Project Euler #1: Multiples of 3 and 5



This problem is a programming version of Problem 1 from projecteuler.net

If we list all the natural numbers below 10 that are multiples of 3 or 5, we get 3, 5, 6 and 9. The sum of these multiples is 23.

Find the sum of all the multiples of ${\bf 3}$ or ${\bf 5}$ below ${\bf \it N}$.

Input Format

First line contains T that denotes the number of test cases. This is followed by T lines, each containing an integer, N.

Constraints

- $1 \leqslant T \leqslant 10^5$
- $1 \le N \le 10^9$

Output Format

For each test case, print an integer that denotes the sum of all the multiples of ${\bf 3}$ or ${\bf 5}$ below N.

Sample Input 0

2 10 100

Sample Output 0

23 2318

Explanation 0

For N=10, if we list all the natural numbers below 10 that are multiples of 3 or 5, we get 3,5,6 and 9. The sum of these multiples is 23.

Similarly for N=100, we get 2318.

(*) Solution:

. Multiples of 3 in [1, n] interval:

$$= 3.1 + 3.2 + 3.3 + ... + 3.(n//3)$$

$$=3.(1+2+3+...+n/13)$$

$$=3. \frac{n/3}{2}.(1+n/3)$$

· Sum of consecutive numbers:

$$1 + 2 + 3 + ... + N = \frac{N \cdot (N+1)}{2}$$

· (Sum of Multiples) of 3 and 5 (8 = S(3) + S(5) - S(15)