

# LINEAR ALGEBRA REFRESHER

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# Single subscript

NumChairs<sub>i</sub>

Student (i)	Height
1	5' 7" <del>4</del>
2	⋮
3	⋮
⋮	⋮
300	6'

$x_i$

$$x_{300} = 6'$$

# Double subscript

$x_{ij}$ : number of chairs  
of type  $i$  to produce  
in factory  $j$

Type of chair		
	1	2
Factory	1	
	2	40
	3	

$x_{ij}$

$x_{12}$

$x_{22,31}$   $i=22$   
 $j=31$

Factory	Type	$x$
1	1	10
1	2	15
2	1	40
2	2	30
3	1	20
3	2	10

# Single summation

$$\sum_{i=1}^N x_i$$

$$\sum_i x_i$$

$$x_1 + x_2 + x_3 + x_4 =$$

Student $i$	Pets $x$
1	0
2	3
3	1
4	0

$$0 + 3 + 1 + 0$$
$$\sum_{i=1}^4 x_i$$

# Summation Constant Rules

$$\sum_{i=1}^N a = Na$$

$$a = 3 \quad N = 2$$

$$\sum_{i=1}^2 3 = 3 + 3 = 6 = 3 \cdot 2$$

$$\sum_{i=1}^N ax_i = a \sum_{i=1}^N x_i$$

Type cost	
1	10
2	12

$$a = 3$$

# Distributive Rule

$x_i \rightarrow$  number of chairs to prod. on line  $i$ ;

$y_i \rightarrow$  number of tables to produce on line  $i$ ;

$$\sum_{i=1}^N (x_i + y_i) = \sum_{i=1}^N x_i + \sum_{i=1}^N y_i$$

# Double summation

$$\sum_i \sum_j (x_{ij} + y_{ij}) = \sum_{i,j} x_{ij} + \sum_{i,j} y_{ij}$$

i	j	j ≥ i
1	1	✓
1	2	✓
2	1	✗
2	2	✓
3	1	✗
3	2	✗

$$\sum_{i=1}^2 \sum_{j=1}^3 x_{ij}$$

$$x_{11} + x_{12} + x_{22} = \sum_{j \geq i} x_{ij}$$

Type	Line	$x_{ij}$
A	1	$x_{A1}$
B	1	$x_{B1}$
A	2	$x_{A2}$
B	2	$x_{B2}$

$$i = 1, \dots, 3$$

$$j = 2, 3$$

i	2	3
1	✓	✓
2	✓	✓
3	✗	✓

Total amount of calories from the following meal: grilled salmon (40 cal.), two sides of asparagus (8 cal. each) and one side of potatoes (5 cal.)

$Amt_i$ : amount of calories in food  $i$

$$\sum_{i=1}^3 Amt_i = Amt_1 + Amt_2 + Amt_3$$

$$= 40 + \underline{2}(8) + 5$$

Food	Amt	Num
1	40	1
2	8	2
3	5	1

$$\sum_{i=1}^3 Num_i \cdot Amt_i + Num_2 \cdot Amt_2 + Num_3 \cdot Amt_3$$



How many physician-hours are required for one day with the following procedures scheduled:  
 ① six appendectomies (2 hr. each), five skin biopsies (30 mins. each), two fracture cares (2.5 hr. each) and three catheters' placements (1 hr. each)

Procedure (i)	Time <sub>i</sub>	Num <sub>i</sub>
1	2	6
2	0.5	5
3	2.5	2
4	1	3

$$\sum_{i=1}^4 \text{Num}_i \cdot \text{Time}_i = 6(2) + 5(0.5) + 2(2.5) + 3(1)$$