Constraints on models for the initial collision geometry in ultra relativistic heavy ion collisions

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Monte Carlo simulations are used to compute the centrality dependence of the collision zone eccentricities $(\varepsilon_{2,4})$, for both spherical and deformed ground state nuclei, for different model scenarios. Sizable model dependent differences are observed. They indicate that measurements of the 2nd and 4^{th} order Fourier flow coefficients $v_{2,4}$, expressed as the ratio $\frac{v_4}{(v_2)^2}$, can provide robust constraints for distinguishing between different theoretical models for the initial-state eccentricity. Such constraints could remove one of the largest impediments to a more precise determination of the specific viscosity from precision $v_{2,4}$ measurements at the Relativistic Heavy Ion Collider (RHIC).

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the plane transverse to the beam direction [7, 8]. At midrapidity, the magnitude of this momentum anisotropy is characterized by the even order Fourier coefficients;

$$v_{\rm n} = \left\langle e^{in(\phi_P - \Phi_{RP})} \right\rangle, \ n = 2, 4, ..,$$
 (1)

where ϕ_p is the azimuthal angle of an emitted particle, Φ_{RP} is the azimuth of the reaction plane and the brackets 16 denote averaging over particles and events. The elliptic 17 flow coefficient v_2 is observed to dominate over the higher order coefficients in Au+Au collisions at RHIC (i.e. $v_n \propto$ $(v_2)^{\frac{n}{2}}$ and $v_2 \ll 1$ [9, 10].

The magnitudes and trends of $v_{2,4}$ are known to be 21 sensitive to the transport properties of the expanding 22 partonic matter [3, 4, 6, 11–17]. Consequently, there is 23 considerable current interest in their use for quantitative ²⁴ extraction of the specific shear viscosity, i.e. the ratio of shear viscosity η to entropy density s of the plasma. 26 Such extractions are currently being pursued via com-₂₇ parisons to viscous relativistic hydrodynamic simulations ₂₈ [16–18], transport model calculations [14, 15] and hybrid approaches which involve the parametrization of scaling violations to ideal hydrodynamic behavior [10, 12, 13]. 31 In all cases, accurate knowledge of the initial eccentricity $_{32}$ $\varepsilon_{2,4}$ of the collision zone, is a crucial unresolved prerequisite for quantitative extraction of $\frac{\eta}{s}$.

To date, no direct experimental measurements of $\varepsilon_{2,4}$ 35 have been reported. Thus, the necessary theoretical esti-

Energetic collisions between heavy ions at the Rela- 36 mates have been obtained by way of the overlap geometry tivistic Heavy Ion Collider (RHIC), produce a strongly 37 corresponding to the impact parameter b of the collision, interacting quark gluon plasma (QGP). In non-central $_{38}$ or the number of participants $N_{\rm part}$ in the collision zone. collisions, the hydrodynamic-like expansion of this $_{39}$ A robust constraint for $N_{\rm part}$ values can be obtained via plasma [1-6] results in the anisotropic flow of particles in 40 measurements of the final hadron multiplicity or trans-41 verse energy. However, for a given value of $N_{\rm part}$, the 42 theoretical models used to estimate ε_2 give results which 43 differ by as much as $\sim 25\%$ [19, 20] – a difference which 44 leads to an approximate factor of two uncertainty in the 45 extracted η/s value [16]. Therefore, an experimental con-46 straint which facilitates a clear choice between the differ-47 ent theoretical models is essential for further progress 48 toward precise extraction of η/s .

> In ideal fluid dynamics, anisotropic flow is directly pro-50 portional to the initial eccentricity of the collision zone. ₅₁ A constant ratio for the flow coefficients $\frac{v_4}{(v_2)^2} \approx 0.5$ is also 52 predicted [21]. It is well established that initial eccen-53 tricity fluctuations also influence the magnitude of $v_{2,4}$ 54 significantly [5, 10, 21–23], i.e. the presence of these fluc-55 tuations serve to increase the value of $v_{2,4}$. Therefore, 56 one avenue to search for new experimental constraints, ₅₇ is to use $\varepsilon_{2,4}$ as a proxy for $v_{2,4}$ and study the model 58 dependencies of their magnitudes and trends vs. $N_{\rm part}$.

> In this communication we present calculated results of $\varepsilon_{2,4}$ for collisions of near-spherical and deformed isotopes, 61 for the Glauber [22, 24] and the factorized Kharzeev-62 Levin-Nardi (fKLN) [25, 26] models, i.e. the two primary 63 models currently employed for eccentricity estimates. We 64 find sizable differences, both in magnitude and trend, for 65 the the ratios $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ obtained from both models. This sug-66 gests that systematic comparisons of the measurements ₁ for the N_{part} dependence of the ratio $\frac{v_4}{(v_2)^2}$ for these iso-

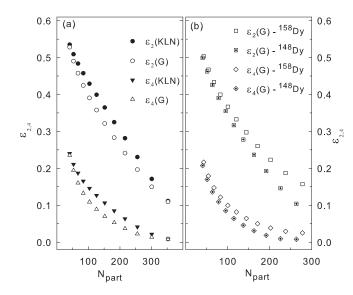


FIG. 1. Calculated values of $\varepsilon_{2,4}$ vs. $N_{\rm part}$ for MC-Glauber (open symbols) and MC-KLN (closed symbols) for Au+Au collisions (a) and near-spherical ¹⁴⁸Dy and deformed ¹⁵⁸Dy as indicated in (b).

2 topic systems, can give direct experimental constraints 3 for these models.

Monte Carlo (MC) simulations were used to calculate event averaged eccentricities (denoted here as $\varepsilon_{2.4}$) within the framework of the Glauber (MC-Glauber) and fKLN (MC-KLN) models, for near-spherical and deformed nuclei which belong to an isobaric or isotopic series. Here, the essential point is that, for such series, a broad range of ground state deformations have been observed for relatively small changes in the the number of protons or neutrons [27, 28]. For each event, the spatial distribution of nucleons in the colliding nuclei were generated according to the deformed Woods-Saxon function:

$$\rho(\mathbf{r}) = \frac{\rho_0}{1 + e^{(\mathbf{r} - R_0(1 + \beta_2 Y_{20}(\theta) + \beta_4 Y_{40}(\theta)))/d}},$$
 (2)

4 where R_0 and d are the radius and diffuseness parameters $_{5}$ and $\beta_{2,4}$ are the deformation parameters which charac-6 terizes the density distribution of the nucleus about its z polarization axis (z').

To generate collisions for a given centrality selection, 10 the orientation of the polarization axis for each nucleus $\theta_1, \phi_1 \text{ and } \theta_2, \phi_2 \text{ respectively}$ was randomly chosen in $_{12}$ the coordinate frame whose z axis is the beam direc-13 tion. For each collision, the values for $N_{\rm part}$ and the 60 16 then evaluated from the two-dimensional profile of the 17 density of sources in the transverse plane $\rho_s(\mathbf{r}_{\perp})$, using 18 modified versions of MC-Glauber [24] and MC-KLN [26]

For each event, we compute an event shape vector S_n

22 harmonic of the shape profile [29];

$$S_{nx} \equiv S_n \cos(n\Psi_n^*) = \int d\mathbf{r}_{\perp} \rho_s(\mathbf{r}_{\perp}) \omega(\mathbf{r}_{\perp}) \cos(n\phi), (3)$$

$$S_{ny} \equiv S_n \sin(n\Psi_n^*) = \int d\mathbf{r}_{\perp} \rho_s(\mathbf{r}_{\perp}) \omega(\mathbf{r}_{\perp}) \sin(n\phi), (4)$$

$$\Psi_n^* = \frac{1}{n} \tan^{-1} \left(\frac{S_{ny}}{S_{nx}}\right), \qquad (5)$$

where ϕ is the azimuthal angle of each source and the weight $\omega(\mathbf{r}_{\perp}) = \mathbf{r}_{\perp}^2$. The eccentricities were calculated

$$\varepsilon_2 = \langle \cos 2(\phi - \Psi_2^*) \rangle \quad \varepsilon_4 = \langle \cos 4(\phi - \Psi_2^*) \rangle$$
 (6)

30 where the brackets denote averaging over sources, as well 31 as events belonging to a particular centrality or impact 32 parameter range. For the MC-Glauber calculations, an 33 additional entropy density weight was applied reflecting 34 the combination of spatial coordinates of participating 35 nucleons and binary collisions [19, 23];

$$\rho_s(\mathbf{r}_\perp) \propto \left[\frac{(1-\alpha)}{2} \frac{dN_{\text{part}}}{d^2 \mathbf{r}_\perp} + \alpha \frac{dN_{\text{coll}}}{d^2 \mathbf{r}_\perp} \right],$$
(7)

where $\alpha = 0.14$ was constrained by multiplicity measurements as a function of N_{part} for Au+Au collisions [30].

The procedures outlined above (cf. Eqs. 2 - 7) ensure 40 that, in addition to the fluctuations which stem from the 41 orientation of the initial "almond-shaped" collision zone 42 [relative to the impact parameter], the shape-induced 43 fluctuations due to nuclear deformation are also taken 44 into account. Note that $\varepsilon_{2,4}$ (cf. Eq. 6) correspond $_{45}$ to $v_{2,4}$ measurements in the so-called participant plane 46 [22, 24]. That is, the higher harmonic ε_4 is evaluated 47 relative to the principal axis determined by maximizing 48 the quadrupole moment. This is analogous to the mea-49 surement of v_4 with respect to the 2nd order event-plane 50 in actual experiments. One consequence is that the den-51 sity profile is suppressed, as well as the moment for the 52 higher harmonic.

Calculations were performed for a variety of isotopes 54 and isobars with a broad range of known $\beta_{2,4}$ values. 55 Here, we show and discuss only a representative set of 56 results for ¹⁹⁷Au (R = 6.38 fm, $\beta_2 = -0.13$, $\beta_4 = -0.03$), ₅₇ ¹⁴⁸Dy $(R = 5.80 \,\text{fm}, \, \beta_2 = 0.00, \, \beta_4 = 0.00)$ and ¹⁵⁸Dy $_{58}$ $(R = 5.93 \,\mathrm{fm}, \,\beta_2 = 0.26, \,\beta_4 = 0.06) \,[27, \,28].$ For these 59 calculations we used the value d=0.53 fm.

Figure 1(a) shows a comparison of $\varepsilon_{2,4}$ vs. $N_{\rm part}$ for $_{14}$ number of binary collisions $N_{\rm coll}$ were determined within $_{61}$ MC-Glauber (open symbols) and MC-KLN (filled sym-15 the Glauber ansatz [24]. The associated $\varepsilon_{2.4}$ values were ω_{2} bols) for Au+Au collisions. The filled symbols indicate $_{63}$ larger $\varepsilon_{2,4}$ values for MC-KLN over most of the consid- $_{64}$ ered $N_{
m part}$ range. The effect of shape deformation is il-65 lustrated in Fig. 1(b) where a comparison of $\varepsilon_{2.4}$ vs. $_{66}$ $N_{
m part}$ [for MC-Glauber] is shown for the two Dy isotopes ₁ indicated. Both ε_2 and ε_4 show a sizable increase for $_{21}$ and the azimuth of the the rotation angle Ψ_n^* for n-th $_{2}$ the isotope with the largest ground state deformation

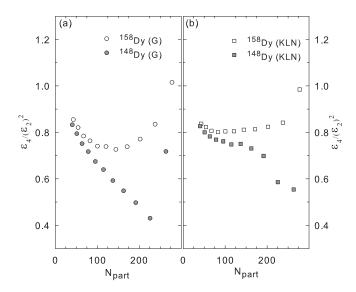


FIG. 2. Comparison of $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ vs. $N_{\rm part}$ for near-spherical ¹⁴⁸Dy (filled symbols) and deformed ¹⁵⁸Dy (open symbols) collisions. Results are shown for MC-Glauber (a) and MC-KLN (b) respectively.

 $_{3}$ (158 Dy). This reflects the important influence of shape-4 driven eccentricity fluctuations in collisions of deformed 5 nuclei [31–34]. The magnitudes and trends of all of these 6 eccentricities are expected to influence the measured val $v_{2,4}$ for these systems.

A priori, the model-driven and shape-driven eccentric-10 ity differences shown in Fig. 1, need not be the same 11 for ε_2 and ε_4 . Therefore, we present the ratio $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ vs. 12 $N_{\rm part},$ for both models in Fig. 2. The ratios obtained for 13 $^{148}{\rm Dy}$ (near-spherical) and $^{158}{\rm Dy}$ (deformed) with MC-Glauber are compared in Fig. 2(a); the same comparison 15 is given in Fig. 2(b) but for MC-KLN calculations. Fig. 16 2(a) indicates a significant difference between the ratio 17 $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ for 148 Dy and 158 Dy over the full range of $N_{\rm part}$ 18 considered. This difference stems from additional shape-¹⁹ driven fluctuations present in in collisions of ¹⁵⁸Dy, but 20 absent in collisions of ¹⁴⁸Dy. The same comparison for MC-KLN results, shown in Fig. 2(b), points to a smaller difference for these ratios, as well as a different N_{part} dependence. We attribute this to the difference in the transverse density distributions employed in MC-Glauber and MC-KLN.

28 collisions, are expected to reflect the magnitude and trend of the ratio $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ (note that a constant ratio ≈ 0.5 30 is predicted for ideal hydrodynamics without the influ-31 ence of fluctuations [21]). Fig. 2 suggests that a rela-32 tively clear distinction between fKLN-like and Glauber-33 like initial collision geometries could be made via system-34 atic studies of $\frac{v_4}{(v_2)^2}$ for near-spherical and deformed iso-

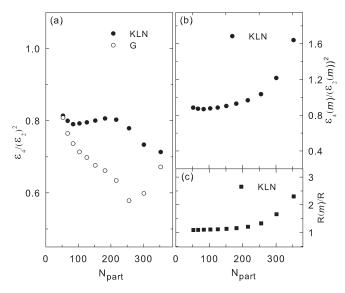


FIG. 3. N_{part} dependence of $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ (a), $\frac{\varepsilon_4(m)}{(\varepsilon_2(m))^2}$ (b) and $\frac{\mathrm{R}(m)}{(\mathrm{R})}$ (c) for Au+Au collisions (see text). The open and closed symbols indicate the results from MC-Glauber and MC-KLN respectively.

36 difference between the ratios $\frac{v_4}{(v_2)^2}$ for each isotope, would 37 be expected for fKLN (Glauber) initial geometries. Sim- $_{38}$ ilarly the scaling of $v_{2,4}$ data from the isotopic or isobaric 39 pair would be expected only for MC-Glauber or MC-KLN 40 eccentricities. Note that the influence of a finite viscosity 41 is expected to be the same for both systems and therefore would not change these conclusions.

The filled symbols in Figs. 2 (a) and (b) also suggest 45 a substantial difference in the $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ ratios predicted by 46 MC-Glauber and MC-KLN respectively, for collisions be-47 tween near-spherical nuclei. This difference is also appar-48 ent in Fig. 3(a) where the calculated ratios for Au+Au 49 $(\beta_2 = -0.13, \beta_4 = -0.03)$ collisions are shown. The $_{50}$ MC-KLN results (filled circles) indicate a relatively flat $_{51}$ dependence for $40 \lesssim N_{\rm part} \lesssim 200$, which contrasts with $_{52}$ the characteristic decrease, for the same $N_{\rm part}$ range, seen 53 in the MC-Glauber results.

As discussed earlier, each of these trends is expected 55 to influence the measured ratios of the flow coefficients $\frac{v_4}{(v_2)^2}$. Therefore, an experimental observation of a rel-57 atively flat $N_{\rm part}$ dependence for $\frac{v_4}{(v_2)^2}$ [over the range For a given value of $N_{\rm part}$, the measured ratio of the $_{58}$ 40 $\lesssim N_{\rm part} \lesssim$ 200], could be an indication for fKLN-like flow coefficients $\frac{v_4}{(v_2)^2}$ for $^{158}{\rm Dy}+^{158}{\rm Dy}$ and $^{148}{\rm Dy}+^{148}{\rm Dy}$ 59 collision geometries in Au+Au collisions. Such a trend $_{60}$ has been observed in the preliminary and final data sets 61 reported in Refs. [10, 21, 35] and is consistent with the ₆₂ conclusions reached in Ref. [10, 36] that the $N_{\rm part}$ and 63 impact parameter dependence of the eccentricity scaled ₆₄ flow coefficients $\frac{v_2}{\varepsilon_2}$ and $\frac{v_4}{\varepsilon_4}$ favor fKLN-like initial collision

The closed symbols in Figs. 2(b) and 3(a) indicate 35 topes/isobars. Specifically, a relatively smaller (larger) 2 a decreasing trend for $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ for near-spherical nuclei for

 $_3$ $N_{
m part} \gtrsim 200$. This decrease can be attributed to the $_{57}$ and deformed isotopes (or isobars) are required to exploit 4 fact that, in each event, ε_4 is computed in the reference 5 frame which maximizes the quadrupole shape distribu-6 tion, i.e. the so-called participant frame. In this frame, $\tau \varepsilon_4$ can take on positive or negative event-by-event val-8 ues. Consequently, smaller mean values are obtained, 9 especially in the most central collisions. Fig. 2 shows 10 that the relatively large ground state deformation for ₁₁ ¹⁵⁸Dy (open symbols) leads to an increase of $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ [rela-12 tive to that for the spherical ¹⁴⁸Dy isotope which is espe-13 cially pronounced in the most central collisions. However, 14 Fig. 3(a) shows that the modest deformation for the Au 15 nuclei does not lead to a similarly increasing trend for $_{16}$ $N_{\mathrm{part}} \gtrsim 200$ as implied by data [21, 35].

The relatively flat N_{part} dependence for $\frac{v_4}{(v_2)^2}$, over the 18 range $40 \lesssim N_{\rm part} \lesssim 200$ in Fig. 3(a), suggests fKLN-like 19 collision geometries. Consequently, it is interesting to in-20 vestigate whether or not the magnitude of the ratios for $_{21}$ $N_{\rm part} \gtrsim 200$, can be influenced without significant im-²² pact on the values for $N_{\rm part}\lesssim 200$. Figure 3(b) shows ²³ that a large increase of $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ can indeed be obtained for $_{24}$ $N_{
m part} \gtrsim 200$ with relatively little change in the magni-₂₅ tude and trend of the ratios for $N_{\rm part} \lesssim 200$. This was ₂₆ achieved by introducing a correlation or mixing (m) beween the principal axes of the quadrupole (Ψ_2^*) and hex-²⁸ adecapole (Ψ_4^*) density profiles associated with ε_2 and ε_4 ²⁹ respectively. That is, the orientation of Ψ_2^* was modified 30 to obtain the new value $\Psi_2^{**} = (1 - \gamma)\Psi_2^* + \gamma\Psi_4^*$, where $_{31}$ $\gamma = 0.2$. This procedure is motivated by the finding that, v_4 in addition to the v_4 contributions which stem from the 33 initial hexadecapole density profile, experimental mea-34 surements could also have a contribution from v_2 [with magnitude $\propto (v_2)^2$ [29, 37]. The correlation has little, $_{36}$ if any, influence on the ε_2 values, but does have a strong ₃₇ influence on $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ in the most central collisions. This is $_{38}$ demonstrated in Fig. 3(c) where the double ratio $\frac{\mathrm{R}(m)}{\mathrm{R}}$ $_{39}$ (R(m) = $\frac{\varepsilon_4(m)}{(\varepsilon_2(m))^2}$ and R = $\frac{\varepsilon_4}{(\varepsilon_2)^2}$) is shown.

In summary, we have presented results for the initial 41 eccentricities $\varepsilon_{2,4}$ for collisions of near-spherical and de-42 formed nuclei, for the two primary models currently em-43 ployed for eccentricity estimates at RHIC. The calculated 44 ratios for $\frac{\varepsilon_4}{(\varepsilon_2)^2}$, which are expected to influence the mea-45 sured values of $\frac{v_4}{(v_2)^2}$, indicate sizable model dependent 101 46 differences [both in magnitude and trend] which can be 102 exploited to differentiate between the models. The $\frac{\varepsilon_4}{(\varepsilon_2)^2}$ $_{48}$ ratios obtained as a function of $N_{\rm part}$ for Au+Au colli-49 sions with the fKLN model ansatz, show trends which so are strongly suggestive of the measured ratios for $\frac{v_4}{(v_2)^2}$ $_{51}$ observed in Au+Au collisions for $40 \lesssim N_{\rm part} \lesssim 200$. $_{52}$ For more central collisions ($N_{\rm part} \gtrsim 200$), the observed $_{109}$ 53 trend is strongly influenced by initial eccentricity fluctu-54 ations if a correlation between the principal axes of the 55 quadrupole and hexadecapole density profiles is assumed. New measurements of $\frac{v_4}{(v_2)^2}$ for collisions of near-spherical 2 [30] B. B. Back et al. (PHOBOS), Phys. Rev., C70, 021902

58 these tests.

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- M. Gyulassy and L. McLerran, Nucl. Phys., A750, 30 (2005).
- P. Huovinen, P. F. Kolb, U. W. Heinz, P. V. Ruuskanen, and S. A. Voloshin, Phys. Lett., **B503**, 58 (2001).
- D. Teaney, Phys. Rev., C68, 034913 (2003).
- P. Romatschke and U. Romatschke, Phys. Rev. Lett., 99, 172301 (2007).
- Y. Hama et al., Phys. Atom. Nucl., 71, 1558 (2008).
- [6] H. Song and U. W. Heinz, Phys. Rev., C77, 064901
- R. A. Lacey, Nucl. Phys., A698, 559 (2002).
- R. J. M. Snellings, Nucl. Phys., A698, 193 (2002).
- J. Adams et al., Phys. Rev. Lett., 92, 062301 (2004).
- R. A. Lacey, A. Taranenko, and R. Wei, arXiv:0905.4368 [nucl-ex].
- U. W. Heinz and S. M. H. Wong, Phys. Rev., C66, 014907 (2002).
- [12] R. A. Lacey and A. Taranenko, PoS, CFRNC2006, 021
- H.-J. Drescher, A. Dumitru, C. Gombeaud, and J.-Y. 84 [13] Ollitrault, Phys. Rev., C76, 024905 (2007).
- 86 [14] Z. Xu, C. Greiner, and H. Stocker, Phys. Rev. Lett., **101**, 082302 (2008).
 - V. Greco, M. Colonna, M. Di Toro, and G. Ferini, (2008), arXiv:0811.3170 [hep-ph].
 - M. Luzum and P. Romatschke, Phys. Rev., C78, 034915
 - A. K. Chaudhuri, (2009), arXiv:0910.0979 [nucl-th].
 - H. Song and U. W. Heinz, J. Phys., G36, 064033 (2009).
 - T. Hirano, U. W. Heinz, D. Kharzeev, R. Lacey, and Y. Nara, Phys. Lett., **B636**, 299 (2006).
 - H.-J. Drescher, A. Dumitru, A. Hayashigaki, and Y. Nara, Phys. Rev., C74, 044905 (2006).
- Gombeaud and J.-Y. (2009),arXiv:0907.4664 [nucl-th].
- B. Alver et al., Phys. Rev. Lett., 98, 242302 (2007).
- T. Hirano and Y. Nara, Phys. Rev., C79, 064904 (2009).
- M. L. Miller, K. Reygers, S. J. Sanders, and P. Steinberg, Ann. Rev. Nucl. Part. Sci., 57, 205 (2007).
- T. Lappi and R. Venugopalan, Phys. Rev., C74, 054905
- H.-J. Drescher and Y. Nara, Phys. Rev., C76, 041903 (2007).
- S. Raman and C. W. Nestor, Jr., Atom. Data Nucl. Data Tabl., 42, 1 (1989).
- P. Moller, J. R. Nix, W. D. Myers, and W. J. Swiatecki, Atom. Data Nucl. Data Tabl., 59, 185 (1995).
- W. Broniowski, P. Bozek, and M. Rybczynski, Phys. Rev., C76, 054905 (2007).

- (2004).
- ⁴ [31] E. V. Shuryak, Phys. Rev., **C61**, 034905 (2000).
- ⁵ [32] B.-A. Li, Phys. Rev., **C61**, 021903 (2000).
- 6 [33] U. W. Heinz and A. Kuhlman, Phys. Rev. Lett., 94, 132301 (2005).
- C80, 054903 (2009).

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- $_{\rm 10}$ [35] and A. Adare (The PHENIX), $\,$ (2010), $\rm arXiv:1003.5586$ [nucl-ex]. 11
- 12 [36] U. W. Heinz, J. S. Moreland, and H. Song, Phys. Rev., C80, 061901 (2009). 13
- 8 [34] P. Filip, R. Lednicky, H. Masui, and N. Xu, Phys. Rev., 14 [37] P. F. Kolb, L.-W. Chen, V. Greco, and C. M. Ko, Phys. Rev., **C69**, 051901 (2004).