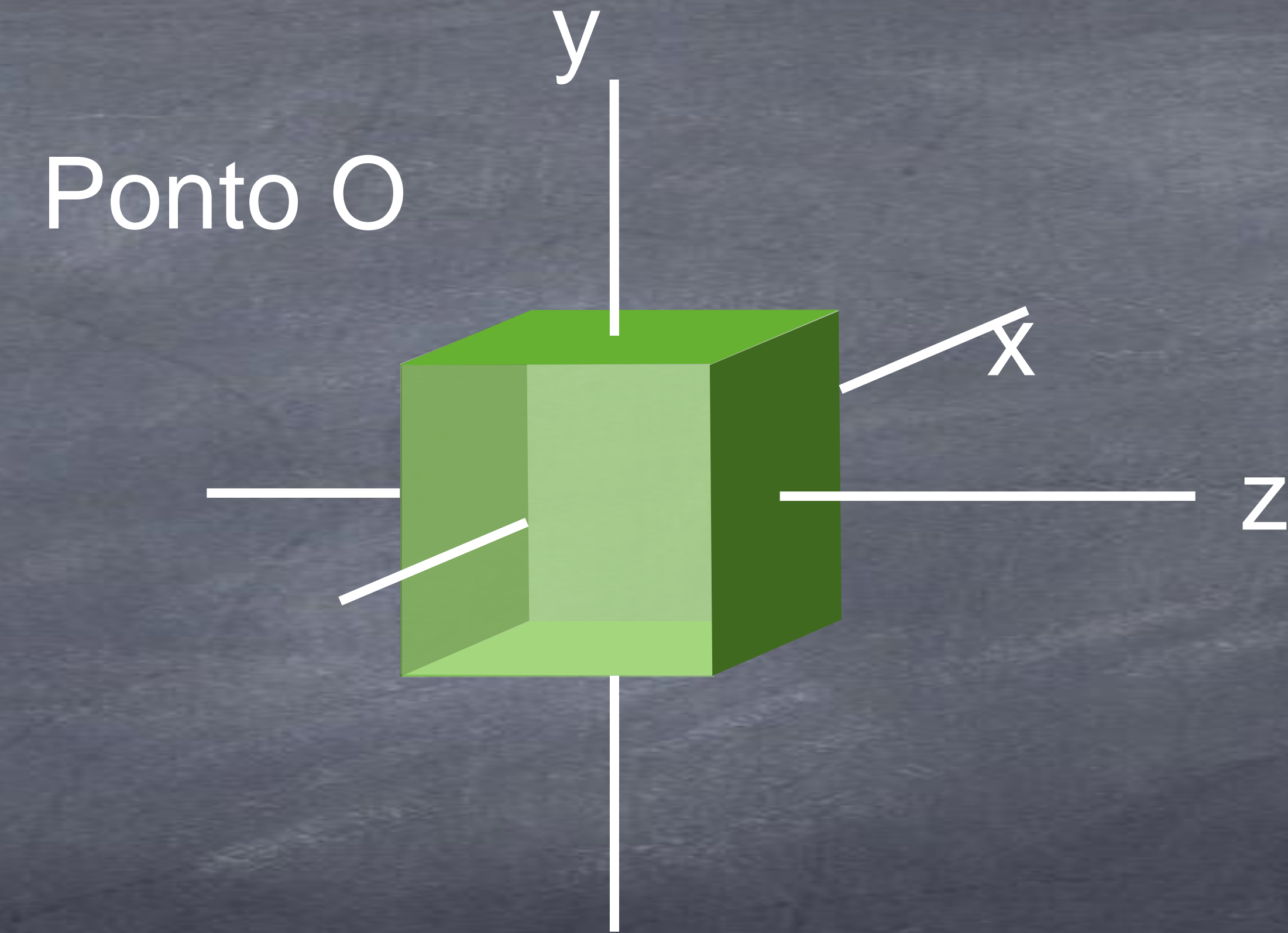
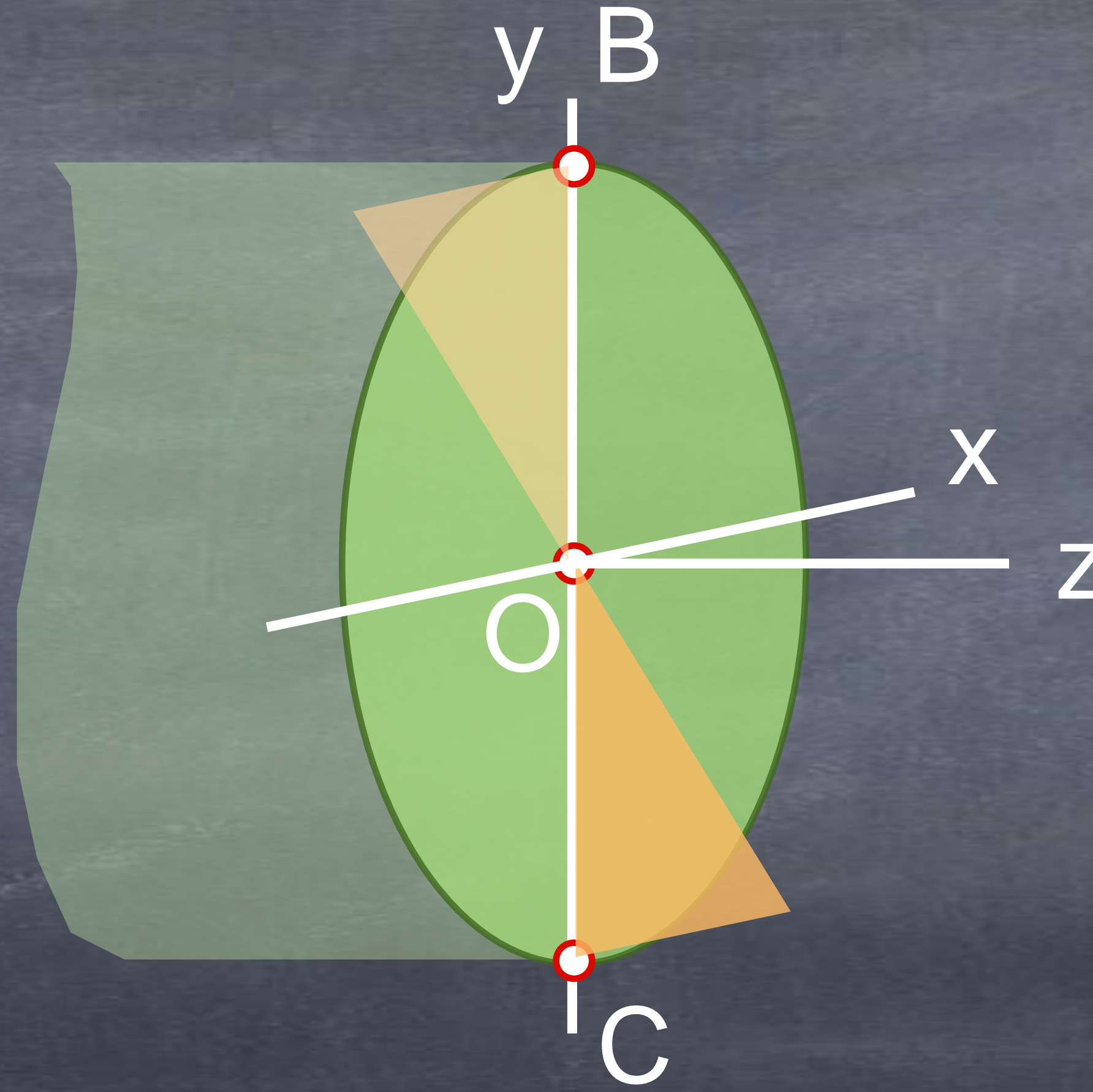
Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$

d.3) $\tau_{\max} = T \cdot r / J$



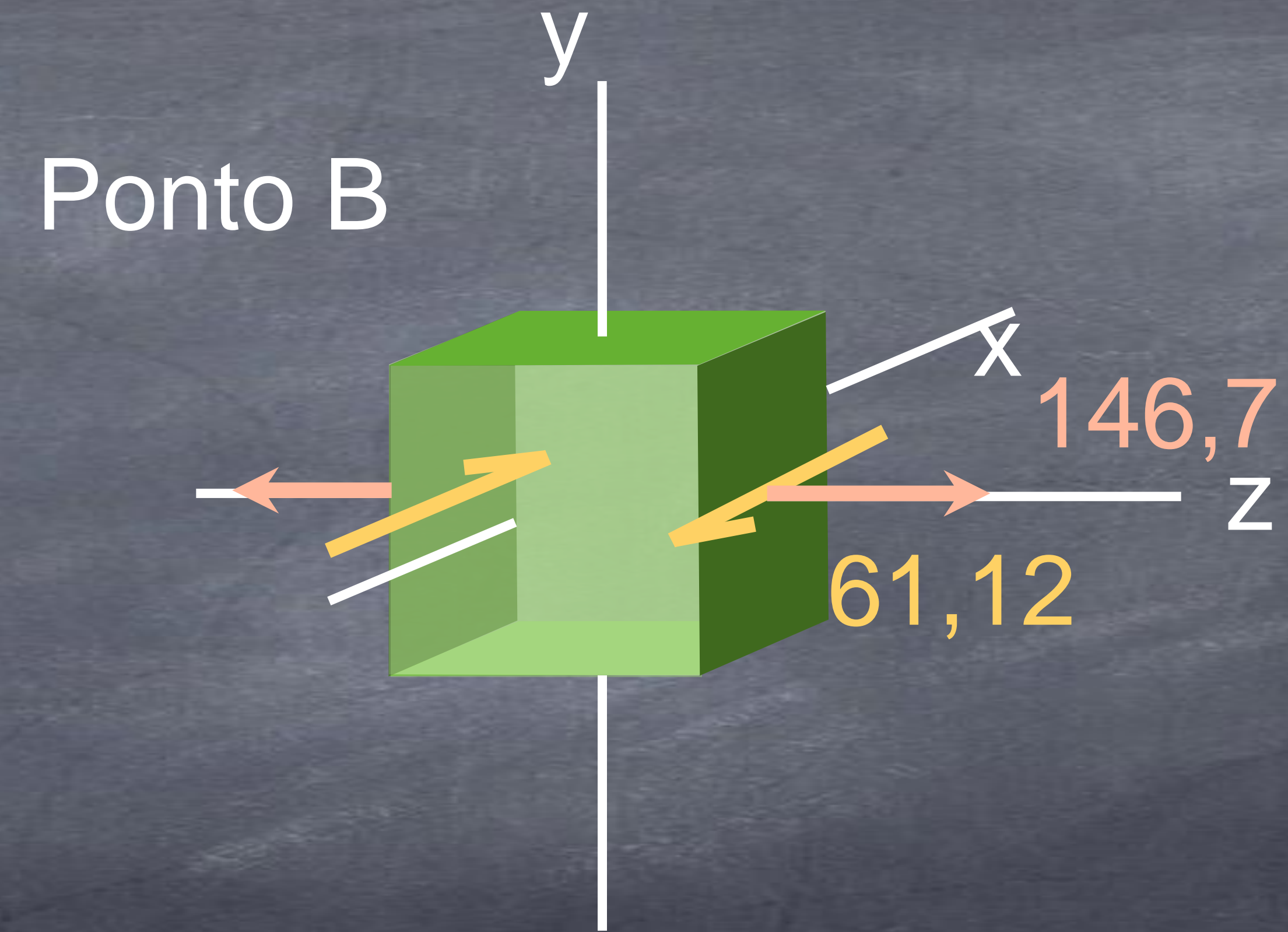
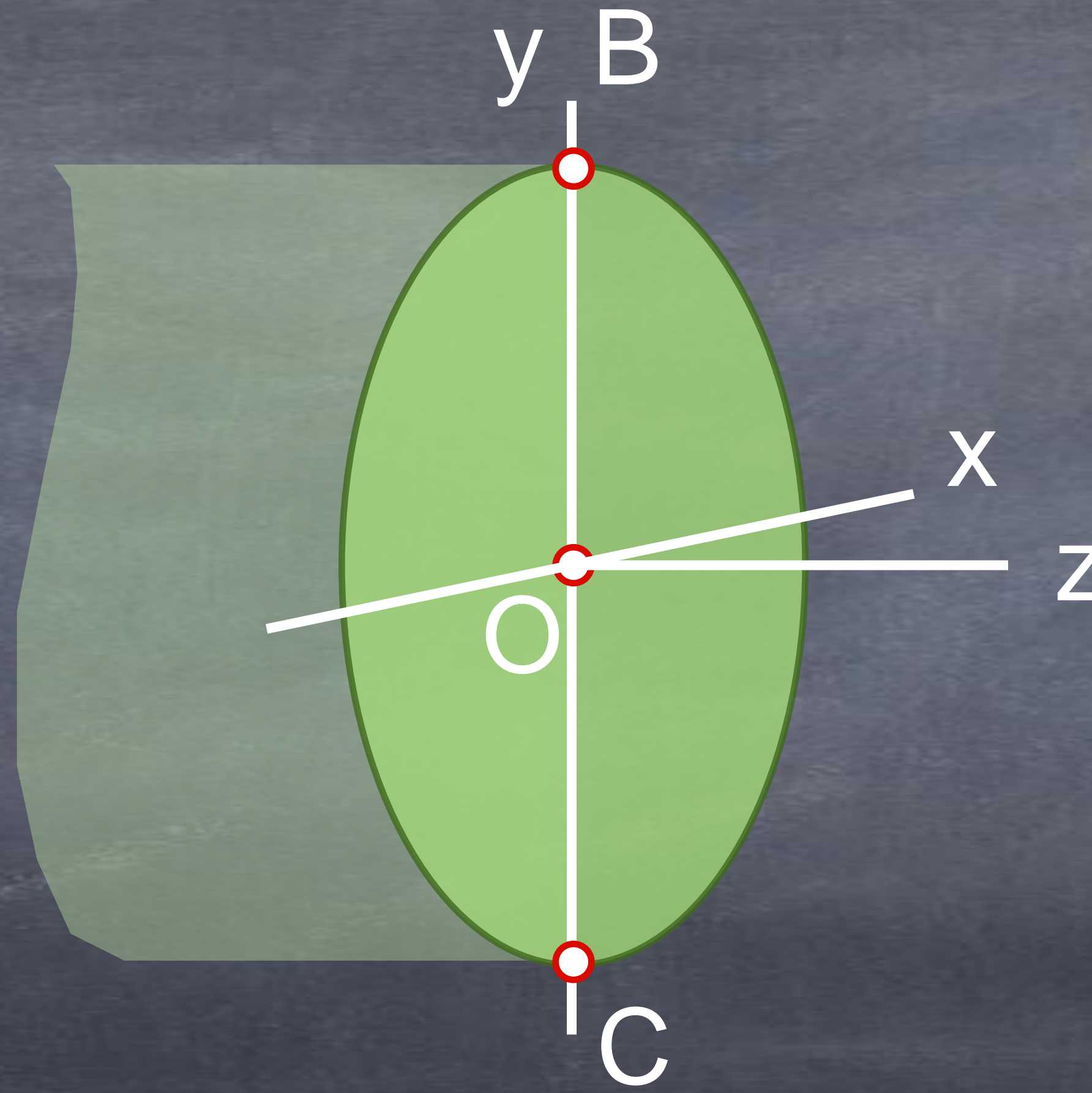
Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$

d.3) $\tau_{\max} = T \cdot r / J$



Outros exemplos

d) Superposição das tensões

d.1) $\tau = V / A$

d.2) $\sigma_{\max} = \pm M_x \cdot r / I_{xx}$

d.3) $\tau_{\max} = T \cdot r / J$

