

Circuit Theory and Electronics Fundamentals

Special Season Exam – July/28/2021. Duration: 3h00m

Only calculator e and scratch paper are allowed. Closed-book exam.

1. Consider the circuit in Figure 1, where $I_s = 6\text{mA}$ and $V_B = 12\text{V}$.

a) Consider the Superposition Theorem for calculating $V_\alpha - V_\gamma$ and I_B . Present the results, symbolically and numerically, in matrix **A** (2x2).

$$\begin{bmatrix} V_\alpha - V_\gamma \\ I_B \end{bmatrix} = A \begin{bmatrix} I_s \\ V_B \end{bmatrix}$$

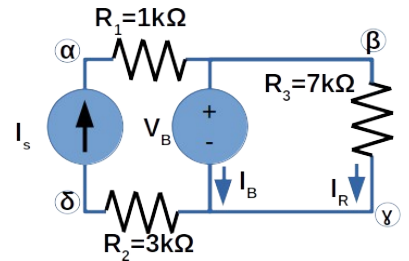


Figure 1

b) Compute the power in sources I_s e V_B , and indicate, justifying, if each source is receiving or supplying energy.

c) Compute the parameters of the Thévenin's and Norton's Equivalents, R_{eq} , V_{eq} and I_{eq} , seen from node β to node α . Consider two terminals connected to these nodes.

2. Consider the circuit in Figure 2, where $I_s = 6\text{mA}$ and $V_K = k(V_\beta - V_\alpha)$, $k = -2\text{ V/V}$

a) Using the Mesh Method, compute, symbolically and numerically, matrix **A** (2x2) and vector **B** (2x1).

$$A \begin{bmatrix} I_1 \\ I_3 \end{bmatrix} = B$$

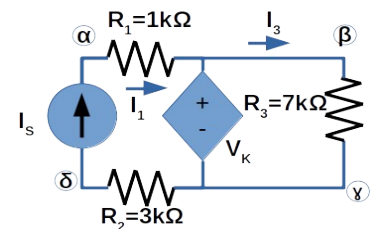


Figure 2

b) Using the Node Method, and assuming that γ is ground, compute, symbolically and numerically, matrix **A** (3x3), and vector **B** (3x1).

$$A \begin{bmatrix} V_\alpha \\ V_\beta \\ V_\delta \end{bmatrix} = B$$

3. Consider the circuit in Figure 3, where $i_s(t) = -20 \cos(\omega t - \pi/4)\text{ mA}$ and $f = 10\text{Hz}$.

a) Determine the forced solution $v_1(t) = v_\beta(t) - v_\alpha(t)$.

b) Compute the active and reactive power associated with the current source.

c) Compute the Transfer Function $T(s) = V_1(s)/I_s(s)$ symbolically, where $V_1(s) = V_\beta(s) - V_\alpha(s)$, and indicate the implemented filter type, justifying your answer.

4. Consider again the circuit in Figure 3, where $i_s(t) = 10 \text{sign}(\sin(\omega t))\text{ mA}$, for

$$f = 10\text{Hz} \text{ and } \text{sign}(x) = \begin{cases} 1, & x \geq 0 \\ -1, & x < 0 \end{cases}$$

a) Assuming the capacitor is discharged at instant $t = 0\text{s}$, plot the voltage $v_2(t) = v_\beta(t) - v_\gamma(t)$ during the first period T , numerically calculating its values at instants 0 , $T/2$ and T .

b) Determine the maximum instantaneous power associated with the energy dissipated by R_2 in the time interval $[0, T]$, and the instant when that happens.

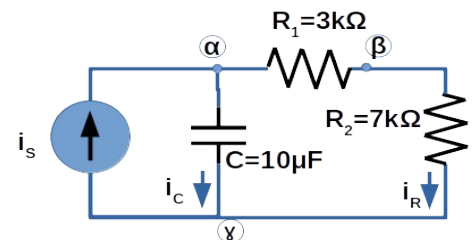
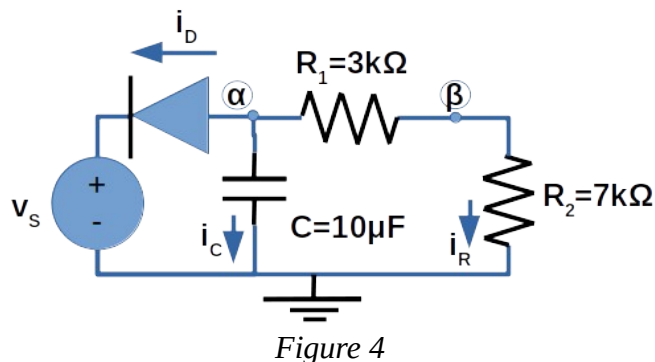


Figure 3

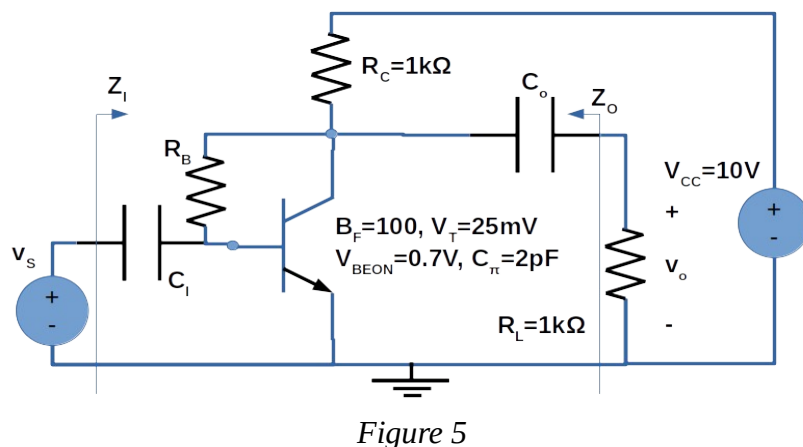
5. Consider the circuit in Figure 4 where the diode is ideal.

- a)** For $v_s(t) = 10 \text{ V}$ and $v_a(0) = 9.5 \text{ V}$, compute $i_D(t)$ for $t \geq 0 \text{ s}$.
- b)** For $v_s(t) = 10 \cos(\omega t) \text{ V}$, $f = 1 \text{ kHz}$, plot $v_s(t)$, $v_B(t)$ and $i_D(t)$ during 2 periods.
- c)** For $v_s(t) = 10 \cos(\omega t) \text{ V}$ and $f = 1 \text{ kHz}$, answer only one of the following two questions: **(i)** Compute the time instants t_{OFF} when the diode goes from being ON to being OFF. **(ii)** Compute V_{ripple} , the voltage ripple peak-to-peak value in node β (difference between the maximum and minimum voltages), using a linear approximation for the capacitor's voltage variation during one period. Assume $t_{\text{OFF}} = 250 \text{ ns}$.



6. Consider the voltage amplifier in Figure 5.

- a)** Compute the value of R_B so that the collector is at 5V at the quiescent operating point. If you have not answered this question assume for the following questions that $R_B=100k\Omega$.
- b)** Draw the amplifier's incremental circuit in the pass-band, and determine the voltage gain and the input and output impedances.
- c)** Determine the circuit's frequency response $V_O(\omega)/V_S(\omega)$, for $C_I=\infty$, $C_O=2\mu F$ and $C_{\pi}=2pF$.



7. Consider the circuit in Figure 6 and assume the OP-AMPs never saturate.

- a)** Determine $v_Z(v_X, v_W)$, $v_Y(v_Z)$ and $v_W(v_Y)$ and, based on the obtained results, establish the differential equation that relates v_X and v_Y .
- b)** Compute $v_Y(t)$ in the sinusoidal steady-state (without the initial transient), for $v_X(t)=2 \cos(\omega t)$, $R=1k\Omega$, $C=1\mu F$ and $f=1kHz$.
Suggestion: establish the algebraic equation that relates \tilde{V}_X and \tilde{V}_Y .
- c)** Determine the Transfer Function $V_Z(s)/V_X(s)$ and indicate, justifying, the implemented filter type.

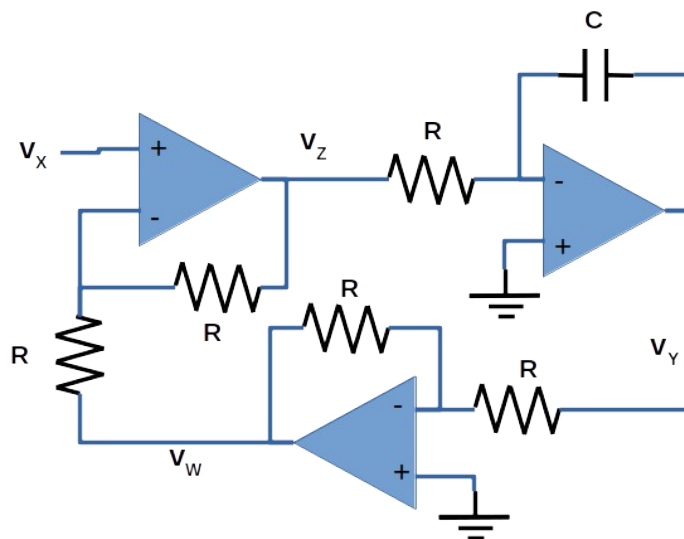


Figure 6

Question grading

[illegible]