

Circuit Theory and Electronics Fundamentals

Lecture 15: The Bipolar Junction Transistor

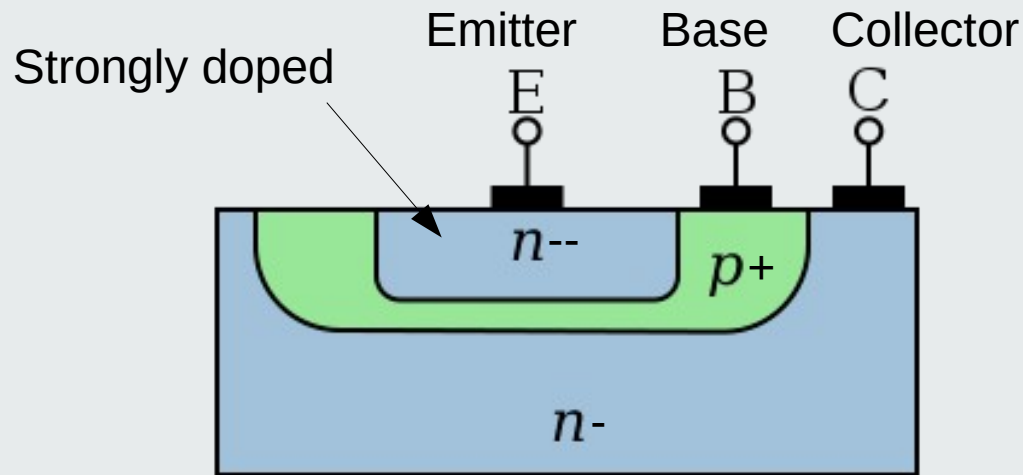
- The transistor
- The Bipolar Junction Transistor (BJT):
 - Operation regions
 - Large signal model (DC)
 - Small signal model (AC)
 - Spice model

The transistor

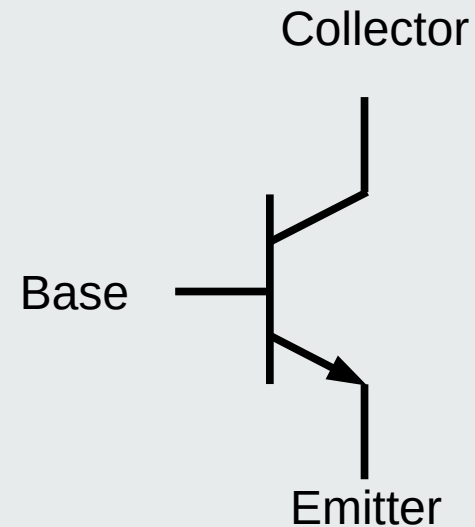
- The transistor is the most widespread semiconductor device
- The transistor is used in both analogue and digital electronic circuits
 - In analogue circuits it is mostly used as a controlled voltage or current amplifier
 - In digital circuits it is used as controlled switch useful for logic operations
- The main transistor types are
 - Bipolar Junction Transistors (BJT)
 - Field effect transistors
- In this lecture we focus on BJTs

The BJT: npn and pnp junctions

- The diode is a *pn junction*
- The transistor is a *npn* or *pnp junction*
- Let's focus on *npn* first



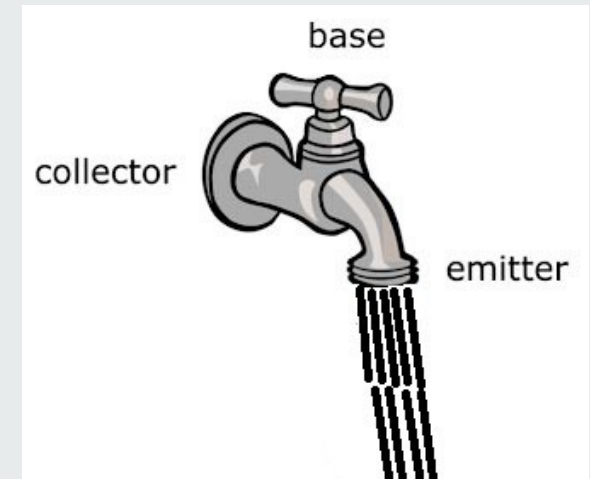
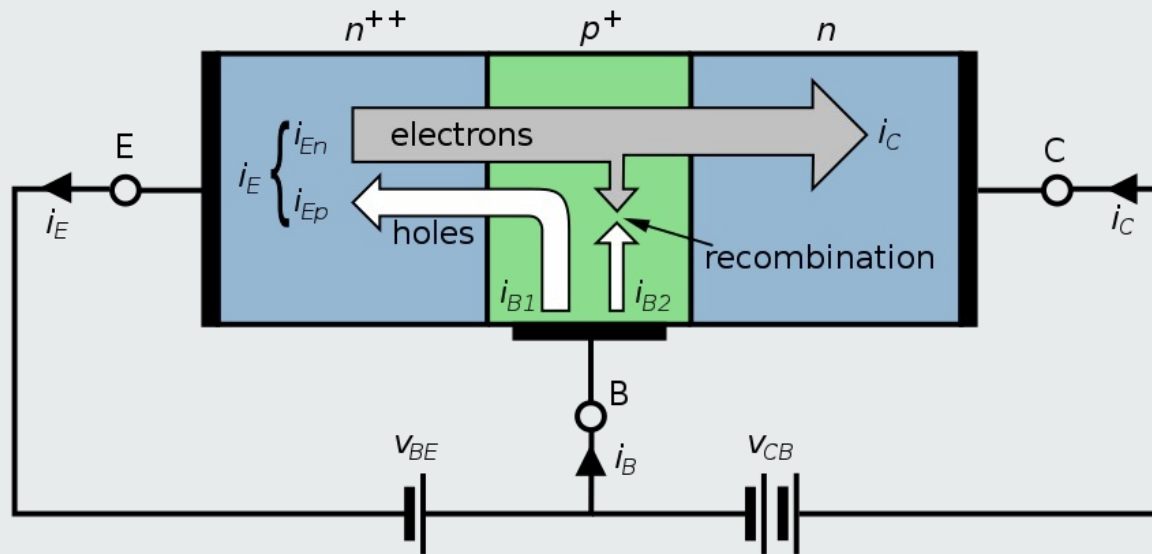
npn junction cross section



npn transistor circuit symbol

How the BJT works

- The npn BJT is not two back to back diodes!
- The the two pn junctions interact with each other!



Base-emitter junction forwardly biased
Bias voltage is V_{BE}

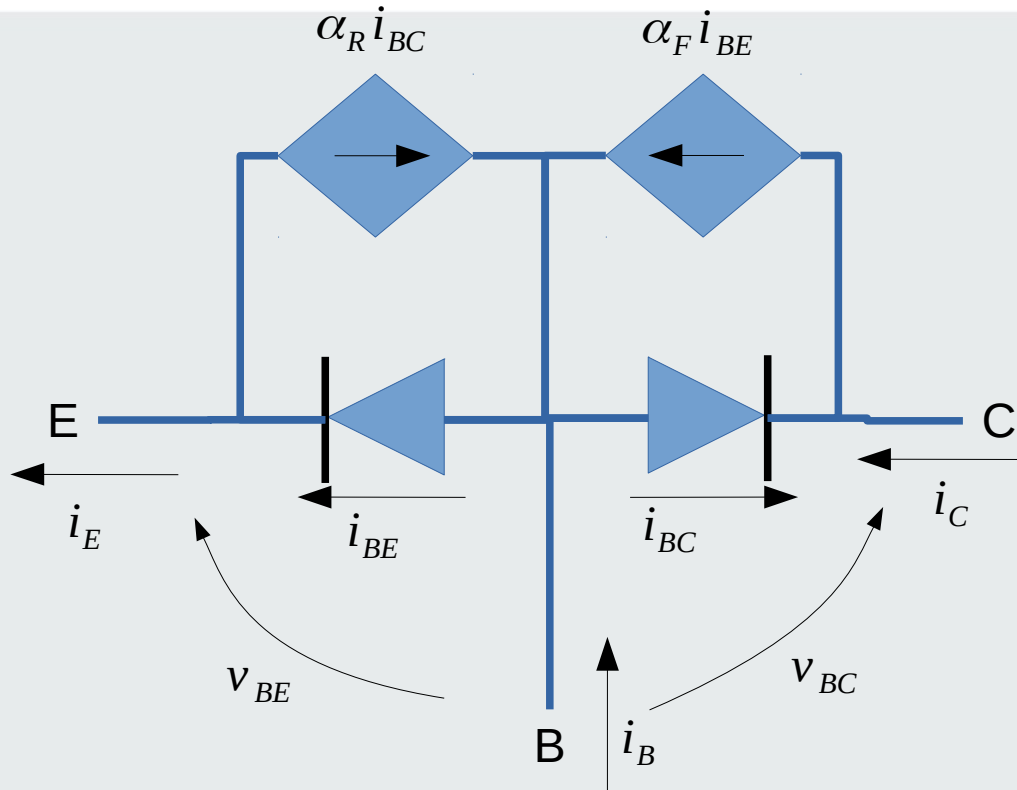
Base-collector junction reversely biased
Bias voltage is V_{CB}

$$I_E = I_B + I_C \text{ (KCL)}$$

The BJT operation regions

- The bipolar is a highly non-linear device with four different operation regions:
 - 1) Forward active region: base-emitter junction forwardly biased and base-collector junction reversely biased. In this region $I_C = \beta_F I_B$
 - 2) Reverse active region: base-emitter junction reversely biased and base-collector junction forwardly biased. In this region $-I_E = \beta_R I_B$
 - 3) Saturation region: both base-emitter and base-collector junctions forwardly biased
 - 4) Cut-off region: both base-emitter and base-collector junctions reversely biased

The Ebers-Moll bipolar npn transistor model



$$i_B = \left[\frac{I_S}{\beta_F} \left(e^{\frac{v_{BE}}{V_T}} - 1 \right) + \frac{I_S}{\beta_R} \left(e^{\frac{v_{BC}}{V_T}} - 1 \right) \right]$$

$$i_C = \left[I_S \left(e^{\frac{v_{BE}}{V_T}} - e^{\frac{v_{BC}}{V_T}} \right) - \frac{I_S}{\beta_R} \left(e^{\frac{v_{BC}}{V_T}} - 1 \right) \right]$$

$$i_E = \left[I_S \left(e^{\frac{v_{BE}}{V_T}} - e^{\frac{v_{BC}}{V_T}} \right) + \frac{I_S}{\beta_F} \left(e^{\frac{v_{BE}}{V_T}} - 1 \right) \right]$$

$$\beta_F = \frac{\alpha_F}{1 - \alpha_F}$$

$$\beta_R = \frac{\alpha_R}{1 - \alpha_R}$$

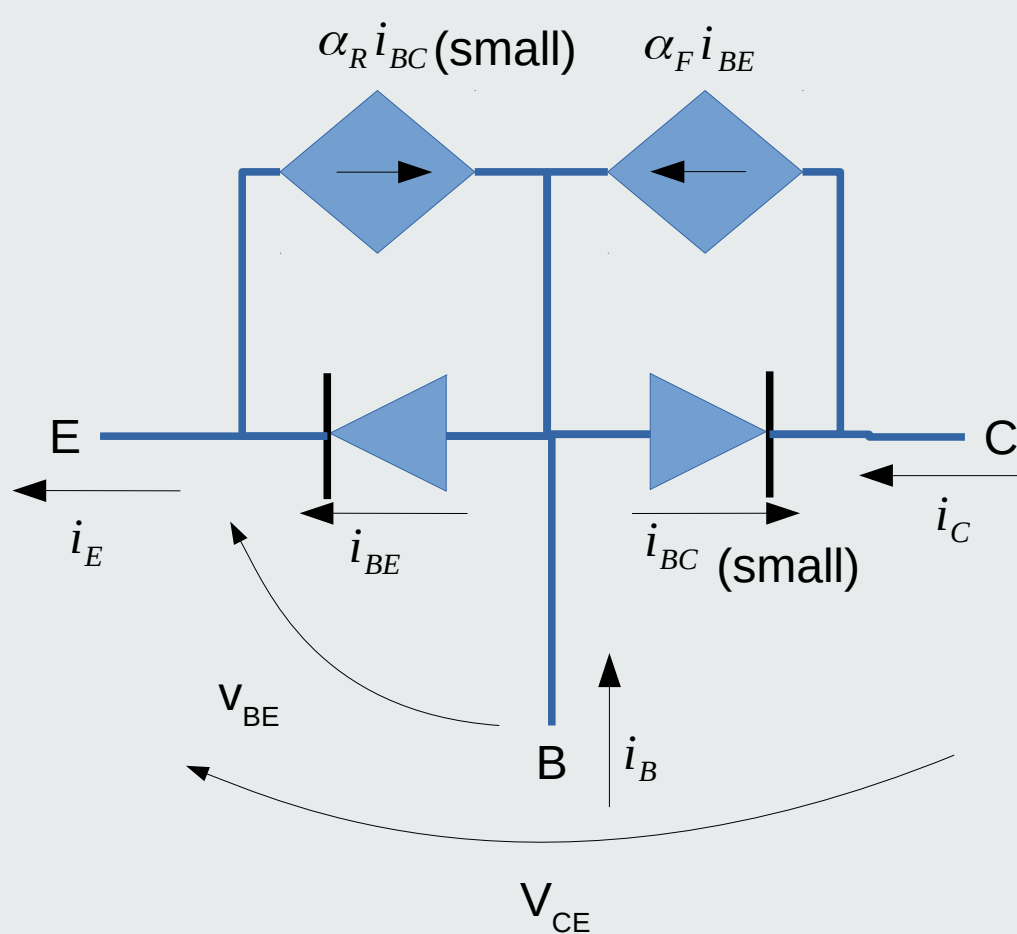
α_F is the forward common base current gain (0.98 to 0.998)

α_R is the reverse common base current gain (0 to 0.952)

β_F is the forward common emitter current gain (20 to 500)

β_R is the reverse common emitter current gain (0 to 20)

Forward active region (Ebers-Moll model)

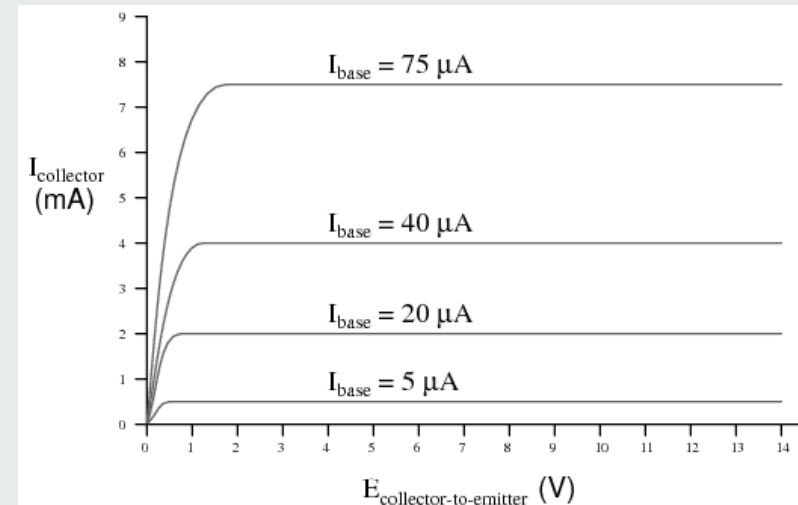


$$i_B = \frac{I_S}{\beta_F} e^{\frac{V_{BE}}{V_T}}$$

$$i_C = I_S e^{\frac{V_{BE}}{V_T}}$$

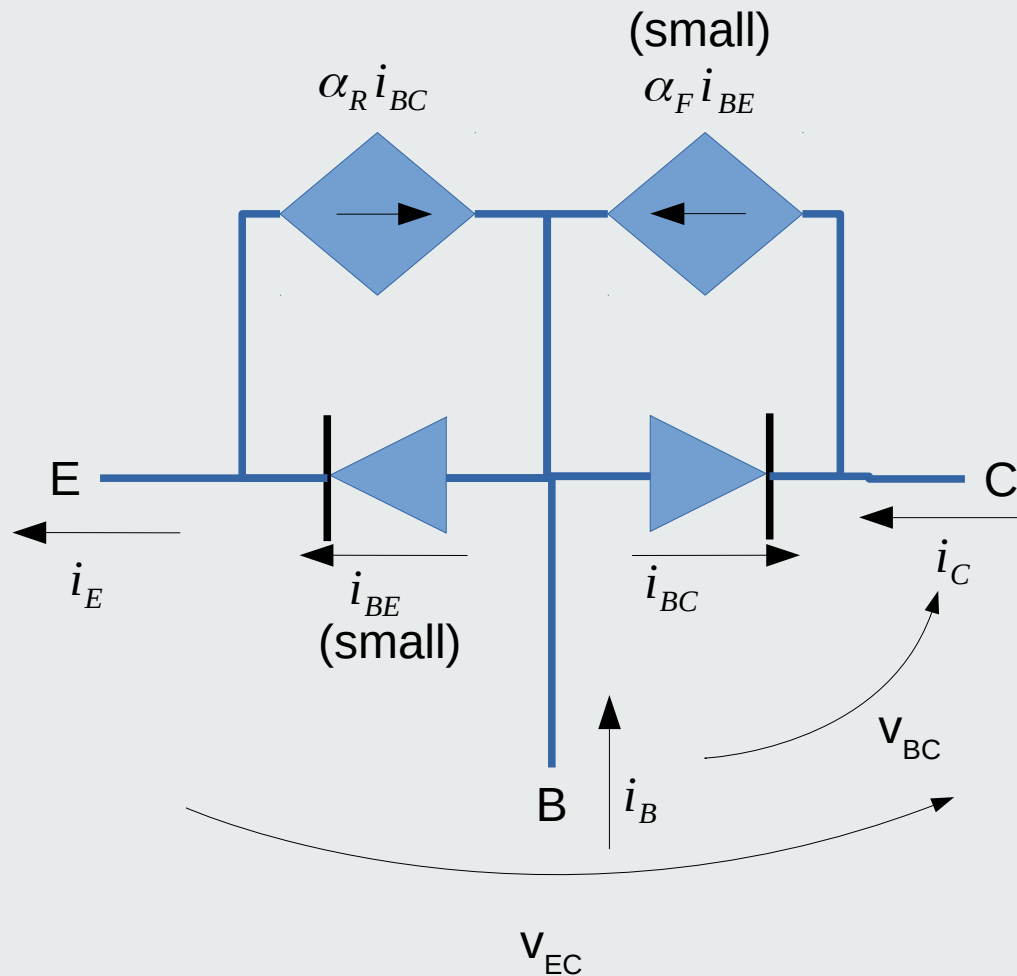
$$i_C = \beta_F i_B$$

Use Ebers-Moll equations
and neglect the reverse
biased terms



Collector-emitter voltage

Reverse active region (Ebers-Moll model)



$$i_B = \frac{I_S}{\beta_R} e^{\frac{V_{BC}}{V_T}}$$

$$-i_E = I_S e^{\frac{V_{BC}}{V_T}}$$

$$-i_E = \beta_R i_B$$

Emitter-collector voltage

Bipolar transistor large signal Ebers-Moll model (DC)

Forward active region

$$i_C = \alpha_F i_E$$

$$i_C = \beta_F i_B$$

$$\text{KCL: } i_E = i_B + i_C = (1 + \beta_F) i_B = \left(1 + \frac{1}{\beta_F}\right) i_C$$

$$\alpha_F = \frac{\beta_F}{1 + \beta_F} \Leftrightarrow \beta_F = \frac{\alpha_F}{1 - \alpha_F}$$

Saturation region

$$i_C < \beta_F i_B$$

Cut-off region

$$i_C = i_B = i_E = 0$$

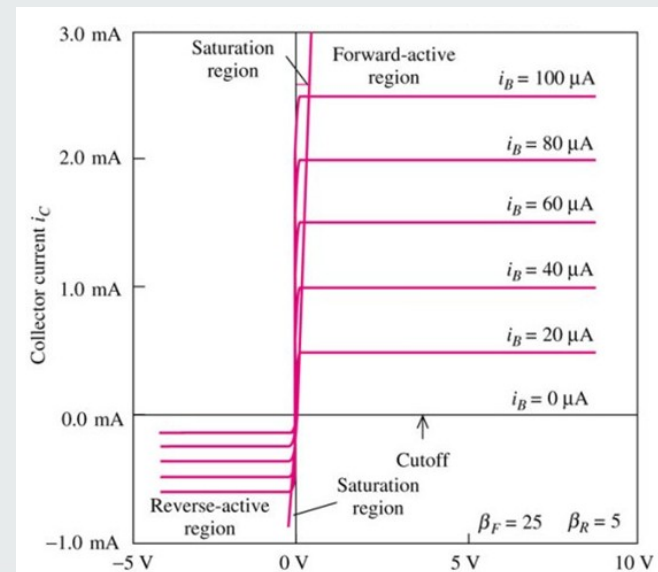
Reverse active region

$$i_E = \alpha_R i_C$$

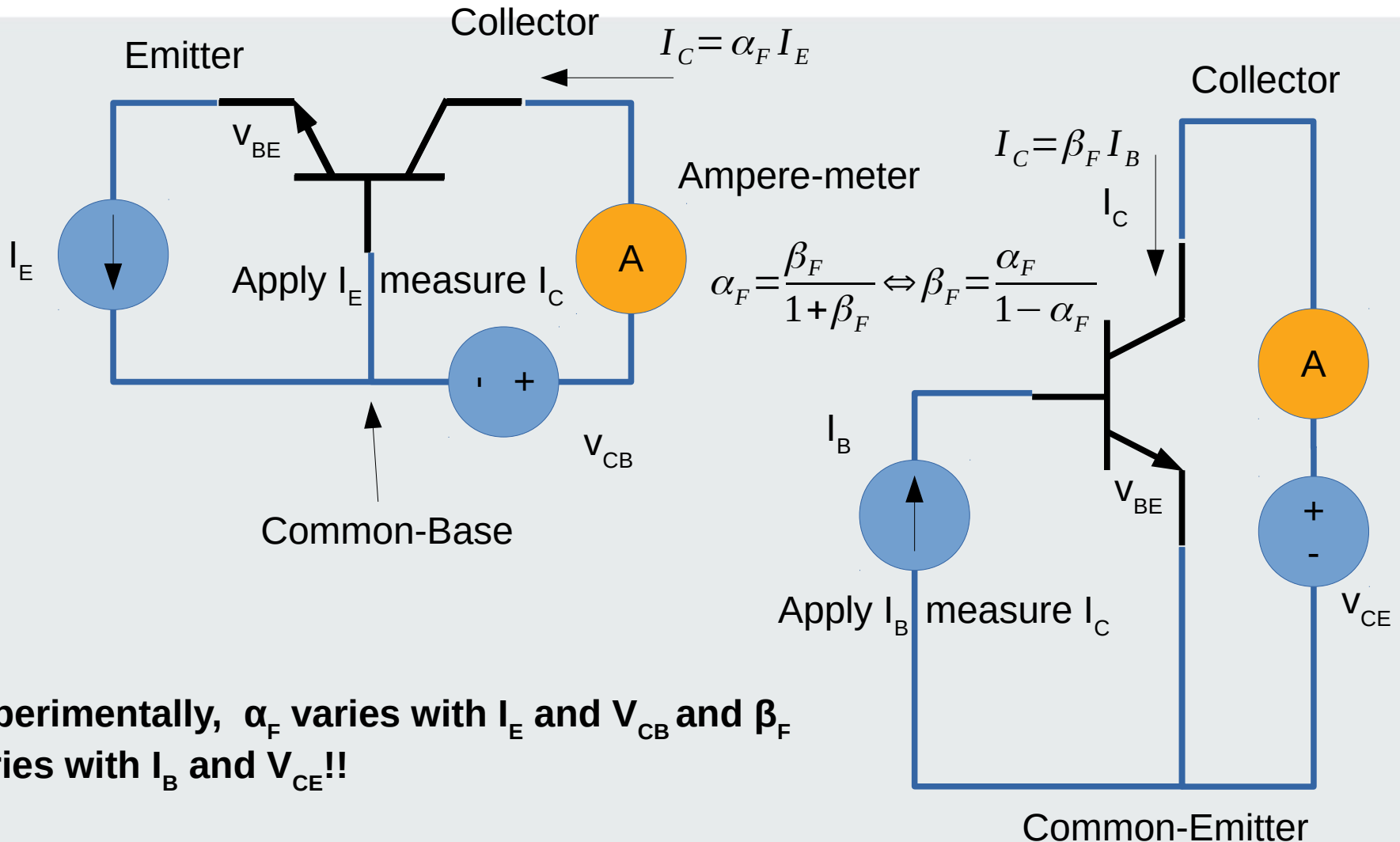
$$-i_E = \beta_R i_B$$

$$\text{KCL: } -i_C = i_B - i_E$$

$$\alpha_R = \frac{\beta_R}{1 + \beta_R} \Leftrightarrow \beta_R = \frac{\alpha_R}{1 - \alpha_R}$$



Experimental setup to measure α_F or β_F



Experimentally, α_F varies with I_E and V_{CB} and β_F varies with I_B and V_{CE} !!

It's called the Early Effect!

The Early Effect: base width modulation

$$i_C = I_s e^{\frac{v_{BE}}{V_T}} \left(1 + \frac{V_{CE}}{V_A} \right)$$

Ebbers-Moll with Early correction

$$i_C' = I_s e^{\frac{v_{BE}}{V_T}}$$

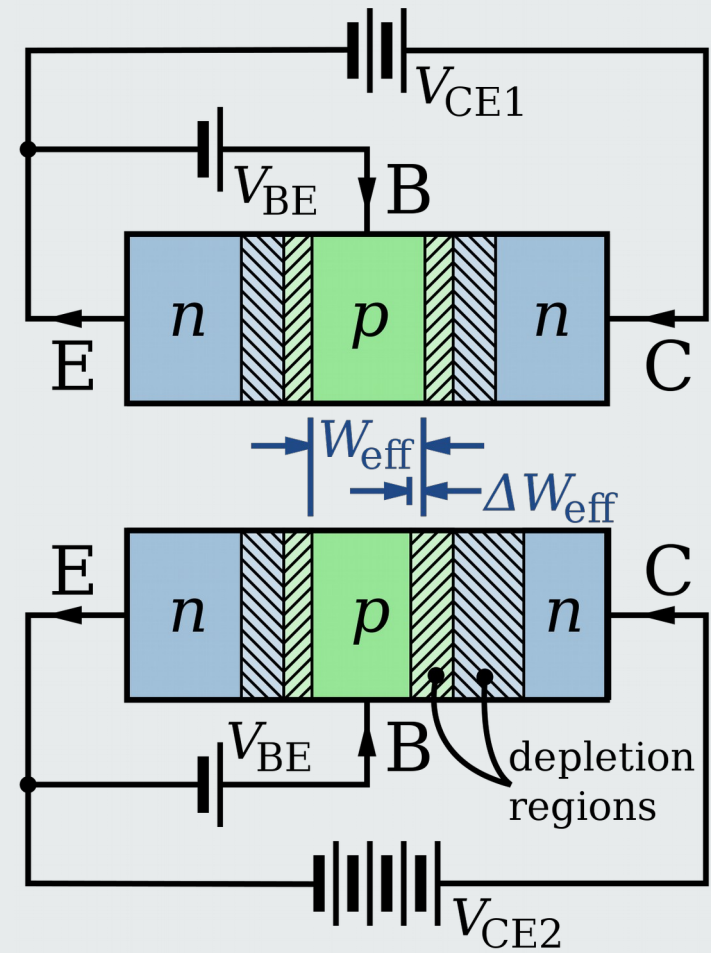
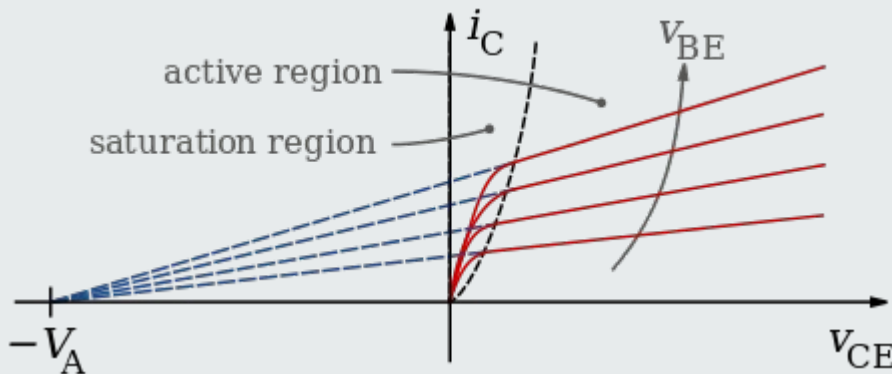
Ebbers-Moll given

$$i_C = i_C' \left(1 + \frac{V_{CE}}{V_A} \right)$$

corrected

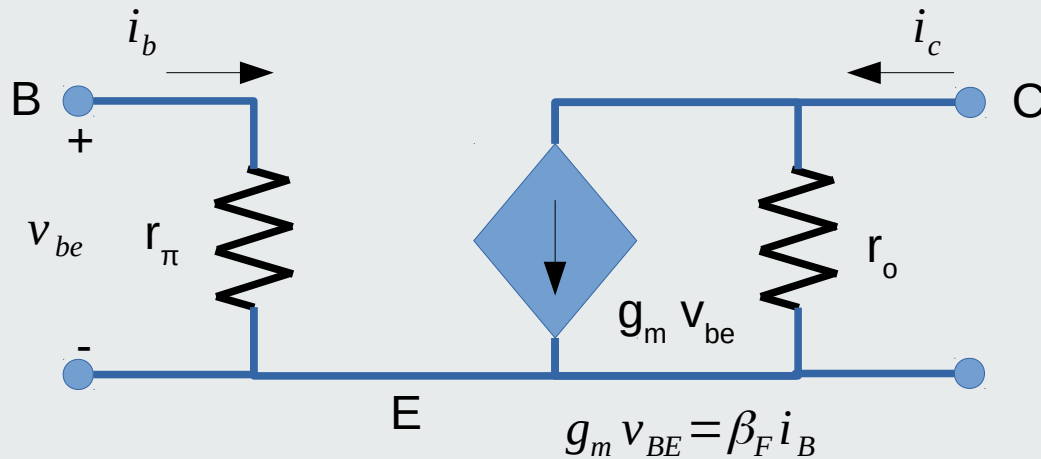
$$\beta_F = \beta_{F0} \left(1 + \frac{V_{CB}}{V_A} \right)$$

corrected



Bipolar transistor small signal model (AC)

Forward active region ONLY



$$g_m = \frac{\partial i_C}{\partial v_{BE}} = \frac{i_C}{V_T} \approx \frac{i_C'}{V_T}$$

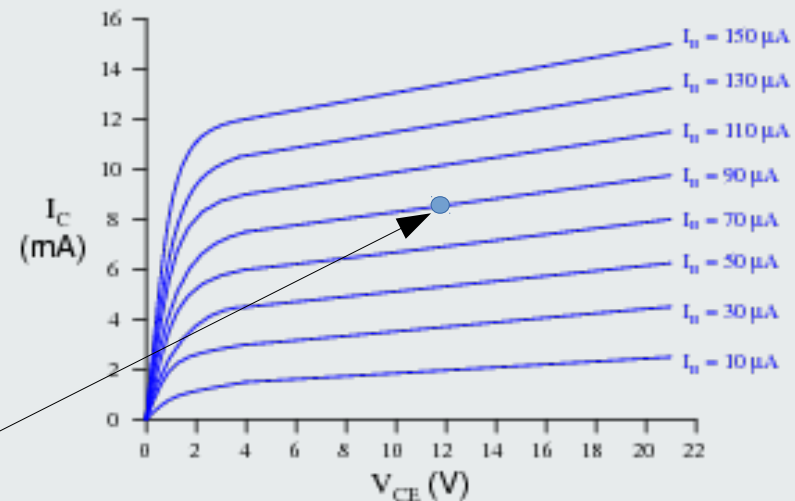
$$r_\pi = \frac{\partial v_{BE}}{\partial i_B} = \frac{\beta_F}{g_m}$$

$$r_o = \frac{\partial v_{CE}}{\partial i_C} = \frac{V_A + V_{CE}}{i_C} \approx \frac{V_A}{i_C'}$$

Incremental parameters

g_m	Transconductance
r_π	Input (incremental) impedance
r_o	Output (incremental) impedance

Computed using operating point



Bipolar pnp transistor DC model

Switch the direction of the currents and use the same equations!

Forward active region

$$i_C = \alpha_F i_E$$

$$i_C = \beta_F i_B$$

$$\beta_F = \beta_{F0} \left(1 + \frac{V_{CB}}{V_A} \right)$$

$$i_E = i_B + i_C = (1 + \beta_F) i_B = \left(1 + \frac{1}{\beta_F} \right) i_C$$

$$\alpha_F = \frac{\beta_F}{1 + \beta_F} \Leftrightarrow \beta_F = \frac{\alpha_F}{1 - \alpha_F}$$

AC model

Saturation region

$$i_C < \beta_F i_B$$

Cut-off region

$$i_C = i_B = i_E = 0$$

$$g_m = \frac{\partial i_C}{\partial v_{BE}} = \frac{i_C}{V_T}$$

$$r_\pi = \frac{\partial v_{BE}}{\partial i_B} = \frac{\beta_F}{g_m}$$

$$r_o = \frac{\partial v_{CE}}{\partial i_C} \approx \frac{V_A}{I_C}$$

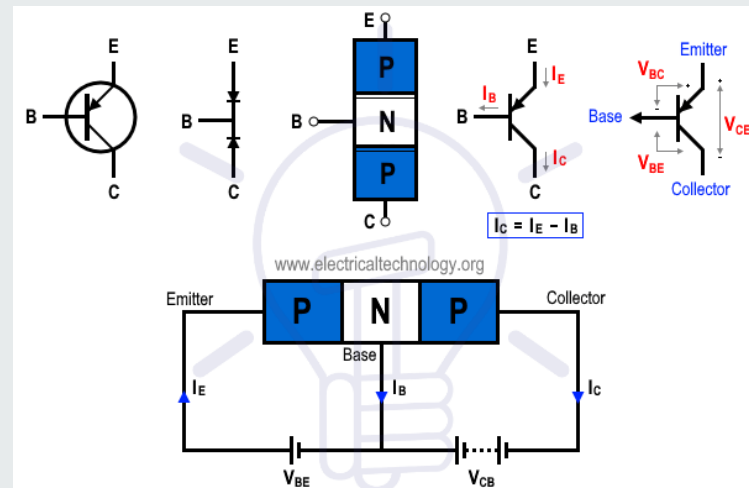
Reverse active region

$$i_E = \alpha_R i_C$$

$$-i_E = \beta_R i_B$$

$$-i_C = i_B - i_E$$

$$\alpha_R = \frac{\beta_R}{1 + \beta_R} \Leftrightarrow \beta_R = \frac{\alpha_R}{1 - \alpha_R}$$



PNP Transistor - Construction & Working

Spice's BJT model

- Ngspice has very sophisticated BJT models
- Let's consider a reduced parameter set one
 - **BF**: Forward active current gain
 - VJE Base-emitter built-in potential
 - **BR**: Reverse active current gain
 - VJC Base-collector built-in potential
 - **IS**: Transport saturation current
 - **VAF** Forward mode Early voltage
 - CJE: Base-emitter zero-bias junction capacitance
 - **VAR** Reverse mode Early voltage
 - NF Forward mode ideality factor
 - NR Reverse mode ideality factor
 - CJC Base-collector zero-bias junction capacitance
- Check out l15.net: simulates $I_C(v_{CE})$ for constant v_{BE} using DC analysis (DC sweep) for a real commercial discrete transistor: the BC547

Conclusion

- The transistor
- The Bipolar Junction Transistor:
- Operation regions
- Large signal model (DC)
- Small signal model (AC)
- Spice model