

## On-Line Learning • Randomized weighted majority algorithm

$\mathcal{A} = \{1, \dots, N\}$ : available actions. At each round  $t \in [T]$ , an on-line algorithm  $\mathcal{A}$  selects a distribution  $\vec{p}_t$  over the set of actions, receives a loss vector  $\vec{\ell}_t$ , whose  $i^{\text{th}}$  component  $\ell_{t,i} \in [0, 1]$  is the loss associated with action  $i$ , and incurs the expected loss  $L_t = \sum_{i=1}^N p_{t,i} \ell_{t,i}$ . The total loss incurred by the algorithm over  $T$  rounds is  $L_T = \sum_{t=1}^T L_t$ . The total loss associated to action  $i$  is  $L_{T,i} = \sum_{t=1}^T \ell_{t,i}$ .

### RANDOMIZED-WEIGHTED-MAJORITY (N)

1. for  $i \leftarrow 1$  to  $N$  do
2.    $w_{1,i} \leftarrow 1$
3.    $p_{1,i} \leftarrow 1/N$ .
4. for  $t \leftarrow 1$  to  $T$  do
5.   RECEIVE( $\vec{\ell}_t$ )
6.   for  $i \leftarrow 1$  to  $N$  do
7.     if  $(\ell_{t,i} = 1)$  then
8.        $w_{t+1,i} \leftarrow \beta w_{t,i}$
9.     else  $w_{t+1,i} \leftarrow w_{t,i}$
10.    $W_{t+1} \leftarrow \sum_{i=1}^N w_{t+1,i}$
11.   for  $i \leftarrow 1$  to  $N$  do
12.      $p_{t+1,i} \leftarrow w_{t+1,i} / W_{t+1}$

⊕  $\ell_{t,i} \in \{0, 1\}$  in our cases

20 5 μήνες Σπάρες ( $N=5$ ) με κωδικό 0 ως 4.

$$C_1 \neq 0 \text{ για τις περιπτώσεις } 184 \bmod 5 = 4, \quad -48 \bmod 5 = 0$$

$$x = 9 - k = 9 - 4 \Rightarrow x = 5, \text{ οπότε } \beta = 0.5$$

Τότε  $w_{1,i} = 1, \forall i = 0, \dots, 4$  και  $P_{1,i} = 0.2, \vec{e}_1 = [1, 0, 0, 0, 1]$

Αρα  $w_{2,i} = \begin{cases} 1, & \text{αν } i = 1, 2, 3 \\ 0.5, & \text{αν } i = 0, 4 \end{cases}, \text{ οπότε } W_2 = 1 + 1 + 1 + 0.5 + 0.5 = 4$

Τότε  $P_{2,i} = \begin{cases} \frac{1}{4}, & \text{αν } i = 1, 2, 3 \\ \frac{1}{8}, & \text{αν } i = 0, 4 \end{cases}$