

1.

Solution:

$$U(\text{Win, bet}) = W - B$$

$$U(\text{lose, bet}) = L - B$$

$$\begin{aligned}\text{So } U(\text{bet}) &= P_w * U(\text{win, bet}) + P_l * U(\text{lose, bet}) \\ &= P_w * (W - B) + (1 - P_w) * (L - B)\end{aligned}$$

If  $U(\text{bet}) > 0$  we would like to bet so

$$U(\text{bet}) > 0 \rightarrow P_w * (W - B) + (1 - P_w) * (L - B) > 0$$

$$P_w * W - P_w * B + L - B - P_w * L + P_w * B > 0$$

$$P_w * W + L - B - P_w * L > 0$$

Because  $W > L$

$$\text{So when } P_w > (B - L) / (W - L)$$

It should be accepted to bet

2.

Solution:

For the green wallet, the probability to pull a dime followed by two pennies =  
 $(4/10) \times (6/9) \times (5/8) = 120/720 = 1/6$

For the black wallet, the probability pulled a dime followed by two pennies =  $(2/10)$   
 $\times (8/9) \times (7/8) = 112/720$

**. Which wallet were you more likely to have picked if you pulled a dime followed by two pennies from it?**

For this question:

We assume that the probability to use one of the wallets is same and equal to  $\frac{1}{2}=50\%$ ;

So:

For the green wallet, the  $P=$

$$(0.5*(120/720))/(0.5*(120/720)+0.5*(112/720))=120/(120+112)= 0.517241379$$

For the black wallet, the  $P=$

$$(0.5*(112/720))/(0.5*(120/720)+0.5*(112/720))=112/(120+112)= 0.482758621$$

**.What is the probability that the optimal answer you gave in the previous question was wrong?**

Because we should consider about the past experience, the probability of using the wallet is not equal to  $\frac{1}{2}=0.5$

The  $P_b=1/5$  and the  $P_g=4/5$

So

For the green wallet, the  $P=$

$$(4/5*(120/720))/(4/5*(120/720)+1/5*(112/720))= 0.810810811$$

For the black wallet, the  $P=$

$$(1/5*(112/720))/(4/5*(120/720)+1/5*(112/720))= 0.189189189$$

3.

1).

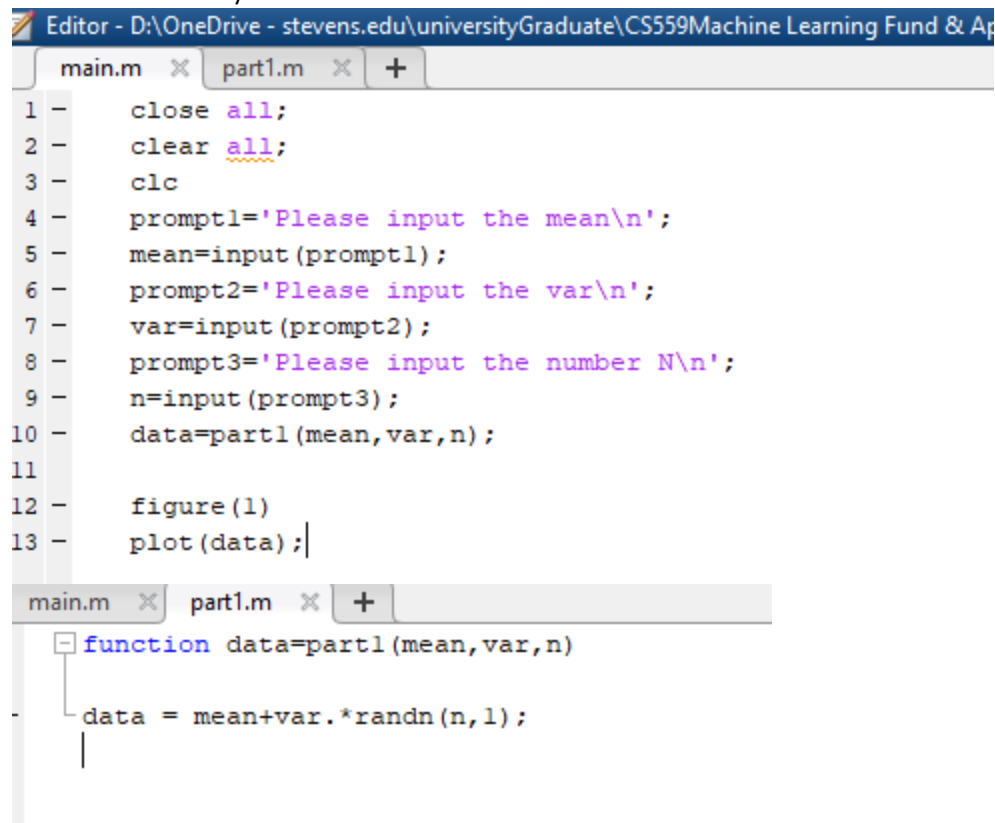
```
function data=part1(mean,var,n)
```

```
data = mean+var.*randn(n,1);
```

```
figure(1)
```

```
plot(data);
```

I also attach my codes below



The screenshot shows the MATLAB Editor interface. The top window is 'main.m' with the following code:

```
1 - close all;
2 - clear all;
3 - clc
4 - prompt1='Please input the mean\n';
5 - mean=input(prompt1);
6 - prompt2='Please input the var\n';
7 - var=input(prompt2);
8 - prompt3='Please input the number N\n';
9 - n=input(prompt3);
10 - data=part1(mean,var,n);
11
12 - figure(1)
13 - plot(data);
```

The bottom window is 'part1.m' with the following code:

```
- function data=part1(mean,var,n)
- data = mean+var.*randn(n,1);
```

2).

We all know the function randn() generates datasets with a normal distribution.

So:

We all know the formula of variance:

$$s^2 = \frac{(x_1 - M)^2 + (x_2 - M)^2 + (x_3 - M)^2 + \dots + (x_n - M)^2}{n} \text{ and var=s}$$

$$\text{Mean3} = (2000 \cdot 1 + 1000 \cdot 4) / (2000 + 1000) = 2$$

$$\text{Var1}^2 = \sum (X1 - 1)^2 / 2000 = 2$$

$$\text{Var2}^2 = \sum (X_2 - 4)^2 / 1000 = 3$$

$$\text{Var3}^2 = \sum (X_3 - \text{mean3})^2 / (n_1 + n_2)$$

**Important:**

$$\text{Var3}^2 = [n_1(\text{var1}^2 + \text{mean1}^2) + n_2(\text{var2}^2 + \text{mean2}^2)] / (n_1 + n_2)$$

$$n_1 * \text{var1}^2 = \sum (X_1 - \text{mean})^2$$

$$n_2 * \text{var}^2 = \sum (X_2 - \text{mean})^2$$

$$\text{Var3}^2 = [n_1 * \text{var1}^2 + n_2 * \text{var}^2 + n_1 * (\text{mean1} - \text{mean3})^2 + n_2 * (\text{mean2} - \text{mean3})^2] / (n_1 + n_2)$$

There's a formula for the combined variance:

$$S_c^2 = \frac{n_1 S_1^2 + n_2 S_2^2 + n_1 (\bar{X}_1 - \bar{X}_c)^2 + n_2 (\bar{X}_2 - \bar{X}_c)^2}{n_1 + n_2}$$

Apparently We can see that:

$$\text{Var3}^2 = (2000 * 4 + 1000 * 9 + 2000 * (1 - 2)^2 + 1000 * (4 - 2)^2) / 3000$$

$$= (8000 + 9000 + 2000 + 4000) / 3000$$

$$= 23/3$$

$$\text{So var3} = \sqrt{23/3} = 2.77$$

I also attach my Codes:

```
close all;
clear all;
clc
data1=part1(1,2,2000);
data2=part1(4,3,1000);
data3=[data1;data2];
figure(1)
histfit(data1,2000);
figure(2)
histfit(data2,1000);
figure(3)
histfit(data3,3000);
```

The following is my plots in matlab:

