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Rasterization and Rendering in a Console



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Abstract

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Symbols

texel

TODO

# Introduction

TODO

# Rendering theory

Drawing anything is quite math heavy, so here we will go through the process of rasterizing and rendering common objects, as well as explain the algorithms we will be using in a python-style pseudocode. We will also go over our chosen display method of the Windows console.

## Window

TODO

## Canvas

Before rendering anything to the console we will first need a canvas to draw things on. In this case our canvas is a 2D array of pixels in which each pixel can be individually colored. A common color format is RGBA which uses a total of 4 bytes per pixel, however our canvas will only have 16 colors due to the limitations of CMD, so we can use just 1 byte per pixel. We will however have to define how this byte is used to represent the 16 colors. A good convention would be to just use the colors Microsoft uses which range from 0 to 15, then we can also fit transparency in there, however we can only have one value of transparency so a simple method would be to consider the color transparent if it is greater than 15. A canvas also needs a PutPixel function which will change the color of a pixel at a specified x and y coordinate. With it we can already draw points. [1.]

canvas = Color[][]

PutPixel(x, y, color):

canvas[x][y] = color

## Rasterization

Rasterization is the process of taking a vector-based image, or vertice based 3D object, and converting it to pixels. It is a much faster process of rendering than alternatives such as raytracing but does not directly give information about what color the pixel should be. Therefore rasterization, especially of 3D objects is often combined with pixel shaders to determine the final color of the pixel. [2.] However, we will not be covering shaders since they are outside the scope of this paper, which means the final color of our pixels will be decided entirely based on the material color or texture of the object.

### Rasterizing Lines

The simplest geometric shape to draw after a point is a line, so we might as well start from there. Lines are often represented in slope-intercept form, which is y = mx + b where x and y are the coordinates of individual points on the line, m is the change in y per x, or the slope, and b is the vertical offset, or the y coordinate where the line intercepts the y-axis. Drawing a line with this formula is as easy as iterating over every x position and plotting the corresponding y value. However we want a function in the form of DrawLine(x0, y0, x1, y1), since drawing line segments with a given start and end point is much more useful. In this case we start drawing from (x, y) = (x0, y0) and add m to x for every integer y position. B will not be useful for us, so we can just ignore it. [1.] The function would look something like this, where x and y are integers:

DrawLine(x0, y0, x1, y1, color):

//Slope is rise/run

m = (y1 - y0) / (x1 - x0)

y = y0

//For each x position, plot the corresponding y

for x from x0 to x1:

PutPixel(x, y, color)

y += m

A black and white line

Description automatically generatedA black and white line

Description automatically generated

Drawing some lines with this function produces some interesting results. Line one is {TODO add start and end points and slope}, and line 2 is {TODO}. The lines look jagged because we only have a finite number of pixels to represent a line, and this is the simplest approximation. There are anti-aliasing techniques one can use to smooth out these lines such as FXAA and MSAA, but that is beyond the scope of this paper [1]. The bigger problem is that the second line is missing some pixels.

Since this is a very simple function, there are multiple problems with it. First, the failure to properly draw the line in {line pic 1} where the slope is greater than 1 is because our function can only draw one pixel per x coordinate, thus not being able to draw lines where y increases faster than x. Second, it will not work for vertical lines, as in that case we would divide by 0 when calculating m. Third, if x0 is greater than x1 nothing will be drawn due to the loop immediately terminating. [1.]

We can fix the first two problems by making a copy of the function to draw the line based on the y axis and using that function if the absolute value of the slope is greater than one. The second problem is also easily fixed by swapping the start and end points so that x0 or y0 is always less than x1 or y1. [1.]

DrawLine(x0, y0, x1, y1, color):

//If slope is less than 1

if abs(x1 - x0) > abs(y1 - y0):

//Make sure x1 is smaller than x2

if x0 > x1:

swap(x0, x1)

swap(y0, y1)

//Slope is rise/run

m = (y1 - y0) / (x1 - x0)

y = y0

//For each x position, plot the corresponding y

for x from x0 to x1:

PutPixel(x, y, color)

y += m

else:

//Make sure y1 is smaller than y2

if y0 > y1:

swap(x0, x1)

swap(y0, y1)

//Slope is run/rise

m = (y1 - y0) / (x1 - x0)

x = x0

//For each y position, plot the corresponding x

for y from y0 to y1:

PutPixel(x, y, color)

x += m

A black and white image of a arrow

Description automatically generated

{TODO: Add more different lines} This completed function allows us to draw any line between any two points. However, this function is far from optimal since we use a floating-point number for m, meaning there is some expensive division and rounding. It would be nice to get rid of those to get our function running fast on a CPU. For this we can implement Bresenham's line algorithm. It is the best line drawing algorithm for our purpose since it works on any line and is also optimized to only use integer arithmetic. Its main downside is the lack of anti-aliasing, but we won't be using that anyways. [3.]

Bresenham's line algorithm works by tracking the accumulated error in the line's actual y and the plotted y at every x position. After each pixel is plotted, the error is increased by the slope. Next, the algorithm decides if the plotted y should be incremented by 1 based on the amount of error: if the error is more than 1/2, y should be incremented and the error should be decremented, thus we always plot the closest possible pixel to the actual y. [3.]

DrawLine(x0, y0, x1, y1, color):

m = (y1 - y0) / (x1 - x0)

y = y0

error = 0.0

//For each x position, plot the corresponding y

for x from x0 to x1:

PutPixel(x, y, color)

error += m

if error > 0.5:

y += 1

error -= 1.0

This implementation still has floating point arithmetic, so to write it in a form which only uses integers we have to change around our two problematic lines: "error += m", and "if error > 0.5".

To rewrite the function to work with only integers we first expand m:

dy = y0 – y1, dx = x0 – x1

error = error + dy / dx

Then, to get rid of the fraction:

dx \* error = dx \* error + dy

Next, to get rid of the fraction in *if error > 0.5*:

if error \* 2 > 1

To make these two lines work in code:

2 \* dx \* error = 2 \* dx \* error + 2 \* dy

if error \* 2 \* dx > 1 \* dx

Simplify by grouping together 2 \* dx \* error:

error = error + 2 \* dy

if error > dx

Rewriting the function this way avoids floating point division and allows every number to be an integer, which makes the function faster [3]. We will still need to apply the fixes for different slopes from our original algorithm, as well as account for a negative slope by decrementing x or y instead of incrementing. The complete function looks something like this:

DrawLine(x0, y0, x1, y1, color):

//If slope is less than 1

if abs(x1 - x0) > abs(y1 - y0):

//Make sure starting point is before ending point

if x0 > x1:

swap(x0, x1)

swap(y0, y1)

dx = x1 – x0;

dy = y1 – y0;

//If slope is positive increment y, else decrement

yi = 1

if dy < 0:

yi = -1

dy = -dy

y = y0

error = 0

//For each x position, plot the corresponding y

for x from x0 to x1:

PutPixel(x, y, color)

error += 2 \* dy

if error > dx:

y += yi

error -= 2 \* dx

else:

//Make sure starting point is before ending point

if y0 > y1:

swap(x0, x1)

swap(y0, y1)

//If slope is positive increment x, else decrement

xi = 1

if dx < 0:

xi = -1

dx = -dx

x = x0

error = 0

//For each y position, plot the corresponding x

for y from y0 to y1:

PutPixel(x, y, color)

error += 2 \* dy

if error > dx:

x += xi

error -= 2 \* dx

### Rasterizing Triangles

The next geometric shape we want to draw is a triangle, since most 3D models are made exclusively of triangles and all polygons can be decomposed into triangles. A triangle is formed by three vertices we will refer to as v0, v1, and v2. Since we're working on a 2D canvas, these vertices will consist of only an x and y coordinate. We can use our DrawLine function to draw a triangle just by drawing lines connecting the vertices: [1.]

{TODO: maybe wireframe triangle picture}

DrawWireframeTriangle(v0, v1, v2):

DrawLine(v0, v1)

DrawLine(v1, v2)

DrawLine(v2, v0)

This function, however, only draws a wireframe triangle, meaning only its edges are colored in. We also need a function to draw a filled in triangle. A simple method for doing this is drawing the triangle entirely out of horizontal lines. To do this, we can simply iterate over every y position in between the triangle's top and bottom vertices and draw a line from the left side to the right: [1.]

for y from topY to bottomY:

rightBound, leftBound = CalculateBounds()

DrawLine(rightBound, y, leftBound, y)

To get the topY and bottomY, we can simply sort the vertices before drawing. The actual tricky part of this implementation is calculating the right and left bounds. To solve this, we can consider that the x bounds are defined by the lines [v0, v1], [v1, v2], and [v0, v2], where one of these lines will be an entire side and the other side will be made up of the remaining two. Since we sorted the vertices, we know [v0, v2] will always be the continuous side, while [v0, v1] and [v1, v2] will make up the segmented side. [1.] Now, to calculate the x bounds we can use a slightly modified version of our line drawing algorithm, where instead of drawing the point, we store the x value in a list whenever y changes: {TODO add picture explaining triangle and vertices and sides}

This function will return a list of x coordinates for every y position. To get the bounds all we need to do is combine the lists for the segmented side and figure out which list is the left and which is the right one. To figure this out we can calculate a directional vector from v0 to v1 and v2 and check which has a bigger x value, since we know v0 will always be above v1 and v2, this holds true for every triangle. There will also be a duplicate x position in the segmented list right where the two lines meet, so we must make sure to remove that. Puttin all this together we have a simple function to draw filled triangles: [1.]

CalculateXBounds(x0, y0, x1, y1):

**//Store the x positions in a list**

**xBounds = []**

if abs(x1 - x0) > abs(y1 - y0):

. . .

for x from x0 to x1:

error += 2 \* dy

if error > dx:

**//Add the x position to the list instead of drawing it**

**xBounds.append(x)**

y += yi

error -= 2 \* dx

else:

. . .

for y from y0 to y1:

**//Add the x position to the list instead of drawing it**

**xBounds.append(x)**

error += 2 \* dy

if error > dx:

x += xi

error -= 2 \* dx

**return xBounds**

This is quite a simple function, but it will do for now. We will be coming back to it in the following sections. Notice we also did not use our DrawLine function here. That is due to our lines being exclusively horizontal, so we can make a more optimized implementation for this specific purpose.

DrawTriangle(v0, v1, v2, color):

//Sort the vertices in descending y

if v0.y < v1.y: swap(v0, v1)

if v0.y < v2.y: swap(v0, v2)

if v1.y < v2.y: swap(v1, v2)

//Calculate the x bounds of every edge

v01Bounds = CalculateXBounds(y0, x0, y1, x1)

v12Bounds = CalculateXBounds(y1, x1, y2, x2)

v02Bounds = CalculateXBounds(y0, x0, y2, x2)

//Combine the two lists of the segmented side

v01Bounds.removeLast()

v012Bounds = v01Bounds.append(v12Bounds)

//Check which side is left and right

leftBounds = v02Bounds

rightBounds = v012Bounds

v01 = Normalize(v1 – v0)

v02 = Normalize(v2 – v0)

if v01.x < v02.x:

swap(leftBounds, rightBounds)

//Draw each horizontal line

for y from y0 to y2:

for x from leftBounds[y - y0] to rightBounds[y - y0]:

PutPixel(x, y, color)

{TODO add filled triangle picture}

## Rendering

Being able to draw triangles is very useful, because every other polygon can be decomposed into multiple triangles [1]. For example, to draw a rectangle defined by the vertices (v0, v1, v2, v3) we can draw two triangles (v0, v1, v3) and (v1, v2, v3).

{TODO add picture of above}

This works for drawing any 2D polygon, but there are still numerous problems. We need to be able to draw 3D objects, move them, and move the camera. We also need to take perspective into account to render images the way they appear in real life. To solve these, we need to expand our render pipeline to further process the objects before passing them to the rasterizer. The below image is an overview of everything we need to do in the pipeline.

model space -> apply model matrix -> world space -> calculate normals -> cull backwards faces -> apply view matrix -> view space -> clip faces -> apply projection matrix -> clip space -> apply viewport transform -> screen space -> send to rasterizer

{TODO Add picture of above}

### 3D Models

First, we need to figure out a way to represent 3D objects in a general form. For example, take a cube with the vertices v0 – v7. These vertices are only points in space, so without more information we would have no idea which ones to use to draw the triangles of the cube. Therefore, we also need a list of those triangles describing which three vertices make each triangle. Since a cube has 6 rectangular faces, we need a list of 12 triangles to draw it. These two lists we call *vertices* and *indices* are enough information to render any 3D object made of triangles. [1.]

{TODO Add picture of cube}

This is a very common format for storing 3D objects. File formats, such as .obj, work very similarly with the main difference being that faces can be any polygon, not just triangles. These formats are also capable of storing other information, such as materials and textures, which we will cover in a later section. Loading these models from files is outside the scope of this paper, but there are many existing libraries, such as *Assimp*, which are easy to implement and do some useful operations, such as triangulating the faces at load time. [4.]

To render objects stored this way, all we need to do is loop over every entry in indices and call DrawTriangle() with the corresponding vertices:

vertices = [v0, v1, v2, v3, …]

indices = [[0, 1, 3], [1, 2, 3], …]

RenderIndexed(vertices, indices, color):

for tri in indices:

DrawTriangle(vertices[tri.v0],

vertices[tri.v0],

vertices[tri.v0],

color)

### Transforms

Another very important feature for our renderer is being able to move around objects. Right now, we are rendering them all in model space, which means they are relative to the object’s local origin. We want to be able to move these objects around the world without having to redefine the model itself. To do this we apply a transformation to each vertex before passing them to the rasterizer. We also need to set a convention for the x, y, and z axes of our world space. A good convention is the one used by graphics API’s such as OpenGL, where +Y is up. [5.]

There are three main transforms we want to do: translation, rotation, and scaling. The proper method of applying these is with a transformation matrix, therefore it is important to have at least a basic understanding of matrix multiplication before trying to understand transformations. 3-dimensional transformation matrices are represented in homogenous coordinates (4x4 matrices), but all our vertices are in cartesian coordinates (3x1 matrices, or vector 3s). Therefore, we need to first understand the basic idea of homogenous coordinates and how they are useful for us. [1.]

For us the useful difference is the distinction between points and vectors. Take A = (1, 2, 3), for example. There is no way to know if A is a point or a vector, but if we add a fourth value w, we can now represent a vector when w = 0 and a point when w = 1. The cases where w is some other number also represent point, the important part is the ratio between xyz and w. So, to convert from cartesian to homogenous coordinates, we can simply add the proper value of w, so A = (1, 2, 3, 0) is a vector, and A = (1, 2, 3, 1) is a point. Converting back from homogenous coordinates to cartesian coordinates is also simple; we divide xyz by w. [1.]

Now to finally transform our objects we need to construct the translation, rotation, and scale matrices, multiply them together for the transformation matrix, and finally multiply each vertex by this matrix.

Translation by vector *T*:

Scale by vector *S*:

There are three rotation matrices we will need to use: one for rotating around each axis. The order of applying these is also important as rotations are not commutative [6]:

Rotation θ around the X axis:

Rotation θ around the Y axis:

Rotation θ around the Z axis:

The final rotation matrix can be calculated by multiplying these three together. We will use the order z, y, x as a convention:

Note that this method of rotation is not perfect and introduces a problem called gimbal lock. Fixing this would require representing rotations using quaternions, but that is outside the scope of this paper. [5.]

Now that we have these matrices, we can multiply them together to get our transformation matrix, which we will call the model matrix to avoid confusion with future transformation matrices. The order of multiplication also matters, the first transformation will be the last multiplication. Since we want to apply the transforms in the order scale, rotation, translation, the final model matrix is calculated as such: [5.]

scale = Scale(sX, sY, sZ)

rotation = RotateZ(rZ) \* RotateY(rY) \* RotateX(rX)

translation = Translate(tx, ty, tz)

model = translation \* rotation \* scale

### Camera

We can now move around objects; next we need a camera that we can move around the scene. The actual implementation of the camera might, however, be counterintuitive at first. Instead of moving the camera, we keep the camera still, pointing at -Z and move the entire world around it. Since rotating the camera by R produces identical results to rotating everything in the world by -R, there is no difference in the result. The same goes for translation. [1.]

{TODO: add picture}

This is much better than the alternative since it greatly simplifies the projection of 3D vertices to 2D points. It is also easy to implement. We can use the same matrices as in the last section, just apply them in the reverse order and invert all the transforms. Here we will also only need rotation and translation since a camera's scale works slightly differently and will be implemented in the next section. Therefore, our camera transformation matrix, which we will call the view matrix, is: [1.]

//An easier way to apply the inverse transforms in code is

//inverting them before constructing the matrices

translation = Translate(tx, ty, tz)

rotation = RotateZ(-rZ) \* RotateY(-rY) \* RotateX(-rX)

view = rotation \* translation

### Perspective Projection

https://www.scratchapixel.com/lessons/3d-basic-rendering/perspective-and-orthographic-projection-matrix/opengl-perspective-projection-matrix.html

The last thing we need to do to get our objects rendering as they would in real life is apply a perspective projection to them. The idea with this is to convert 3D points into 2D points on the viewport and render them as a real camera would see them, with farther away objects appearing smaller. We will also want to normalize these points into the range (-1, 1), which is called normalized device coordinates, or NDC. Our vertices will then be in clip space. [5.]

Perspective projection of a point can be calculated using basic trigonometry. Consider the below diagram where P is the point we want to project, P' is the projected point, n is the projection plane, also known as the near clip plane, and the camera is at the origin facing toward -Z. [sp]

{TODO Add picture}

The points ABP and ACP' form two similar triangles, whose properties we can use to calculate p'. By the properties of similar triangles AC/AB = CP'/BP, substituting our known values and solving for BP we get BP = P'y = n \* Py / -Pz. Also note that since the camera is facing towards -Z, Pz is inverted to preserve the sign of the y coordinate. The same logic works for P'x = n \* Px / -Pz. [sp]

Now we have point P projected to the near clip plane, but we still need to map it to NDC. APIs like OpenGL calculate this by defining the left (l), right (r), top (t), and bottom (b) edges of the camera and mapping the point inside those bounds, we will do the same. We also need to map the z coordinate to between (-1, 1) or (0, 1), which we do with the help of the near (n) and far (f) clip planes. The OpenGL projection matrix maps z to (-1, 1), but (0, 1) is a more standard range and easier for us to work with, so we will slightly modify the matrix to achieve this result. [sp]

{TODO maybe explain derivation}

Now that we have the projection matrix, we still need to calculate the values it needs. The near and far planes are easy, as they are given by the user. The other values are slightly more difficult, since we will want to calculate them based on the camera's field of view, or fov, and aspect ratio. The fov can be defined as either the vertical or horizontal view angle. Here we will define it as the vertical angle, since that is the convention used by OpenGL, and it makes more sense with the standard way of defining aspect ratio as width/height. Calculating these values is trivial with basic trigonometry.

{TODO add picture}

From the above image you can derive the following:

top = tan(fov / 2) \* near

bottom = -top

And for the width and height, all we have to do is factor in the aspect ratio, which is also given by the user.

right = top \* aspectRatio

left = -right

Now we can construct the final projection matrix and apply it to our vertices. For the final step before sending our triangle to the rasterizer, we need to convert its homogenous coordinates back into cartesian coordinates by diving xyz by w.

{TODO Add pseudocode}

### Clipping

TODO

### Back Face Culling

TODO

### Depth Buffering

TODO

## Texturing

Currently we can only draw shapes consisting of one color, for more detail we need to add a texture, which is an image we essentially “paint” on to the shape.

First, we need to define how the texture is applied to the shape. We will do this on a per-triangle basis by specifying a point on the texture which corresponds to each vertex of the triangle. For this we need a coordinate system to refer to the texels. Since a texture is an image and an image is a 2D array of colors, we could use x and y for the coordinates, however, x and y already refer to the coordinates of the canvas, so by convention we use u and v for the texture coordinates. [1.]

## The Console

{TODO: Rewrite this}

As per Microsoft: "A console is an application that provides I/O services to character-mode applications." This essentially means a console can read user input, such as keypresses or mouse movements, into an input stream, and render the text contents of an output stream onto the screen. The Windows console can render the entire Unicode character set, but we will only be using characters from the Windows-1252 character {TODO: at least for now I might upgrade to Unicode} set since we only need a few characters from it, and it simplifies the actual implementation. [msdoc.] The most important characters for us are 223(▀), 220(▄), and 219(█), as these can be used to represent an upper, a lower, and two stacked pixels, thereby essentially doubling our vertical resolution. Characters 176(░), 177(▒), and 178(▓) are also potentially useful since they could allow us to blend colors through dithering, however using these would mean cutting the vertical resolution in half.

There are two ways to operate the console, either through the console API, or through virtual terminal sequences. The console API uses a set of C++ functions defined by Microsoft to change the state of the console, such as setting the cursor position, changing the pen color, or writing text. Virtual terminal sequences on the other hand are a set of functions represented as non-printable characters which can be output in between normal text to change the state of the terminal. We will use virtual terminal sequence in this paper because Microsoft recommends them over the API, and they are cross compatible with many other terminal emulators besides just CMD and PowerShell. [msdoc.]

The Windows console is capable of rendering 16 different colors in both the background and foreground, each character can have a different color set for its background and foreground color, however we cannot set the background and foreground color to be the same [msdoc]. Since we're using one character to represent two pixels if those pixels have a different color, we need to use the background to represent one of them. It doesn't really matter which of the two is represented by the background, so we can just set a convention of always rendering the 223(▀) character in the case the two pixels are different colors.

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