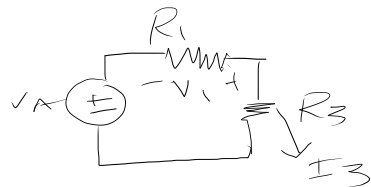


$$V_1 = V_{1A} + V_{1B} \quad \underline{T. \text{ Superposi\c{c}o\~{e}}}$$

$$I_3 = I_{3A} + I_{3B}$$



Contrib. de V_A

$$V_{1A} = -\frac{R_1}{R_1 + R_3} V_A = -\frac{1}{1+3} 25 = -6.25V$$

$$I_{3A} = \frac{V_A}{R_1 + R_3} = \frac{25V}{4k\Omega} = 6.25mA$$



$$V_{1B} = R_1 \parallel R_3 \quad I_B = 7.5V$$

$$= \frac{1000 \times 3000}{4000} = 750\Omega$$

$$I_{3B} = \frac{R_1}{R_1 + R_3} I_B = 2.5mA \parallel$$

$$= \frac{\frac{1}{R_3}}{\frac{1}{R_1} + \frac{1}{R_3}} I_B$$

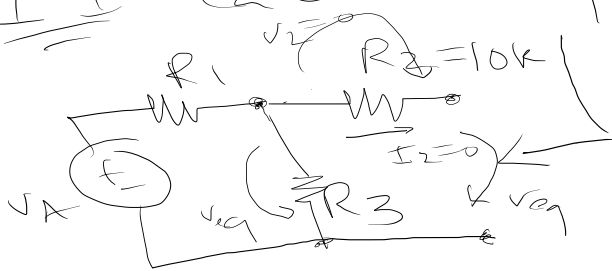
b) V_A recebe energia

Recebe se $V_A I_A > 0$

$$I_A = \frac{V_1}{R} > 0, V_A > 0$$

$\Rightarrow \underline{\underline{SIM}}$

II calcular Equiv. Thivener



R_{eq} ($V_A = 0$)
curto-circuito

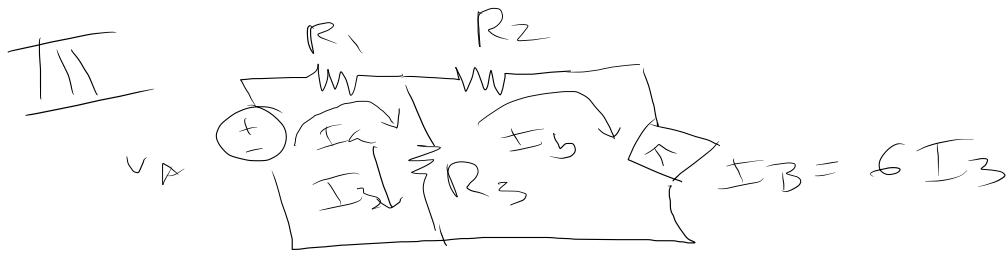
$$R_{eq} = R_2 + R_1 \parallel R_3$$

$$V_{eq} = \frac{R_3}{R_1 + R_3} V_A = \frac{3}{4} V_A$$

$$= 10 + 0.750 = 10.75 \Omega$$

$$= 18.75V //$$

Div. Tensão



Método

das
malhas

sentido
horário

$$-V_A + R_1 I_a + R_3 (I_a - I_b) = 0$$

$$I_B = 6 I_3 = 6 (I_a - I_b) \quad 4 I_a - 3 I_b = V_A$$

$$-I_b = 6 (I_a - I_b)$$

Ω

$$6 I_a - 5 I_b = 0$$

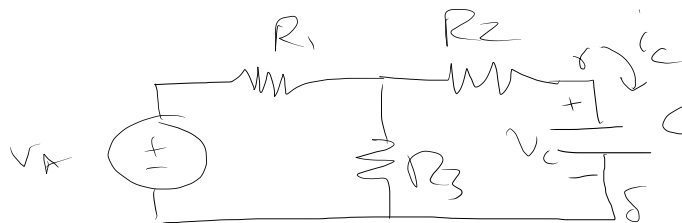
[]

$$-6 I_a + 5 I_b = 0$$

Teste B R3



Fra dual



$$C = 20 \mu F$$

$$v_A(t) = 10 [1 - u(t)] V$$

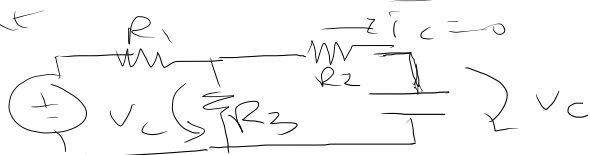
$$t = -5 s$$

Condensador

$$u(t) = \begin{cases} 1, & t \geq 0 \\ 0, & t < 0 \end{cases}$$

$$i_C = C \frac{dv_C}{dt} = 0$$

Circuit to analyze



$$v_C(t < 0) = \frac{R_3}{R_1 + R_3} v_A$$

$$v_A = 10 V$$

$$v_A = \frac{3}{4} v_A = 7.5 V$$

$$a) W_C = \frac{1}{2} C V_C^2 = \frac{1}{2} \times 20 \times 10^{-6} (7.5)^2$$

$$= 562.5 \mu J$$

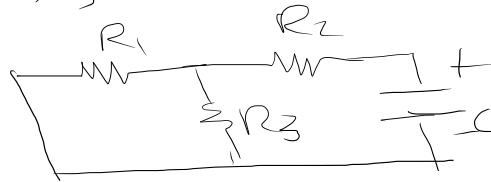
$$b) v_{\delta-\delta} = v_C(t > 0) = k_1 + k_2 e^{-\frac{t}{\tau}}$$

$$\tau = R_{eq} C = 10.75 \times 10^{-3} \times 20 \times 10^{-6} = 215 \text{ ms}$$

$$\frac{1}{\tau} [s^{-1}] \quad \text{rad/s} \quad \omega F = s$$

$$v_A(t) = 10 [1 - u(t)]$$

$$t \geq 0$$



$$v_C(t) = k_1 + k_2 e^{-\frac{t}{\tau}}$$

$$V_c(t) = K_1 + K_2 e^{-\frac{t}{\tau}}$$

$$V_c(t) = V_c(\infty) + [V_c(0) - V_c(\infty)] e^{-\frac{t}{\tau}}$$

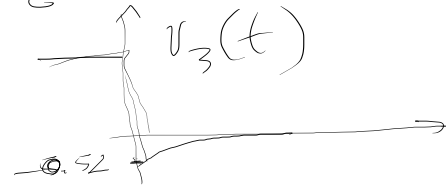
$$V_c(0) = 7.5 \text{ V}$$

$$K_1 = 0$$

$$K_2 = 7.5 \text{ V}$$

$$V_c(\infty) = 0$$

$$\tau = 215 \text{ ms}$$

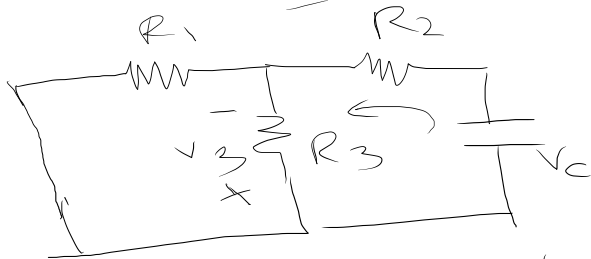


$$c) V_3(t \geq 0)$$

$$V_3(t \geq 0) = V_3(\infty) + [V_3(0) - V_3(\infty)] e^{-\frac{t}{\tau}}$$

$$V_3(0) = \frac{-R_1 \parallel R_3}{R_1 \parallel R_3 + R_2} V_c(0) = \frac{-0.75}{10.75} + 5 = -523.25 \text{ mV}$$

$$V_3(\infty) = 0 \text{ (condensador descarregado)}$$



$$V_3(t < 0) = V_c(t < 0) = 7.5$$

$$v_3(t \geq 0) = v_{31} + v_{32} e^{-t/\tau}$$

$$v_{31} = 0 \quad (v_3(\infty) = 0)$$

$$v_{32} = -523.26 \text{ mV}$$



$$v_A(t) = 40 \cos\left(2\pi \cdot 10^3 t + \frac{\pi}{6}\right)$$

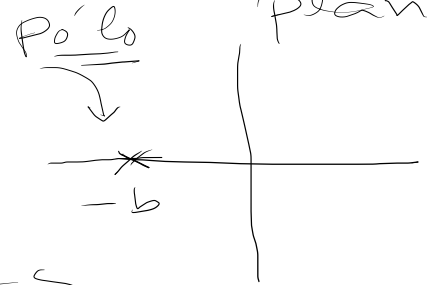
$$a) \quad T(s) = K_0 \frac{1 + \frac{s}{a}}{1 + \frac{s}{b}} = \frac{v_1(s)}{v_A(s)}$$

$K_0 = ?$ Ganho D.C. \Rightarrow C é circuito aberto
 $s = 0$ (freq. nula)

$$\left. \frac{v_1}{v_A} \right|_{s=0} = K_0 = \frac{-R_1}{R_1 + R_3} = -0.25$$

$$T(s) = K_0 \frac{1 + \frac{s}{a}}{1 + \frac{s}{b}}$$

$s_1 = -b$ o denominador anula-se
plano s



$$s_1 = -\frac{1}{R_{eq}C} = -\frac{1}{\tau}$$

Solução eq. características
+ s, t

Solução de forma

de



$$b = \frac{1}{\frac{R_1 R_3}{R_1 + R_3} C}$$

$$b = 66.67 \text{ s}^{-1}$$

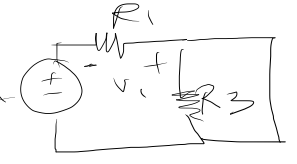
neper/s

s^{-1}

$$T(s) = K_0 \frac{1 + \frac{s}{a}}{1 + \frac{s}{b}}$$

$$v_A = 40 \cos(2\pi \times 10^3 t + \frac{\pi}{6})$$

$s \rightarrow \infty \Rightarrow DC$ e' corto-circuito

$$\left. \frac{v_1}{v_A} \right|_{s=\infty} = K_0 \frac{b}{a} = -1 \quad v_A$$


$v_1 = -v_A$

$$Q = -K_0 b = -0.25 \times 6667 = 16.67 \text{ s}^{-1}$$

$$b) \quad \tilde{v}_A(t) = 40 \cos\left(2\pi \frac{3}{10} t + \frac{\pi}{6}\right)$$

$$\tilde{v}_3(t) = A_3 \cos\left(2\pi \frac{3}{10} t + \phi\right)$$

$$\tilde{v}_A = 40 e^{j\frac{\pi}{6}}$$

$$\tilde{v}_3 = \frac{R_3 \parallel \frac{1}{j\omega C}}{R_3 \parallel \frac{1}{j\omega C} + R_1} \tilde{v}_A$$



$$A_3 = 318.19 \text{ mV}$$

$$\phi^0 = 120.5^\circ$$

DIV. TEN \tilde{v}_A 0

$$\tilde{I}_c = -\frac{\tilde{V}_3}{Z_c} = \tilde{V}_3 j\omega C; \tilde{V}_c = -\tilde{V}_3$$

c) Potência Reativa no C

$$P_{\text{react}} = \text{Im} \left\{ \frac{\tilde{V}_c \tilde{I}_c^*}{2} \right\}$$

potência complexa P_c

d) P_{apparent}

$$= |P_c| = \left| \frac{\tilde{V}_c \tilde{I}_c^*}{2} \right|$$