ACH2033 – Matrizes, Vetores e Geometria Analítica

Lista de Exercícios/Problemas 5

Resolver o sistema linear Ax = b.

$$001) \ A = \begin{pmatrix} 1 & 0 & 1 \\ 1 & 1 & \alpha \\ 1 & 1 & 1 \end{pmatrix}, \ b = \begin{pmatrix} 1 \\ \beta \\ 0 \end{pmatrix} \quad 002) \ A = \begin{pmatrix} 1 & 1 & 1 \\ 2 & \alpha & 0 \\ 4 & 2 & 0 \end{pmatrix}, \ b = \begin{pmatrix} 1 \\ 1 \\ \beta \end{pmatrix} \quad 003) \ A = \begin{pmatrix} 1 & 1 & 1 \\ 2 & \alpha & 0 \\ 4 & 2 & 1 \end{pmatrix}, \ b = \begin{pmatrix} 1 \\ 1 \\ \beta \end{pmatrix}$$

$$004) \ A = \begin{pmatrix} 1 & 1 & 1 \\ 2 & \alpha & \beta \\ 1 & 2 & 0 \end{pmatrix}, \ b = \begin{pmatrix} 1 \\ 1 \\ \gamma \end{pmatrix} \quad 005) \ A = \begin{pmatrix} 1 & \alpha & \beta \\ 2 & 1 & 1 \\ 1 & 2 & 0 \end{pmatrix}, \ b = \begin{pmatrix} 1 \\ \gamma \\ 1 \end{pmatrix} \quad 006) \ A = \begin{pmatrix} 1 & 2 & 3 \\ 2 & 4 & 2 \\ 0 & \alpha & \beta \end{pmatrix}, \ b = \begin{pmatrix} \gamma \\ 0 \\ 1 \end{pmatrix}$$

$$007) \ A = \begin{pmatrix} 1 & 1 & 1 \\ \alpha & 0 & 1 \\ 1 & 1 & \beta \end{pmatrix}, \ b = \begin{pmatrix} \gamma \\ 0 \\ 1 \end{pmatrix} \quad 008) \ A = \begin{pmatrix} \alpha & \beta & \gamma \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{pmatrix}, \ b = \begin{pmatrix} \delta \\ 0 \\ 1 \end{pmatrix} \quad 009) \ A = \begin{pmatrix} \alpha & \beta & \gamma \\ 1 & 1 & 1 \\ 1 & 1 & 0 \end{pmatrix}, \ b = \begin{pmatrix} \delta \\ 0 \\ \epsilon \end{pmatrix}$$

$$010) \ A = \begin{pmatrix} 1 & 1 & 1 & \alpha \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{pmatrix}, \ b = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 1 \end{pmatrix} \ 011) \ A = \begin{pmatrix} 1 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & \alpha \end{pmatrix}, \ b = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 1 \end{pmatrix} \ 012) \ A = \begin{pmatrix} 1 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \\ 0 & \alpha & 0 & 1 \end{pmatrix}, \ b = \begin{pmatrix} 1 \\ 0 \\ 1 \\ \beta \end{pmatrix}$$

Obter a fórmula geral.

013)
$$2a_n = a_{n-1} + 1$$
 com $a_0 = 2$

014)
$$a_n = a_{n-1} + 2a_{n-2} + 3$$
 com $a_0 = a_1 = 1$

015)
$$a_n = 2a_{n-1} - a_{n-2} + 2$$
 com $a_0 = a_1 = 1$

016)
$$a_n = -a_{n-1} + a_{n-2} + 2$$
 com $a_0 = a_1 = 1$

017)
$$a_n = a_{n-1} - a_{n-2} + 7$$
 com $a_0 = a_1 = 1$

018)
$$a_n = a_{n-1} + 2a_{n-2} + 1$$
 com $a_0 = a_1 = 1$

019)
$$a_n = 3a_{n-1} - a_{n-2} - 4$$
 com $a_0 = 0, a_1 = 1$

020)
$$a_n = 2a_{n-1} + 2a_{n-2} - 3$$
 com $a_0 = 1, a_1 = 0$

$$\begin{array}{rcl}
021) \left\{ \begin{array}{rcl}
a_n & = & a_{n-1} + b_{n-1} \\
b_n & = & a_{n-1} + 2b_{n-1}
\end{array} \right. & \text{com} \quad a_0 = \\
\end{array}$$

021)
$$\begin{cases} a_n = a_{n-1} + b_{n-1} \\ b_n = a_{n-1} + 2b_{n-1} \end{cases} \quad \text{com} \quad a_0 = b_0 = 1 \qquad 022) \begin{cases} a_n = b_{n-1} \\ b_n = -a_{n-1} + 3b_{n-1} \end{cases} \quad \text{com} \quad a_0 = b_0 = 2$$

$$\begin{array}{rcl}
023) \left\{ \begin{array}{rcl}
a_n & = & 3a_{n-1} + 5b_{n-1} \\
b_n & = & a_{n-1} + 2b_{n-1}
\end{array} \right.$$