

a)

| $x_3 x_2$ | $x_1 x_0$ | 00 | 01 | 11 | 10 |
|-----------|-----------|----|----|----|----|
| 00 | 0 | X | 0 | 1 | |
| 01 | 1 | 0 | 0 | 1 | 1 |
| 11 | 1 | 0 | X | 1 | 1 |
| 10 | X | 0 | 1 | X | |

$$S = X_1 X_0 + X_2 X_0'$$

②. $X_3 = 0$ and $X_2 = 1$
 $X_1 = 0$ and $X_0 = 0$

$\left. \begin{array}{l} X_3 = 0 \text{ and } X_2 = 1 \\ X_1 = 0 \text{ and } X_0 = 0 \end{array} \right\} X_2 X_0'$

①. $X_3 = 0$ and $X_2 = 0$ and $X_1 = 1$ and $X_0 = 1$

$\left. \begin{array}{l} X_3 = 0 \text{ and } X_2 = 0 \\ X_1 = 1 \text{ and } X_0 = 1 \end{array} \right\} X_1 X_0$

| | |
|------|------|
| 0000 | - 0 |
| 0001 | - 1 |
| 0010 | - 2 |
| 0011 | - 3 |
| 0100 | - 4 |
| 0101 | - 5 |
| 0110 | - 6 |
| 0111 | - 7 |
| 1000 | - 8 |
| 1001 | - 9 |
| 1010 | - 10 |
| 1011 | - 11 |
| 1100 | - 12 |
| 1101 | - 13 |
| 1110 | - 14 |
| 1111 | - 15 |

$\sum \pi m(0, 2, 5, 9, 13) = \sum m(1, 3, 4, 6, 7, 8, 10, 11, 12, 14, 15)$
 $\sum d(1, 8, 10, 15) = \text{DONT CARE}$

b) $\Sigma d(4, 6, 10)$

$\Sigma \pi M(2, 3, 5, 7, 8, 9, 13) = \Sigma m(0, 1, 4, 6, 10, 11, 12, 14, 15)$

| | | | | | |
|-----------|-----------|----|----|----|----|
| | $x_1 x_0$ | 00 | 01 | 11 | 10 |
| $x_3 x_2$ | 00 | 1 | 1 | | |
| 01 | 1 | | | | |
| 11 | | | 1 | 1 | |
| 10 | | | 1 | | |

① $x_3 = 0$

$x_2 = 0$

$x_1 = 0$

$x_0 = 0 \text{ and } 1$

$x_3' x_2' x_1'$

② $x_3 = 0 \text{ and } 1$

$x_2 = 1$

$x_1 = 1 \text{ and } 0$

$x_0 = 0$

$x_2 x_0'$

③ $x_3 = 1$

$x_2 = 1 \text{ and } 0$

$x_1 = 1$

$x_0 = 1 \text{ and } 0$

$x_3 x_2$

$S = x_3' x_2' x_1' + x_2 x_0' + x_3 x_2$

2. Método Algébrico ↗

a)

$$F = ab'c + abc + a'bc + abc'$$

$$c(ab' + \overbrace{ab}^b + a'b) + abc'$$

$$c(ab' + b) + abc'$$

$$c(ab' + b(b + b')) + abc'$$

$$c(\underline{ab'} + b + \underline{b'}) + abc'$$

$$c(a + b) + abc'$$

$$ca + cb + abc'$$

$$ca + b(c + ac')$$

$$ca + b(c(c + c') + ac')$$

$$ca + b(\underline{cc'} + \underline{ac'})$$

$$ca + b(c + a)$$

$$ca + bc + ba$$

$$F = ca + bc + ba$$

$$1 \{ \overbrace{a'b}^1 + ab = b(a + a') = b$$

$$2 \{ \begin{aligned} ab' + ab' &= ab' \\ ab' + ab' &= ab' \end{aligned}$$

$$3 \{ \begin{aligned} (b + b') &= 1 \\ b \cdot b' &= 0 \end{aligned}$$

$$4 \{ \begin{aligned} c \cdot 1 &= c(\overbrace{c + c'}) \\ &= cc' \end{aligned}$$

$$5 \{ cc' + bc' = c + b$$

$$6 \{ abc + ab'c = c(ab + ab')$$

b) MAPA K

$$F = \begin{matrix} abc & abc & a'bc & abc' \\ 101 & 111 & 011 & 110 \end{matrix}$$

$$F = ca + bc + ba$$

b) MAPA K

$$F = \underset{101}{abc'} + \underset{111}{abc} + \underset{011}{a'bc} + \underset{110}{abc'}$$

| | | | | | |
|---|---|----|----|----|----|
| | | cd | | | |
| | | 00 | 01 | 11 | 10 |
| a | 0 | | | 1 | 1 |
| | 1 | | 1 | 1 | 1 |

$$\textcircled{1} - \left. \begin{array}{l} a = 0 \text{ ou } 1 \\ b = 1 \\ c = 1 \end{array} \right\} bc$$

$$\textcircled{2} - \left. \begin{array}{l} a = 1 \\ b = 0 \text{ ou } 1 \\ c = 1 \end{array} \right\} ac$$

$$\textcircled{3} - \left. \begin{array}{l} a = 1 \\ b = 1 \\ c = 0 \text{ ou } 1 \end{array} \right\} ab$$

$$F = ab + ac + bc$$

Ambas Resultados São Iguais $\begin{matrix} \nearrow a) \\ \searrow b) \end{matrix}$

$$3 \quad a'bc' + abc'd' + abd$$

$$a'bc'(d+d') + abc'd' + abd(c+c')$$

$$\frac{a'bc'd}{0101} + \frac{a'bc'd'}{0100} + \frac{abc'd'}{1100} + \frac{abc'd}{1111} + \frac{abd}{1101}$$

| ab \ cd | | | | |
|---------|----|----|----|----|
| | 00 | 01 | 11 | 10 |
| 00 | 0 | 0 | 0 | 0 |
| 01 | 1 | 1 | 0 | 0 |
| 11 | 1 | 1 | 1 | 0 |
| 10 | 0 | 0 | 0 | 0 |

$$\begin{aligned} \textcircled{1} - a &= 0 \text{ and } 1 \\ b &= 0 \\ c &= 0 \text{ and } 1 \\ d &= 0 \text{ and } 1 \end{aligned} \quad \left. \vphantom{\begin{aligned} a &= 0 \text{ and } 1 \\ b &= 0 \\ c &= 0 \text{ and } 1 \\ d &= 0 \text{ and } 1 \end{aligned}} \right\} b'$$

$$\begin{aligned} \textcircled{2} - a &= 0 \\ b &= 0 \text{ and } 1 \\ c &= 1 \\ d &= 0 \text{ and } 1 \end{aligned} \quad \left. \vphantom{\begin{aligned} a &= 0 \\ b &= 0 \text{ and } 1 \\ c &= 1 \\ d &= 0 \text{ and } 1 \end{aligned}} \right\} A' + C$$

$$\begin{aligned} \textcircled{3} - a &= 0 \text{ and } 1 \\ b &= 0 \text{ and } 1 \\ c &= 1 \\ d &= 0 \end{aligned} \quad \left. \vphantom{\begin{aligned} a &= 0 \text{ and } 1 \\ b &= 0 \text{ and } 1 \\ c &= 1 \\ d &= 0 \end{aligned}} \right\} C + D'$$

$$(F')' = (b' + A'C + C'D)' \rightarrow \text{Invertendo com De Morgan}$$

$$F' = b \cdot (A + C')(C' + D) \rightarrow \text{Produto de soma}$$

$$F' = b(A + C')(C' + D)$$