

Circuit Theory and Electronics Fundamentals

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T1 Laboratory Report

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1 Introduction

The objective of this laboratory assignment is to study a circuit containing a voltage source V_a , a current source I_d , a voltage dependent current source I_b , a current dependent voltage source V_c and 7 resistors R_n . The circuit can be seen if Figure 1.

In Section 2, a theoretical analysis of the circuit is presented, using both the nodal and mesh methods. In Section 3, the circuit is analysed by means of a ngspice simulation. The results are then compared to the theoretical results obtained in Section 2. The conclusions of this study are outlined in Section 4.

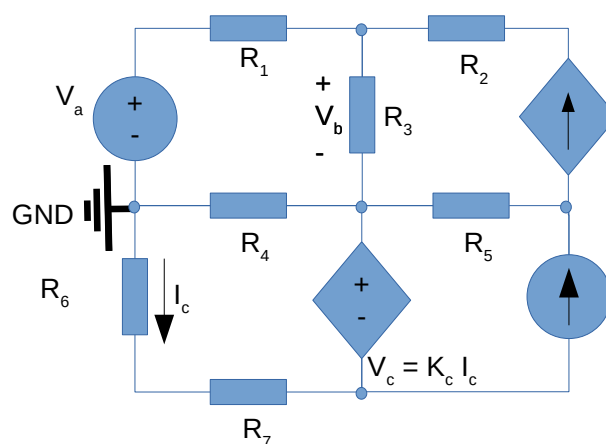


Figure 1: Assigned Circuit.

2 Theoretical Analysis

In this section, the circuit shown in Figure 1 is analysed theoretically, in terms of its time and frequency responses.

2.1 Mesh Analysis

The Figure 2 has both the mesh's currents and the component's admitted direction. This reference is indispensable for the Mesh Analysis. Using KVL in each of the 4 meshes, we achieve the following equations:

Malha A:

$$R_1 * I_A + R_3(I_A + I_B) + R_4(I_A + I_C) = V_A$$

Malha B:

$$I_B = K_c * R_3(I_A + I_B)$$

Malha C:

$$R_4(I_A + I_C) + R_6 * I_C + R_7 * I_C = K_c * I_C$$

Malha D:

$$I_D = I_d$$

After doing some algebra, we can get the following system of equations. After that, we can solve it by enquadrating it in a matrix like shown bellow:

$$\begin{bmatrix} R_1 + R_3 + R_4 & R_3 & R_4 & 0 \\ K_b * R_3 & K_b * R_3 - 1 & 0 & 0 \\ R_4 & 0 & R_6 - K_c + R_7 - R_4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} I_A \\ I_B \\ I_C \\ I_D \end{bmatrix} = \begin{bmatrix} V_a \\ 0 \\ 0 \\ I_d \end{bmatrix}$$

After solving these equations using octave, we get the following results:

	I(mA)
Ia	0.236456
Ib	-0.247520
Ic	0.964663
Id	1.005321

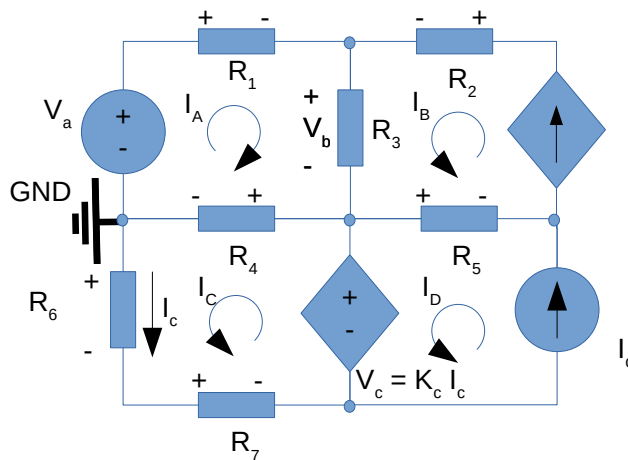


Figure 2: Mesh Analysis

To get the current in each resistor, we use the following equations:

$$I_1 = I_A$$

$$I_2 = I_B$$

$$I_3 = I_A + I_B$$

$$I_4 = I_A + I_C$$

$$I_5 = I_B - I_D$$

$$I_6 = I_C$$

$$I_7 = I_C$$

Leading to the results bellow:

	I(mA)
I1	0.236456
I2	-0.247520
I3	-0.011064
I4	1.201119
I5	-1.252842
I6	0.964663
I7	0.964663

2.2 Nodal Analysis

The Figure 3 has the node references appended. This reference is indispensable for the Nodal Analysis. Using KVL in each of the 4 meshes, we achieve the following equations:

Node 2:

$$(V_1 - V_2)G_1 + (V_3 - V_2)G_2 = (V_2 - V_4)G_3$$

Node 3:

$$(V_3 - V_2)G_2 = K_b(V_2 - V_4)$$

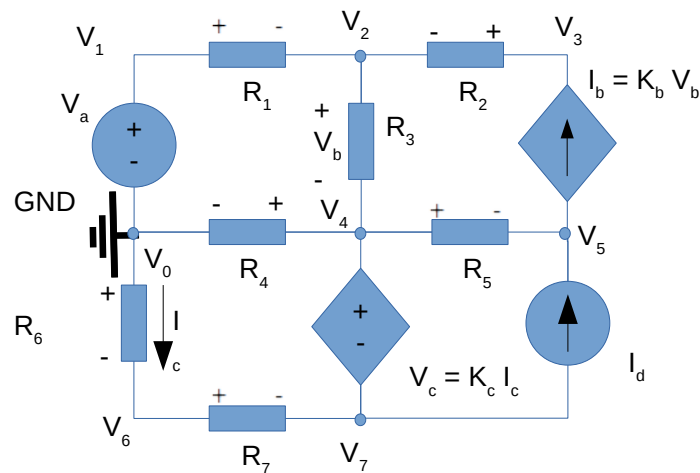


Figure 3: Nodal Analysis

Node 5:

$$(V_4 - V_5)G_5 + I_d = K_b(V_2 - V_4)$$

Node 6:

$$(V_0 - V_6)G_6 = (V_6 - V_7)G_7$$

Additional equation:

$$V_0 = 0$$

$$(V_1 - V_0) = V_a$$

$$V_4 - V_7 = K_c(V_0 - V_6)G_6$$

$$(V_0 - V_6)G_6 - (V_4 - V_0)G_4 + (V_1 - V_2)G_1 = 0$$

Similarly to the last example, the algebraic manipulation brings us to the following system of equations, and the solution can be found by enquadrating it in a matrix like shown below:

$$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & K_c * G_6 & -1 \\ G_1 & -G_1 - G_2 - G_3 & G_2 & G_3 & 0 & 0 & 0 \\ 0 & -K_b & 0 & G_5 + K_b & -G_5 & 0 & 0 \\ 0 & -K_b & 0 & G_5 + K_b & -G_5 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & -G_6 - G_7 & G_7 \\ G_1 & -G_1 & 0 & -G_4 & 0 & -G_6 & 0 \end{bmatrix} \cdot \begin{bmatrix} V_1 \\ V_2 \\ V_3 \\ V_4 \\ V_5 \\ V_6 \\ V_7 \end{bmatrix} = \begin{bmatrix} V_a \\ 0 \\ 0 \\ 0 \\ -I_d \\ 0 \\ 0 \end{bmatrix}$$

After solving these equations using octave, we get the following results:

	V(V)
V1	5.076389
V2	4.828242
V3	4.317617
V4	4.862303
V5	8.665727
V6	-1.946930
V7	-2.953630

2.3 Result Comparison

3 Simulation Analysis

3.1 Operating Point Analysis

Table 1 shows the simulated operating point results for the study case circuit.

4 Conclusion

Even though the theoretical and simulation models might not always give the same results, in our case of study the outcomes were precisely matched. This was in line with what was expected since we were presented with linear components and, to solve the circuit, ngspice utilized the same methods as we did in the theoretical Octave calculation. In conclusion, we believe that the goals of this report were achieved.

Name	Value [A or V]
@gb[i]	-2.47520e-04
@id[current]	1.005321e-03
@r1[i]	2.364560e-04
@r2[i]	-2.47520e-04
@r3[i]	-1.10640e-05
@r4[i]	1.201119e-03
@r5[i]	-1.25284e-03
@r6[i]	9.646630e-04
@r7[i]	9.646630e-04
v(1)	5.076387e+00
v(2)	4.828240e+00
v(3)	4.317615e+00
v(4)	4.862301e+00
v(5)	8.665725e+00
v(6)	-1.94693e+00
v(7)	-2.95363e+00
v(9)	-1.94693e+00

Table 1: Operating point. A variable preceded by @ is of type *current* and expressed in Ampere; other variables are of type *voltage* and expressed in Volt.