

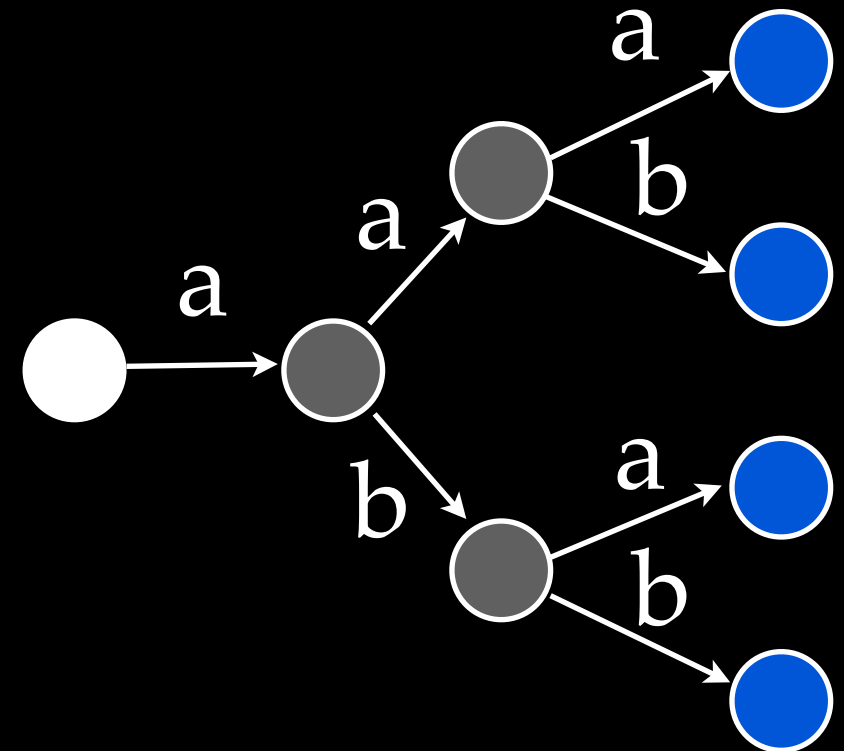
Syntax-Based Translation with Weighted Automata

Review

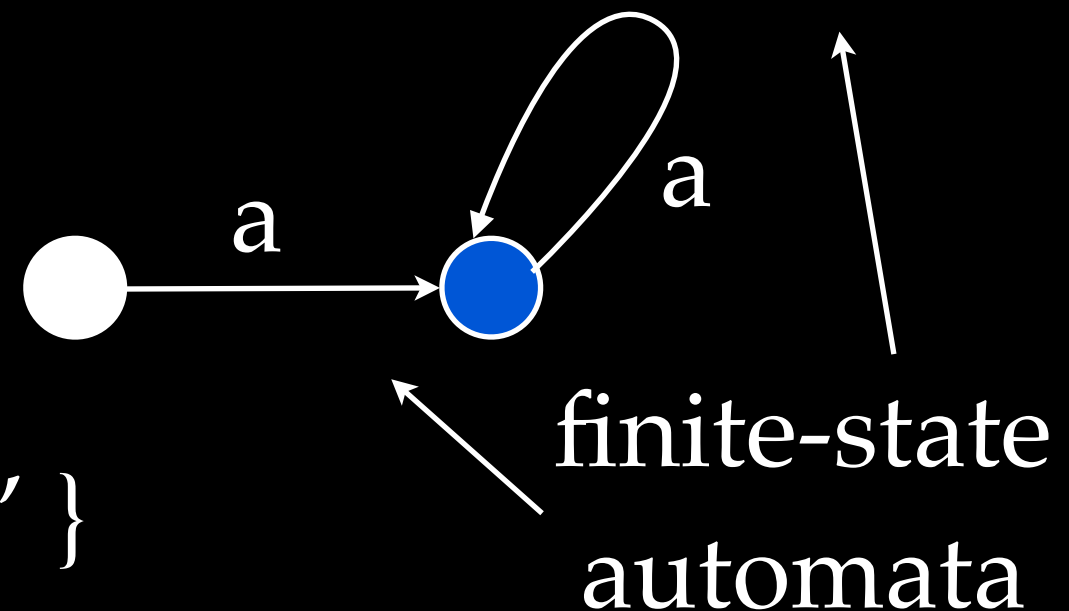
- We need efficient algorithms and data structures to:
 - Encode all of the strings in the language.
 - Assign probabilities to all of those strings.
 - Via products such as $p(e)p(f|e)$.
 - Find the string with the highest probability.
 - Compute expectations over substrings.
 - Compute mappings between strings.

Regular Languages

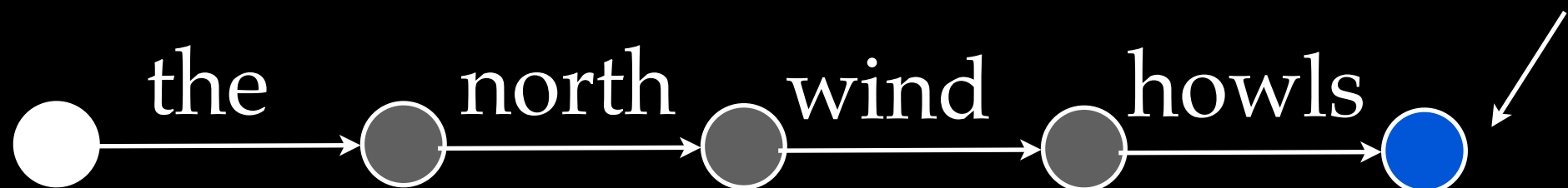
$$\mathcal{L}_1 = \left\{ \begin{array}{c} a a a \\ a b a \\ a a b \\ a b b \end{array} \right\}$$



$$\mathcal{L}_2 = a^* = \{a, aa, aaa, \dots\}$$

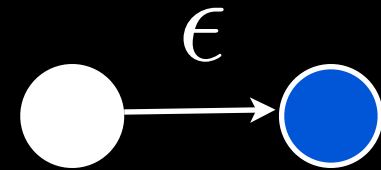


$$\mathcal{L}_3 = \{ \text{"the north wind howls"} \}$$

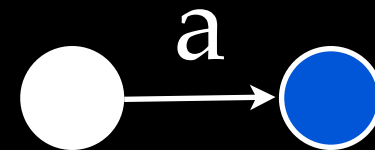


Regular Languages

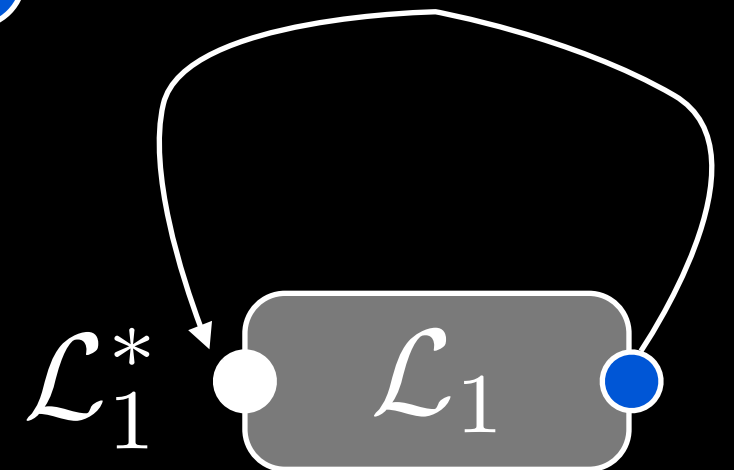
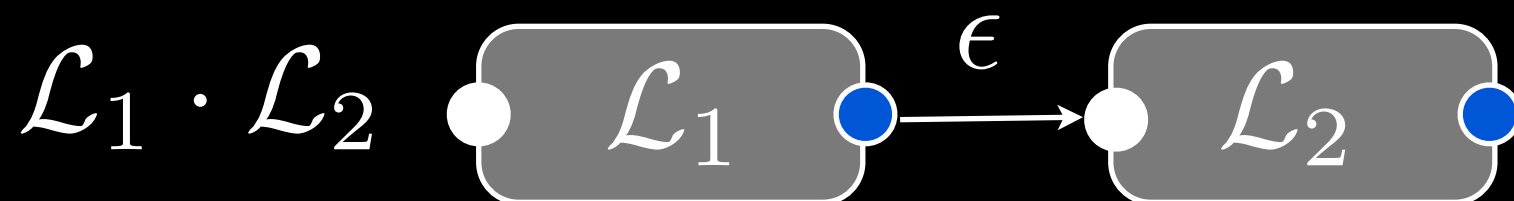
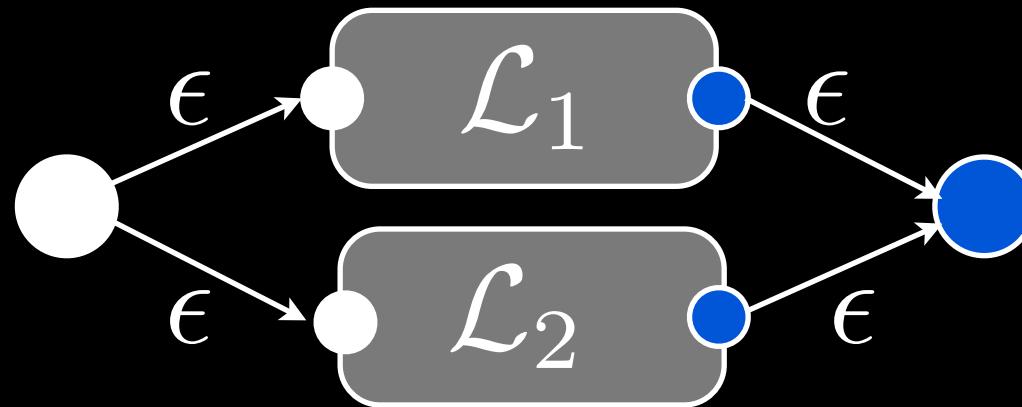
$\{\epsilon\}$ is regular



$\{a\}$ is regular



$\mathcal{L}_1 \cup \mathcal{L}_2$ is regular if \mathcal{L}_1 and \mathcal{L}_2 are regular



Regular Languages

Not all languages are regular!

$$\mathcal{L}_4 = \{ab, aabb, aaabbb, \dots\} = \forall_{n \in [1, \infty)} a^n b^n$$

Over the last two weeks we saw *context-free* languages.

Context-Free Grammar

Context-Free Grammar

$S \rightarrow NP VP$

$NP \rightarrow watashi wa$

$NP \rightarrow hako wo$

$VP \rightarrow NP V$

$V \rightarrow akemasu$

Context-Free Grammar

S

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Context-Free Grammar

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Context-Free Grammar

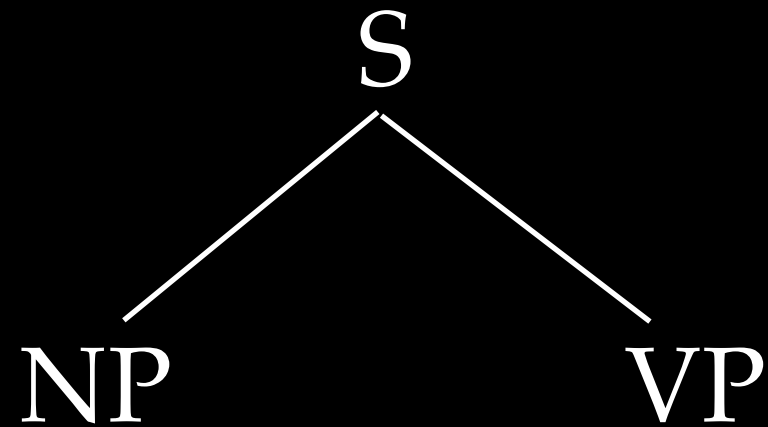
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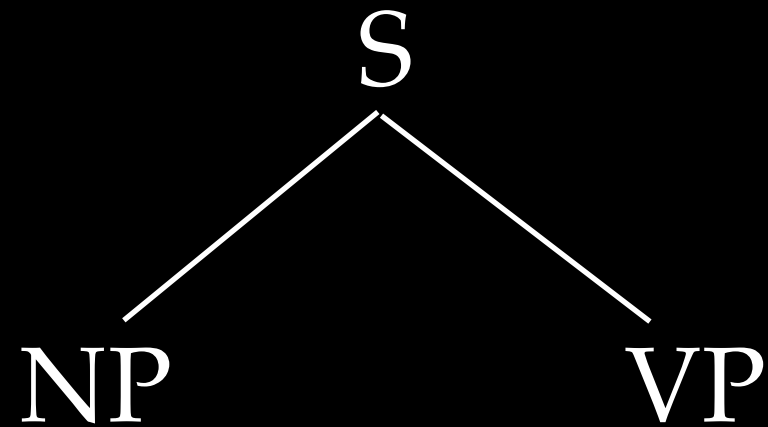
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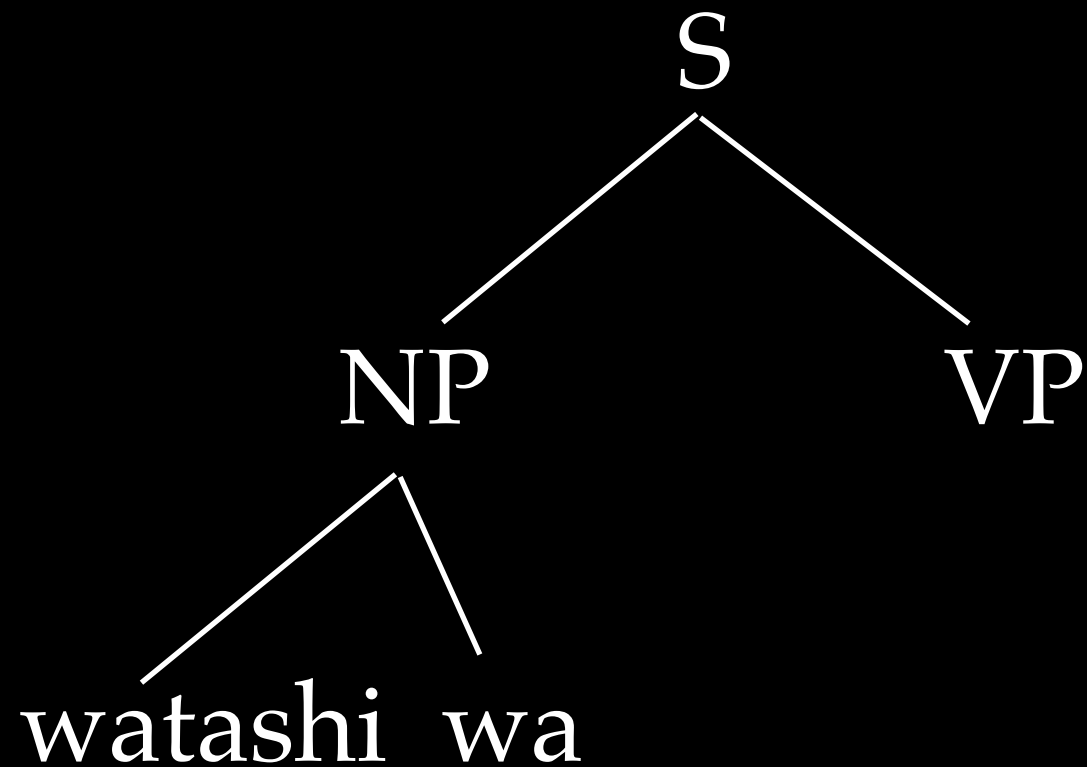
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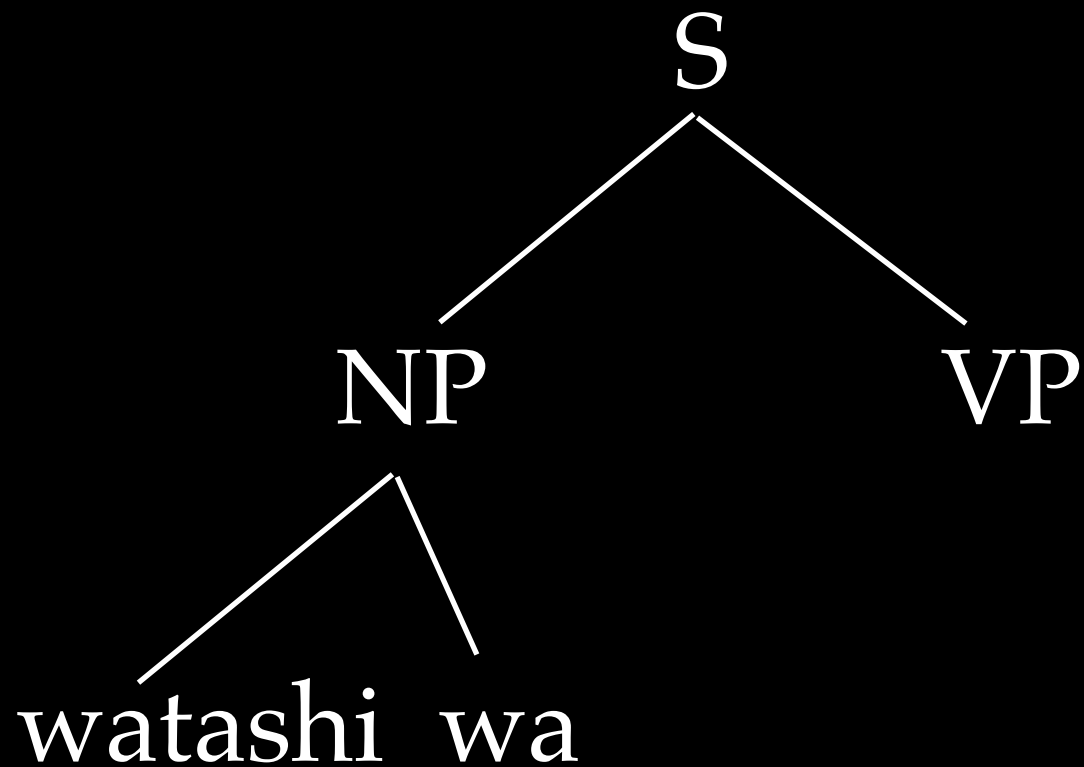
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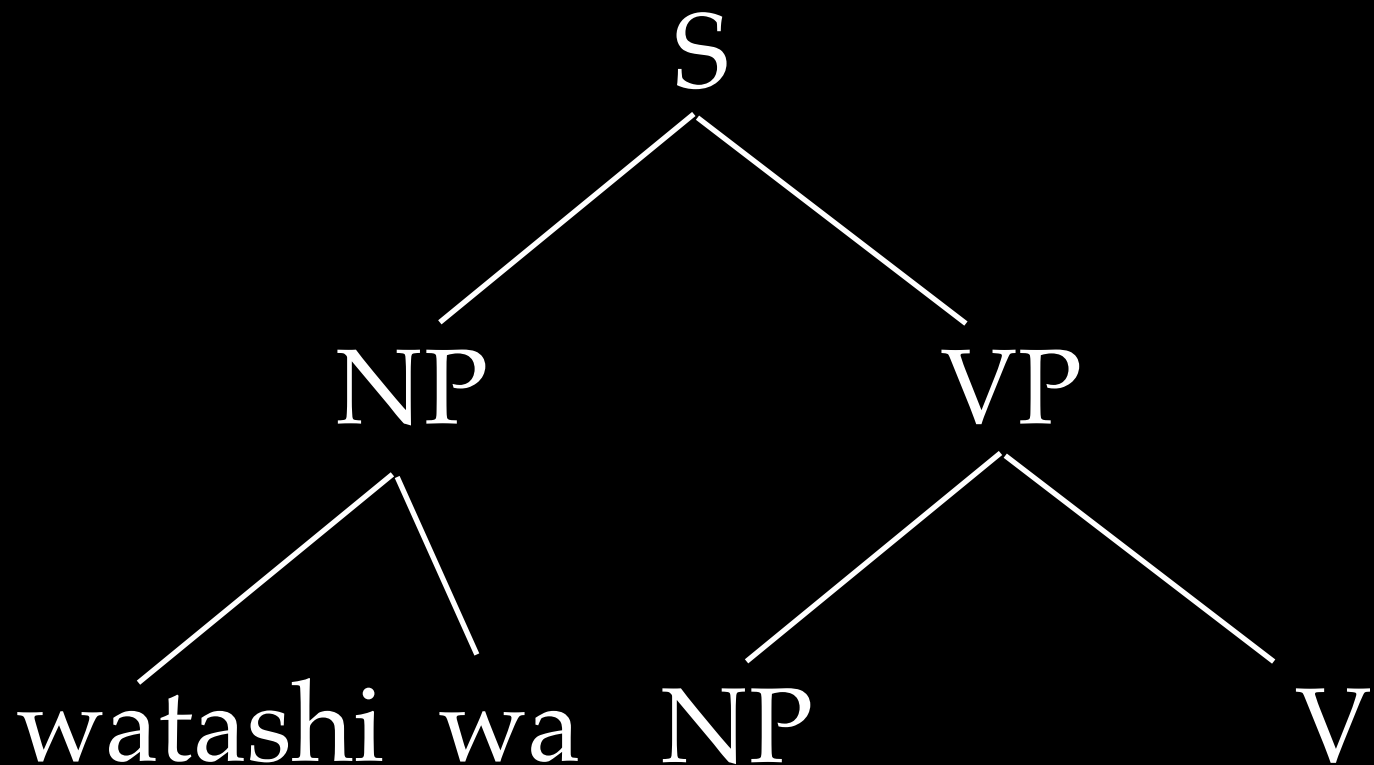
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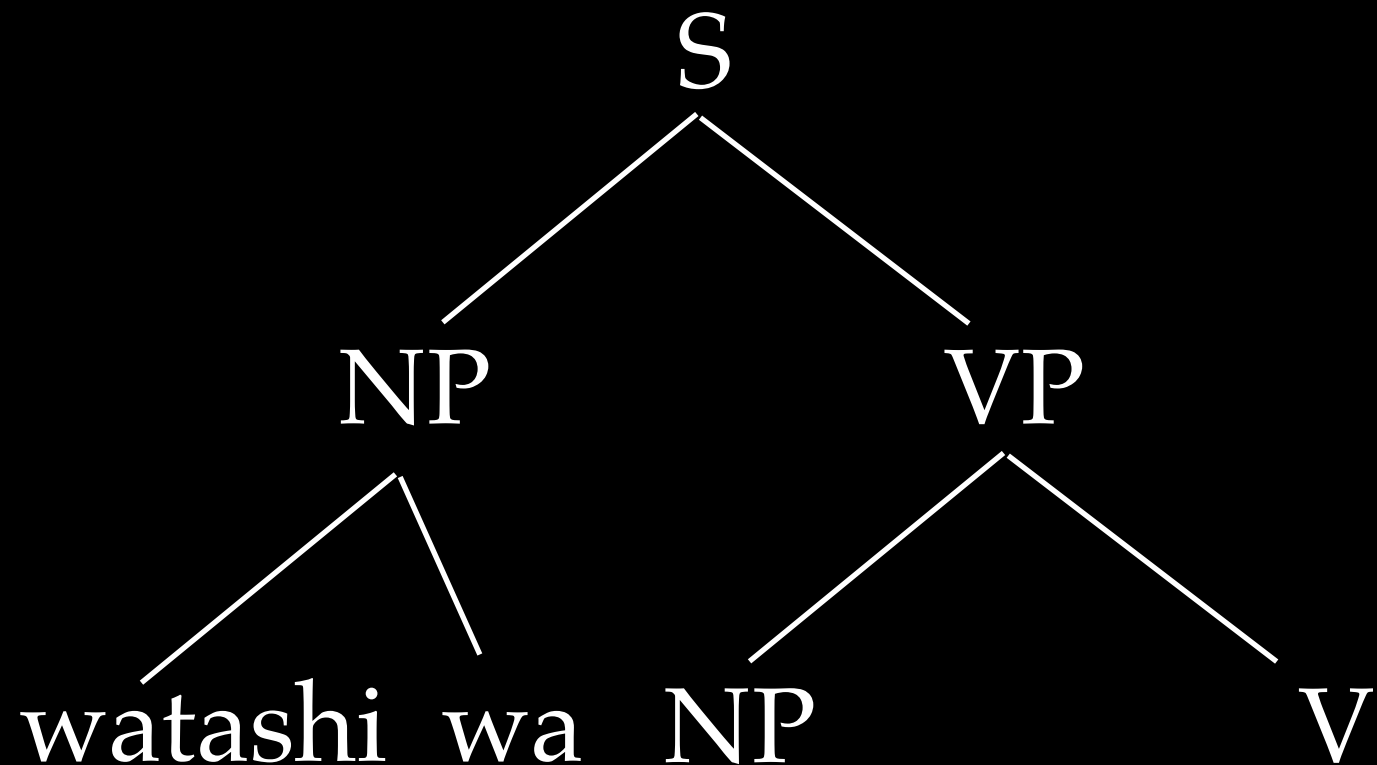
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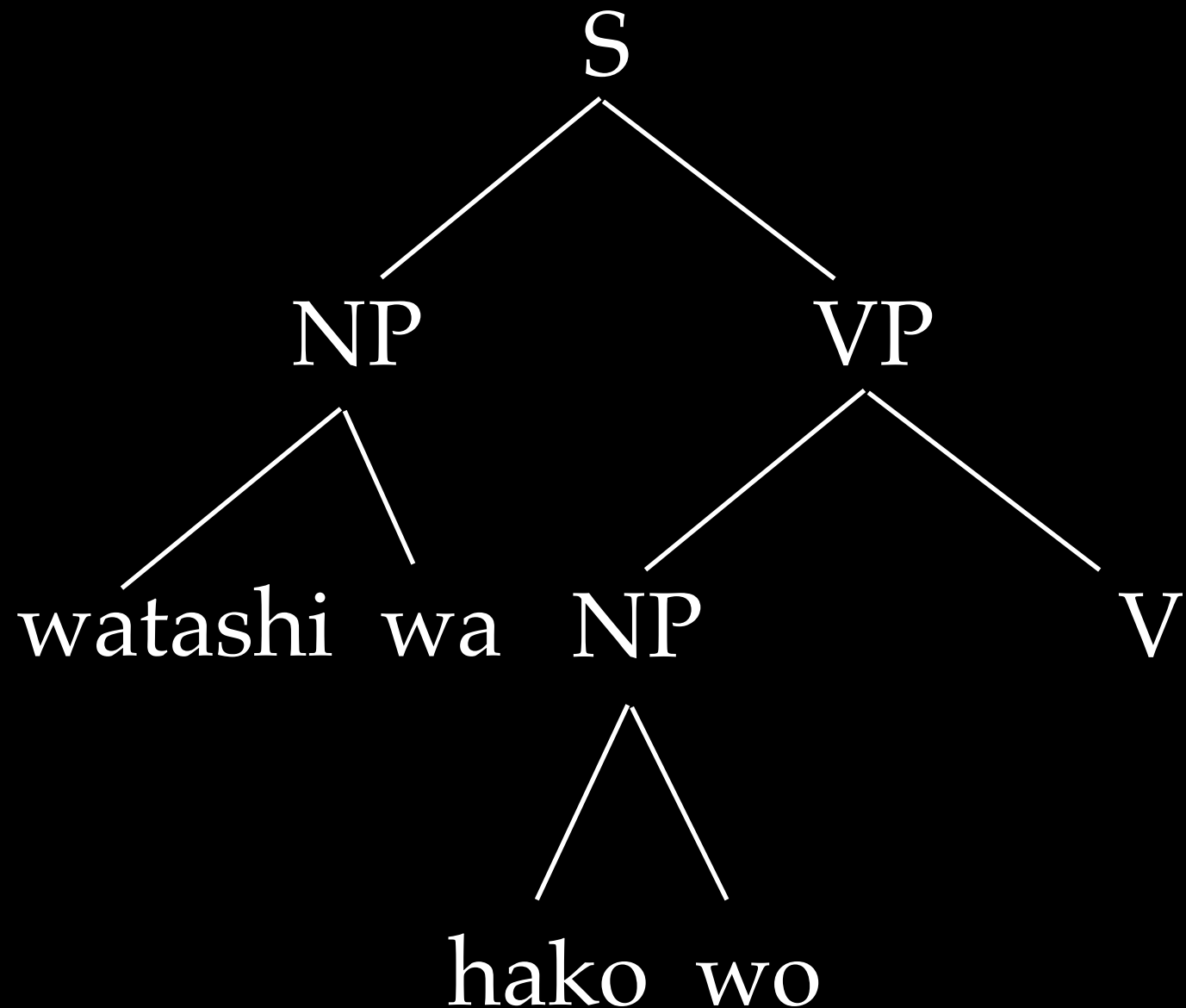
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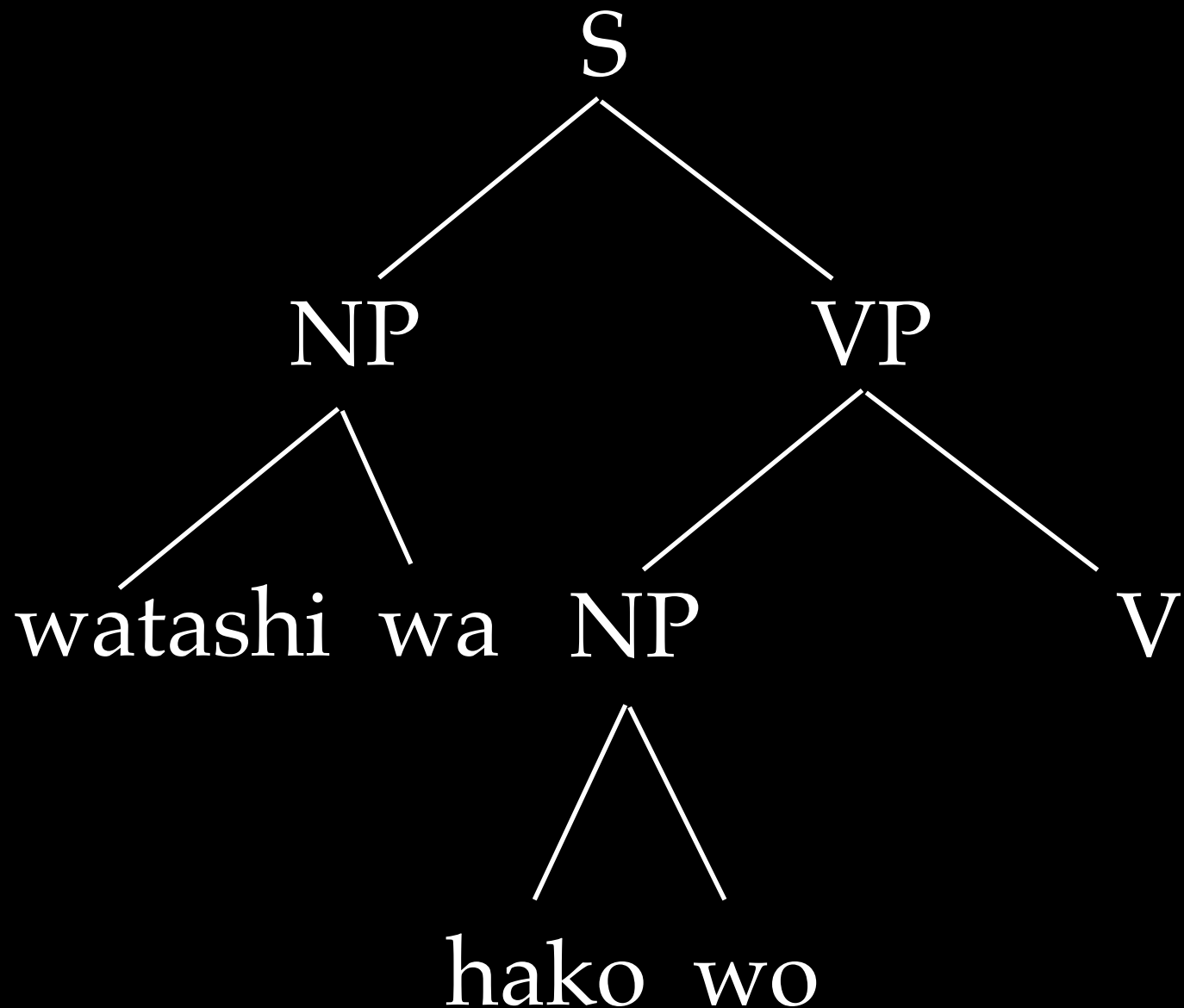
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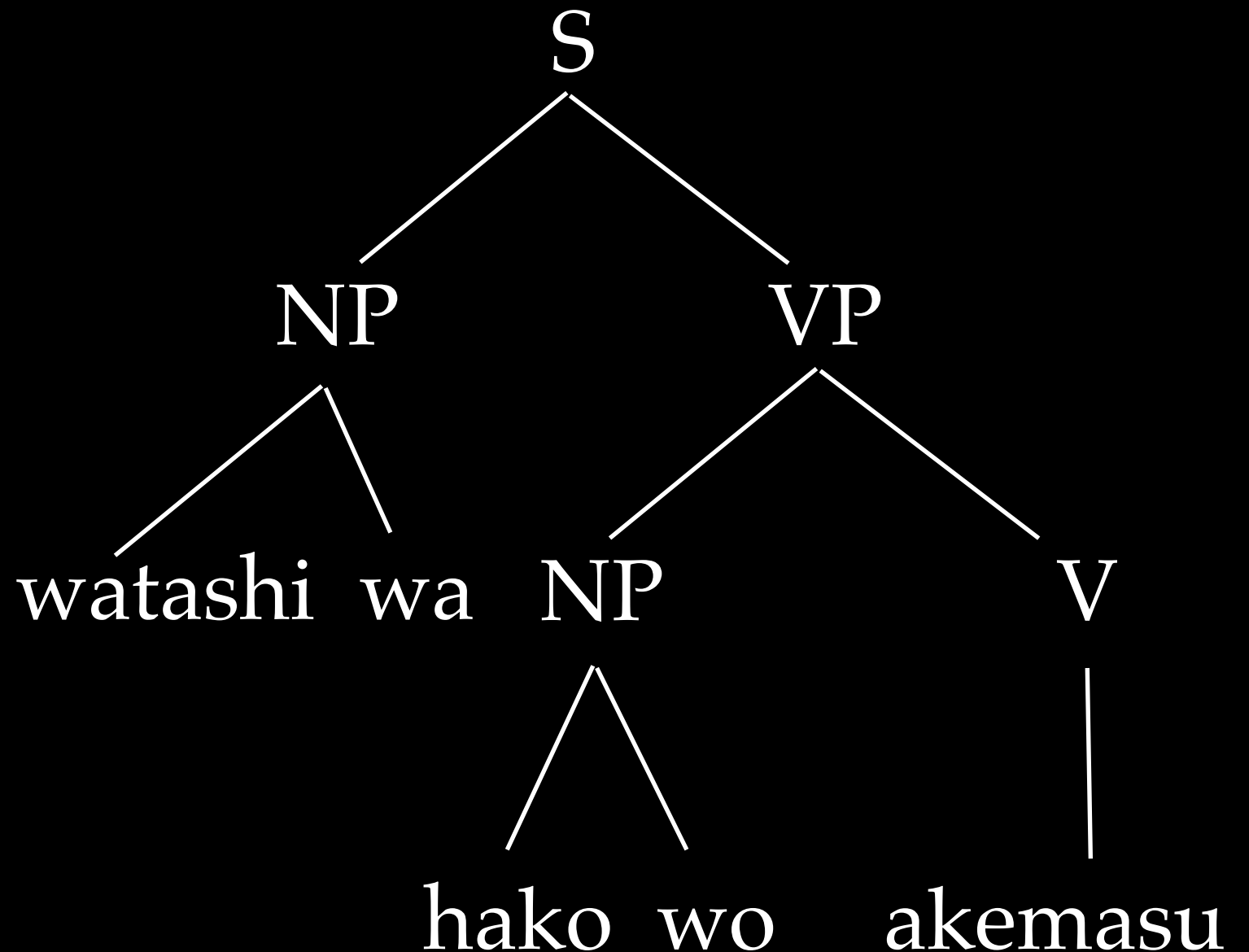
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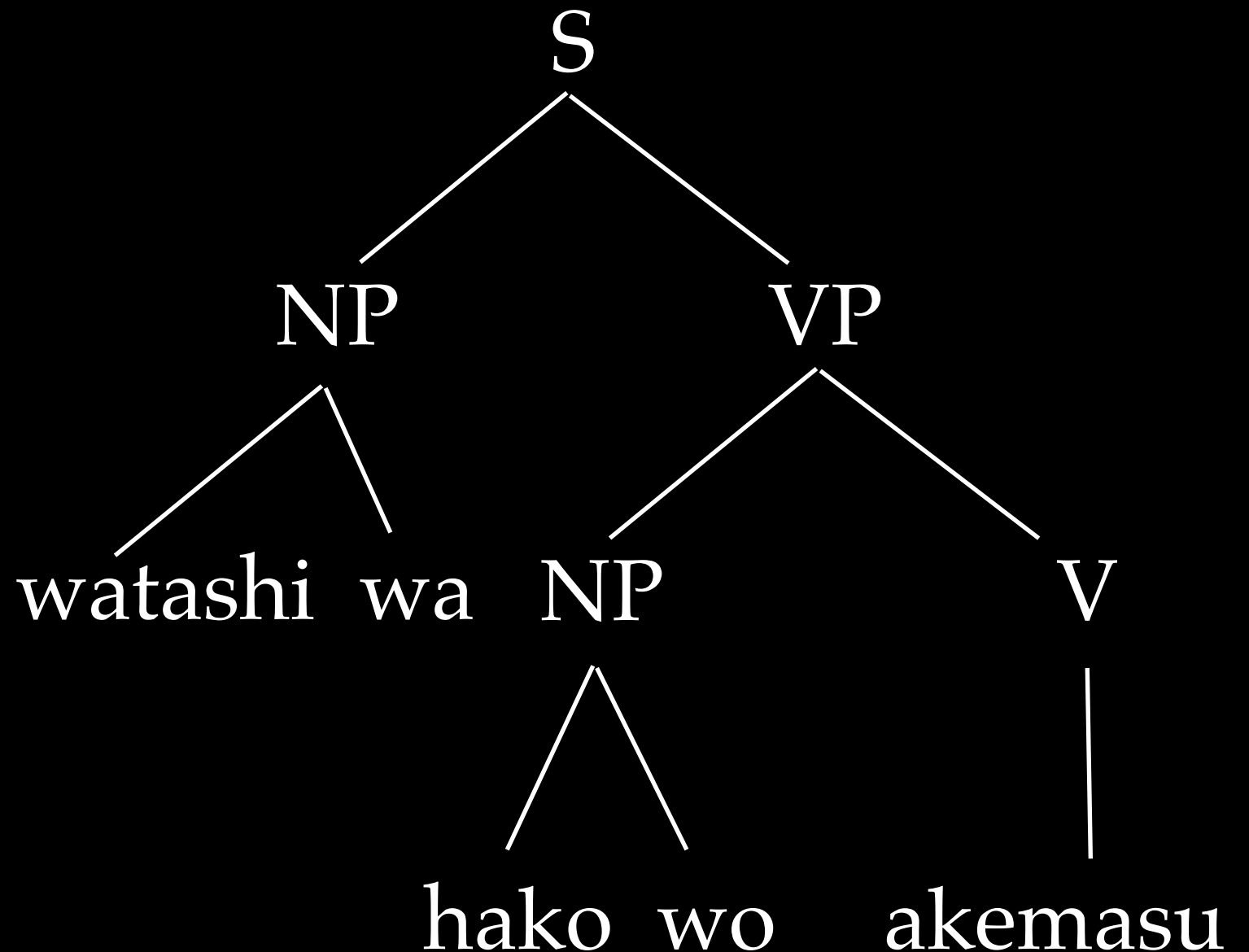
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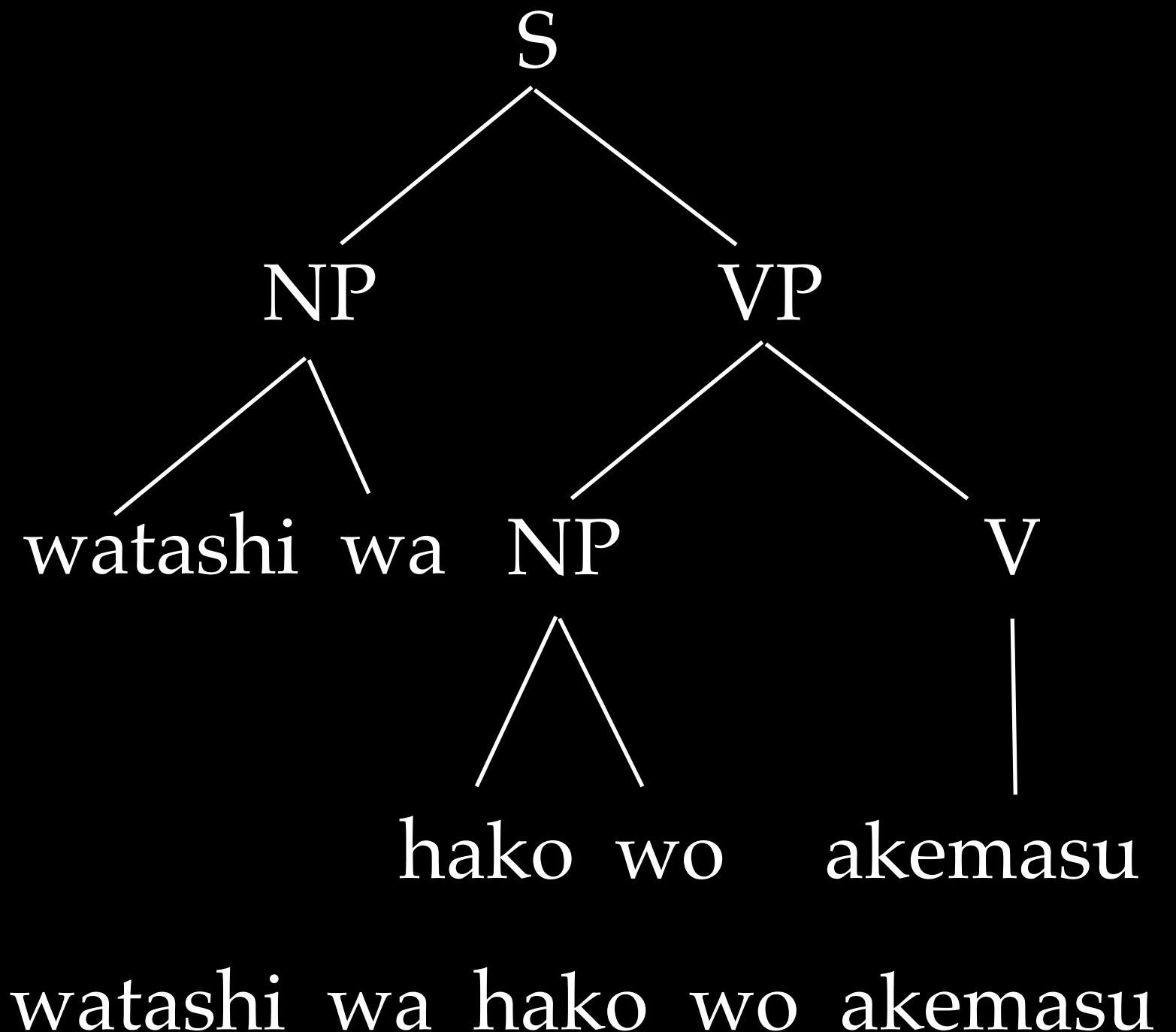
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Context-Free Grammar

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Note: this particular grammar
is finite, hence regular.

$\left\{ \begin{array}{l} watashi wa watashi wa akemasu \\ watashi wa hako wo akemasu \\ hako wo hako wo akemasu \\ hako wo watashi wa akemasu \end{array} \right\}$

Context-Free Grammar

$S \rightarrow A B$

$S \rightarrow A S B$

$A \rightarrow a$

$B \rightarrow b$

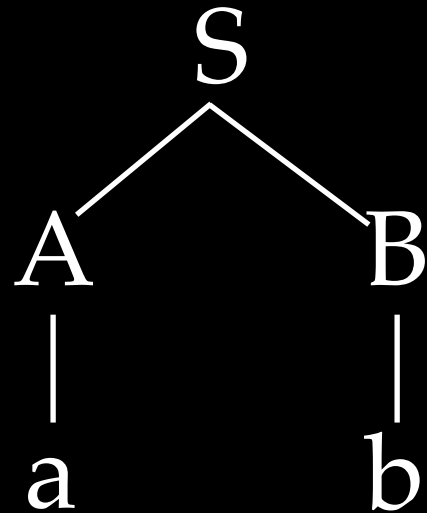
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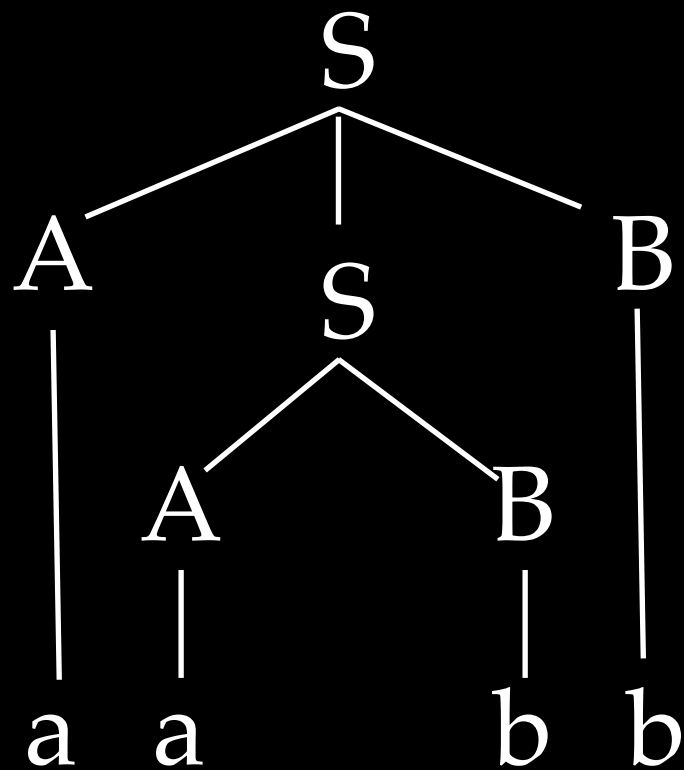
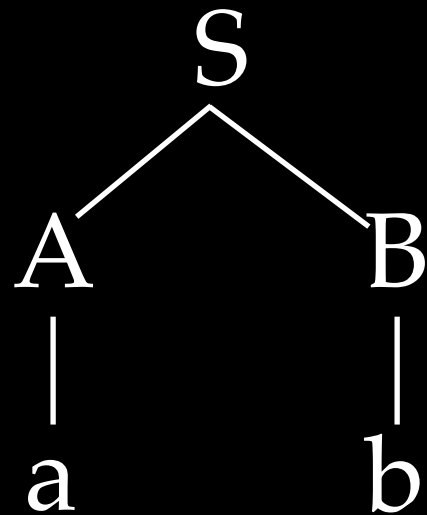
Context-Free Grammar

$S \rightarrow AB$

$S \rightarrow ASB$

$A \rightarrow a$

$B \rightarrow b$



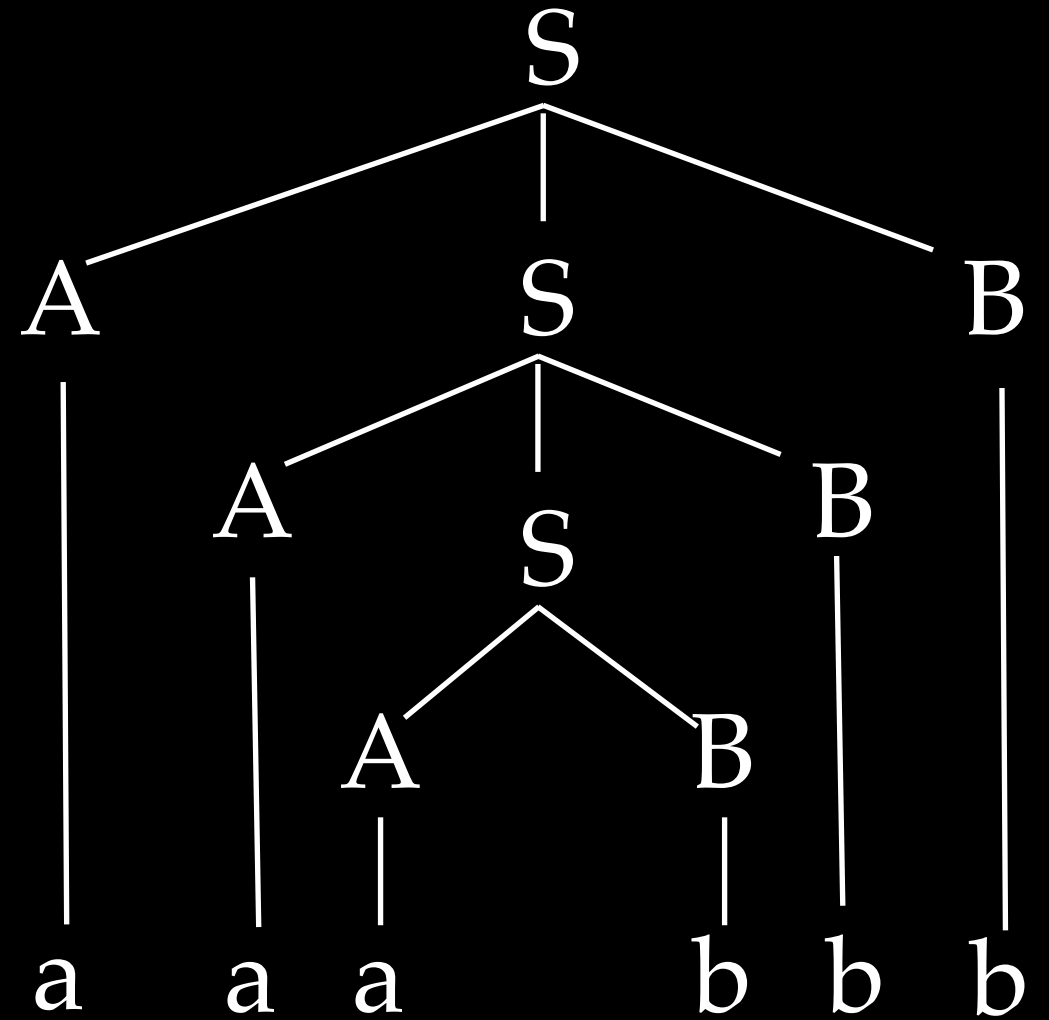
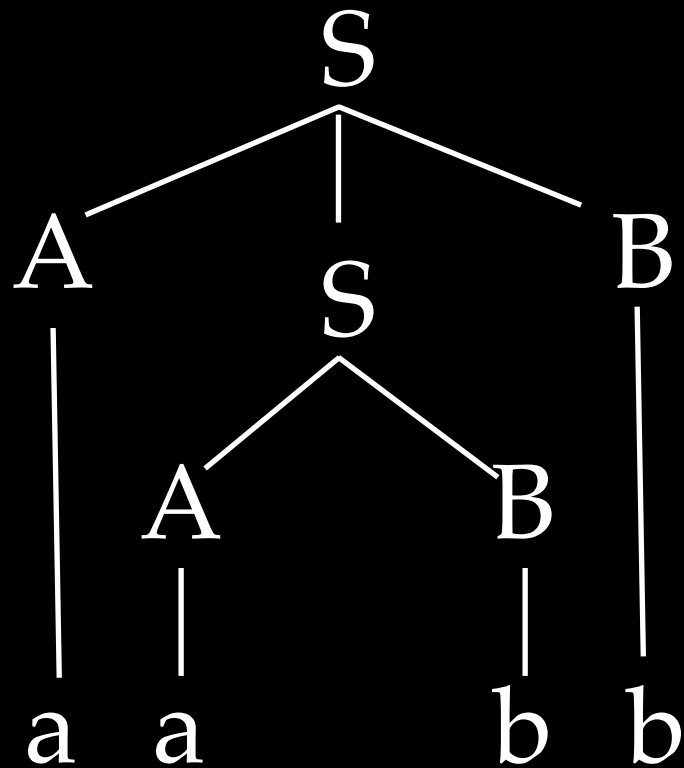
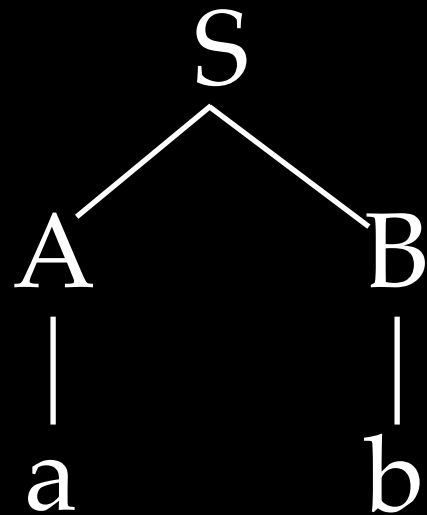
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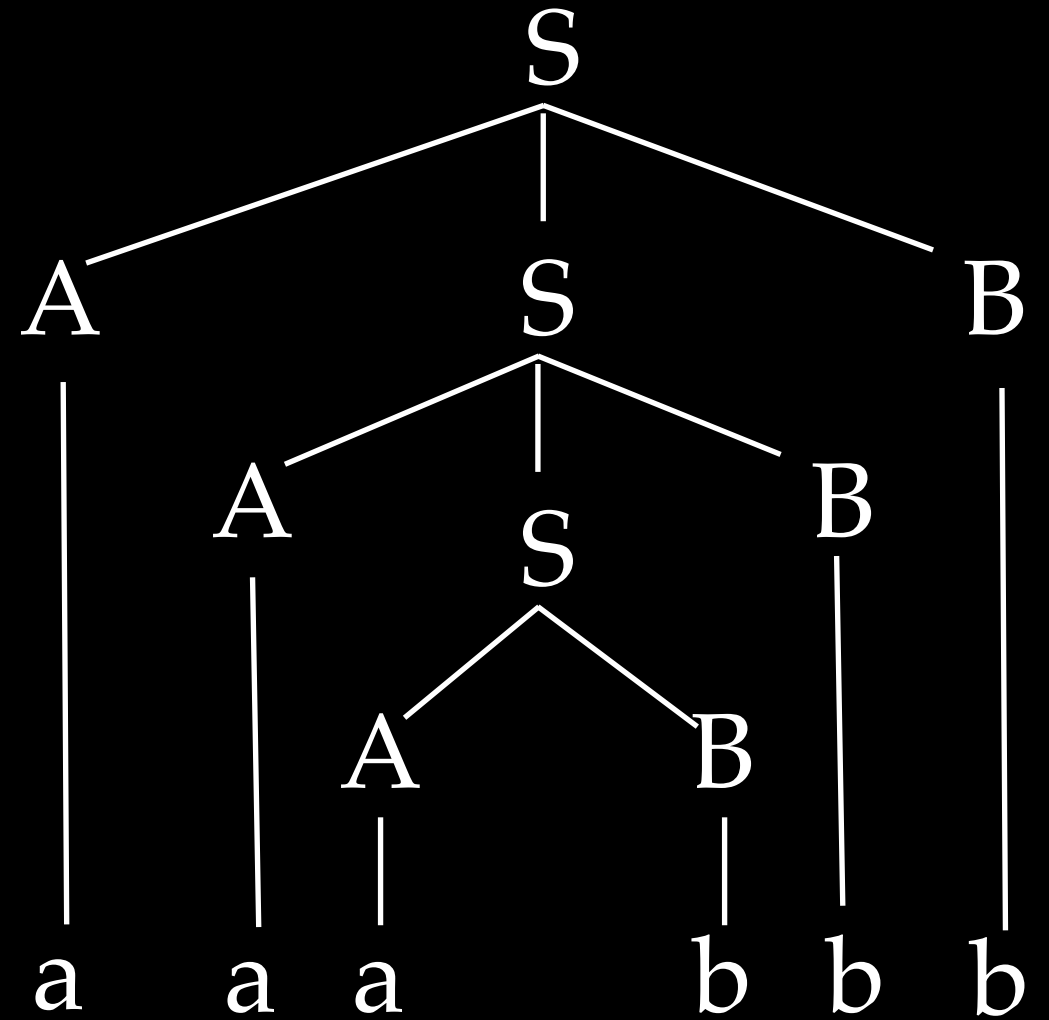
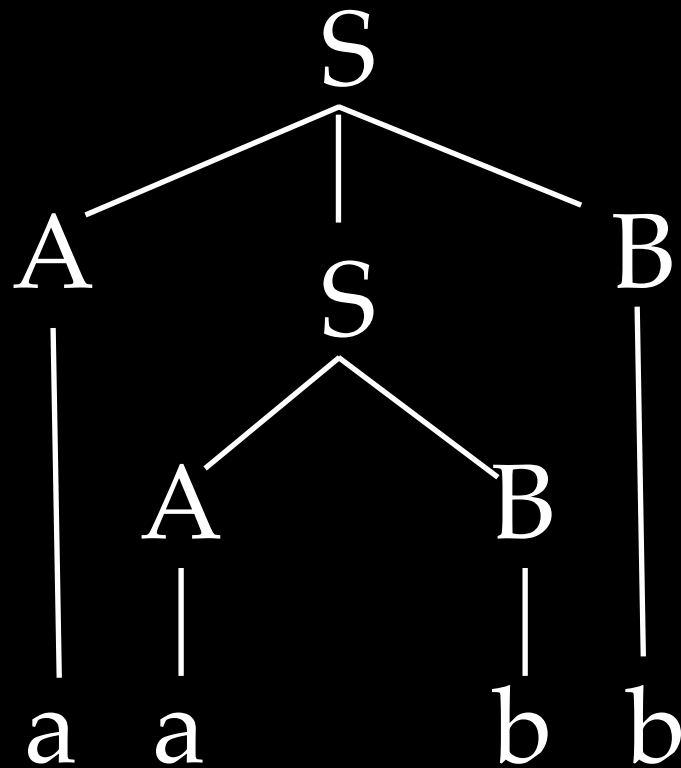
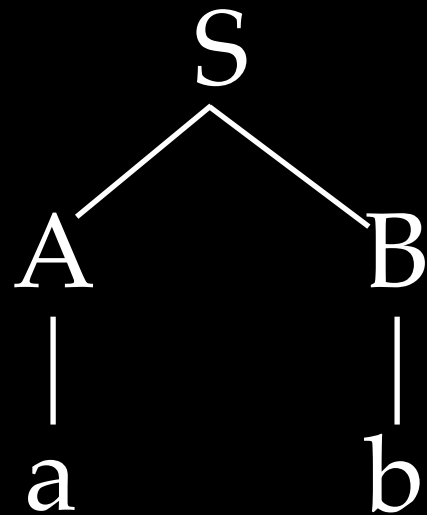
$A \rightarrow a$

$B \rightarrow b$



Context-Free Grammar

$S \rightarrow AB$
 $S \rightarrow ASB$
 $A \rightarrow a$
 $B \rightarrow b$



$$\mathcal{L}_4 = \{ab, aabb, aaabbb, \dots\} = \forall_{n \in [1, \text{inf})} a^n b^n$$

Context-Free vs. Regular

Context-Free vs. Regular

- Regular languages \subset Context-free languages

Context-Free vs. Regular

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- Composition of languages:

Context-Free vs. Regular

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 - Regular \cap Regular = Regular

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$$A \rightarrow BC \in \mathcal{G}_{CFL}$$

Context-Free vs. Regular

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 - Regular \cap Regular = Regular
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$$A \rightarrow BC \in \mathcal{G}_{CFL} \qquad s, r, t \in \text{states}(\mathcal{G}_{RL})$$

Context-Free vs. Regular

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$${}_s A_t \rightarrow {}_s B_r r C_t \in \mathcal{G}_{CFL} \cap \mathcal{G}_{RL}$$

Context-Free vs. Regular

- Regular languages \subset Context-free languages
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Bar-Hillel 1964

Context-Free vs. Regular

- Regular languages \subset Context-free languages
- Composition of languages:
 - Regular \cap Regular = Regular
 - Regular \cap Context-free = Context-free
 - Context-free \cap Context-free = Undecidable

$$A \rightarrow BC \in \mathcal{G}_{CFL} \qquad s, r, t \in \text{states}(\mathcal{G}_{RL})$$

$${}_s A_t \rightarrow {}_s B_r r C_t \in \mathcal{G}_{CFL} \cap \mathcal{G}_{RL}$$

Bar-Hillel 1964

Synchronous Context-Free Grammar

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Synchronous Context-Free Grammar

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$NP \rightarrow watashi wa$

$NP \rightarrow hako wo$

$VP \rightarrow NP V$

$V \rightarrow akemasu$

$S \rightarrow NP VP$

$NP \rightarrow I$

$NP \rightarrow the\ box$

$VP \rightarrow V NP$

$V \rightarrow open$

Synchronous Context-Free Grammar

$S \rightarrow NP_1 VP_2 / NP_1 VP_2$

$NP \rightarrow watashi wa / I$

$NP \rightarrow hako wo / \text{the box}$

$VP \rightarrow NP_1 V_2 / V_1 NP_2$

$V \rightarrow akemasu / \text{open}$

Synchronous Context-Free Grammar

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Synchronous Context-Free Grammar

S

S

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Synchronous Context-Free Grammar

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Synchronous Context-Free Grammar

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Synchronous Context-Free Grammar



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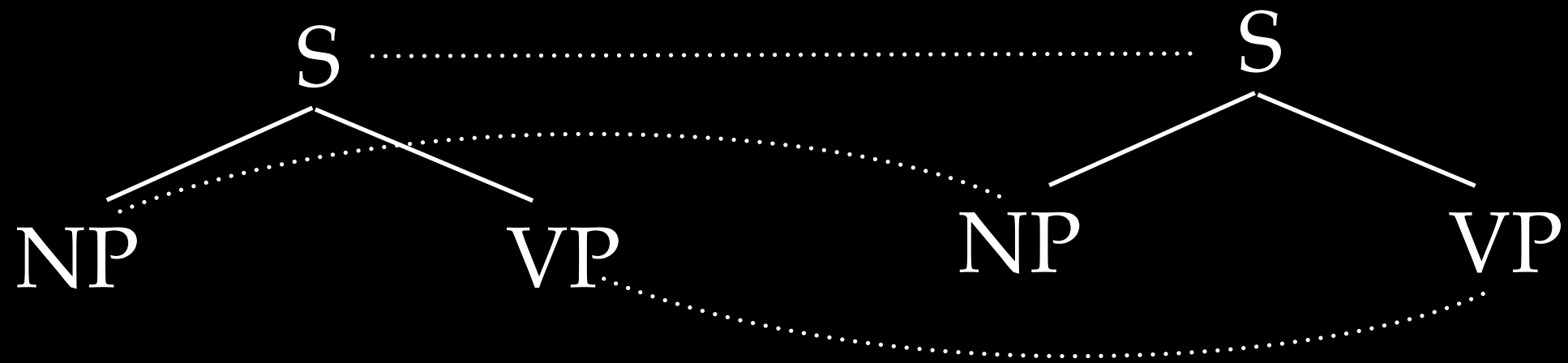
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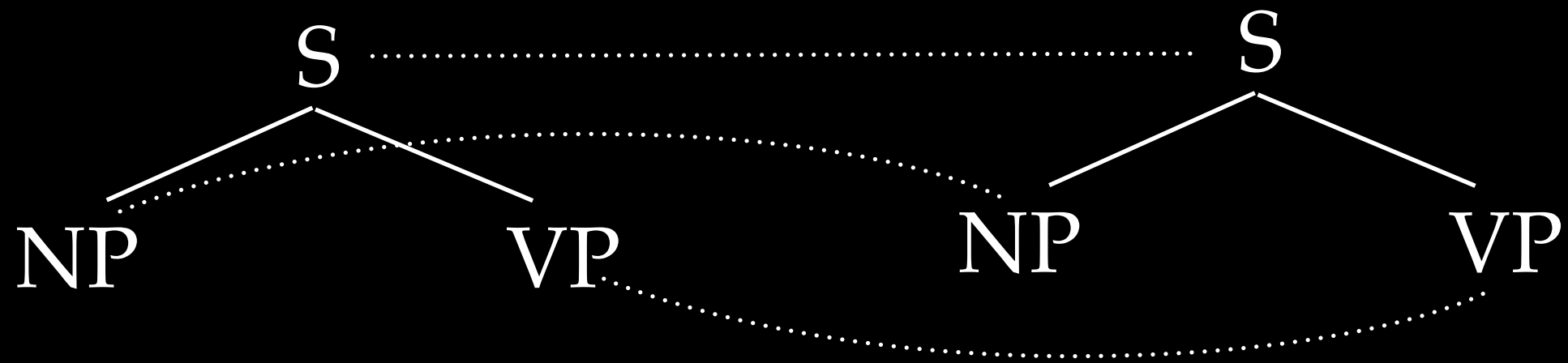
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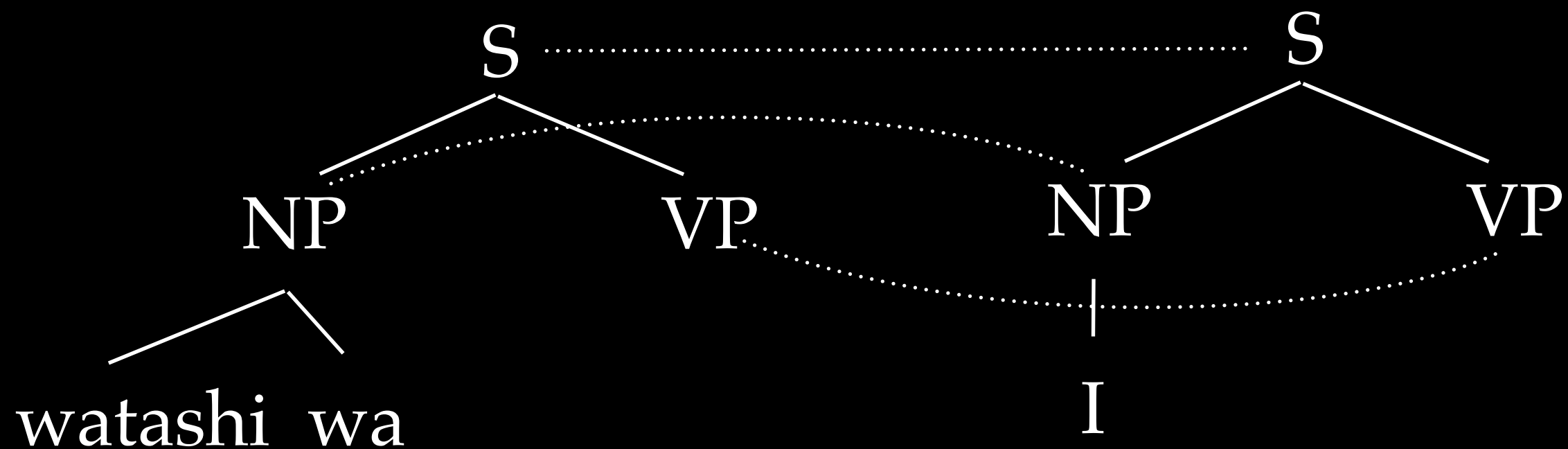
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Synchronous Context-Free Grammar



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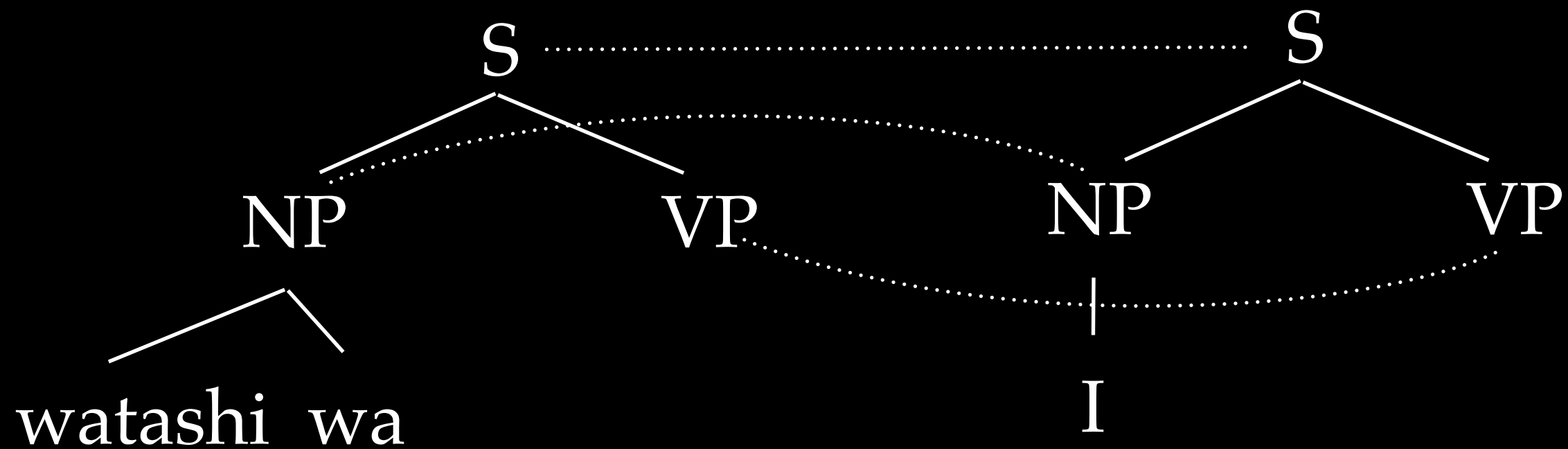
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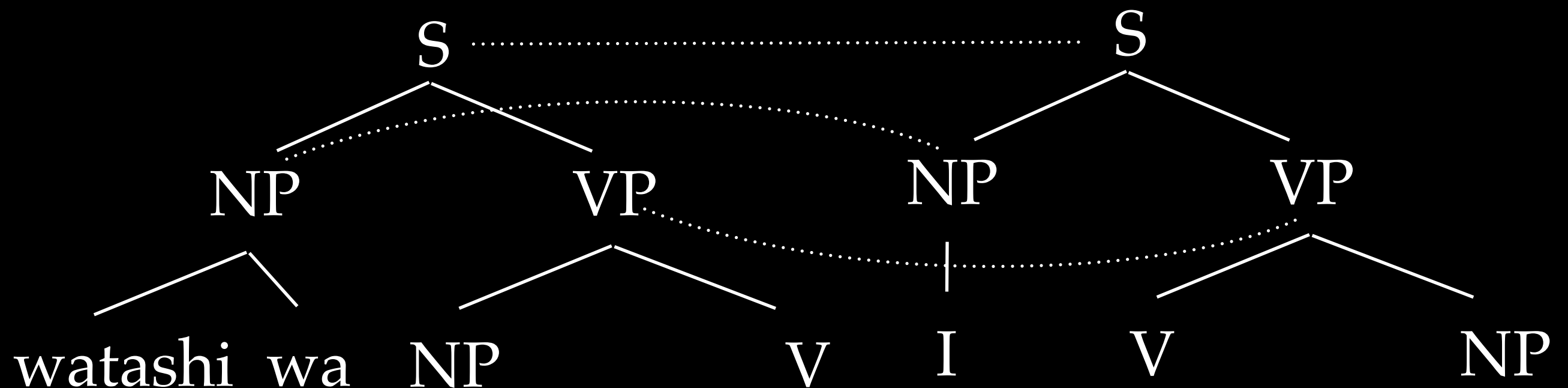
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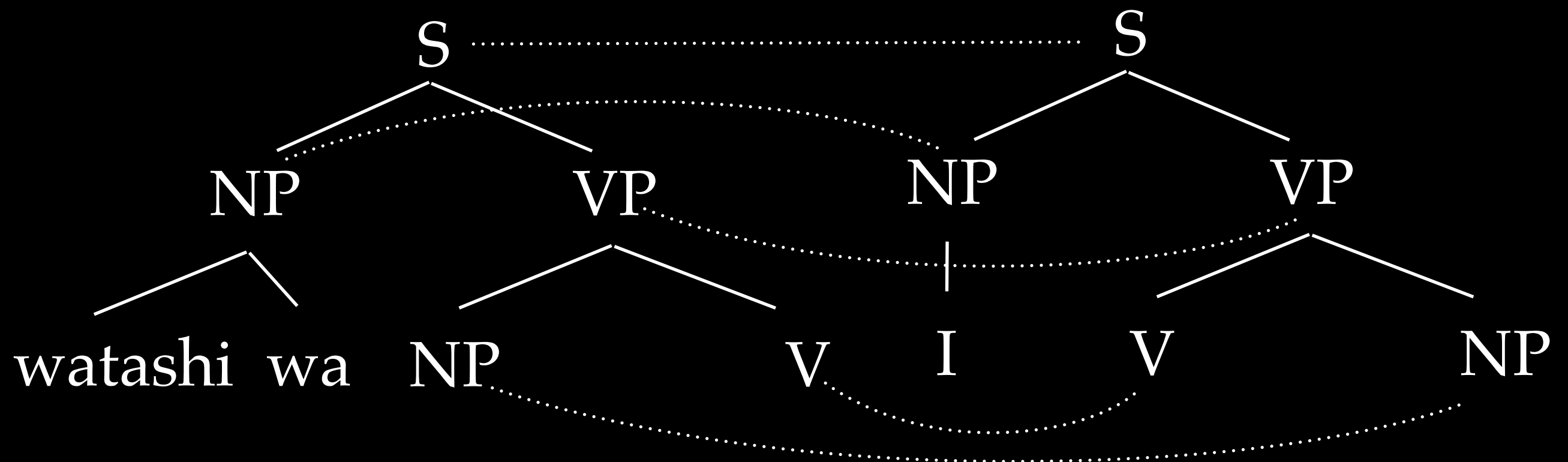
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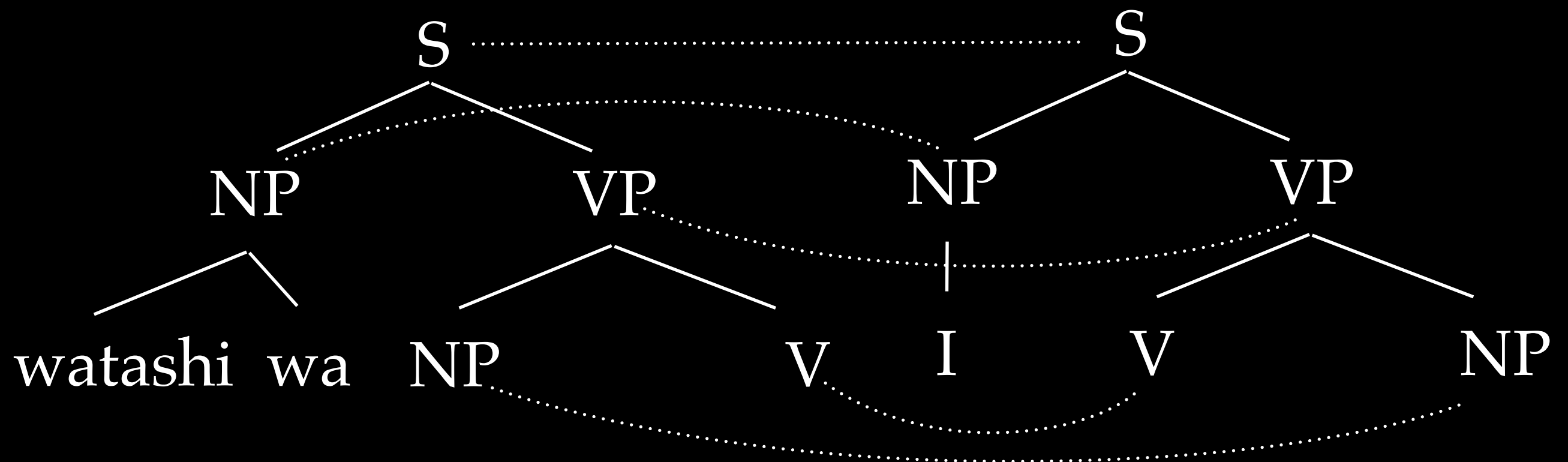
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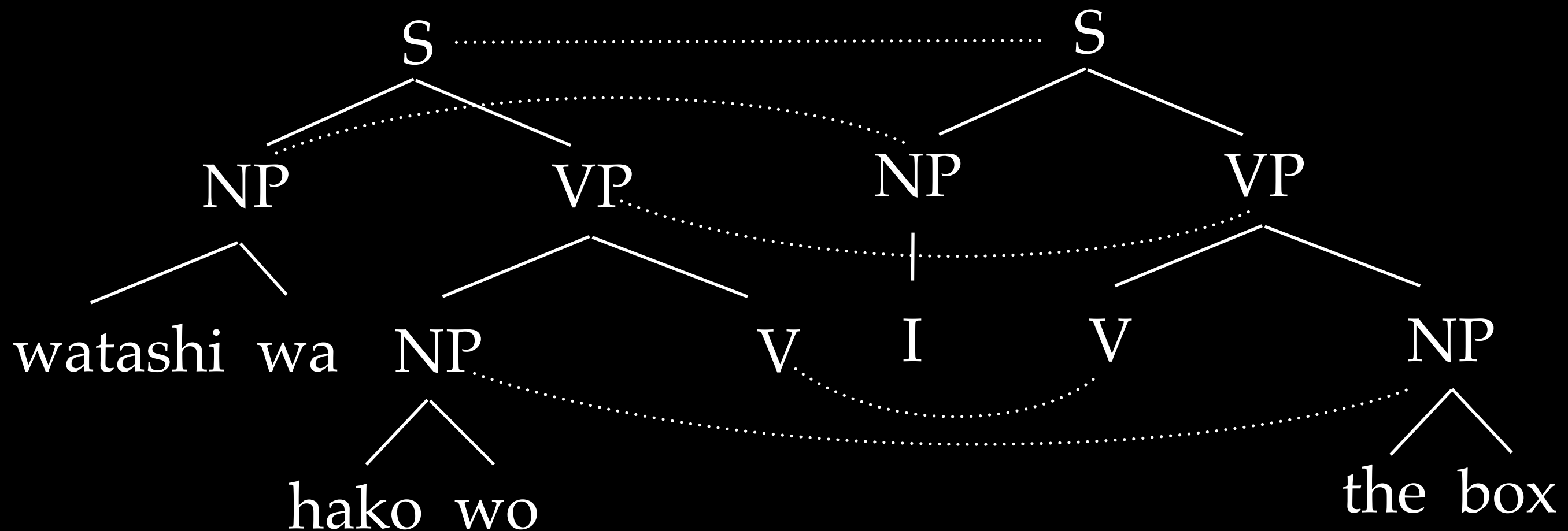
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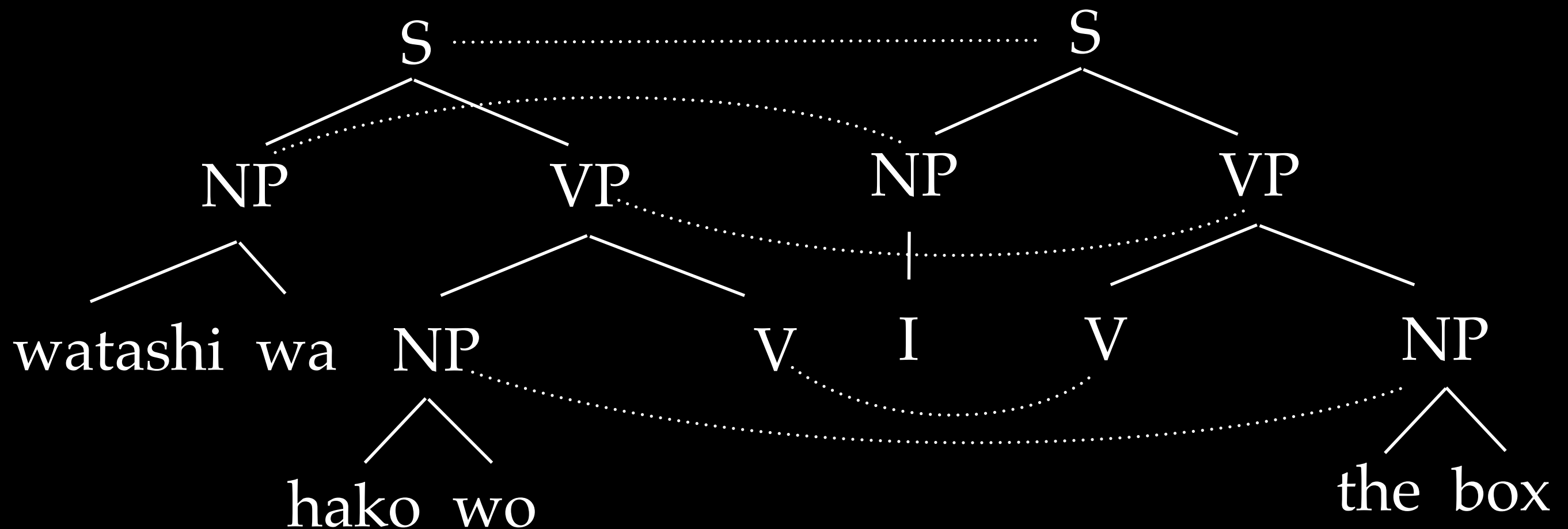
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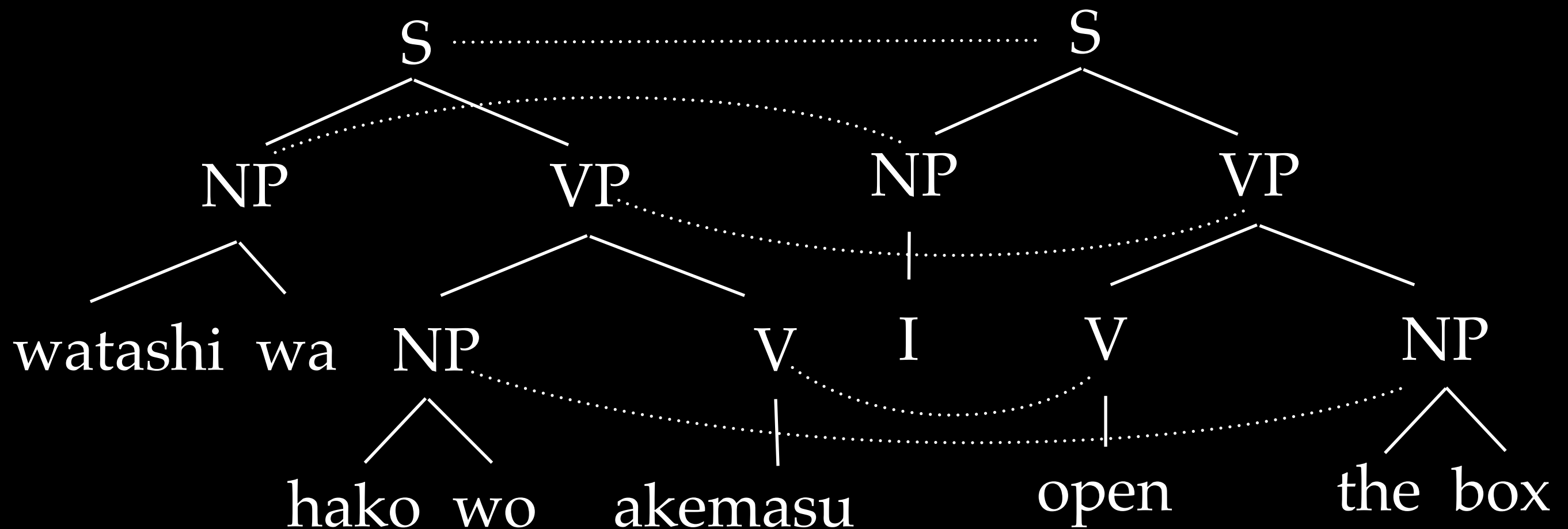
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Synchronous Context-Free Grammar



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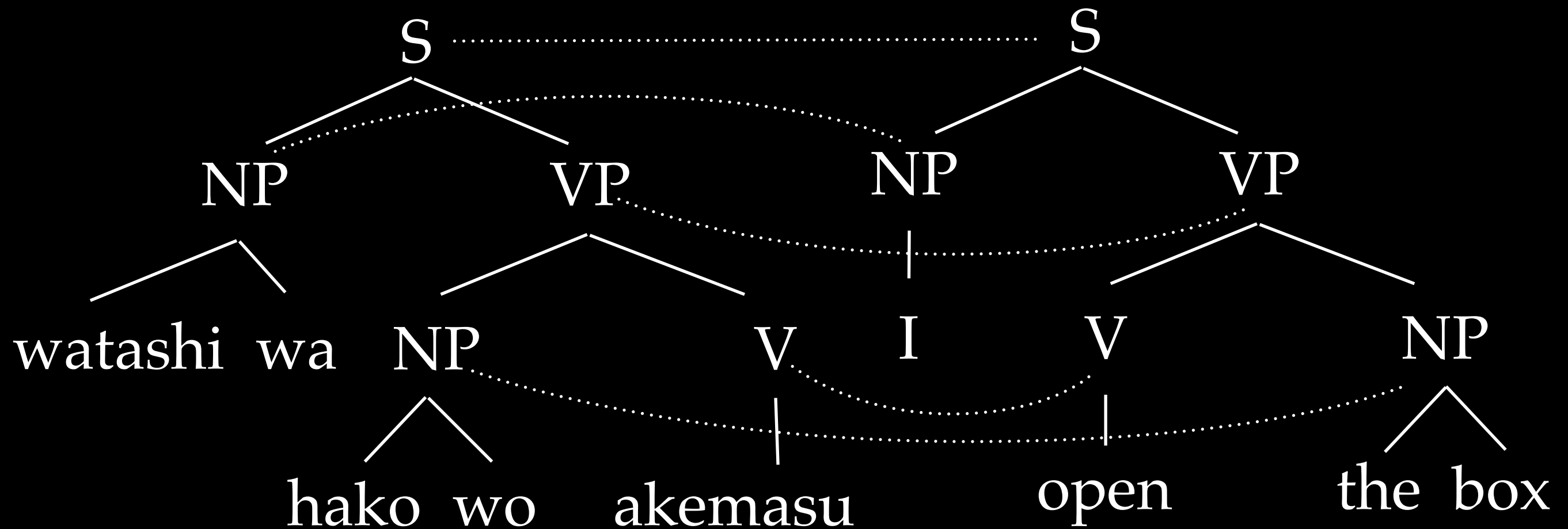
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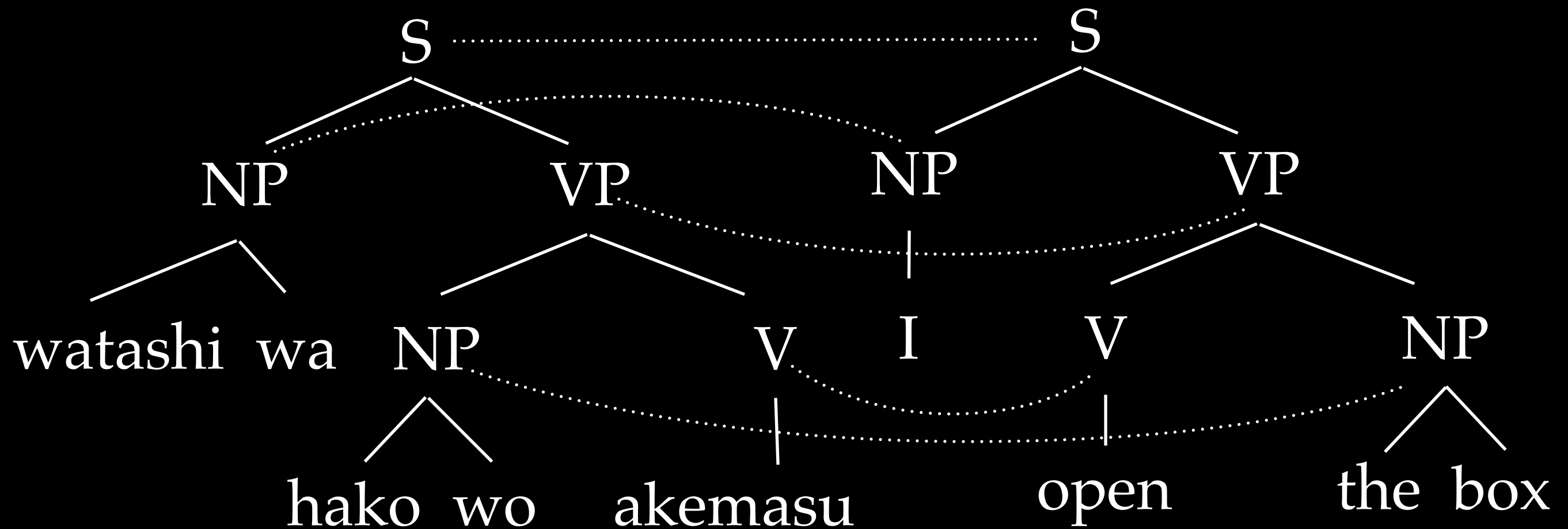
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Synchronous Context-Free Grammar

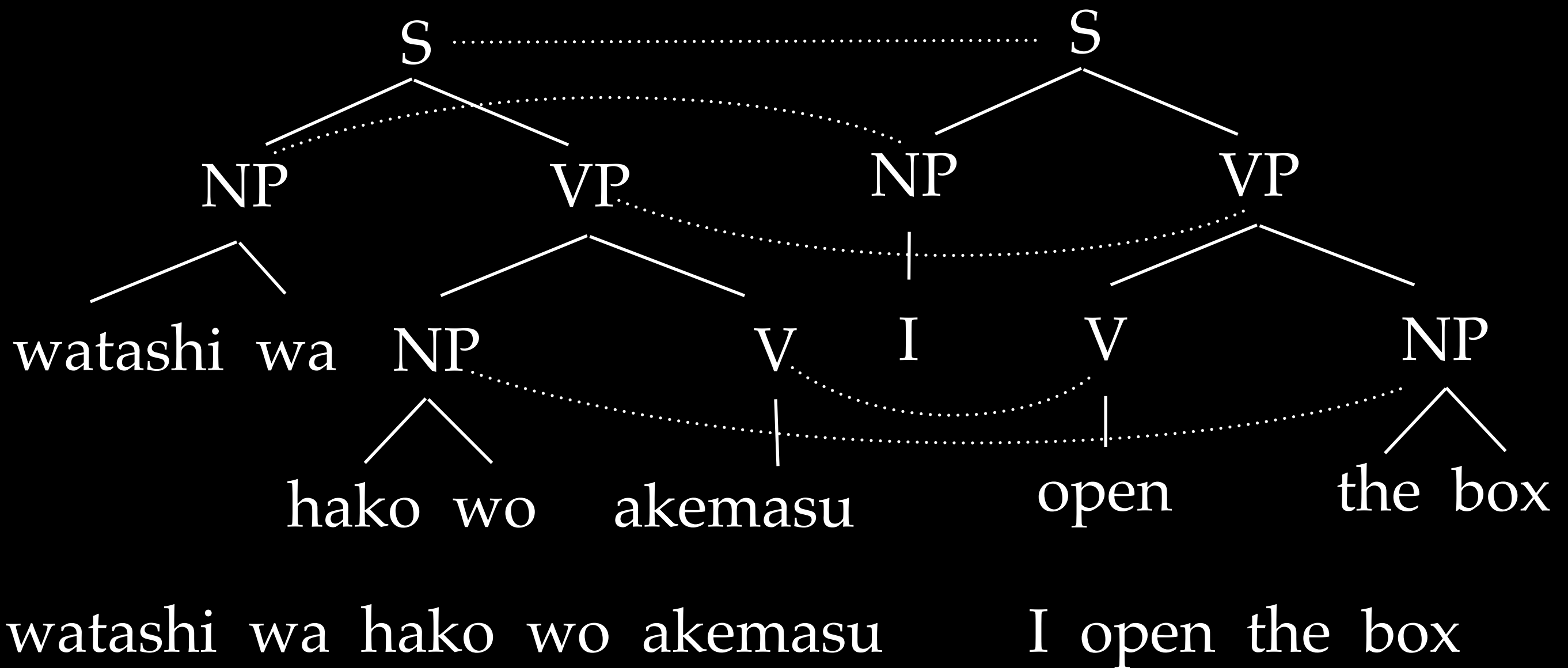


Synchronous Context-Free Grammar



watashi wa hako wo akemasu

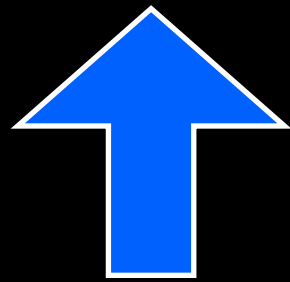
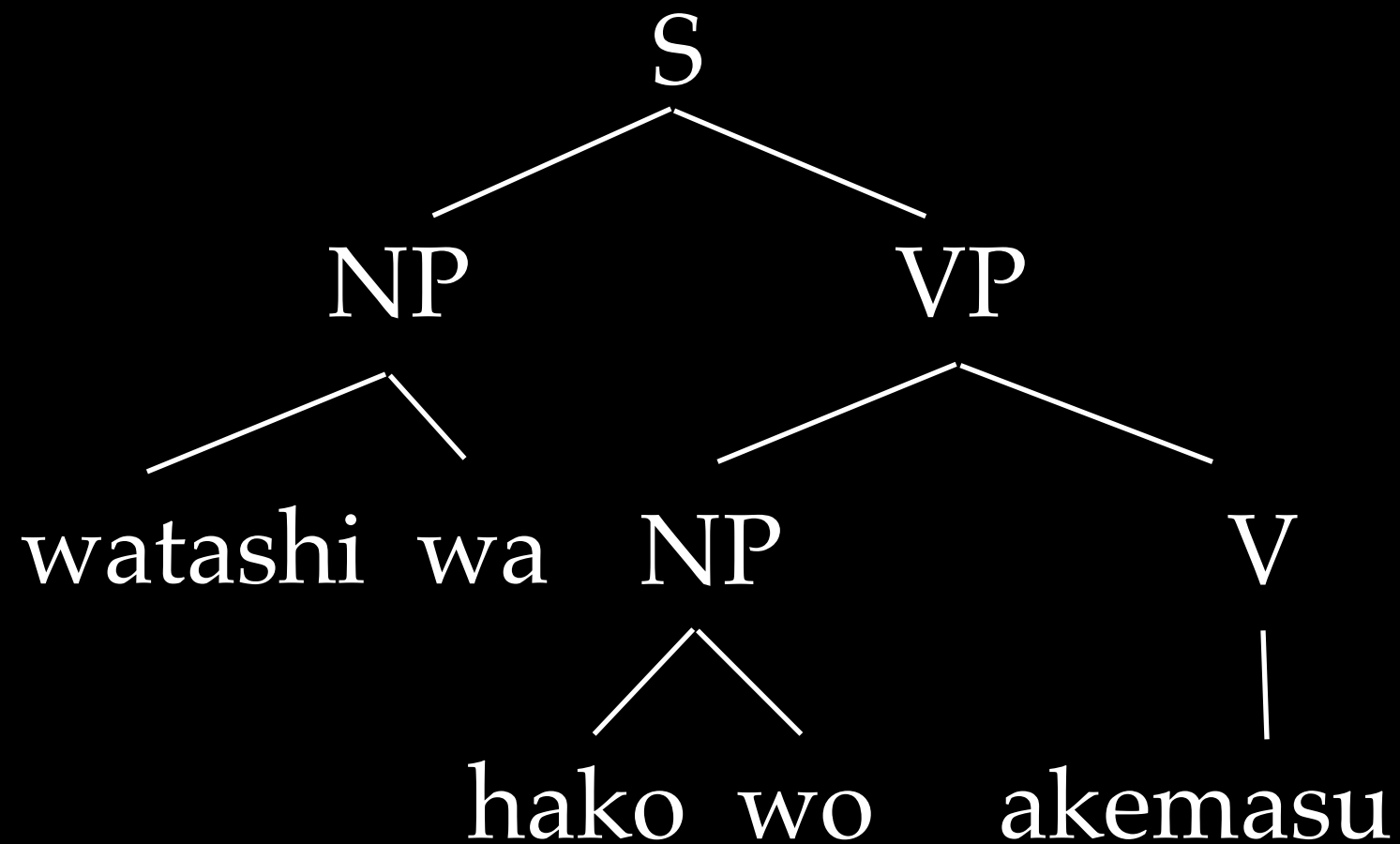
Synchronous Context-Free Grammar



Translation is Parsing

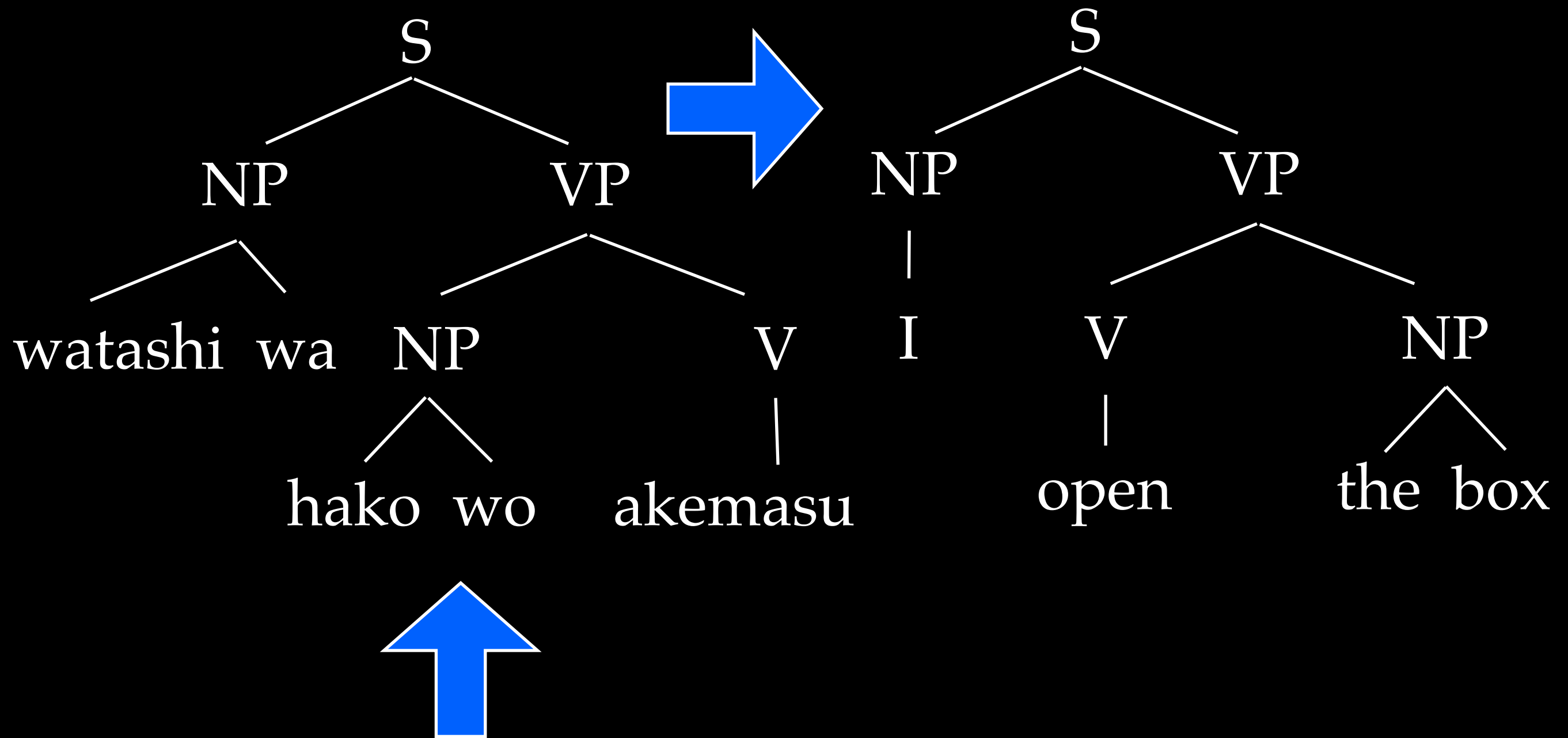
watashi wa hako wo akemasu

Translation is Parsing



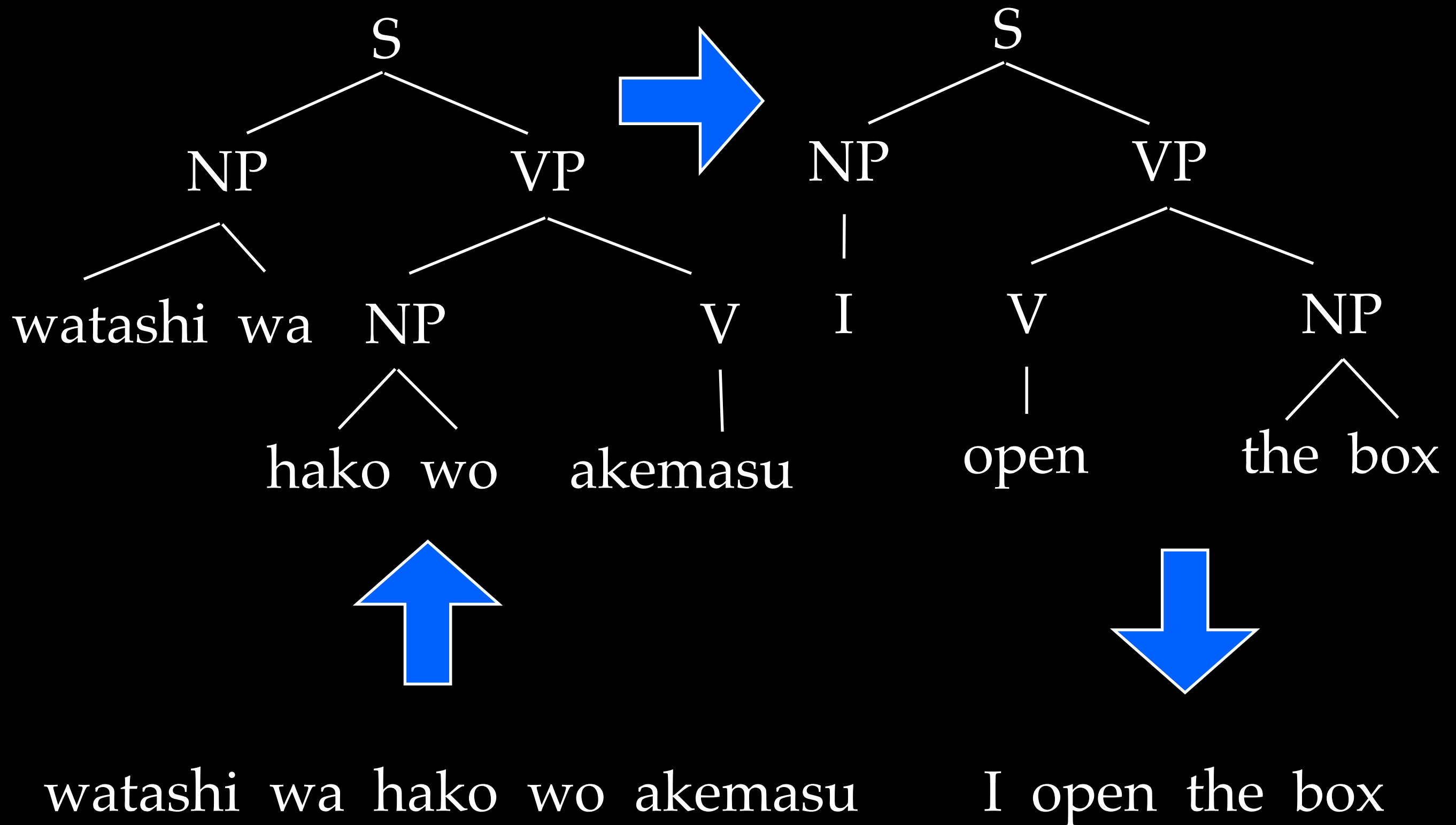
watashi wa hako wo akemasu

Translation is Parsing



watashi wa hako wo akemasu

Translation is Parsing



Translation is Parsing

Translation is Parsing

- How many parses of a sentence are there?

Translation is Parsing

- How many parses of a sentence are there?
 - For binary grammar: Catalan number.

Translation is Parsing

- How many parses of a sentence are there?
 - For binary grammar: Catalan number. $O(\frac{(2n)!}{(n+1)!n!})$

Translation is Parsing

- How many parses of a sentence are there?
 - For binary grammar: Catalan number. $O(\frac{(2n)!}{(n+1)!n!})$
- Dynamic programming to the rescue!

Parsing

Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

I₁ saw₂ her₃ duck₄

Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

I₁ saw₂ her₃ duck₄

Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

I₁

saw₂ her₃ duck₄

Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

I₁

saw₂ her₃ duck₄

Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$PRP_{0,1} \leftarrow (w_1 = I) \wedge (PRP \rightarrow I)$$

I₁

saw₂ her₃ duck₄

Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$PRP_{0,1} \leftarrow (w_1 = I) \wedge (PRP \rightarrow I)$$

$PRP_{0,1}$

I_1

saw₂ her₃ duck₄

Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$PRP_{0,1}$



I₁

saw₂

her₃

duck₄

Parsing

$NN \rightarrow \text{duck}$

$NP \rightarrow PRP\$ NN$

$PRP \rightarrow \text{her}$

$PRP \rightarrow I$

$PRP\$ \rightarrow \text{her}$

$S \rightarrow PRP VP$

$SBAR \rightarrow PRP VB$

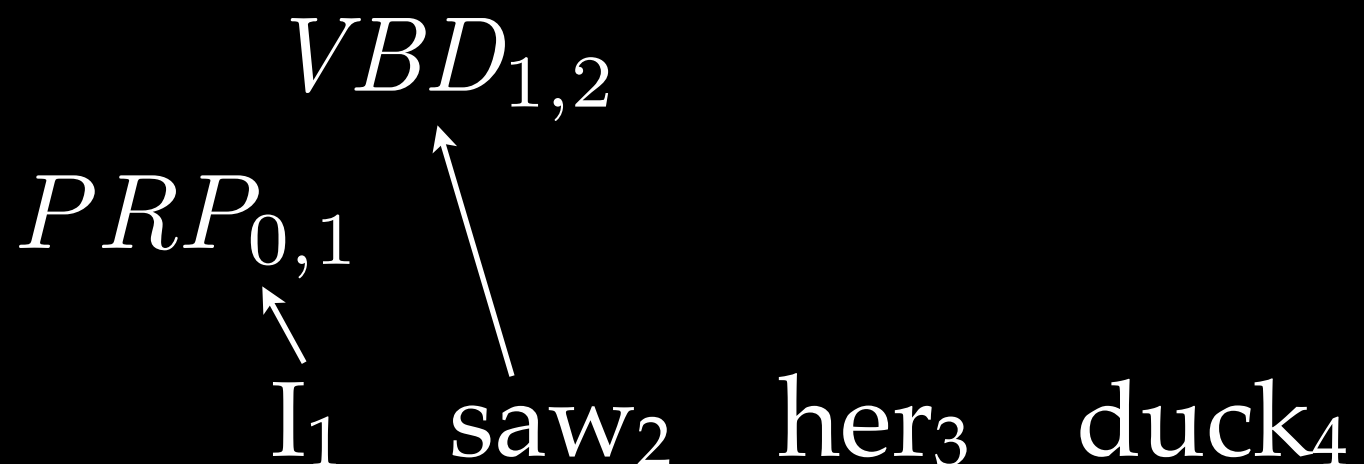
$VB \rightarrow \text{duck}$

$VP \rightarrow VBD NP$

$VP \rightarrow VBD SBAR$

$VBD \rightarrow \text{saw}$

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$



Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

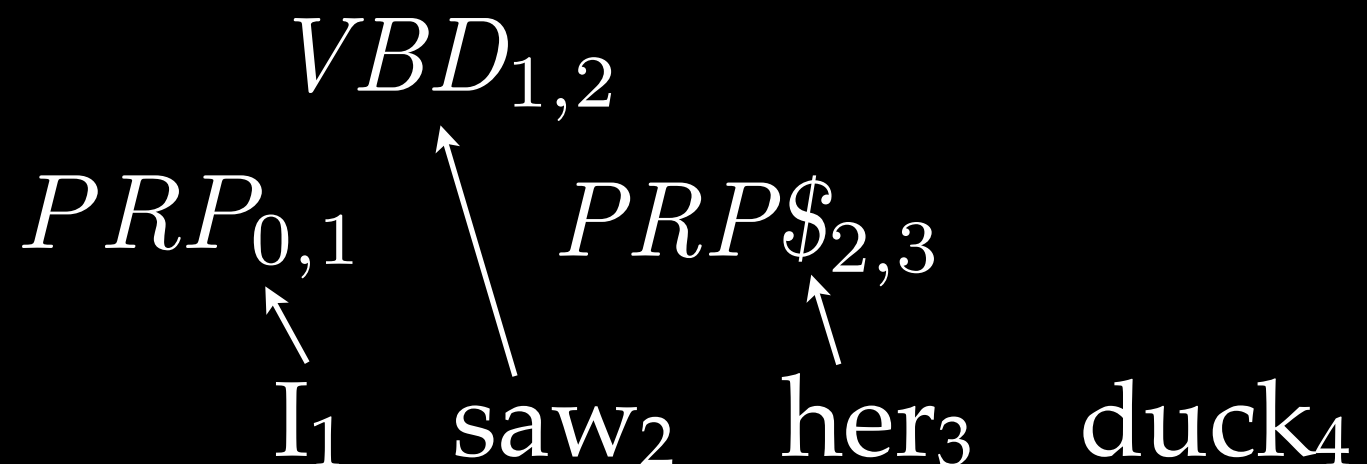
VB \rightarrow duck

VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$



Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

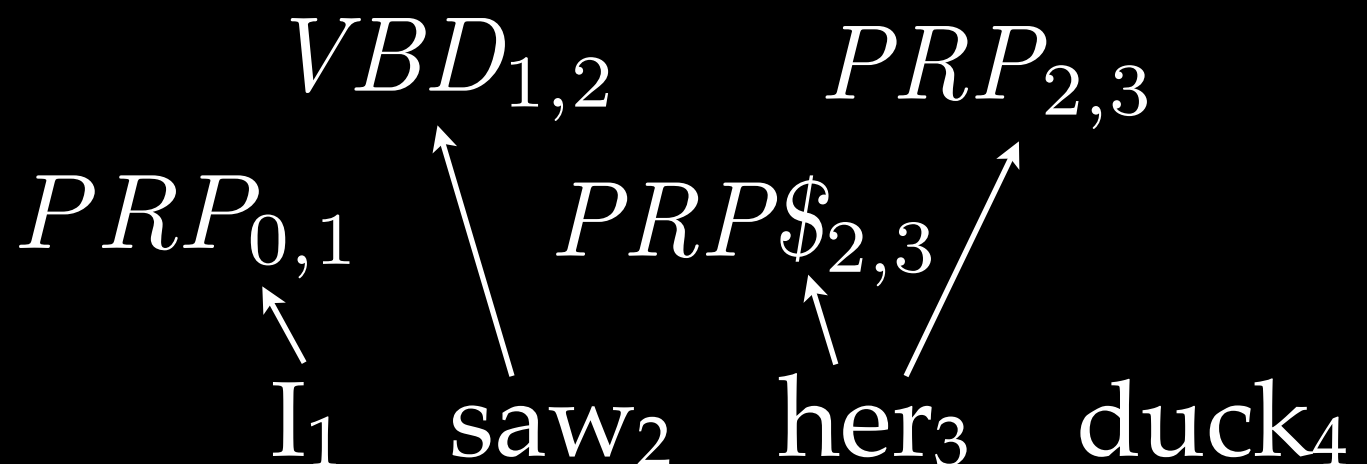
VB \rightarrow duck

VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$



Parsing

NN → duck

$$\text{NP} \rightarrow \text{PRP\$ NN}$$
PRP \rightarrow her
$$\text{PRP} \rightarrow \text{I}$$

PRP\$ → her

$$S \rightarrow \text{PRP VP}$$

SBAR → PRP VB

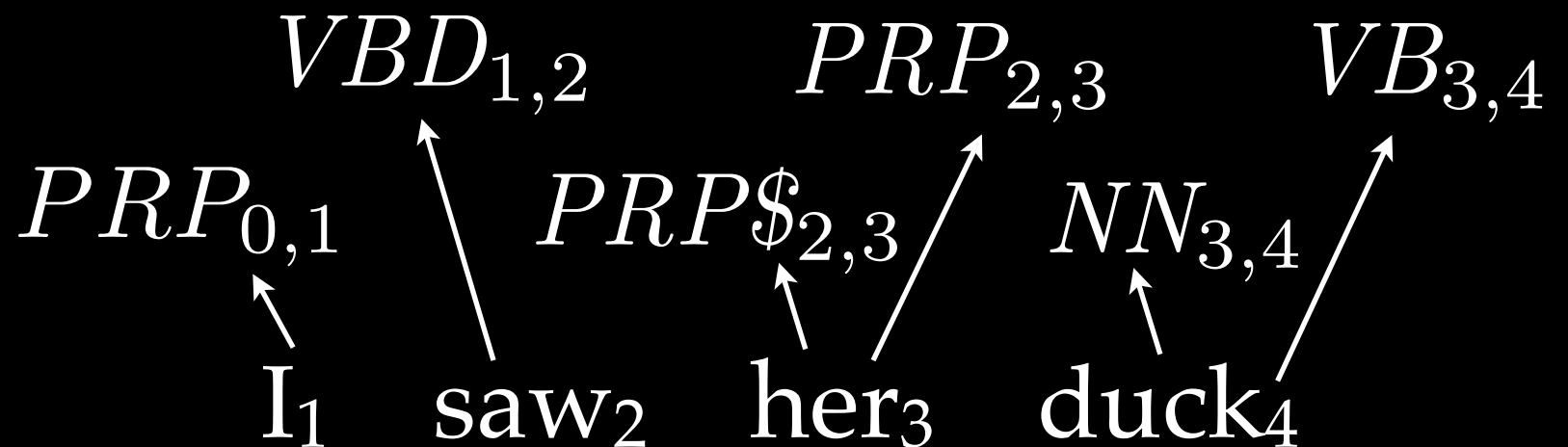
VB \rightarrow duck

$$VP \rightarrow VBD \ NP$$

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$



Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

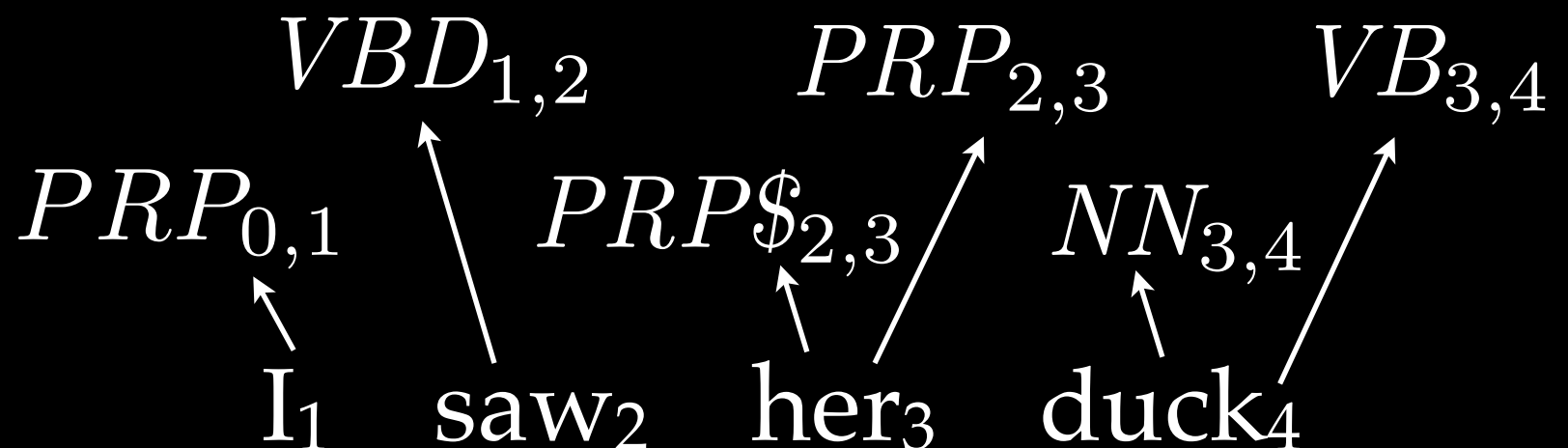
VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$



Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

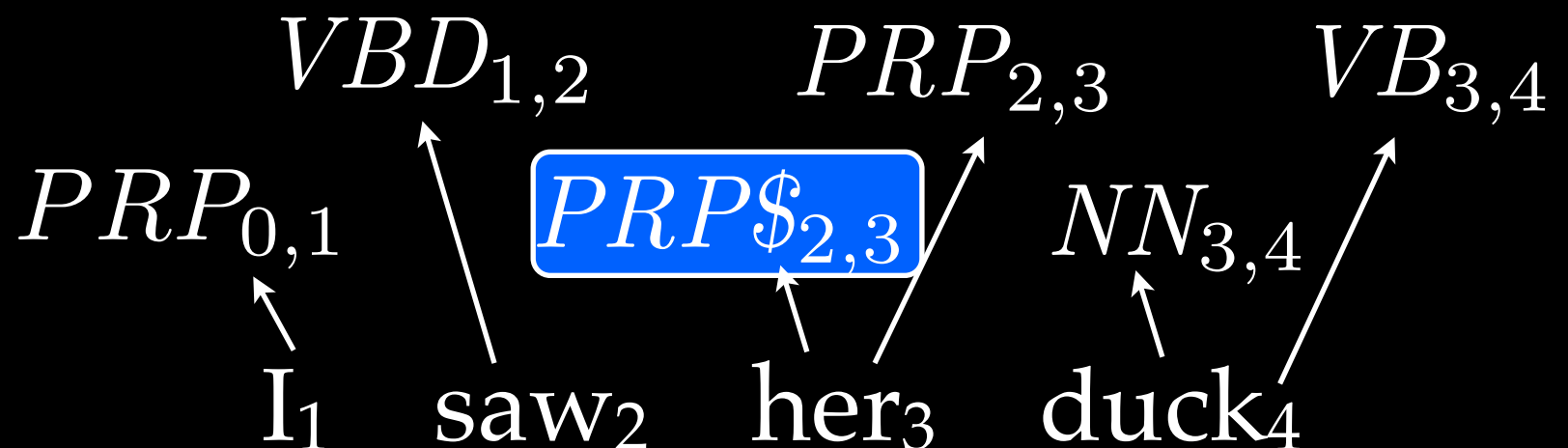
VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$



Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

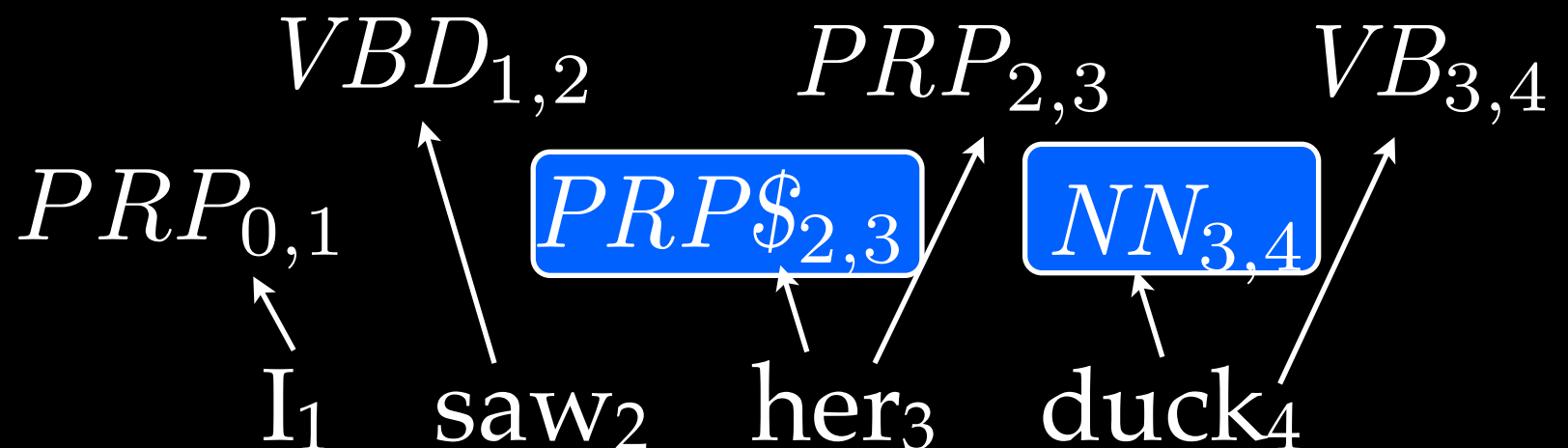
VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$



Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

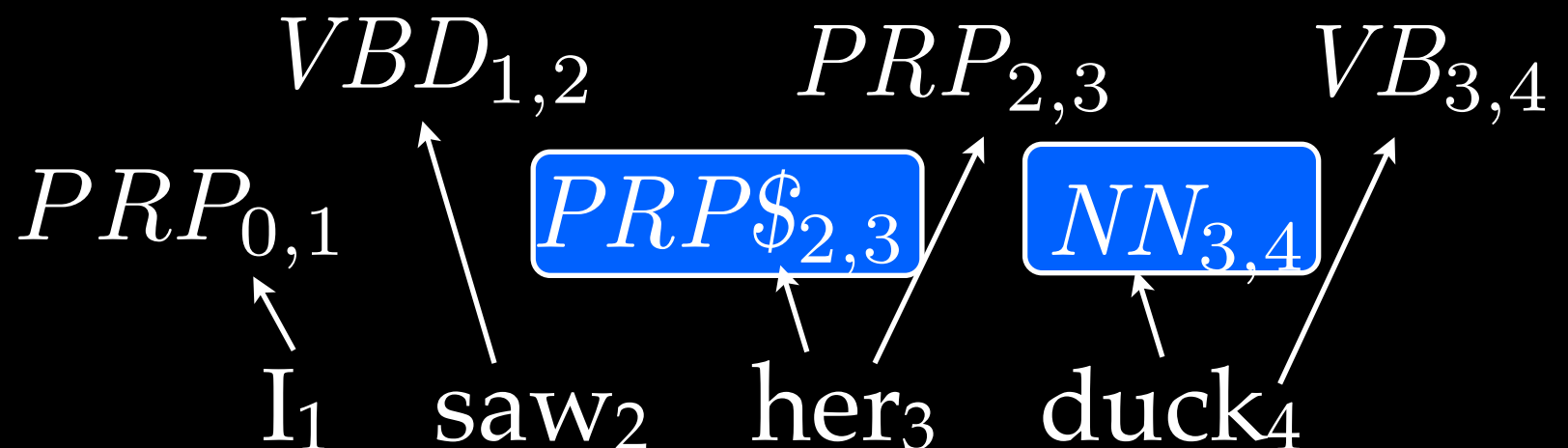
VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$



Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

VP \rightarrow VBD NP

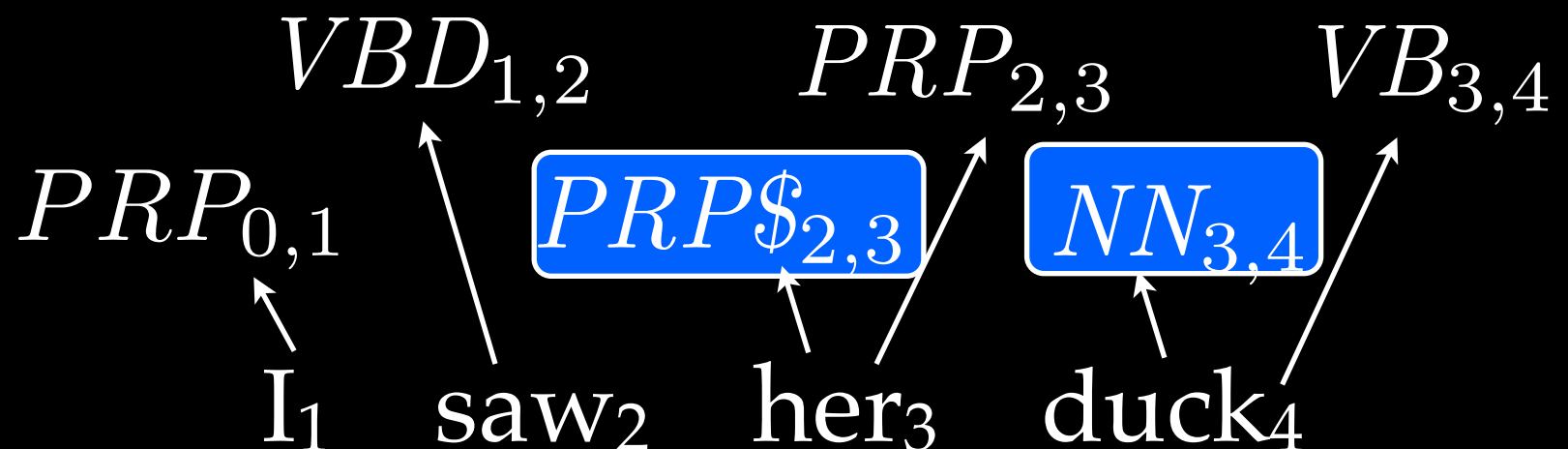
VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$

$$NP_{2,4} \leftarrow PRP\$_{2,3} \wedge NN_{3,4} \wedge (NP \rightarrow PRP\$ NN)$$



Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

VP \rightarrow VBD NP

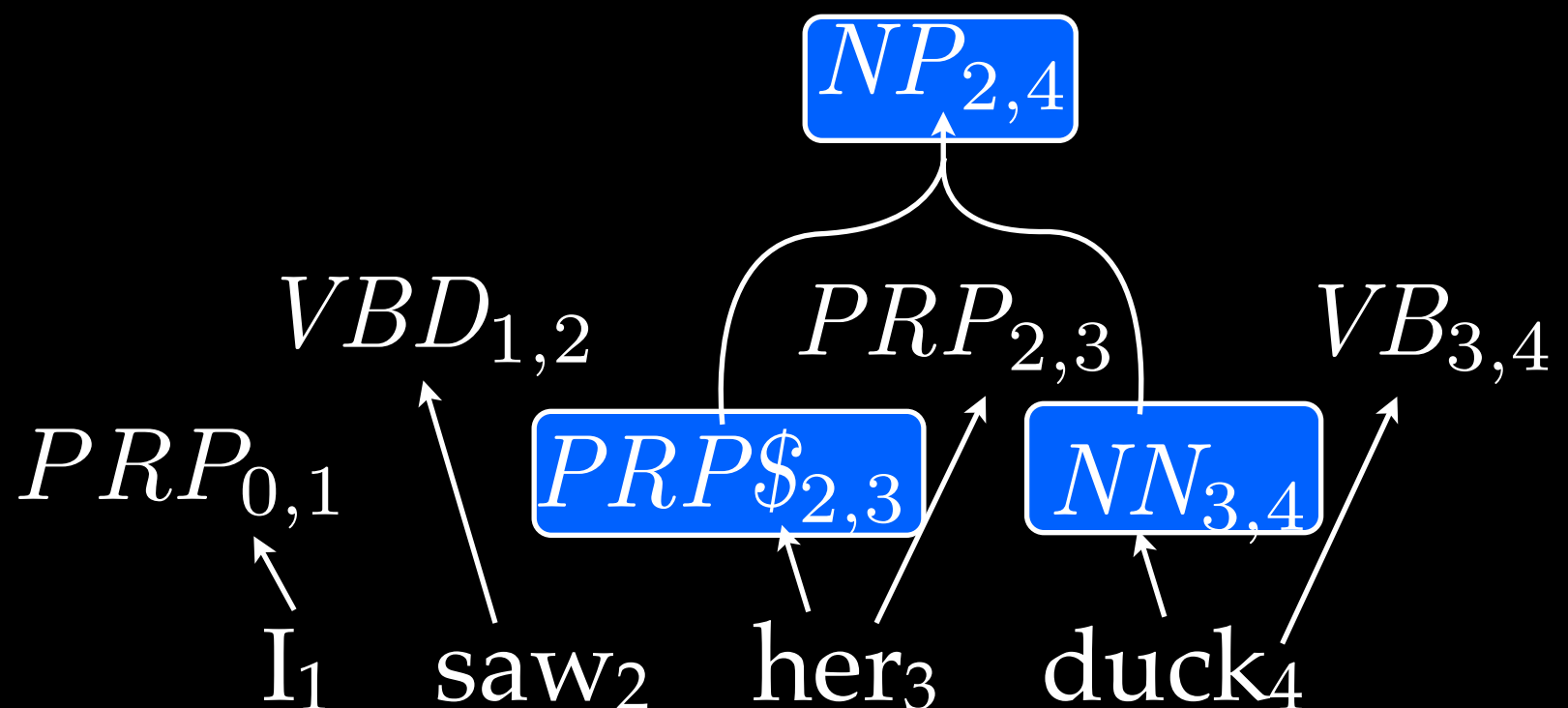
VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$

$$NP_{2,4} \leftarrow PRP\$_{2,3} \wedge NN_{3,4} \wedge (NP \rightarrow PRP\$ NN)$$



Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

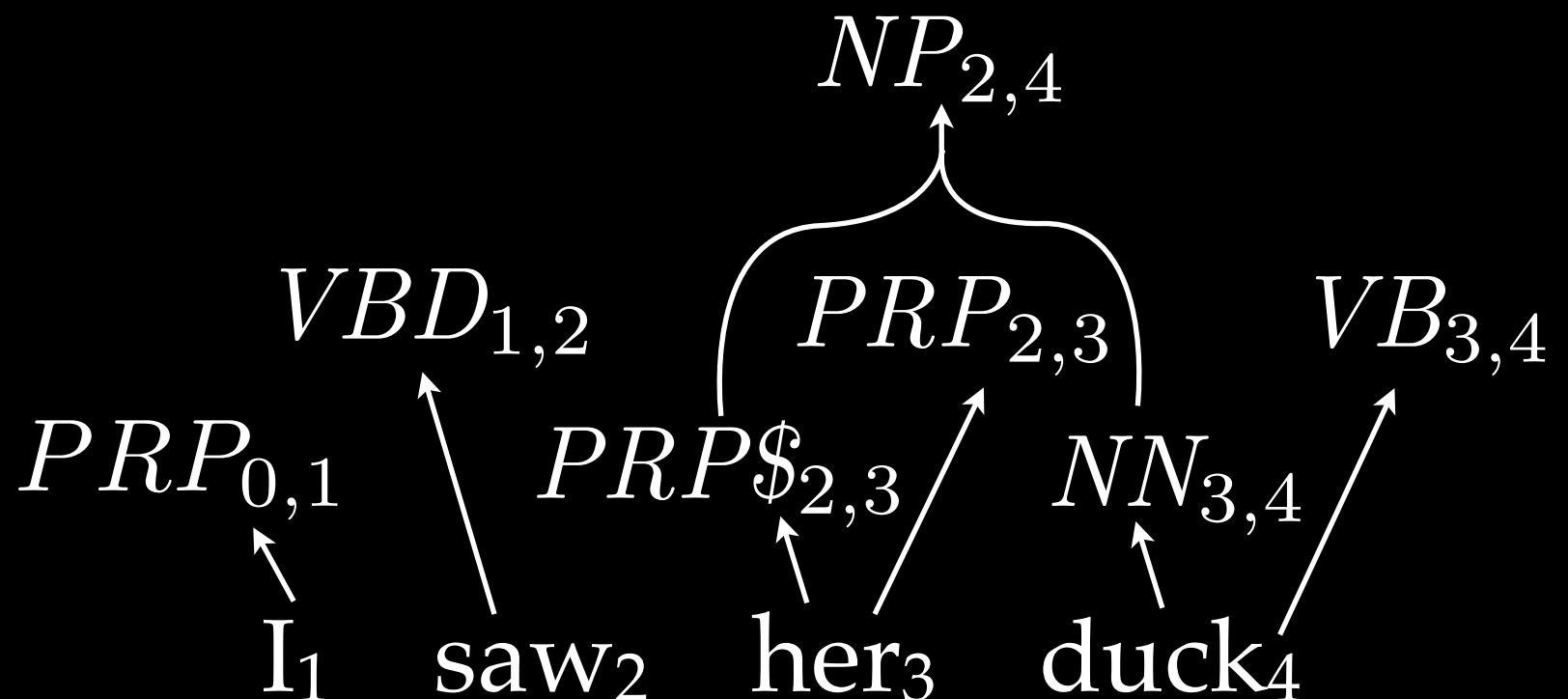
VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$



Parsing

$NN \rightarrow \text{duck}$

$NP \rightarrow PRP\$ NN$

$PRP \rightarrow \text{her}$

$PRP \rightarrow I$

$PRP\$ \rightarrow \text{her}$

$S \rightarrow PRP VP$

$SBAR \rightarrow PRP VB$

$VB \rightarrow \text{duck}$

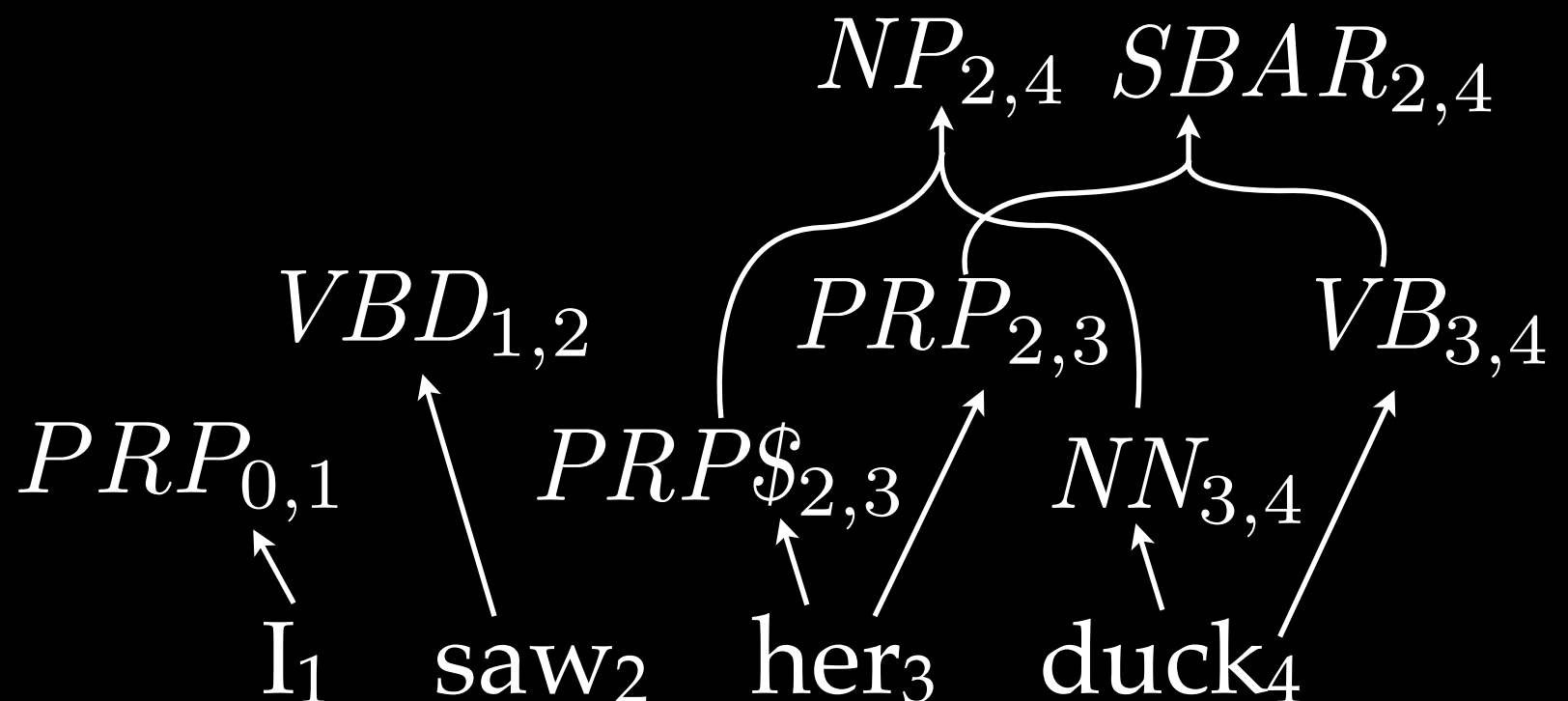
$VP \rightarrow VBD NP$

$VP \rightarrow VBD SBAR$

$VBD \rightarrow \text{saw}$

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$



Parsing

$NN \rightarrow \text{duck}$

$NP \rightarrow PRP\$ NN$

$PRP \rightarrow \text{her}$

$PRP \rightarrow I$

$PRP\$ \rightarrow \text{her}$

$S \rightarrow PRP VP$

$SBAR \rightarrow PRP VB$

$VB \rightarrow \text{duck}$

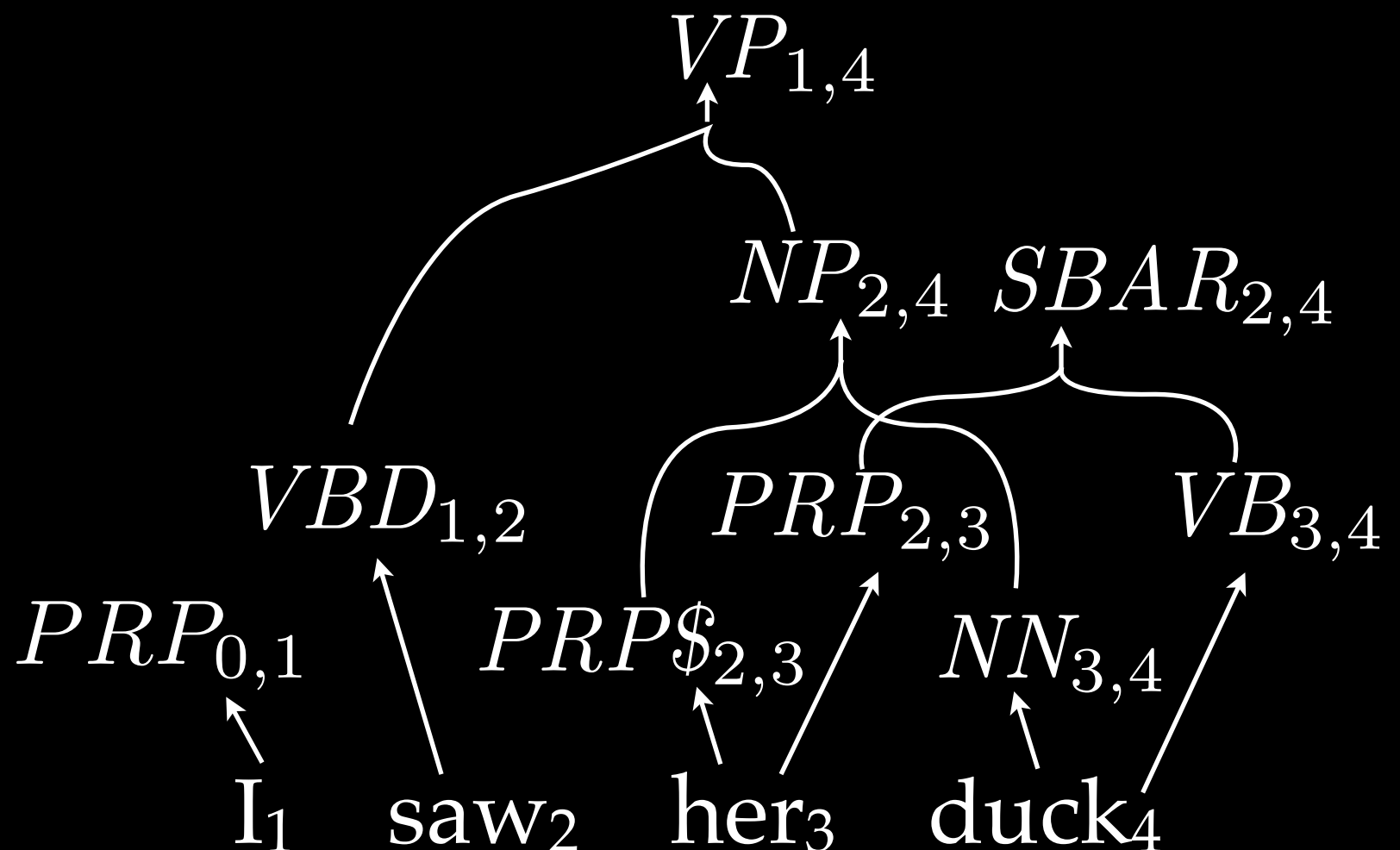
$VP \rightarrow VBD NP$

$VP \rightarrow VBD SBAR$

$VBD \rightarrow \text{saw}$

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$



Parsing

$NN \rightarrow \text{duck}$

$NP \rightarrow PRP\$ NN$

$PRP \rightarrow \text{her}$

$PRP \rightarrow I$

$PRP\$ \rightarrow \text{her}$

$S \rightarrow PRP VP$

$SBAR \rightarrow PRP VB$

$VB \rightarrow \text{duck}$

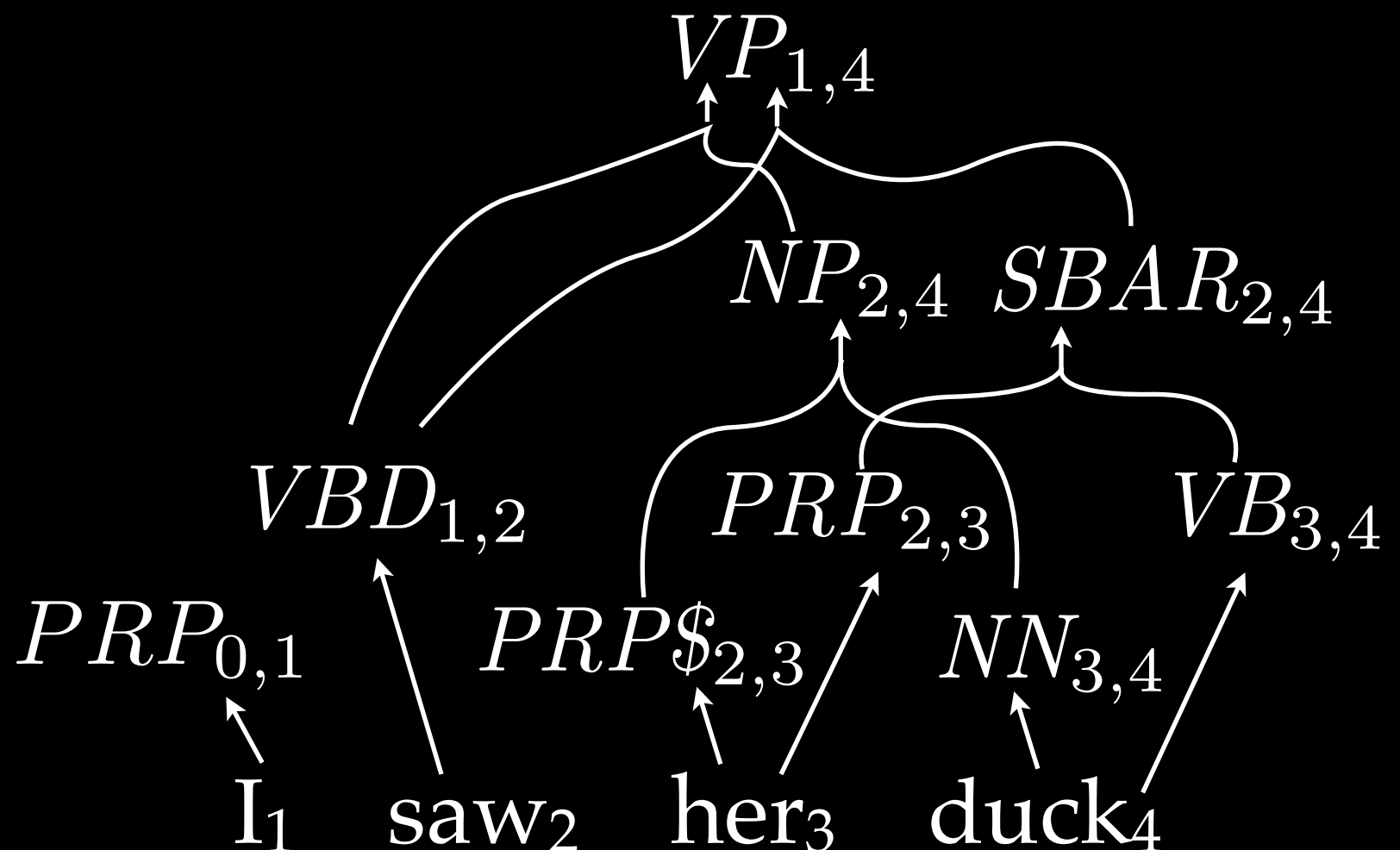
$VP \rightarrow VBD NP$

$VP \rightarrow VBD SBAR$

$VBD \rightarrow \text{saw}$

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$



Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

SBAR \rightarrow PRP VB

VB \rightarrow duck

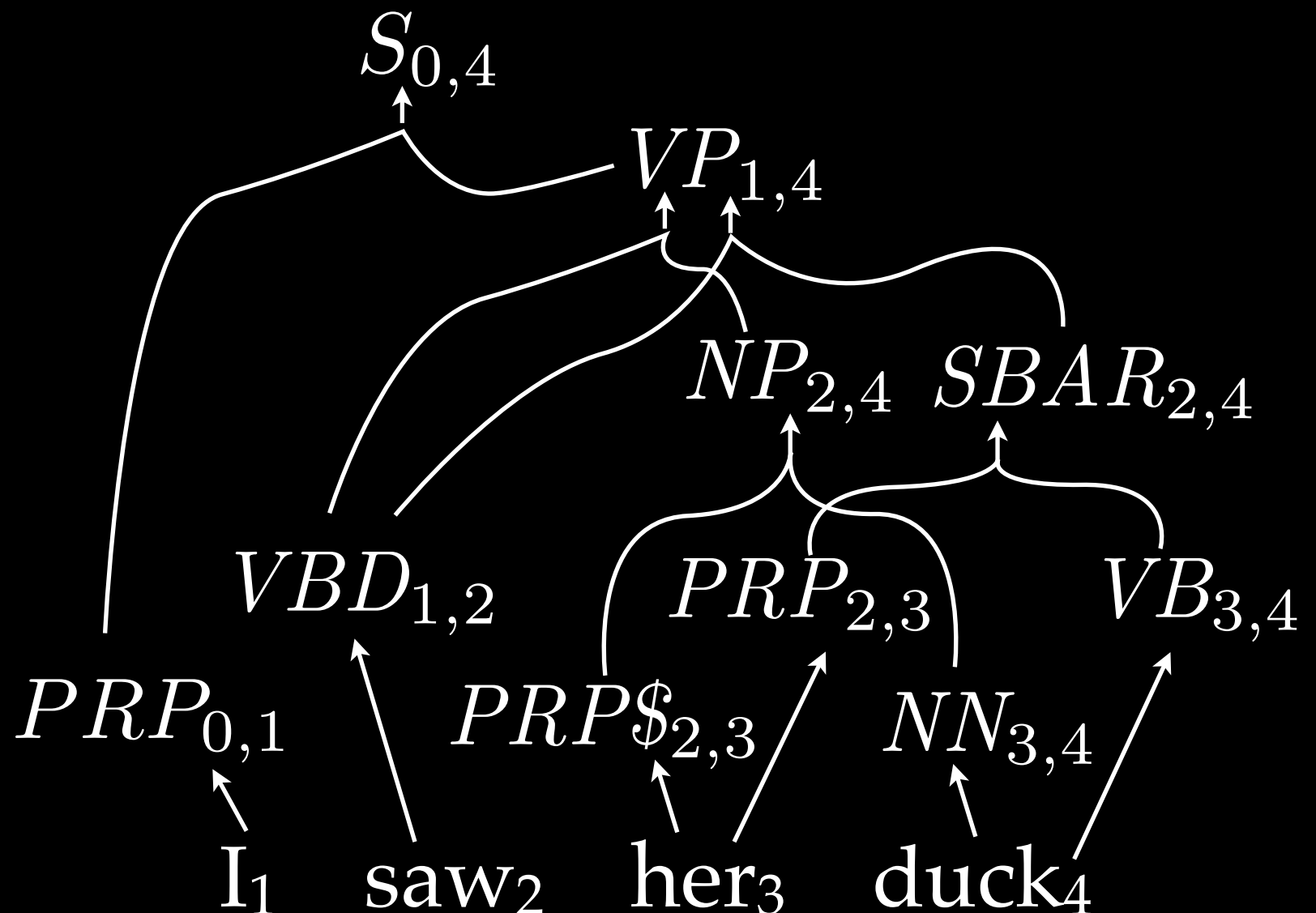
VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

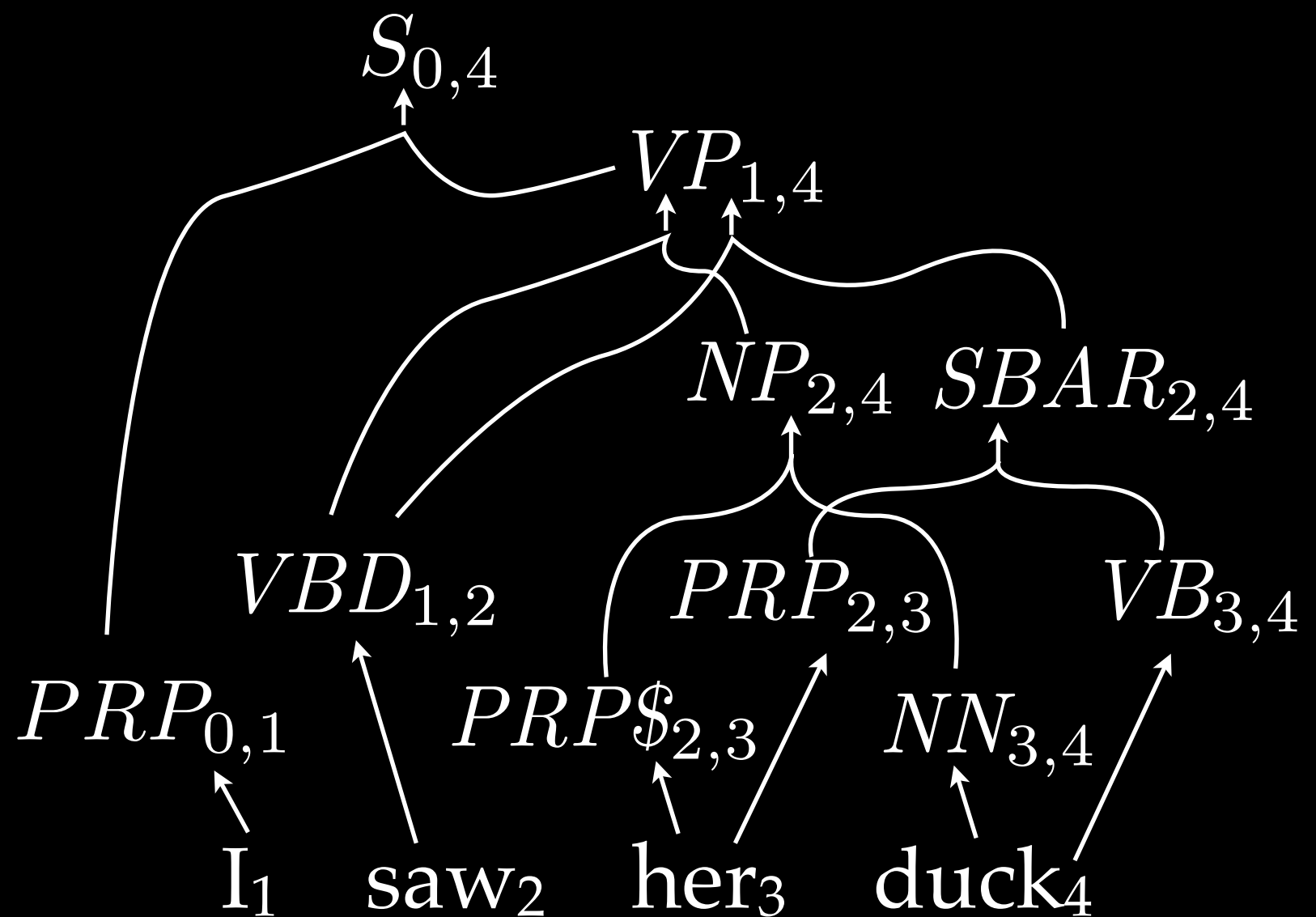
VBD \rightarrow saw

$$X_{i,i+1} \leftarrow (w_{i+1} = w) \wedge (X \rightarrow w)$$

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$

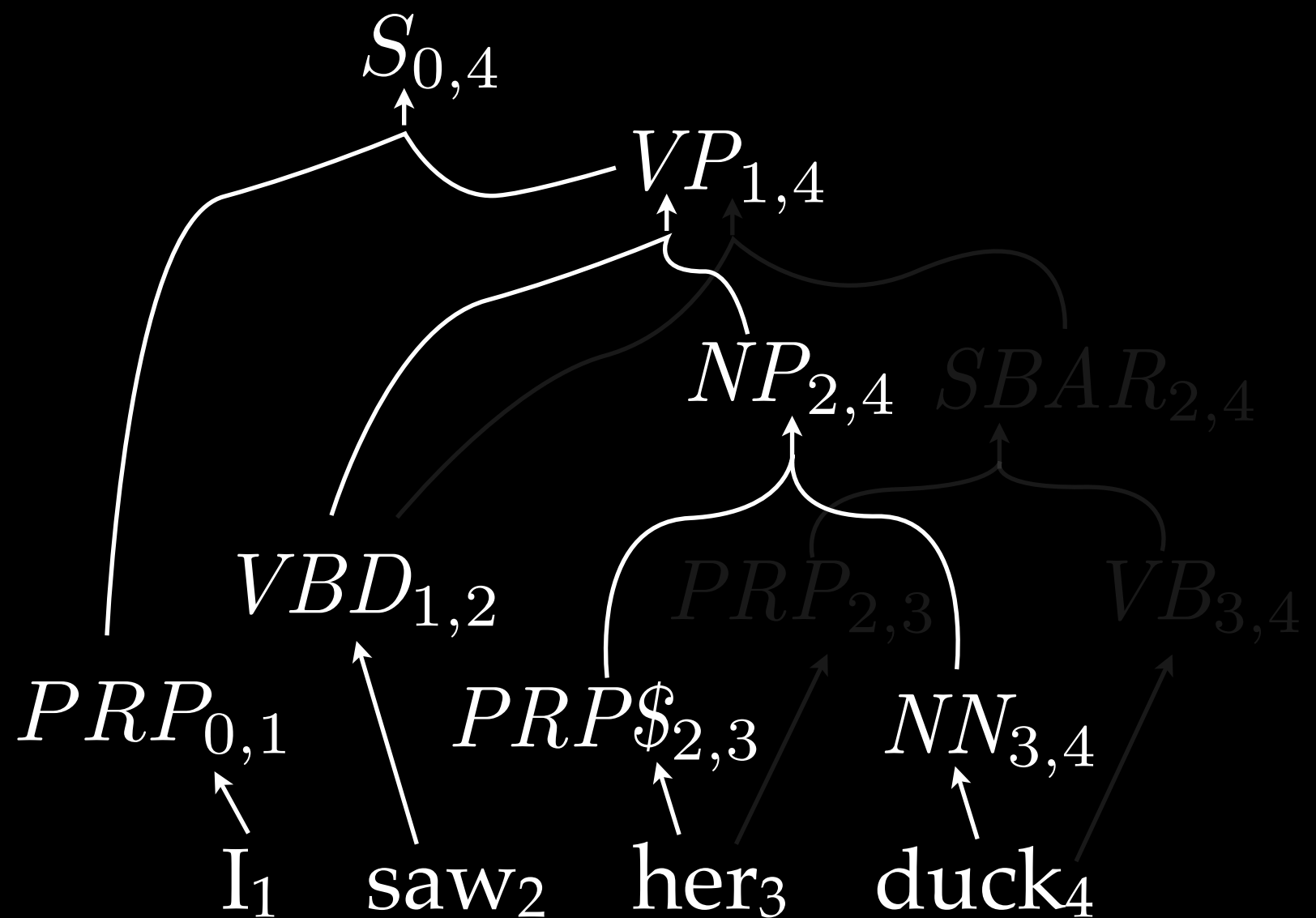
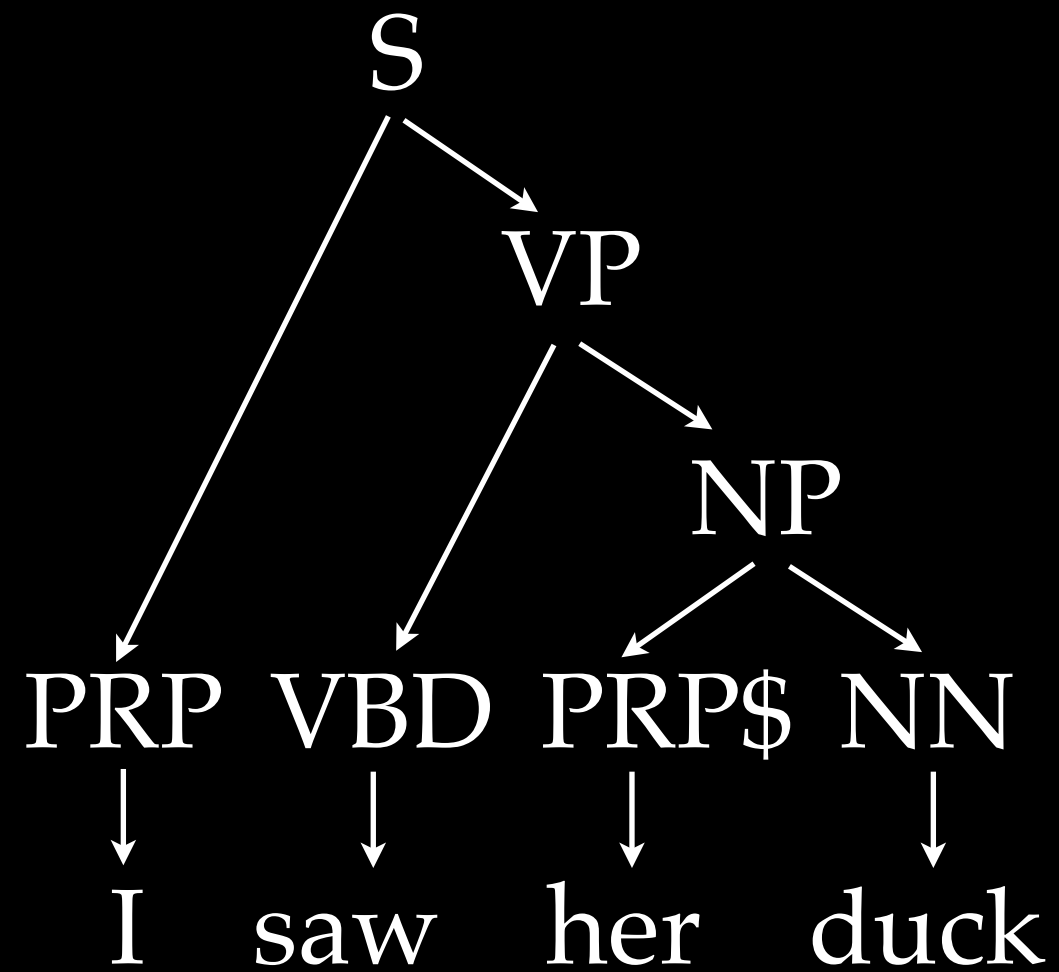


Parsing

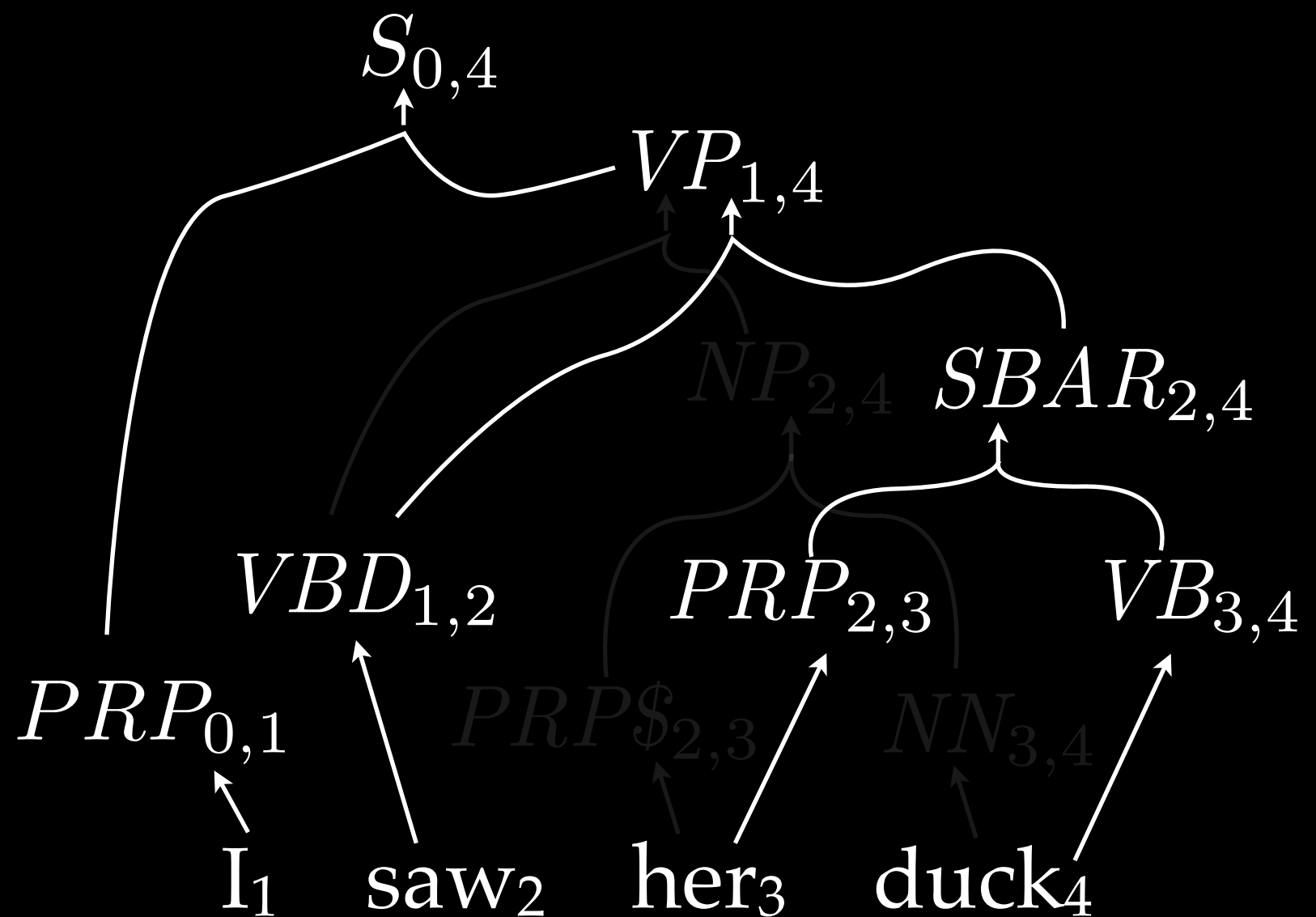
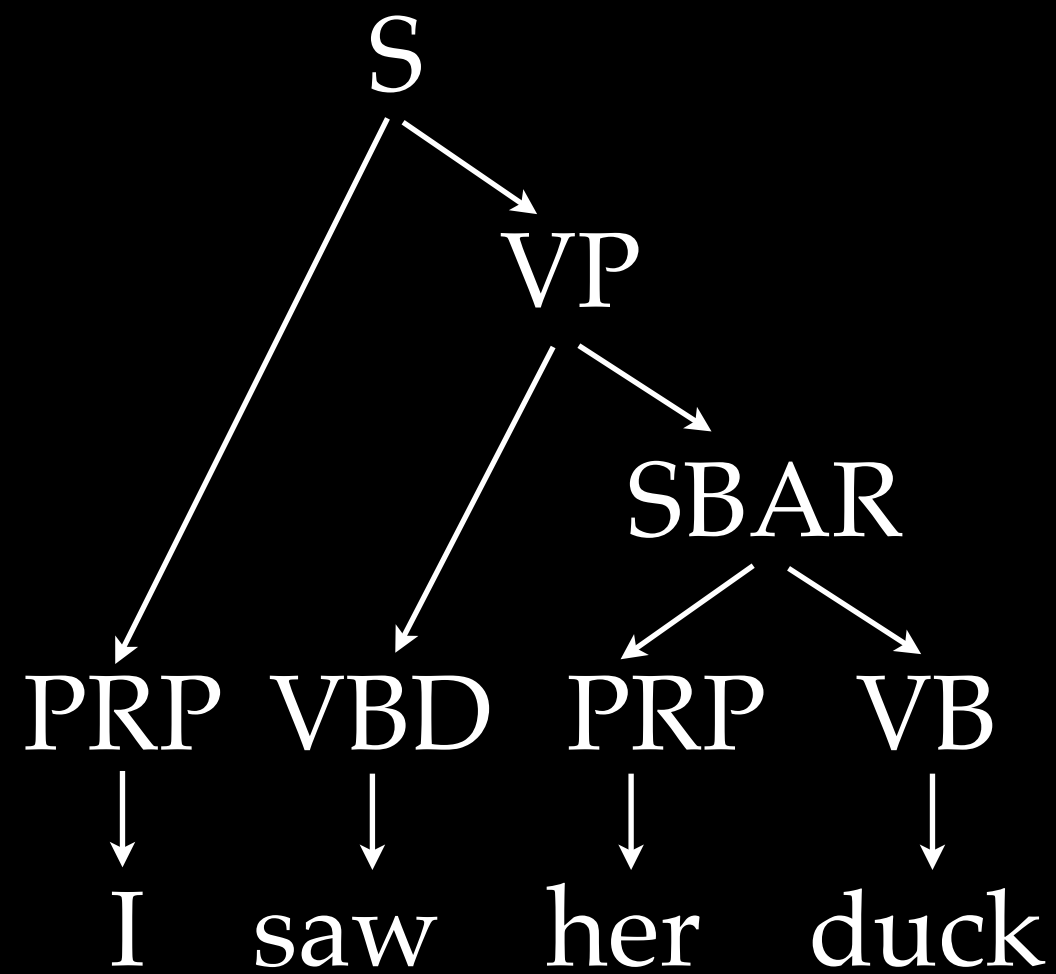


A hierarchical parse tree for the sentence "I saw her duck". The root node is $S_{0,4}$, which branches into $PRP_{0,1}$ (I₁) and $VP_{1,4}$. $VP_{1,4}$ branches into $VBD_{1,2}$ (saw₂) and $NP_{2,4}$. $NP_{2,4}$ branches into $PRP_{2,3}$ (her₃) and $SBAR_{2,4}$. $SBAR_{2,4}$ branches into $PRP_{3,4}$ (duck₄) and $VB_{3,4}$. The nodes $PRP_{2,3}$, $PRP_{3,4}$, and $VB_{3,4}$ are shown in grey, indicating they are not part of the active path for the current task.

Parsing

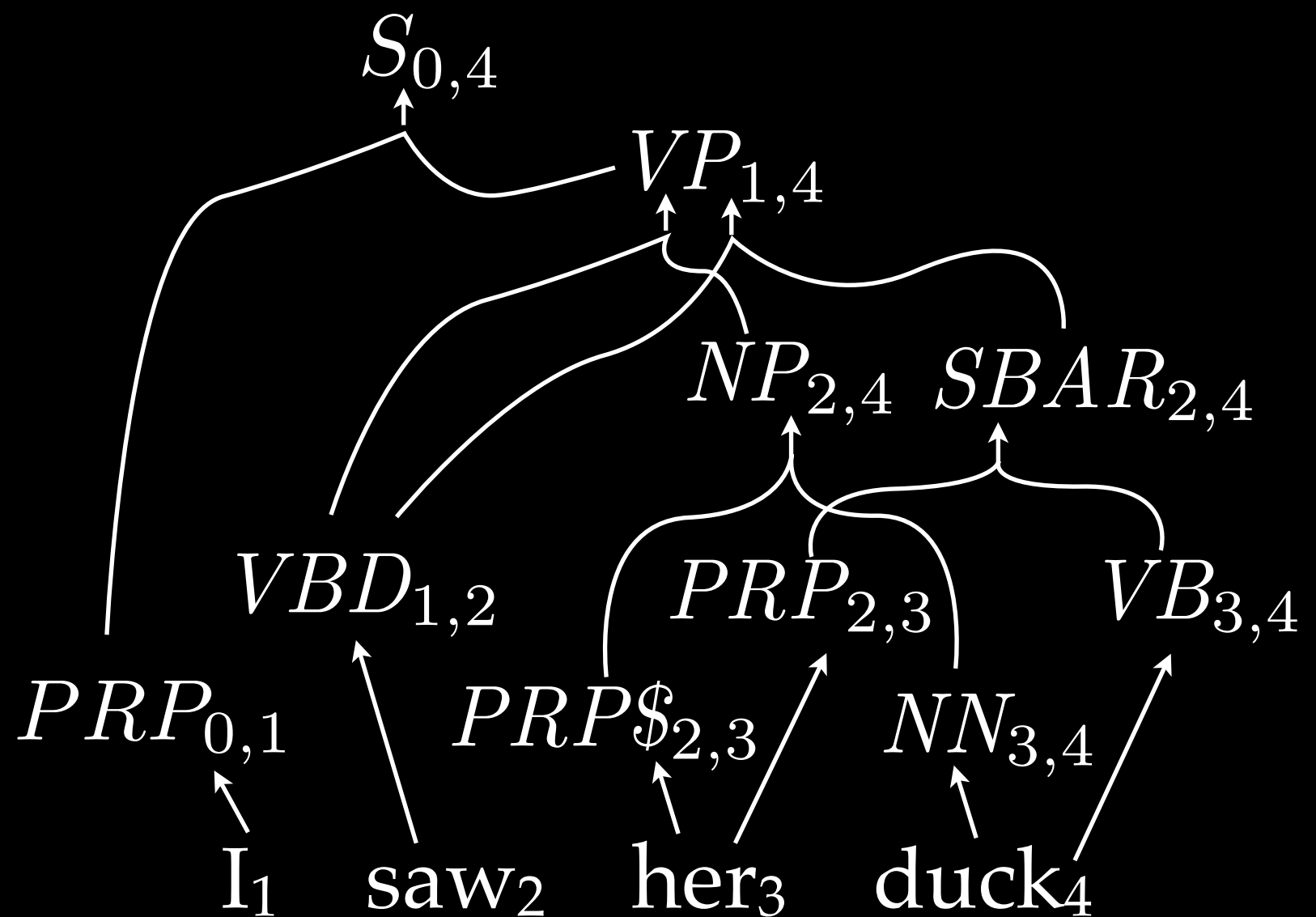


Parsing



Parsing

Analysis

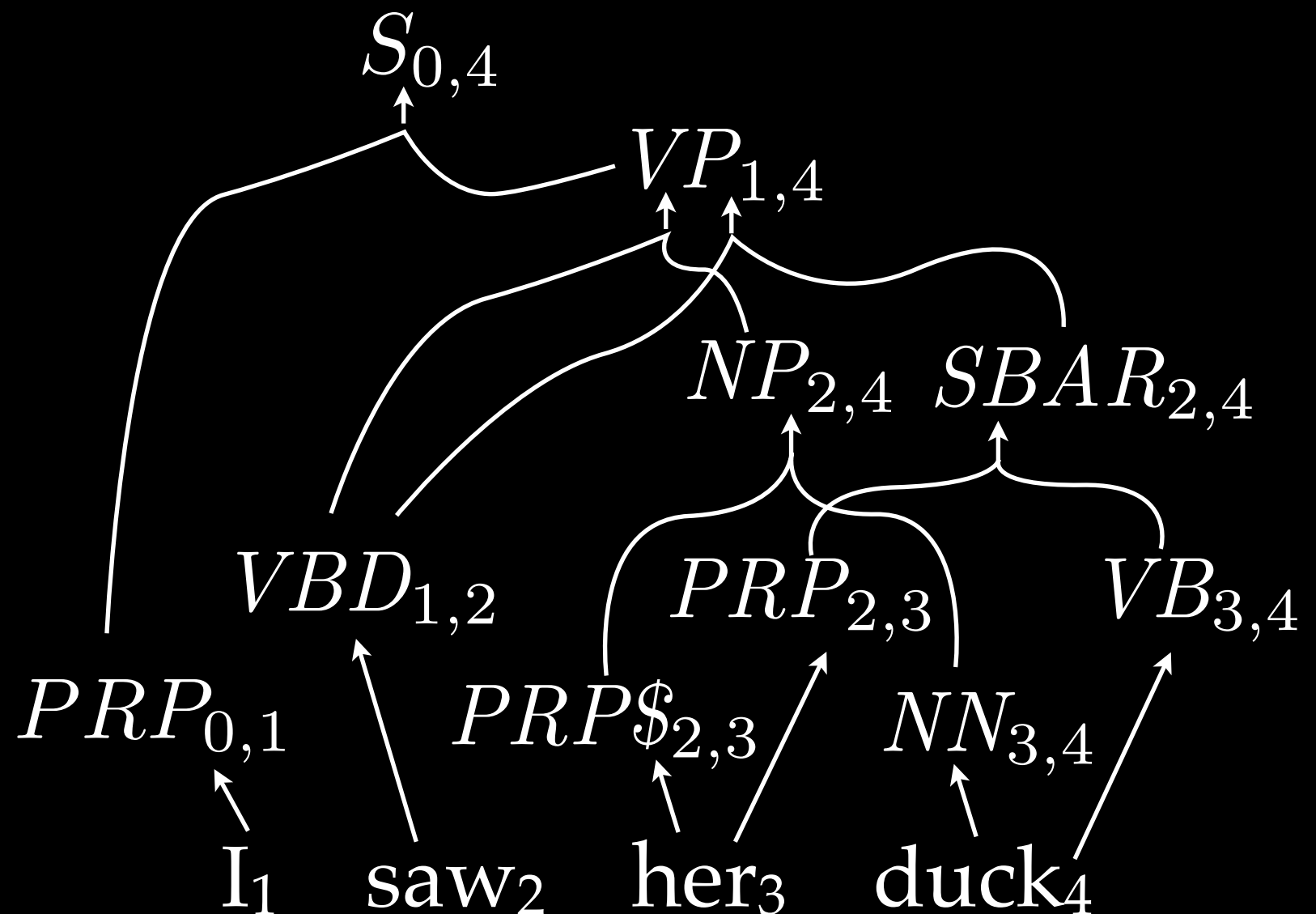


Parsing

Analysis

$O(Nn^2)$ nodes

$O(Gn^3)$ edges



Probabilistic Parsing

NN \rightarrow duck

NP \rightarrow PRP\$ NN

PRP \rightarrow her

PRP \rightarrow I

PRP\$ \rightarrow her

S \rightarrow PRP VP

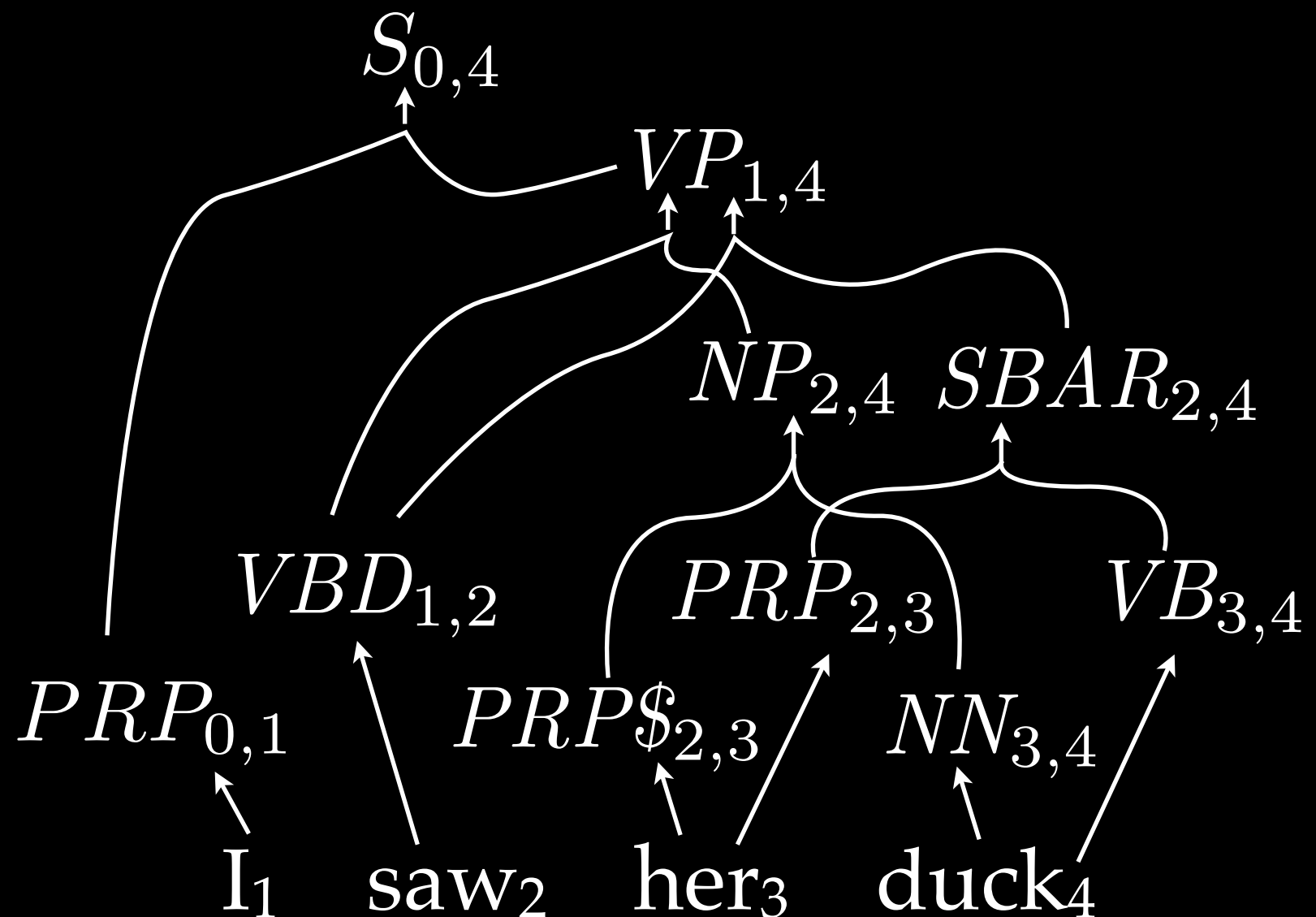
SBAR \rightarrow PRP VB

VB \rightarrow duck

VP \rightarrow VBD NP

VP \rightarrow VBD SBAR

VBD \rightarrow saw



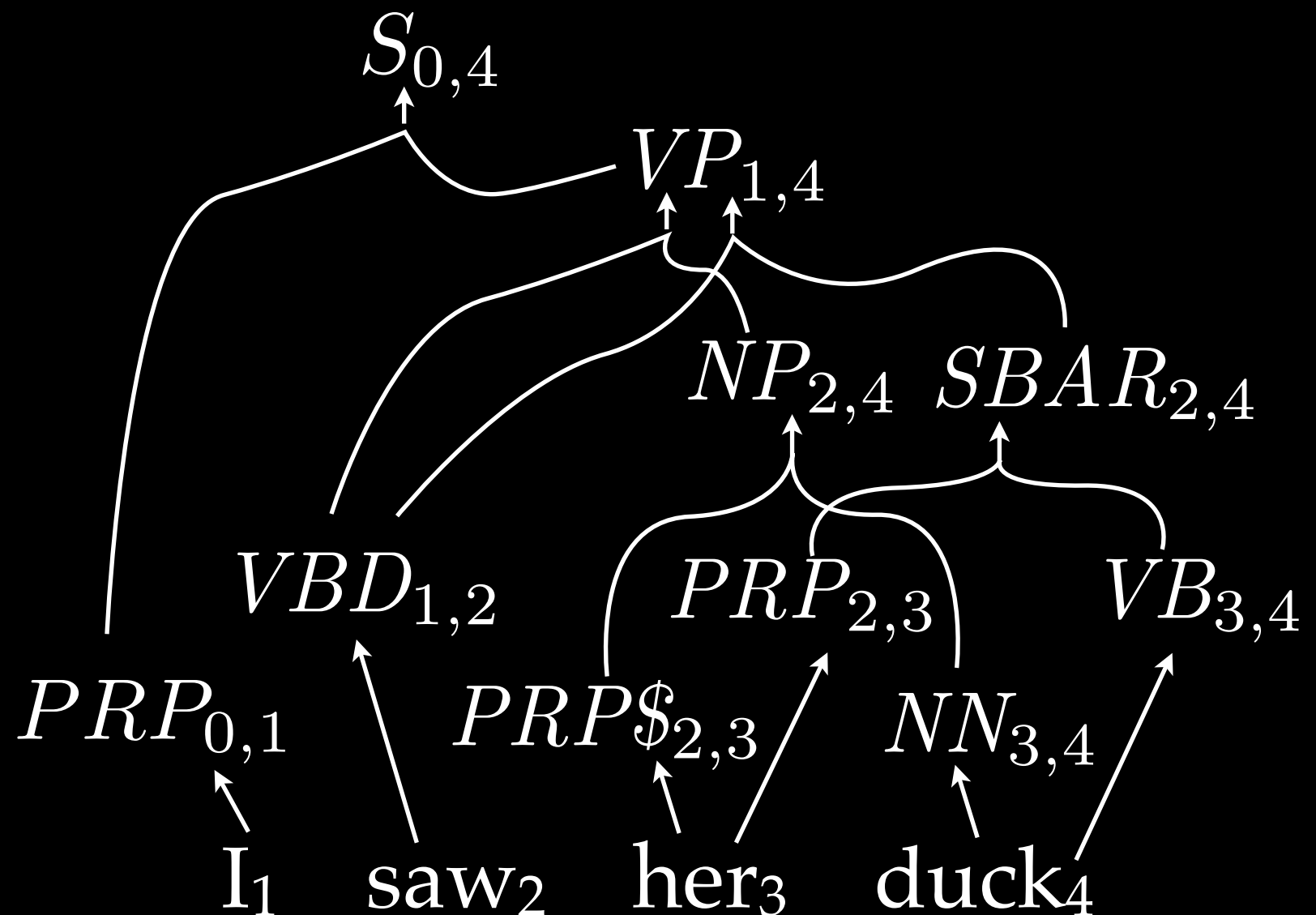
Probabilistic Parsing

NN \rightarrow duck (1.0)

$$\text{NP} \rightarrow \text{PRP\$ NN} \quad (1.0)$$
$$\text{PRP} \rightarrow \text{her} \quad (0.3)$$
$$\text{PRP} \rightarrow \text{I} \quad (0.7)$$
$$\text{PRP\$} \rightarrow \text{her} \quad (1.0)$$
$$S \rightarrow \text{PRP VP} \quad (1.0)$$

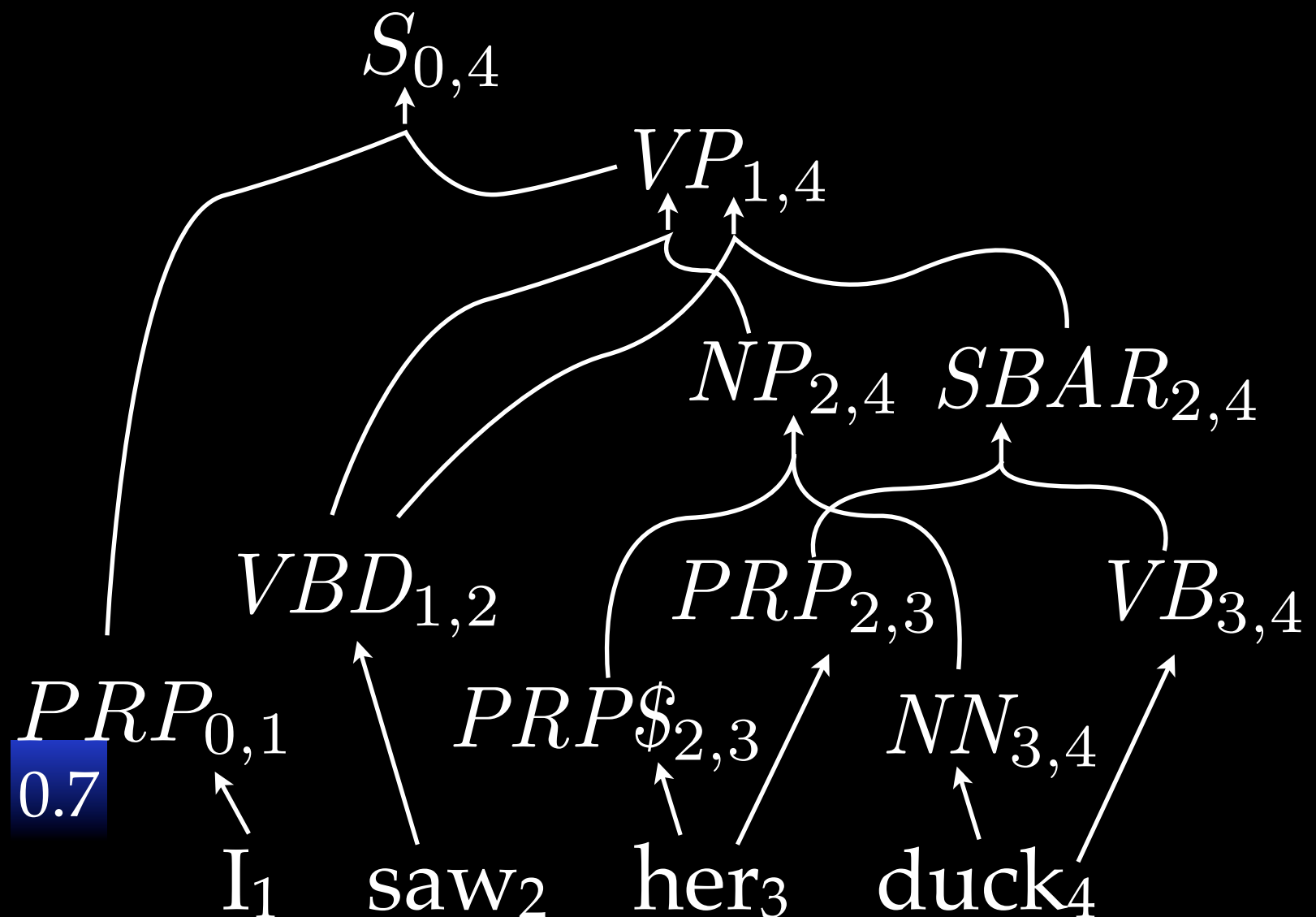
SBAR \rightarrow PRP VB (1.0)

VB → duck (1.0)

$$\text{VP} \rightarrow \text{VBD NP} \quad (0.8)$$
$$\text{VP} \rightarrow \text{VBD SBAR} \quad (0.2)$$
$$\text{VBD} \rightarrow \text{saw} \quad (1.0)$$


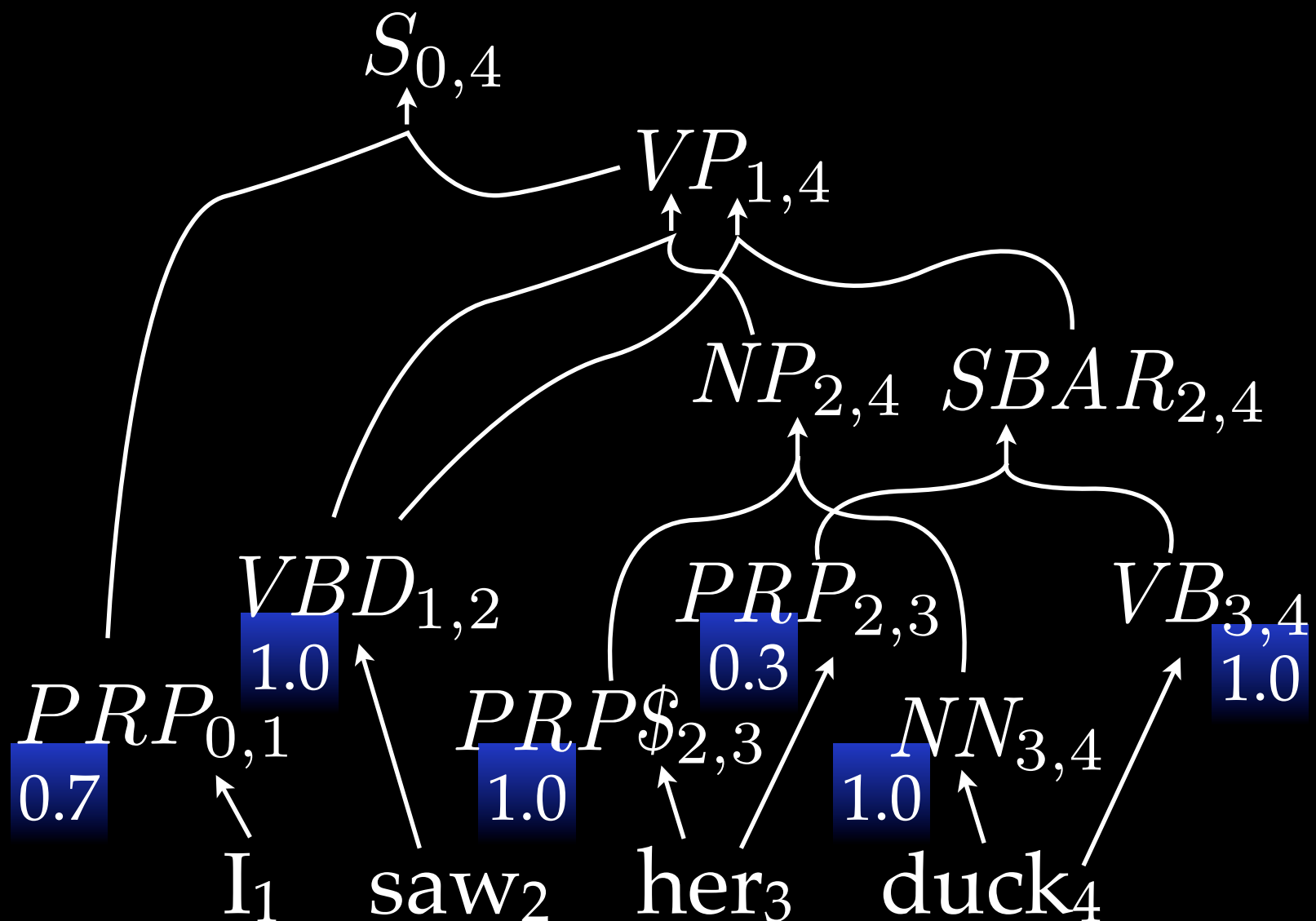
Probabilistic Parsing

$NN \rightarrow \text{duck}$	(1.0)
$NP \rightarrow PRP\$ NN$	(1.0)
$PRP \rightarrow \text{her}$	(0.3)
$PRP \rightarrow I$	(0.7)
$PRP\$ \rightarrow \text{her}$	(1.0)
$S \rightarrow PRP VP$	(1.0)
$SBAR \rightarrow PRP VB$	(1.0)
$VB \rightarrow \text{duck}$	(1.0)
$VP \rightarrow VBD NP$	(0.8)
$VP \rightarrow VBD SBAR$	(0.2)
$VBD \rightarrow \text{saw}$	(1.0)



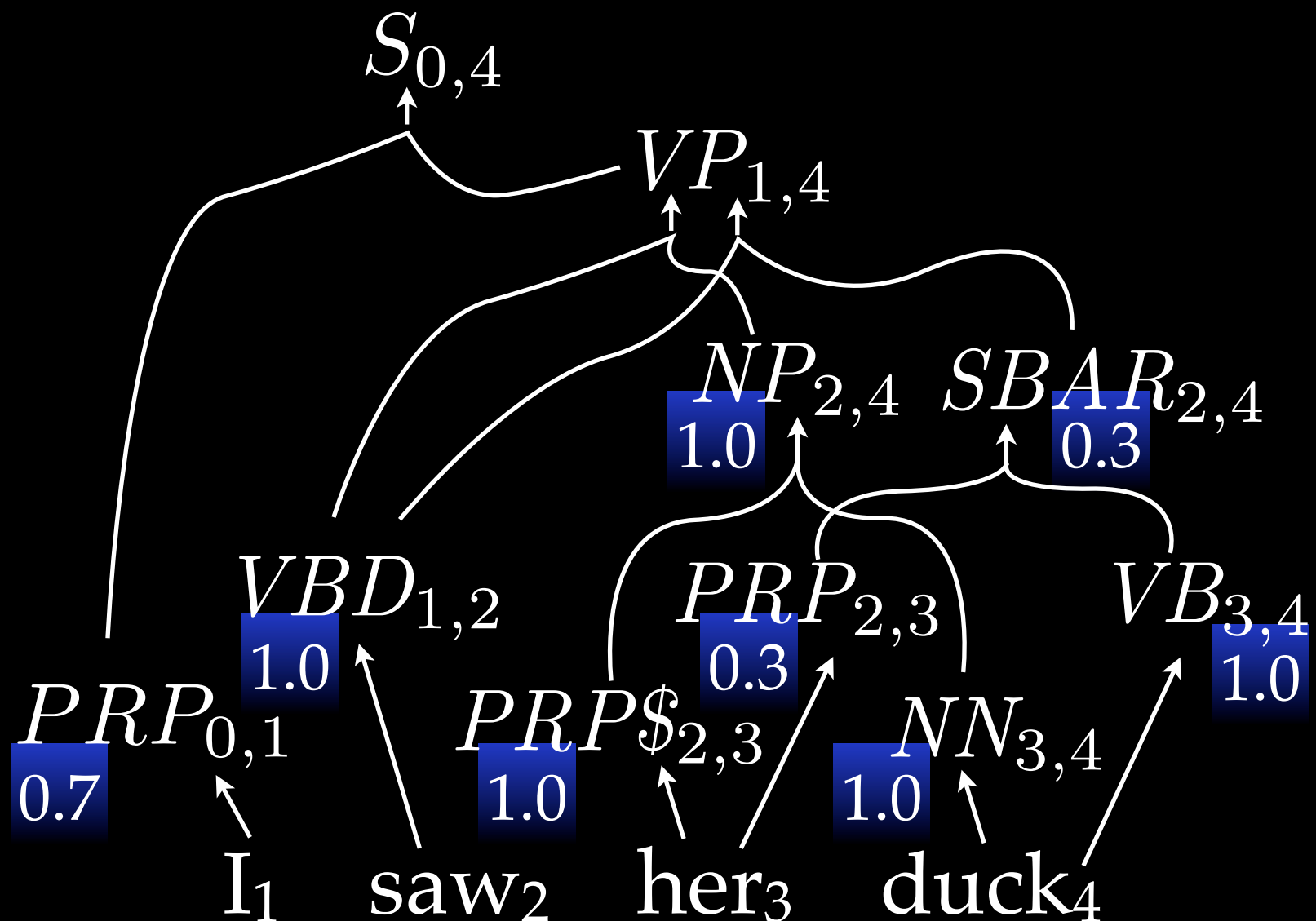
Probabilistic Parsing

$NN \rightarrow \text{duck}$	(1.0)
$NP \rightarrow PRP\$ NN$	(1.0)
$PRP \rightarrow \text{her}$	(0.3)
$PRP \rightarrow I$	(0.7)
$PRP\$ \rightarrow \text{her}$	(1.0)
$S \rightarrow PRP VP$	(1.0)
$SBAR \rightarrow PRP VB$	(1.0)
$VB \rightarrow \text{duck}$	(1.0)
$VP \rightarrow VBD NP$	(0.8)
$VP \rightarrow VBD SBAR$	(0.2)
$VBD \rightarrow \text{saw}$	(1.0)



Probabilistic Parsing

$NN \rightarrow \text{duck}$	(1.0)
$NP \rightarrow PRP\$ NN$	(1.0)
$PRP \rightarrow \text{her}$	(0.3)
$PRP \rightarrow I$	(0.7)
$PRP\$ \rightarrow \text{her}$	(1.0)
$S \rightarrow PRP VP$	(1.0)
$SBAR \rightarrow PRP VB$	(1.0)
$VB \rightarrow \text{duck}$	(1.0)
$VP \rightarrow VBD NP$	(0.8)
$VP \rightarrow VBD SBAR$	(0.2)
$VBD \rightarrow \text{saw}$	(1.0)



Probabilistic Parsing

NN → duck (1.0)

NP → PRP\$ NN (1.0)

PRP → her (0.3)

PRP → I (0.7)

PRP\$ → her (1.0)

S → PRP VP (1.0)

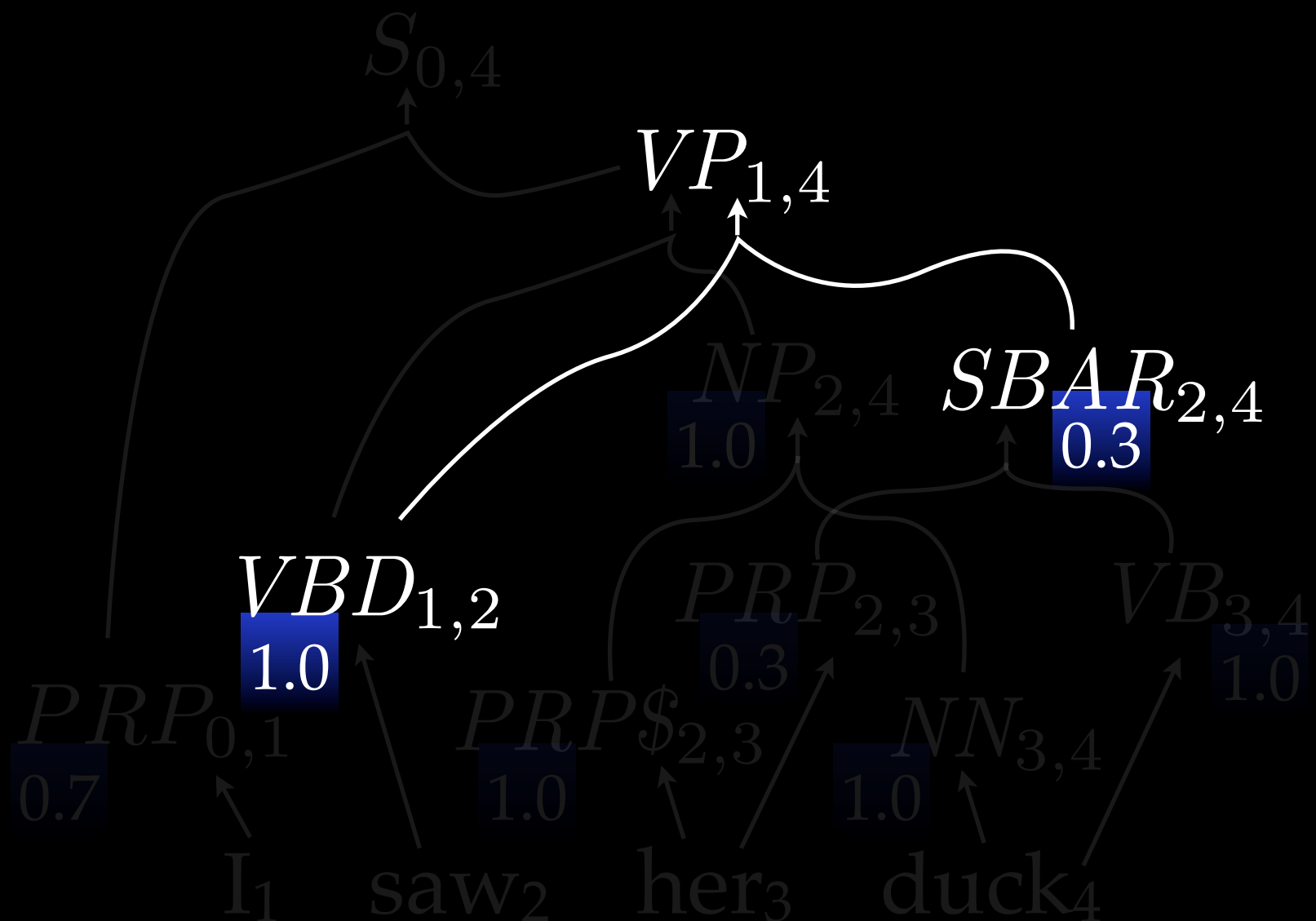
SBAR → PRP VB (1.0)

VB → duck (1.0)

VP → VBD NP (0.8)

VP → VBD SBAR (0.2)

VBD → saw (1.0)



Probabilistic Parsing

NN → duck (1.0)

NP → PRP\$ NN (1.0)

PRP → her (0.3)

PRP → I (0.7)

PRP\$ → her (1.0)

S → PRP VP (1.0)

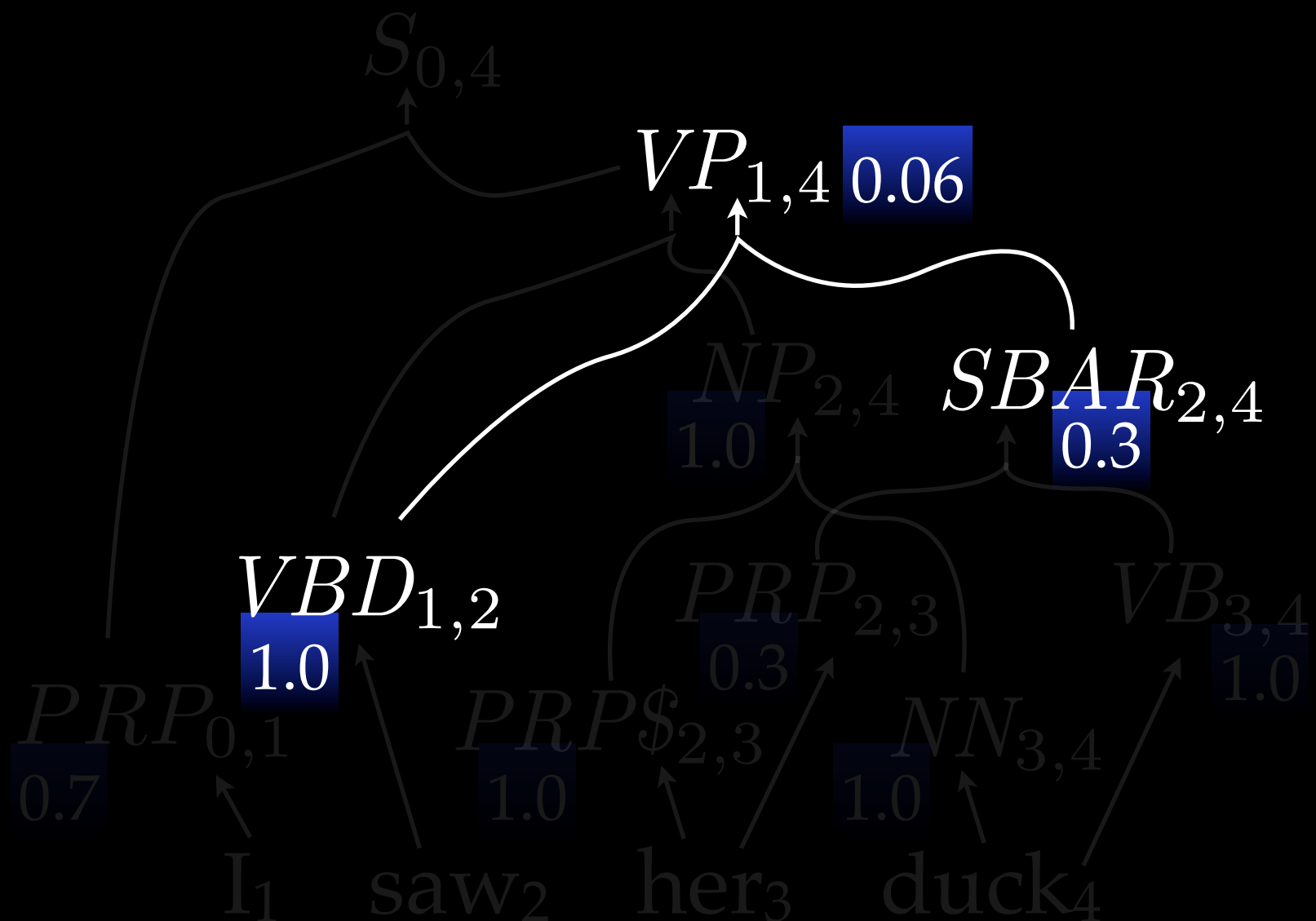
SBAR → PRP VB (1.0)

VB → duck (1.0)

VP → VBD NP (0.8)

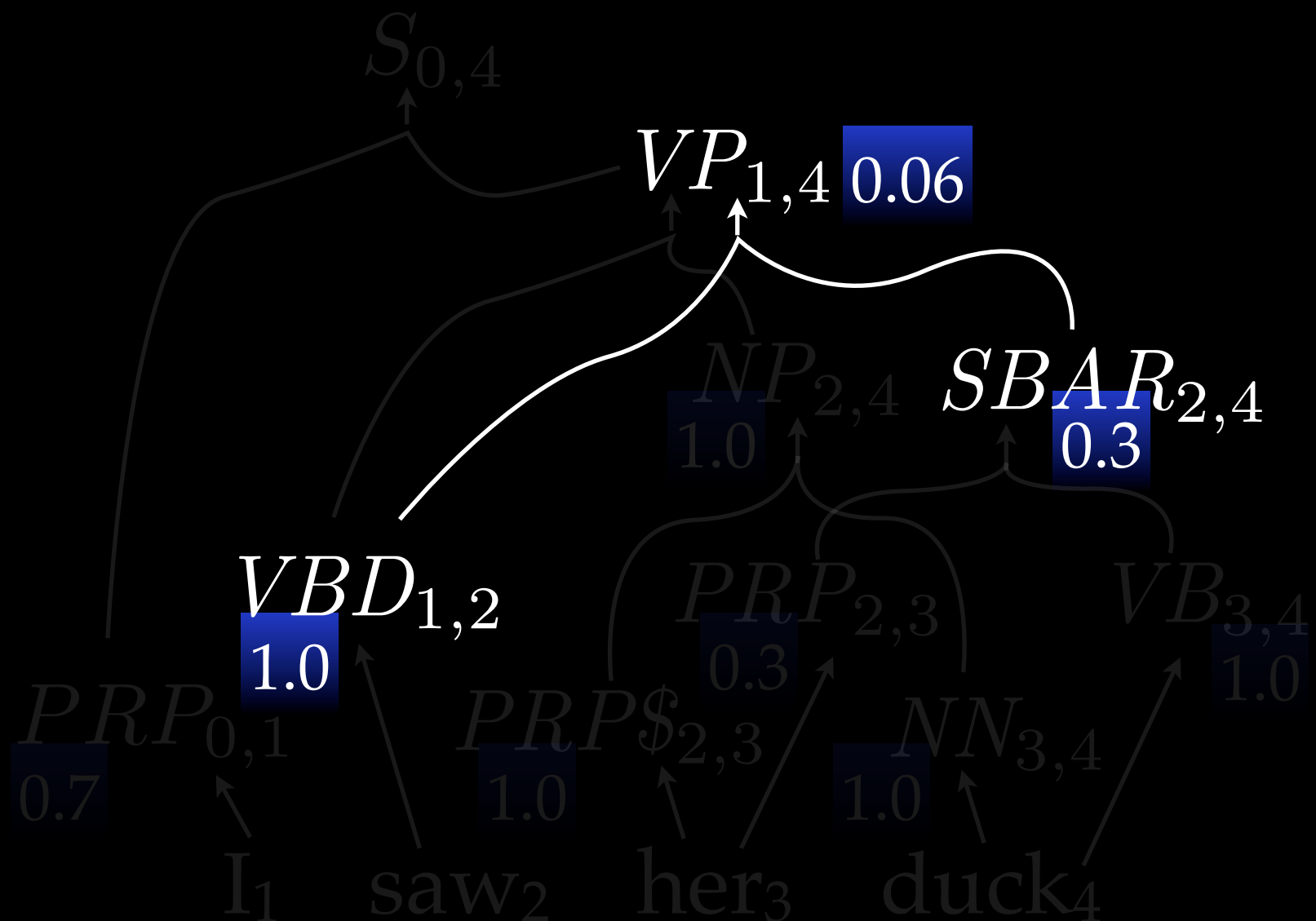
VP → VBD SBAR (0.2)

VBD → saw (1.0)



Probabilistic Parsing

$NN \rightarrow \text{duck}$	(1.0)
$NP \rightarrow PRP\$ NN$	(1.0)
$PRP \rightarrow \text{her}$	(0.3)
$PRP \rightarrow I$	(0.7)
$PRP\$ \rightarrow \text{her}$	(1.0)
$S \rightarrow PRP VP$	(1.0)
$SBAR \rightarrow PRP VB$	(1.0)
$VB \rightarrow \text{duck}$	(1.0)
$VP \rightarrow VBD NP$	(0.8)
$VP \rightarrow VBD SBAR$	(0.2)
$VBD \rightarrow \text{saw}$	(1.0)



Probabilistic Parsing

NN → duck (1.0)

NP → PRP\$ NN (1.0)

PRP → her (0.3)

PRP → I (0.7)

PRP\$ → her (1.0)

S → PRP VP (1.0)

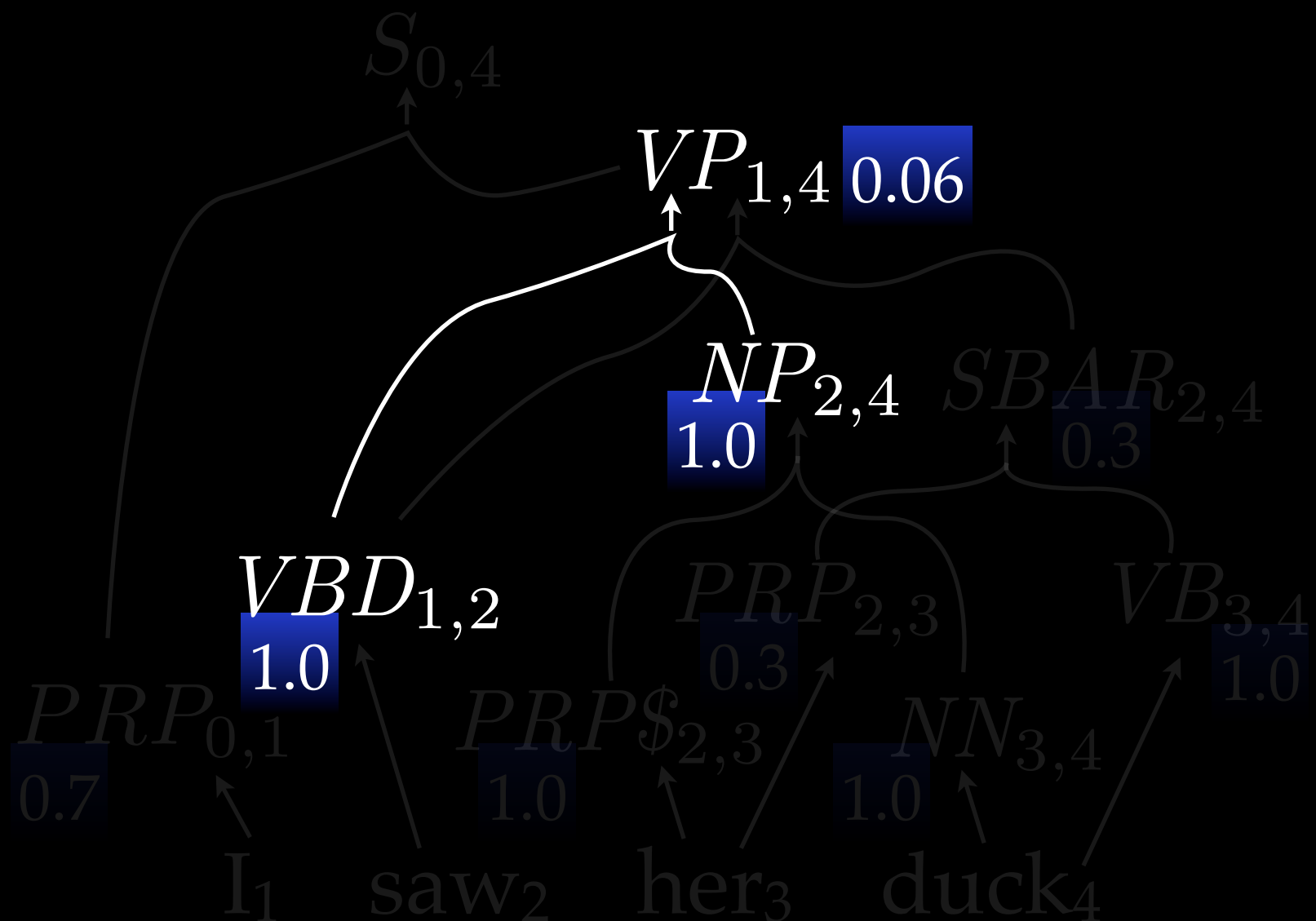
SBAR → PRP VB (1.0)

VB → duck (1.0)

VP → VBD NP (0.8)

VP → VBD SBAR (0.2)

VBD → saw (1.0)



Probabilistic Parsing

NN → duck (1.0)

NP → PRP\$ NN (1.0)

PRP → her (0.3)

PRP → I (0.7)

PRP\$ → her (1.0)

S → PRP VP (1.0)

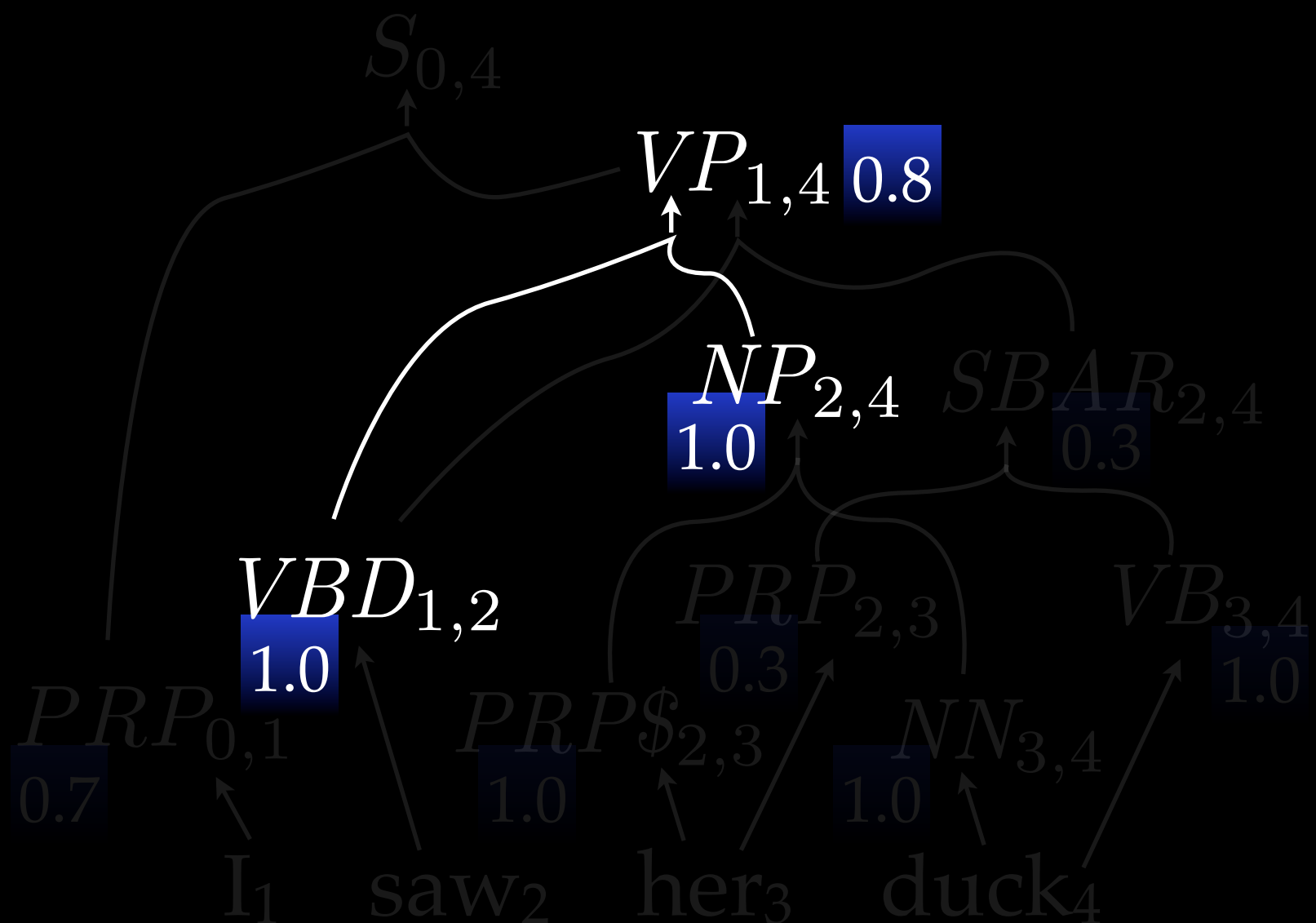
SBAR → PRP VB (1.0)

VB → duck (1.0)

VP → VBD NP (0.8)

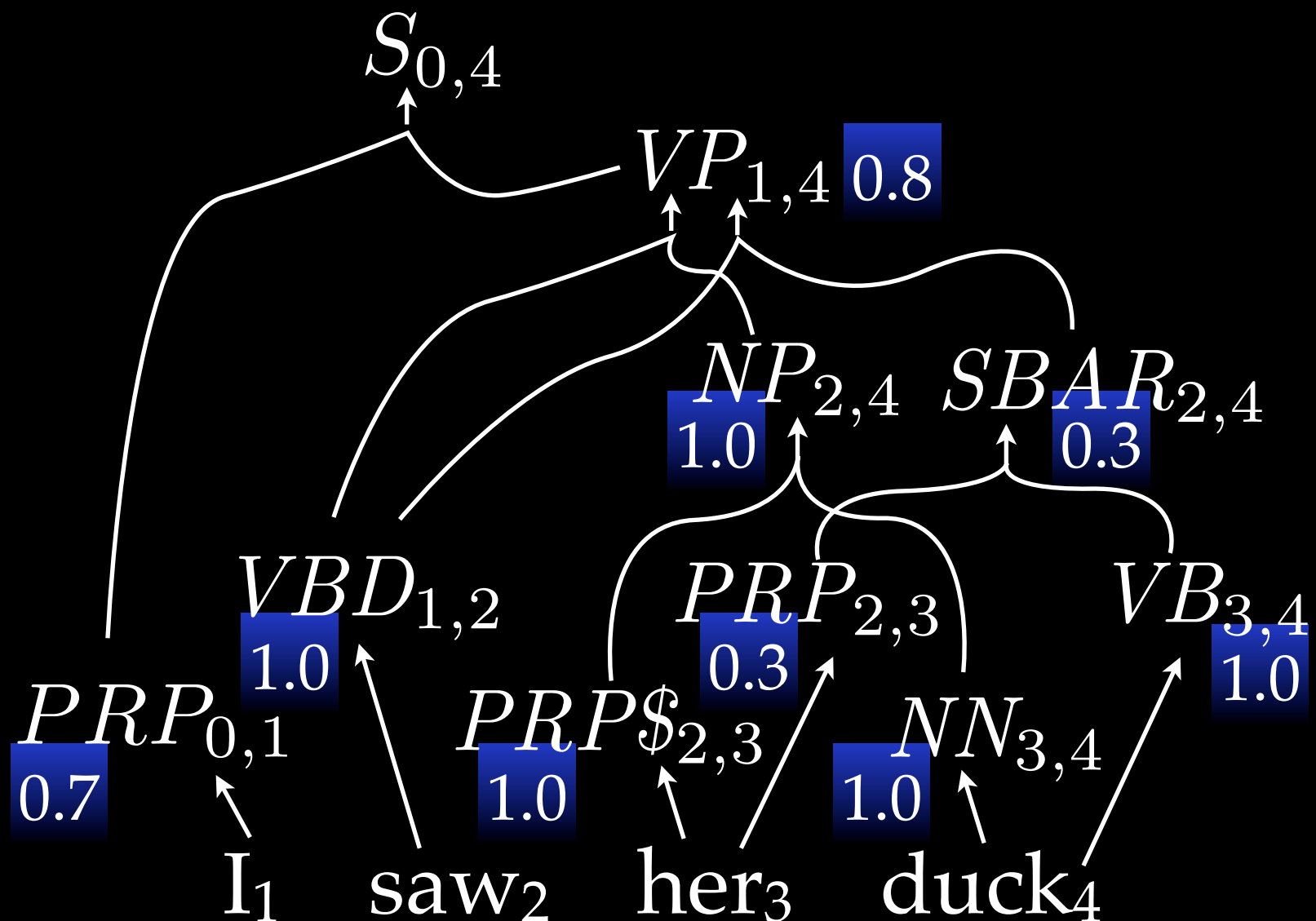
VP → VBD SBAR (0.2)

VBD → saw (1.0)



Probabilistic Parsing

$NN \rightarrow \text{duck}$	(1.0)
$NP \rightarrow PRP\$ NN$	(1.0)
$PRP \rightarrow \text{her}$	(0.3)
$PRP \rightarrow I$	(0.7)
$PRP\$ \rightarrow \text{her}$	(1.0)
$S \rightarrow PRP VP$	(1.0)
$SBAR \rightarrow PRP VB$	(1.0)
$VB \rightarrow \text{duck}$	(1.0)
$VP \rightarrow VBD NP$	(0.8)
$VP \rightarrow VBD SBAR$	(0.2)
$VBD \rightarrow \text{saw}$	(1.0)



Probabilistic Parsing

NN \rightarrow duck (1.0)

NP \rightarrow PRP\$ NN (1.0)

PRP \rightarrow her (0.3)

PRP \rightarrow I (0.7)

PRP\$ \rightarrow her (1.0)

S \rightarrow PRP VP (1.0)

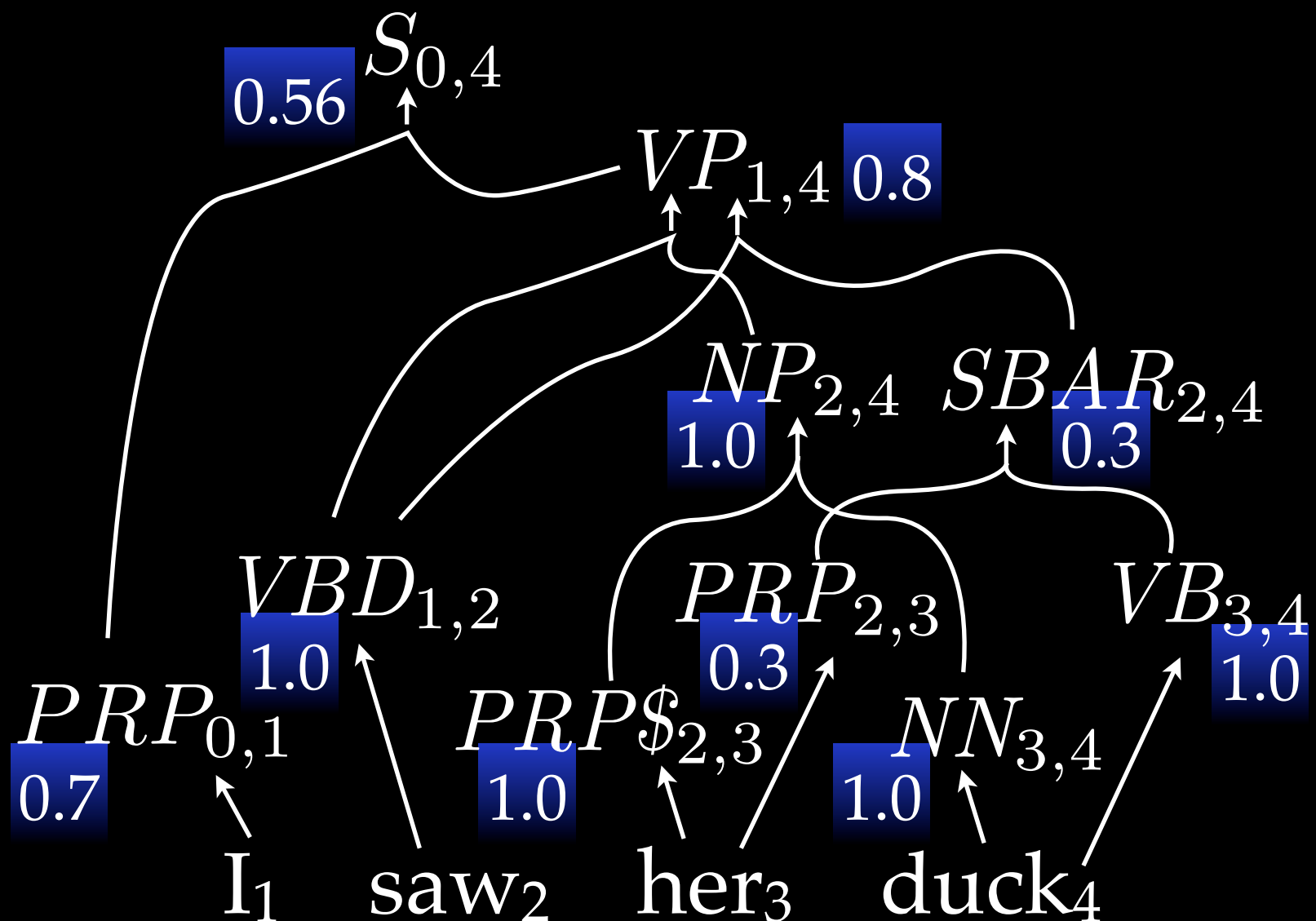
SBAR \rightarrow PRP VB (1.0)

VB \rightarrow duck (1.0)

VP \rightarrow VBD NP (0.8)

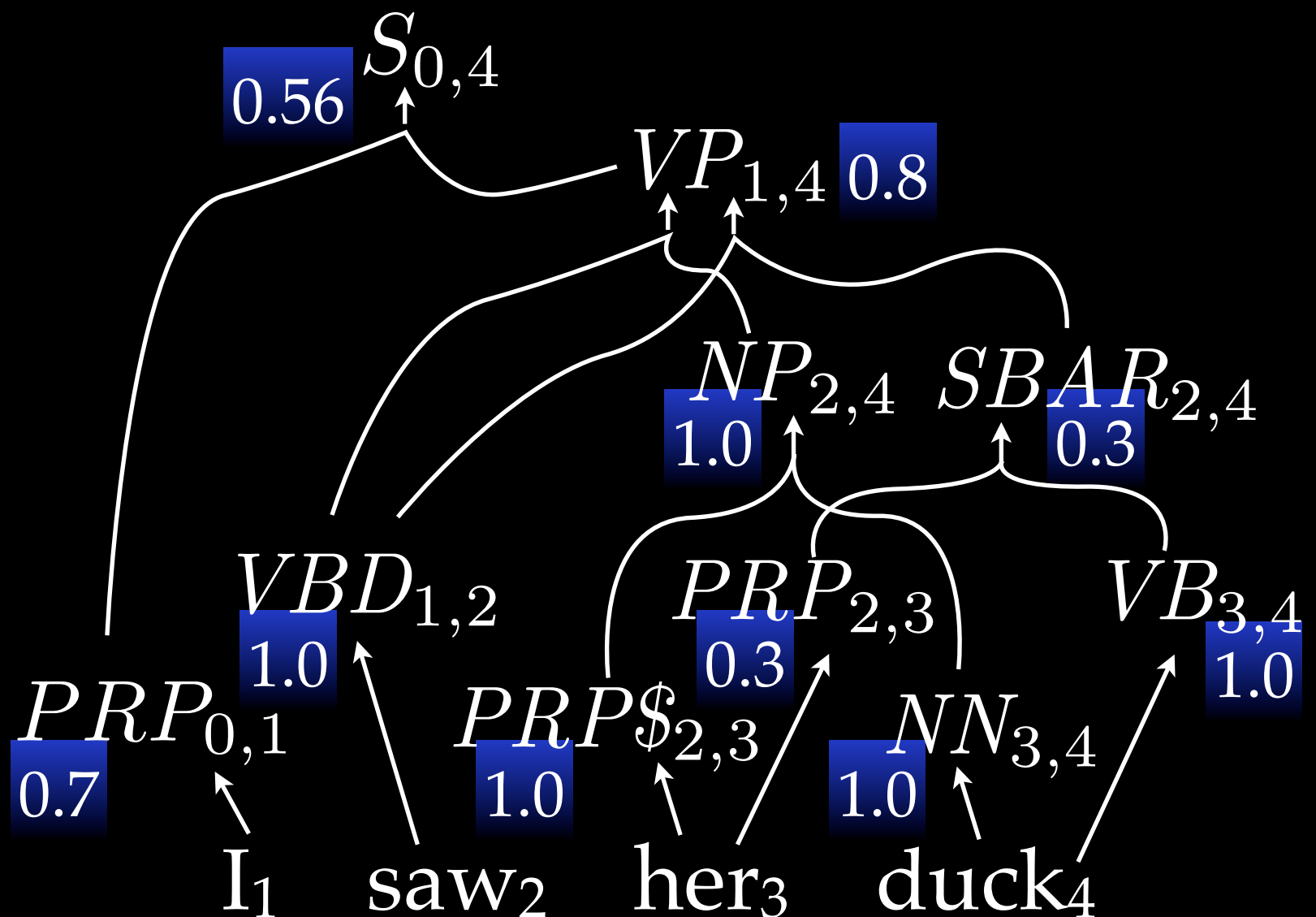
VP \rightarrow VBD SBAR (0.2)

VBD \rightarrow saw (1.0)



Probabilistic Parsing

$$X_{i,j} = \max(X_{i,j}, Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$



Computing Expectations

NN \rightarrow duck (1.0)

NP \rightarrow PRP\$ NN (1.0)

PRP \rightarrow her (0.3)

PRP \rightarrow I (0.7)

PRP\$ \rightarrow her (1.0)

S \rightarrow PRP VP (1.0)

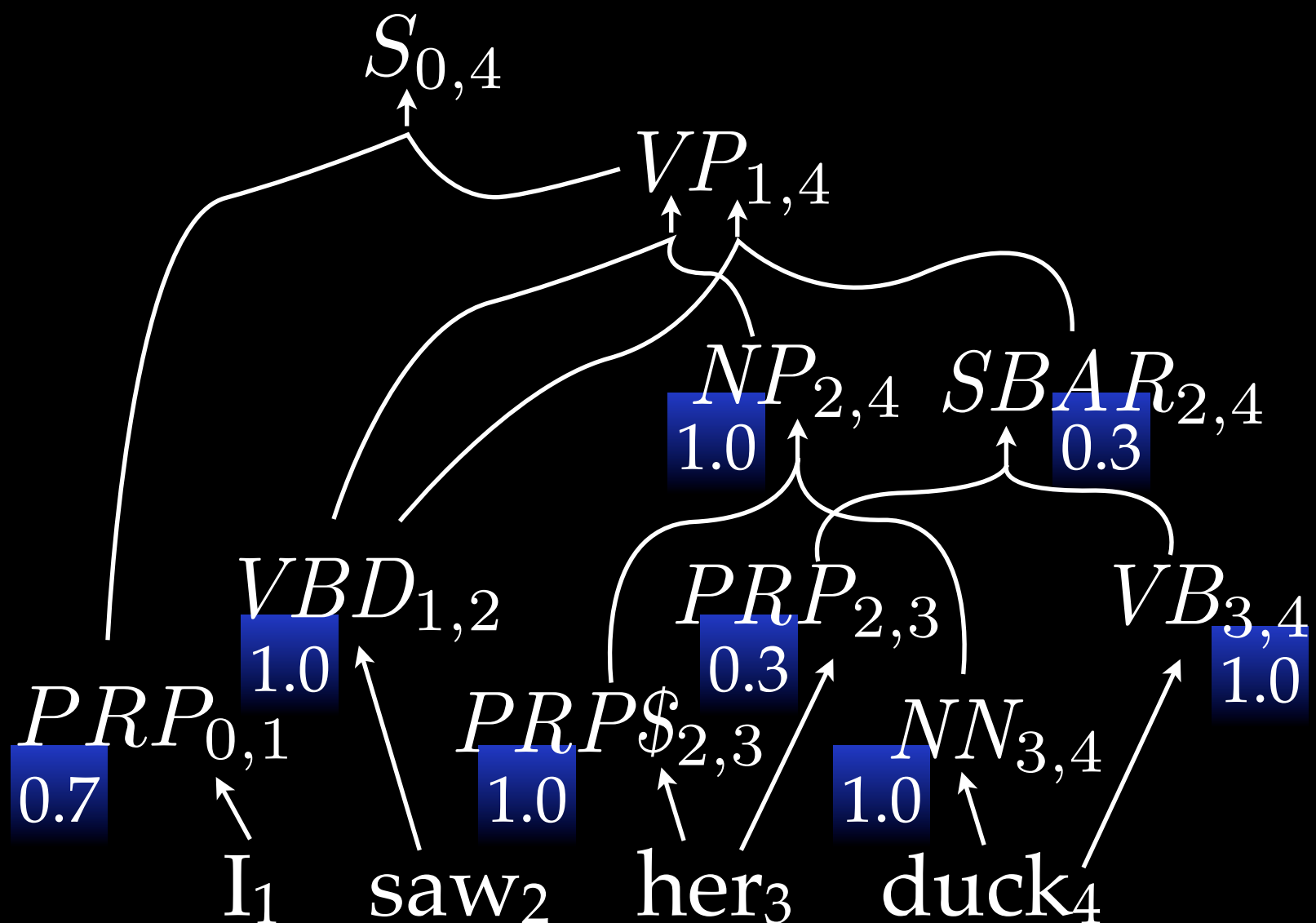
SBAR \rightarrow PRP VB (1.0)

VB \rightarrow duck (1.0)

VP \rightarrow VBD NP (0.8)

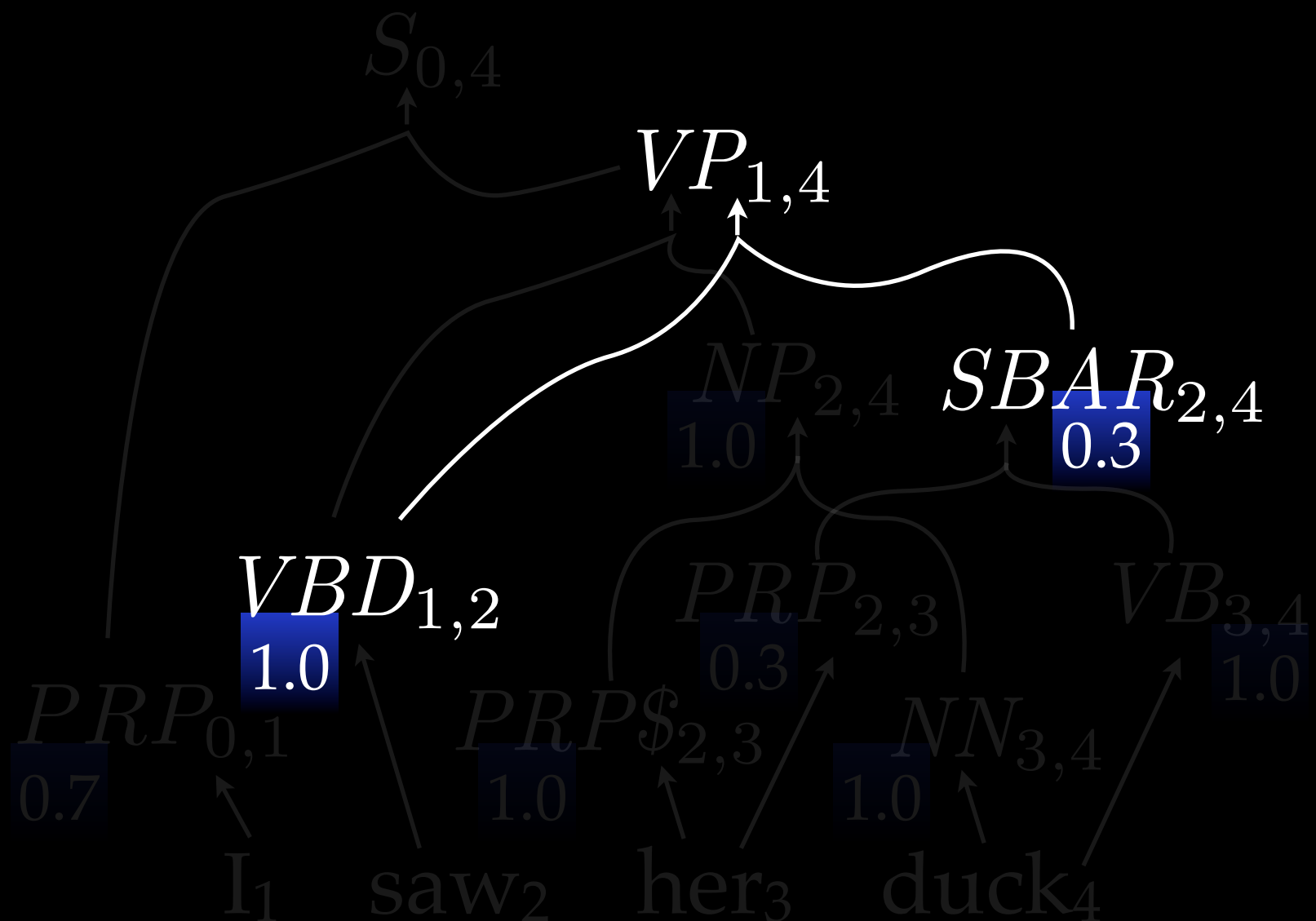
VP \rightarrow VBD SBAR (0.2)

VBD \rightarrow saw (1.0)



Computing Expectations

NN → duck	(1.0)
NP → PRP\$ NN	(1.0)
PRP → her	(0.3)
PRP → I	(0.7)
PRP\$ → her	(1.0)
S → PRP VP	(1.0)
SBAR → PRP VB	(1.0)
VB → duck	(1.0)
VP → VBD NP	(0.8)
VP → VBD SBAR	(0.2)
VBD → saw	(1.0)



Computing Expectations

NN \rightarrow duck (1.0)

NP \rightarrow PRP\$ NN (1.0)

PRP \rightarrow her (0.3)

PRP \rightarrow I (0.7)

PRP\$ \rightarrow her (1.0)

S \rightarrow PRP VP (1.0)

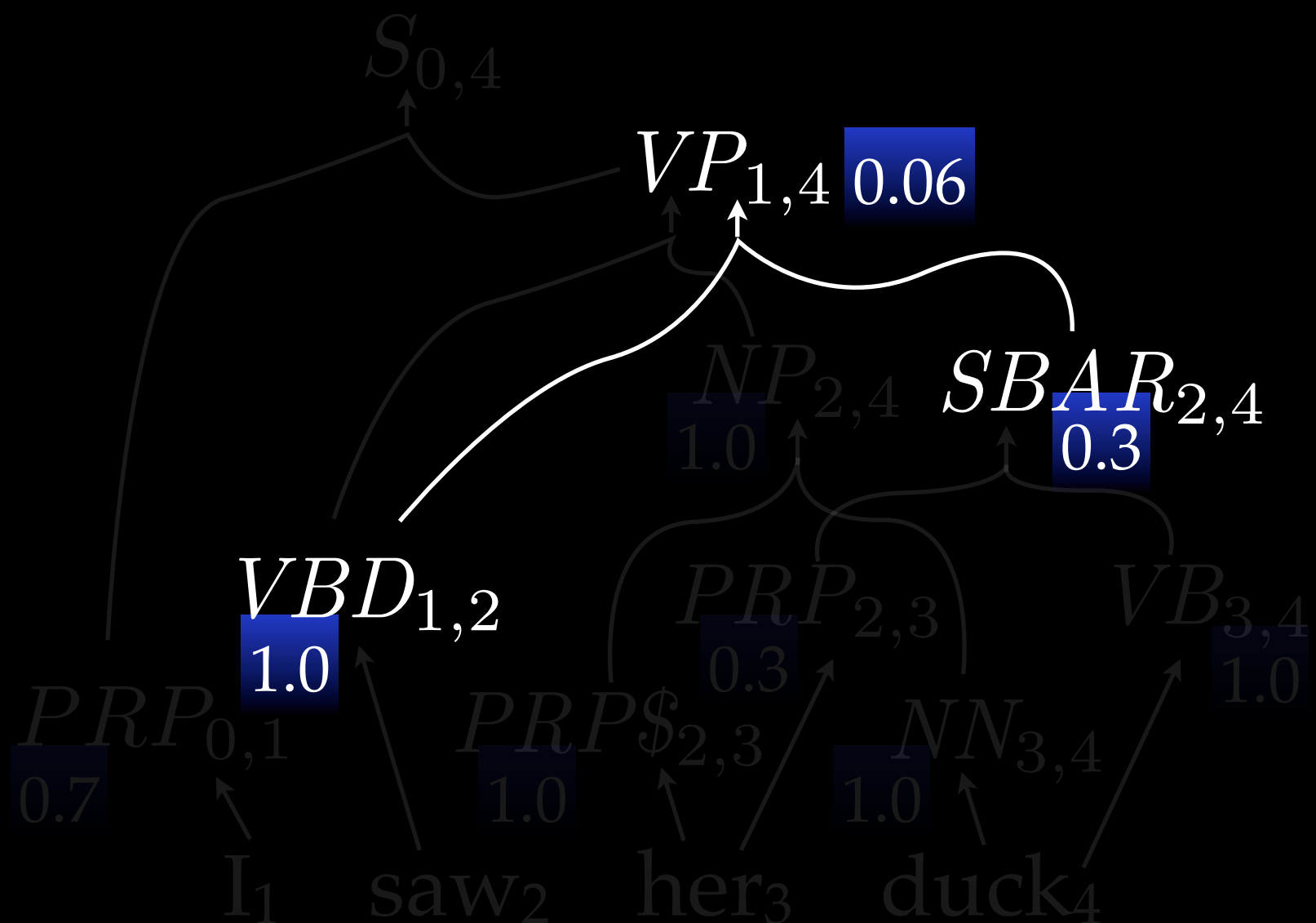
SBAR \rightarrow PRP VB (1.0)

VB \rightarrow duck (1.0)

VP \rightarrow VBD NP (0.8)

VP \rightarrow VBD SBAR (0.2)

VBD \rightarrow saw (1.0)



Computing Expectations

NN \rightarrow duck (1.0)

NP \rightarrow PRP\$ NN (1.0)

PRP \rightarrow her (0.3)

PRP \rightarrow I (0.7)

PRP\$ \rightarrow her (1.0)

S \rightarrow PRP VP (1.0)

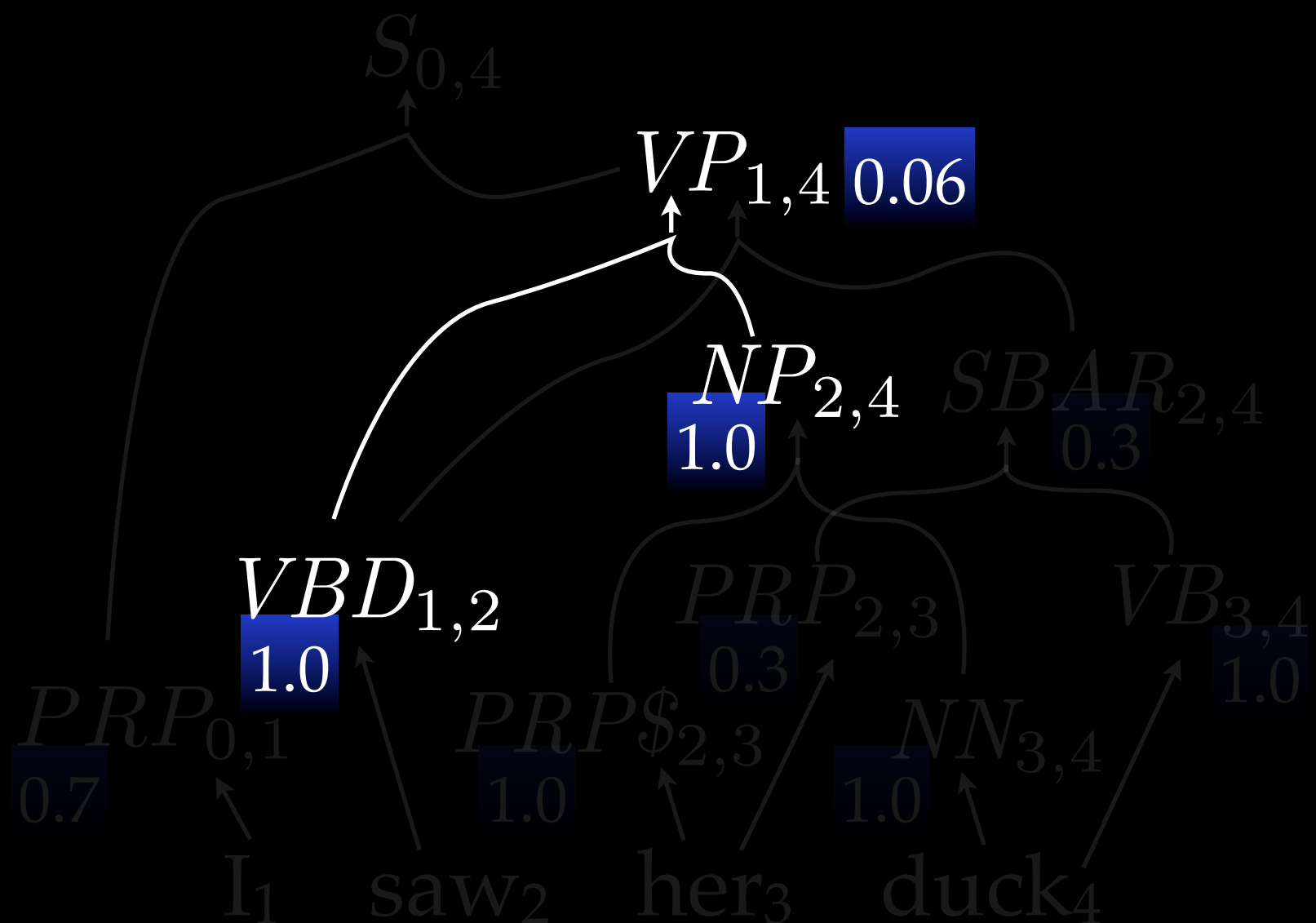
SBAR \rightarrow PRP VB (1.0)

VB \rightarrow duck (1.0)

VP \rightarrow VBD NP (0.8)

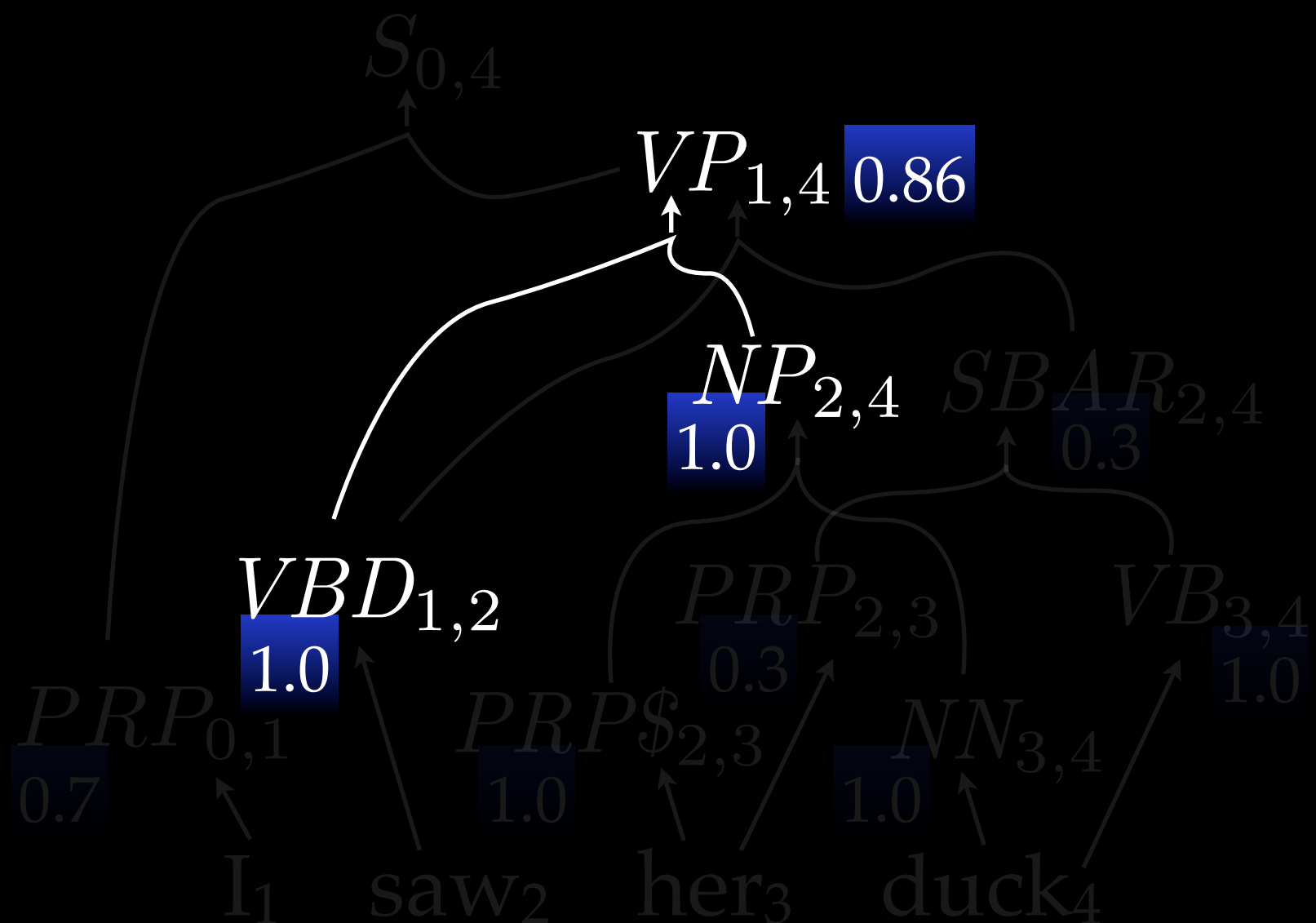
VP \rightarrow VBD SBAR (0.2)

VBD \rightarrow saw (1.0)



Computing Expectations

$NN \rightarrow \text{duck}$	(1.0)
$NP \rightarrow \text{PRP\$ } NN$	(1.0)
$\text{PRP} \rightarrow \text{her}$	(0.3)
$\text{PRP} \rightarrow \text{I}$	(0.7)
$\text{PRP\$} \rightarrow \text{her}$	(1.0)
$S \rightarrow \text{PRP } VP$	(1.0)
$\text{SBAR} \rightarrow \text{PRP } VB$	(1.0)
$\text{VB} \rightarrow \text{duck}$	(1.0)
$VP \rightarrow \text{VBD } NP$	(0.8)
$VP \rightarrow \text{VBD } \text{SBAR}$	(0.2)
$\text{VBD} \rightarrow \text{saw}$	(1.0)



Computing Expectations

NN \rightarrow duck (1.0)

NP \rightarrow PRP\$ NN (1.0)

PRP \rightarrow her (0.3)

PRP \rightarrow I (0.7)

PRP\$ \rightarrow her (1.0)

S \rightarrow PRP VP (1.0)

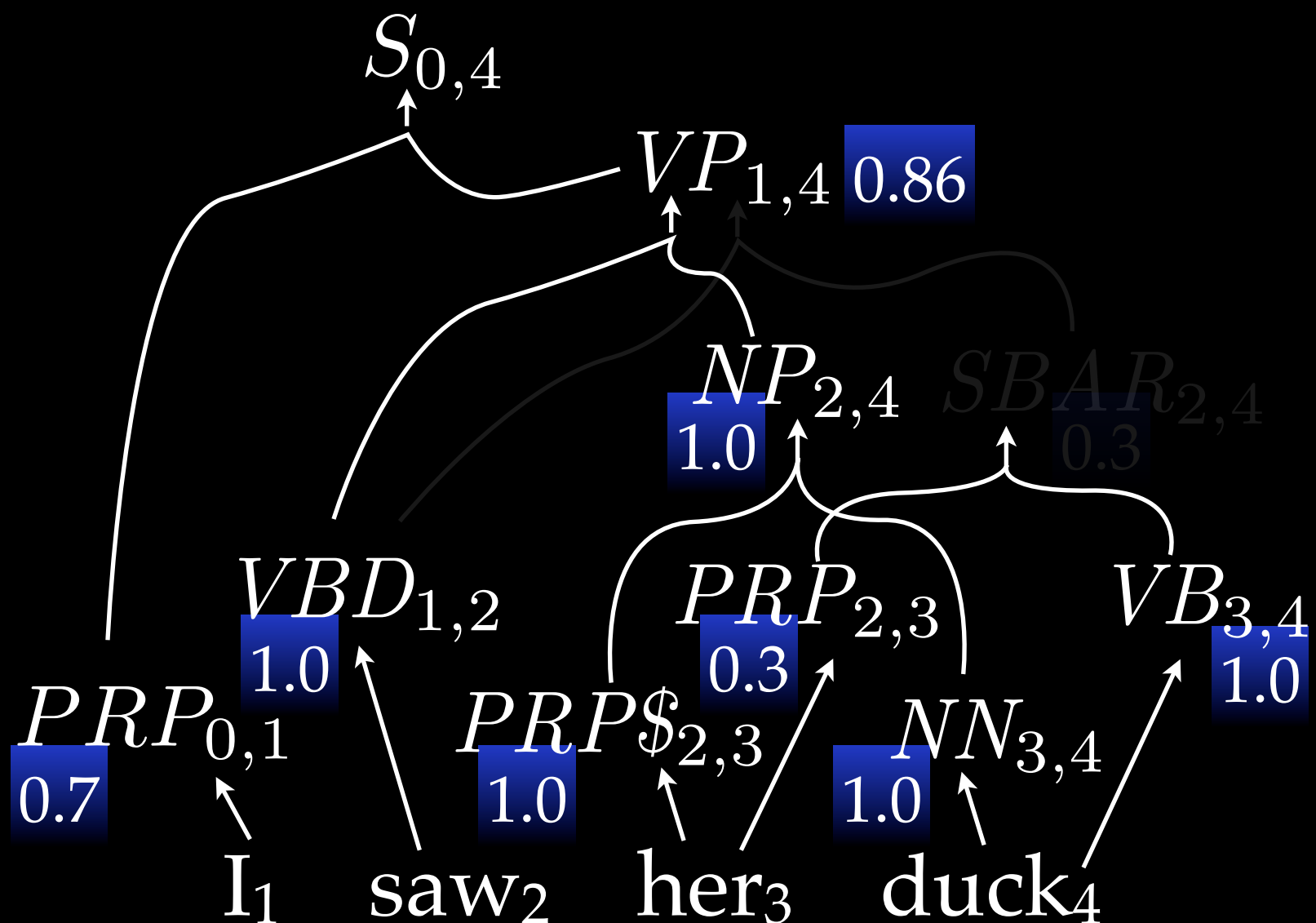
SBAR \rightarrow PRP VB (1.0)

VB \rightarrow duck (1.0)

VP \rightarrow VBD NP (0.8)

VP \rightarrow VBD SBAR (0.2)

VBD \rightarrow saw (1.0)



Computing Expectations

NN \rightarrow duck (1.0)

NP \rightarrow PRP\$ NN (1.0)

PRP \rightarrow her (0.3)

PRP \rightarrow I (0.7)

PRP\$ \rightarrow her (1.0)

S \rightarrow PRP VP (1.0)

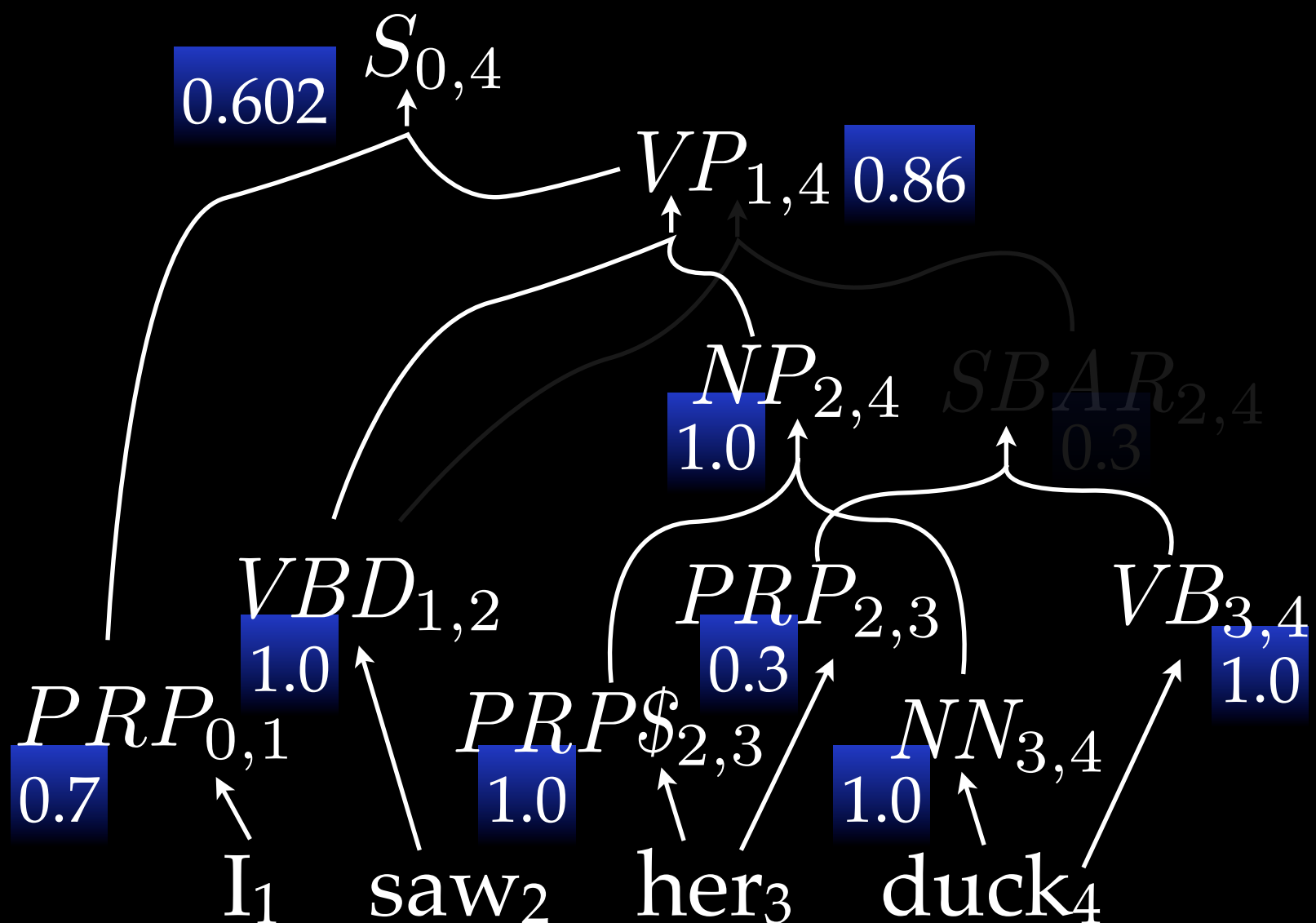
SBAR \rightarrow PRP VB (1.0)

VB \rightarrow duck (1.0)

VP \rightarrow VBD NP (0.8)

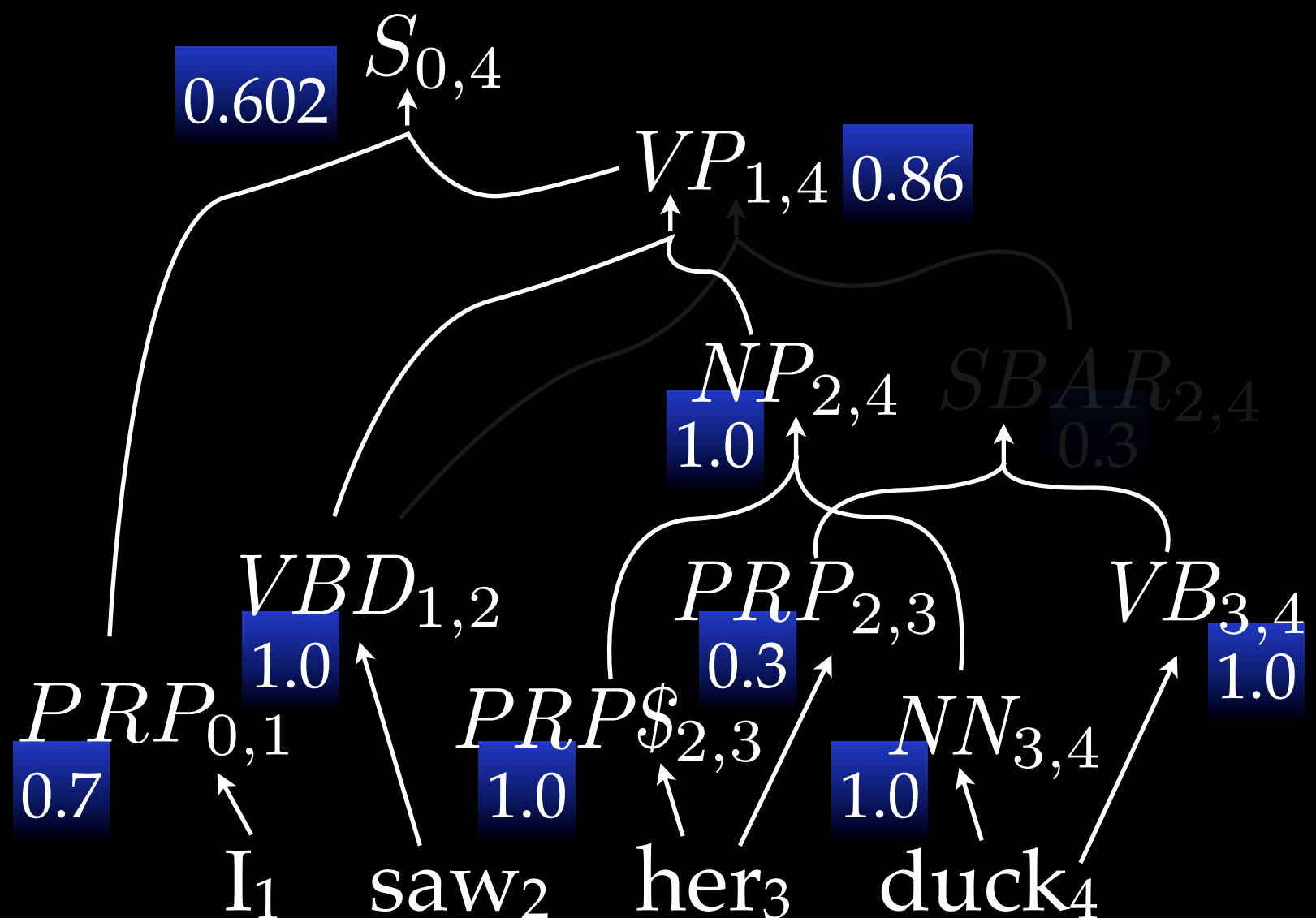
VP \rightarrow VBD SBAR (0.2)

VBD \rightarrow saw (1.0)



Computing Expectations

$$X_{i,j} = X_{i,j} + (Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$



Semiring Parsing

$$X_{i,j} \leftarrow Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ)$$

$$X_{i,j} = \max(X_{i,j}, Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

$$X_{i,j} = X_{i,j} + (Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

Semiring Parsing

$$X_{i,j} = X_{i,j} \vee (Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ))$$

$$X_{i,j} = \max(X_{i,j}, Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

$$X_{i,j} = X_{i,j} + (Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

Semiring Parsing

$$X_{i,j} = X_{i,j} \vee (Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ))$$

$$\langle \{T, F\}, \vee, \wedge \rangle$$

$$X_{i,j} = \max(X_{i,j}, Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

$$X_{i,j} = X_{i,j} + (Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

Semiring Parsing

$$X_{i,j} = X_{i,j} \vee (Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ))$$

$$\langle \{T, F\}, \vee, \wedge \rangle$$

$$X_{i,j} = \max(X_{i,j}, Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

$$\langle \mathbb{R}, \max, \times \rangle$$

$$X_{i,j} = X_{i,j} + (Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

Semiring Parsing

$$X_{i,j} = X_{i,j} \vee (Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ))$$

$$\langle \{T, F\}, \vee, \wedge \rangle$$

$$X_{i,j} = \max(X_{i,j}, Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

$$\langle \mathbb{R}, \max, \times \rangle$$

$$X_{i,j} = X_{i,j} + (Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

$$\langle \mathbb{R}, +, \times \rangle$$

Semiring Parsing

$$X_{i,j} = X_{i,j} \vee (Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ))$$

$$\langle \{T, F\}, \vee, \wedge \rangle$$

$$X_{i,j} = \max(X_{i,j}, Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

$$\langle \mathbb{R}, \max, \times \rangle$$

$$X_{i,j} = X_{i,j} + (Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

$$\langle \mathbb{R}, +, \times \rangle$$

$$X_{i,j} = X_{i,j} \oplus (Y_{i,k} \otimes Z_{k,j} \otimes R(X \rightarrow YZ))$$

Semiring Parsing

$$X_{i,j} = X_{i,j} \vee (Y_{i,k} \wedge Z_{k,j} \wedge (X \rightarrow YZ))$$

$$\text{boolean} \quad \langle \{T, F\}, \vee, \wedge \rangle$$

$$X_{i,j} = \max(X_{i,j}, Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

$$\text{Viterbi} \quad \langle \mathbb{R}, \max, \times \rangle$$

$$X_{i,j} = X_{i,j} + (Y_{i,k} \times Z_{k,j} \times p(X \rightarrow YZ))$$

$$\text{inside} \quad \langle \mathbb{R}, +, \times \rangle$$

$$X_{i,j} = X_{i,j} \oplus (Y_{i,k} \otimes Z_{k,j} \otimes R(X \rightarrow YZ))$$

Parsing

Is Intersection!

$NN_{3,4} \rightarrow \text{duck}$

$NP_{2,4} \rightarrow PRP\$_{2,3} NN_{3,4}$

$PRP_{2,3} \rightarrow \text{her}$

$PRP_{0,1} \rightarrow \text{I}$

$PRP\$_{2,3} \rightarrow \text{her}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

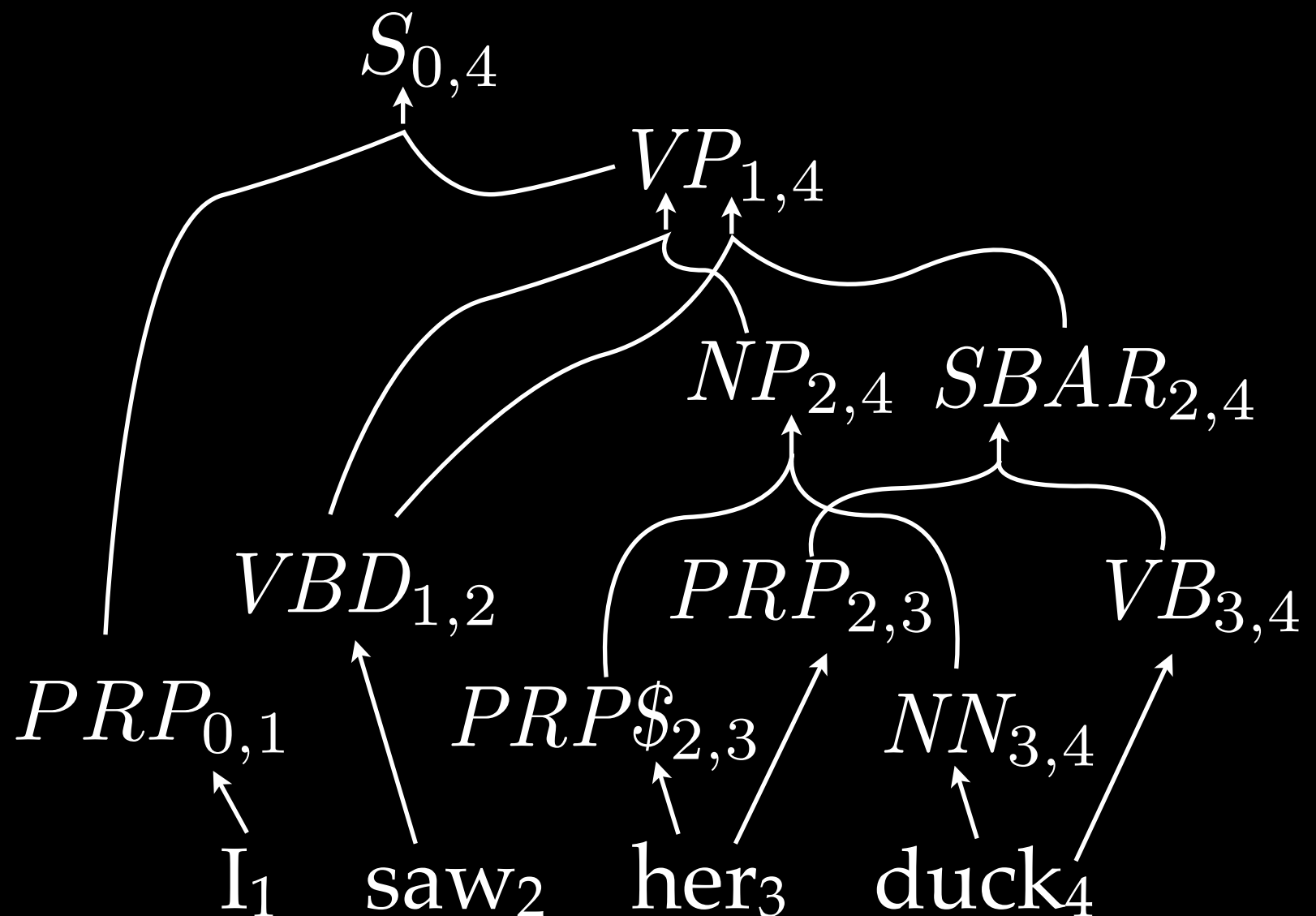
$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{duck}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

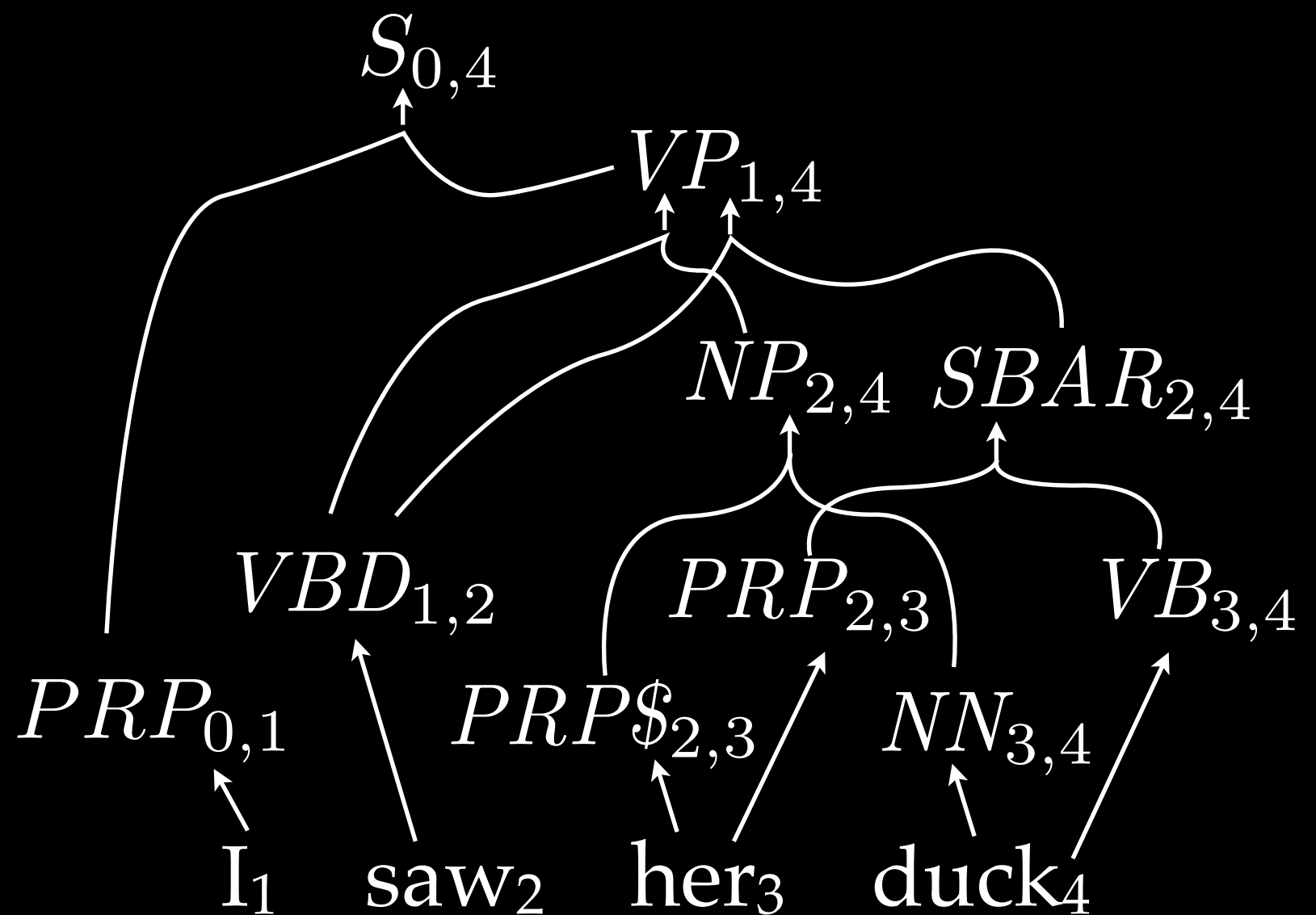
$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{saw}$



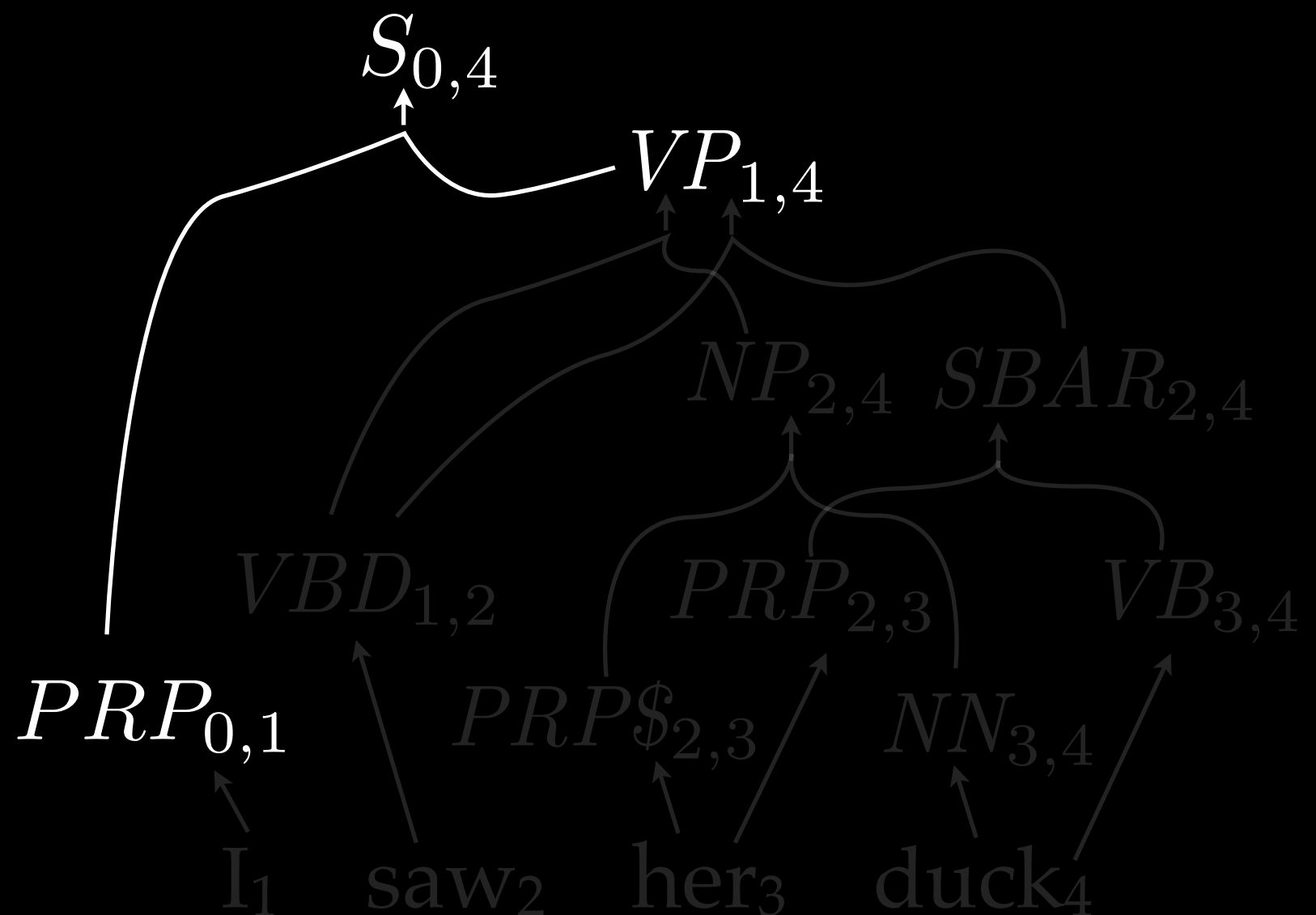
Parsing

Is Intersection!



Parsing

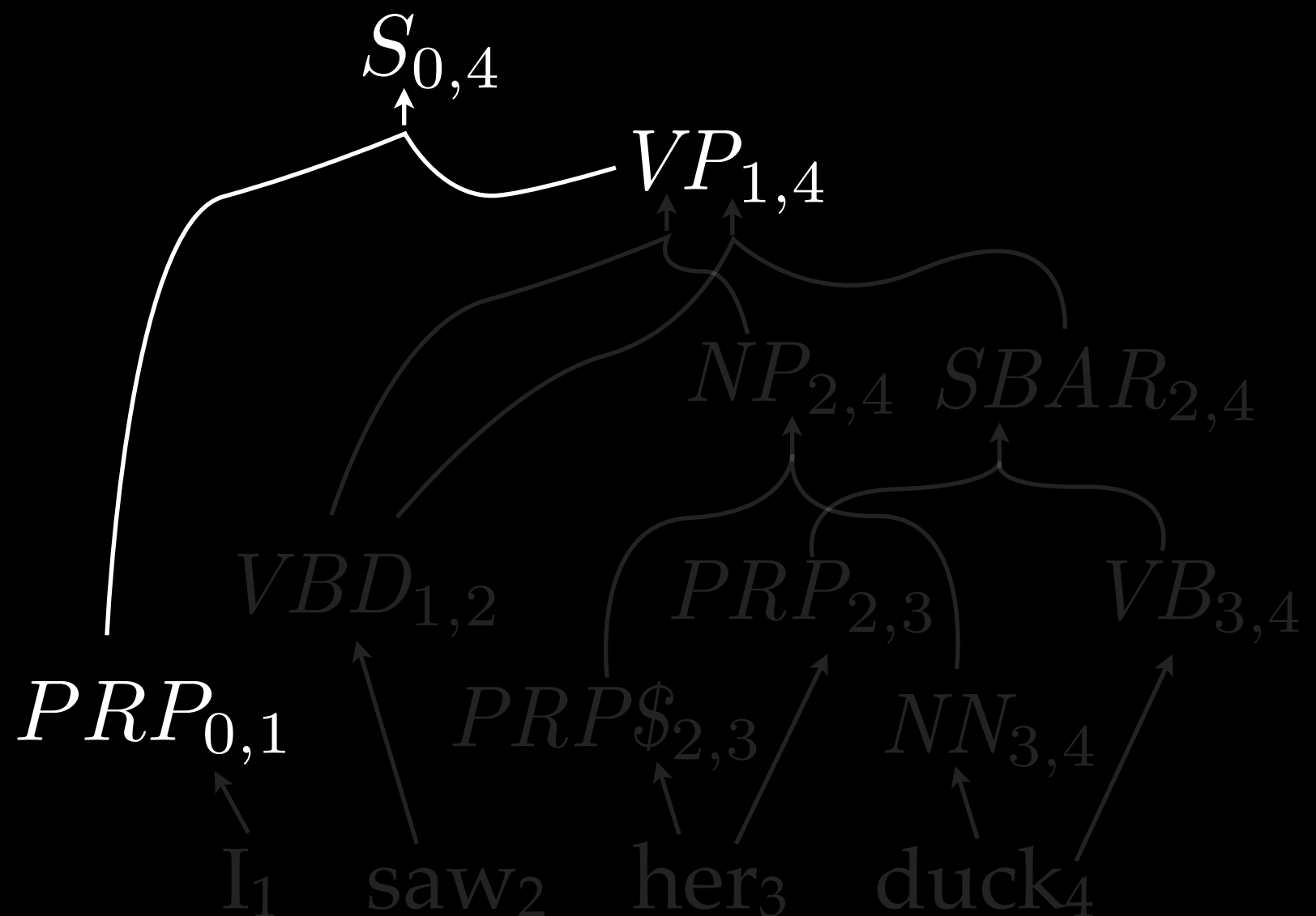
Is Intersection!



Parsing

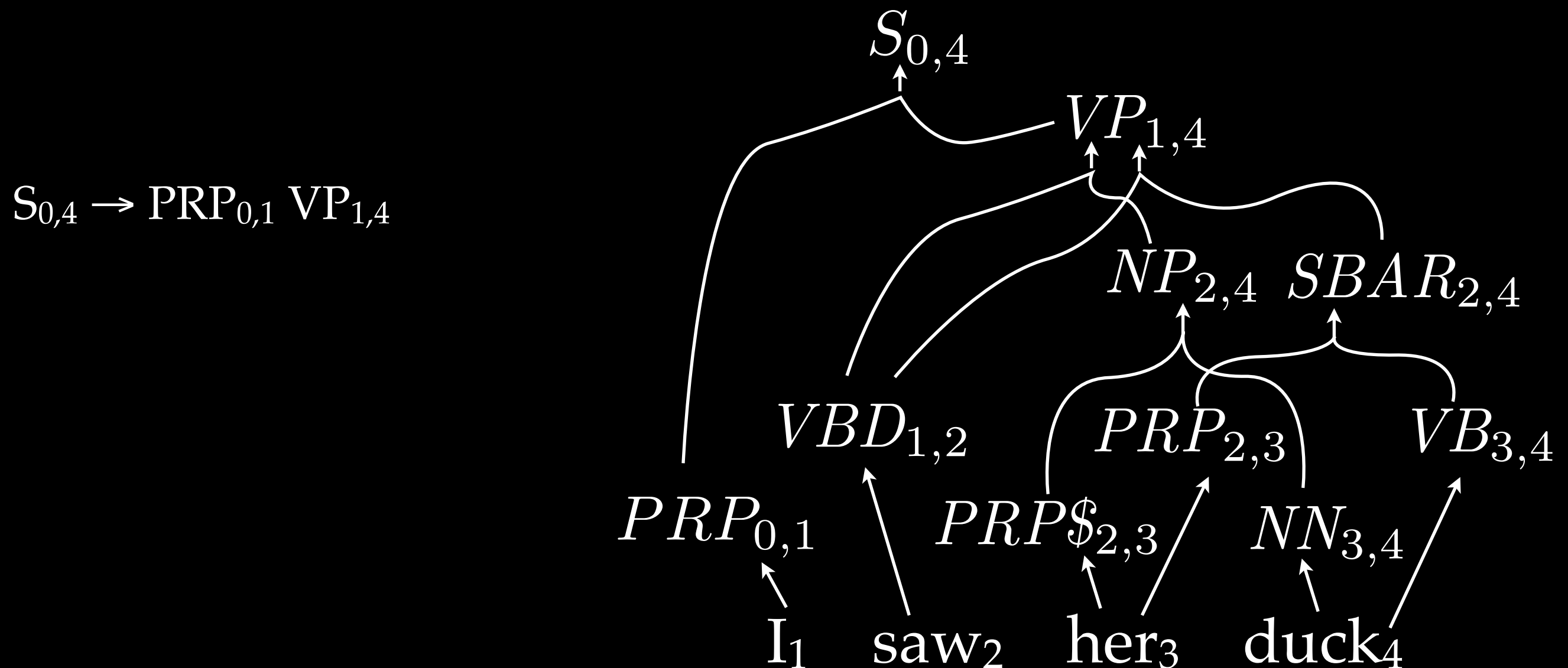
Is Intersection!

$S_{0,4} \rightarrow \text{PRP}_{0,1} \text{VP}_{1,4}$



Parsing

Is Intersection!



Parsing

Is Intersection!

$NN_{3,4} \rightarrow \text{duck}$

$NP_{2,4} \rightarrow PRP\$_{2,3} NN_{3,4}$

$PRP_{2,3} \rightarrow \text{her}$

$PRP_{0,1} \rightarrow \text{I}$

$PRP\$_{2,3} \rightarrow \text{her}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

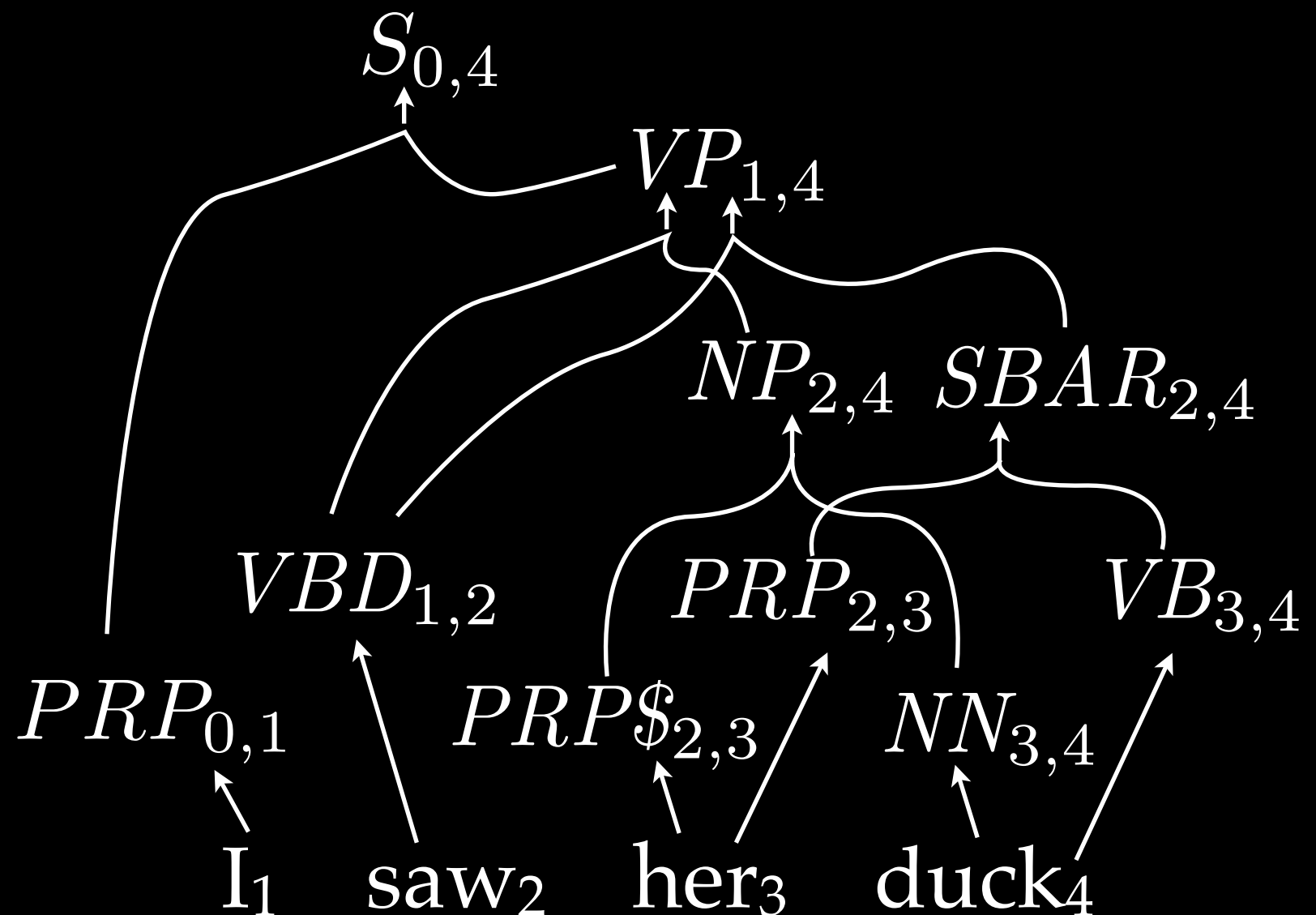
$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{duck}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{saw}$



Parsing

Is Intersection!

$NN_{3,4} \rightarrow \text{duck}$

$NP_{2,4} \rightarrow PRP\$_{2,3} NN_{3,4}$

$PRP_{2,3} \rightarrow \text{her}$

$PRP_{0,1} \rightarrow \text{I}$

$PRP\$_{2,3} \rightarrow \text{her}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{duck}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{saw}$

$NN_{3,4} \rightarrow \text{pato}$

$NP_{2,4} \rightarrow PRP\$_{2,3} NN_{3,4}$

$PRP_{2,3} \rightarrow \text{su}$

$PRP_{0,1} \rightarrow \text{yo}$

$PRP\$_{2,3} \rightarrow \text{ella}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{agacharse}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{vi}$

Parsing

Is Intersection!

$NN_{3,4} \rightarrow \text{duck}$

$NP_{2,4} \rightarrow PRP\$_{2,3} NN_{3,4}$

$PRP_{2,3} \rightarrow \text{her}$

$PRP_{0,1} \rightarrow \text{I}$

$PRP\$_{2,3} \rightarrow \text{her}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{duck}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{saw}$

$NN_{3,4} \rightarrow \text{pato}$

$NP_{2,4} \rightarrow PRP\$_{2,3} NN_{3,4}$

$PRP_{2,3} \rightarrow \text{su}$

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$PRP\$_{2,3} \rightarrow \text{ella}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{agacharse}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{vi}$

yo vi ella agacharse

yo vi su pato

Synchronous Parsing as Intersection

Synchronous Parsing as Intersection

- Parse the English sentence (intersection).

Synchronous Parsing as Intersection

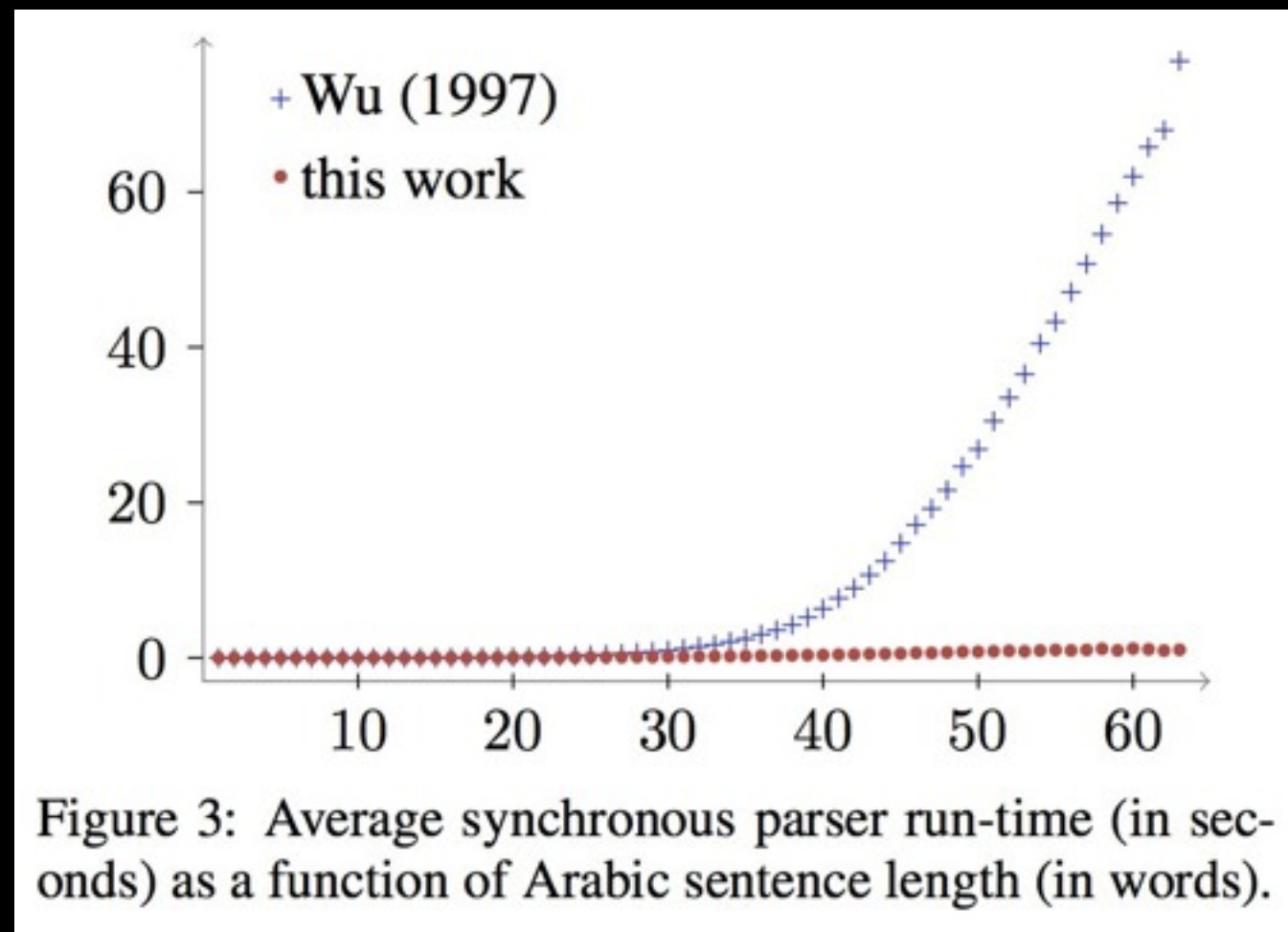
- Parse the English sentence (intersection).
- Project grammar into French.

Synchronous Parsing as Intersection

- Parse the English sentence (intersection).
- Project grammar into French.
- Parse the French sentence (intersection).

Synchronous Parsing as Intersection

- Parse the English sentence (intersection).
- Project grammar into French.
- Parse the French sentence (intersection).



Dyer, NAACL 2010

Translation as Intersection?

$NN_{3,4} \rightarrow \text{duck}$

$NP_{2,4} \rightarrow PRP\$_{2,3} NN_{3,4}$

$PRP_{2,3} \rightarrow \text{her}$

$PRP_{0,1} \rightarrow \text{I}$

$PRP\$_{2,3} \rightarrow \text{her}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{duck}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{saw}$

$NN_{3,4} \rightarrow \text{pato}$

$NP_{2,4} \rightarrow PRP\$_{2,3} NN_{3,4}$

$PRP_{2,3} \rightarrow \text{su}$

$PRP_{0,1} \rightarrow \text{yo}$

$PRP\$_{2,3} \rightarrow \text{ella}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{agacharse}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{vi}$

yo vi ella agacharse

yo vi su pato

Translation as Intersection?

Observation: target grammar generates a *finite language*

$NN_{3,4} \rightarrow \text{duck}$

$NP_{2,4} \rightarrow PRP\$_{2,3} NN_{3,4}$

$PRP_{2,3} \rightarrow \text{her}$

$PRP_{0,1} \rightarrow \text{I}$

$PRP\$_{2,3} \rightarrow \text{her}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{duck}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

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yo vi ella agacharse

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Translation as Intersection?

$NN_{3,4} \rightarrow \text{pato}$

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$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

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$VB_{3,4} \rightarrow \text{agacharse}$

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$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{vi}$

Translation as Intersection?

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$PRP\$_{2,3} \rightarrow \text{ella}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

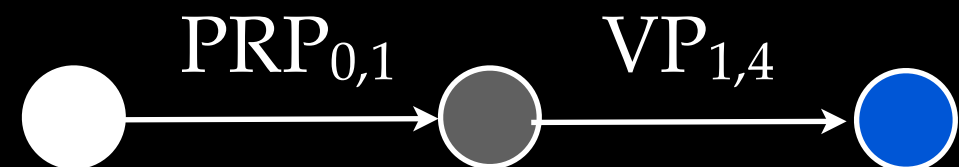
$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{agacharse}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{vi}$



Translation as Intersection?

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$PRP\$_{2,3} \rightarrow \text{ella}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

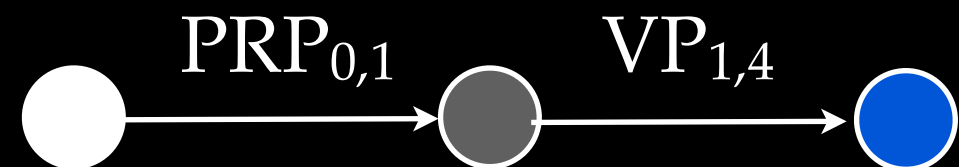
$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{agacharse}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{vi}$



Translation as Intersection?

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$NP_{2,4} \rightarrow PRP\$_{2,3} NN_{3,4}$

$PRP_{2,3} \rightarrow \text{su}$

$PRP_{0,1} \rightarrow \text{yo}$

$PRP\$_{2,3} \rightarrow \text{ella}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

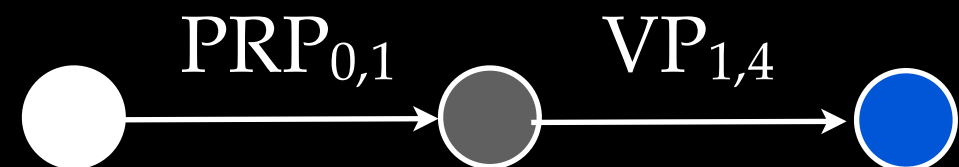
$SBAR_{2,4} \rightarrow PRP_{2,3} VB_{3,4}$

$VB_{3,4} \rightarrow \text{agacharse}$

$VP_{1,4} \rightarrow VBD_{1,2} NP_{2,4}$

$VP_{1,4} \rightarrow VBD_{1,2} SBAR_{2,4}$

$VBD_{1,2} \rightarrow \text{vi}$



Translation as Intersection?

$NN_{3,4} \rightarrow \text{pato}$

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$PRP_{0,1} \rightarrow \text{yo}$

$PRP\$_{2,3} \rightarrow \text{ella}$

$S_{0,4} \rightarrow PRP_{0,1} VP_{1,4}$

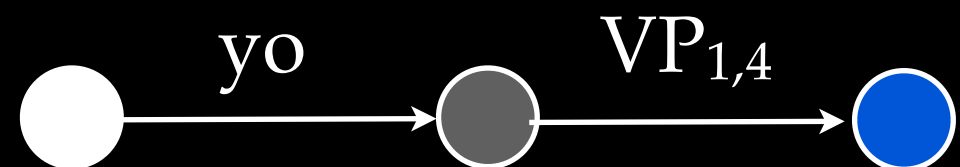
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Translation as Intersection?

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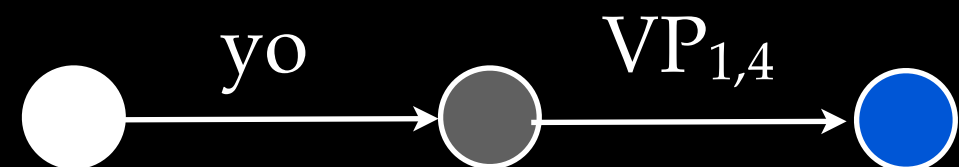
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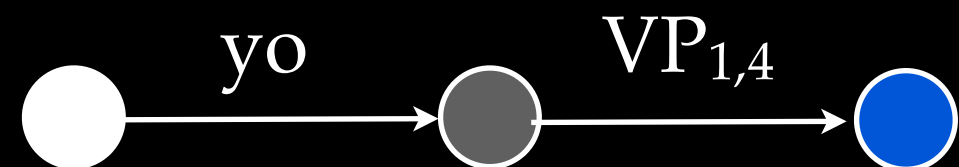
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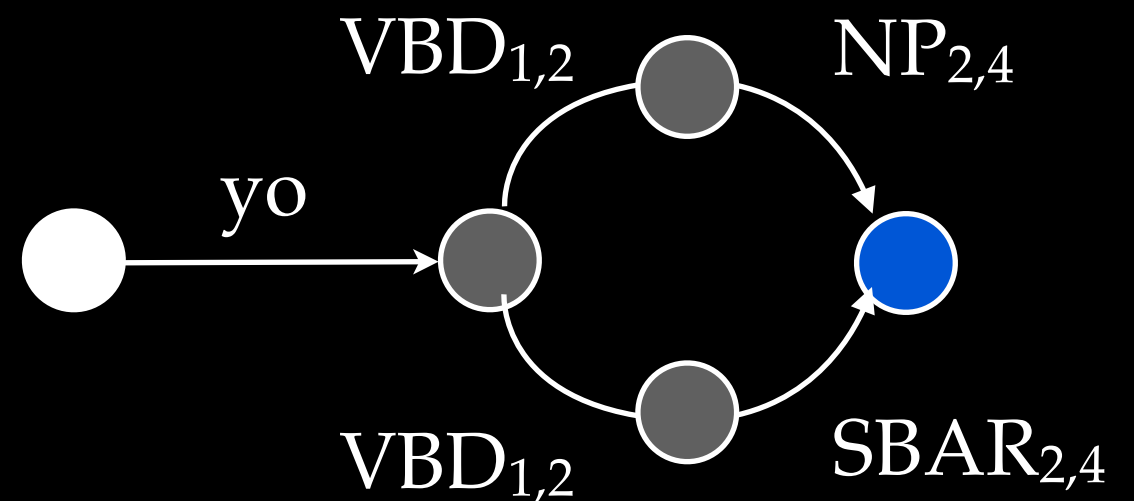
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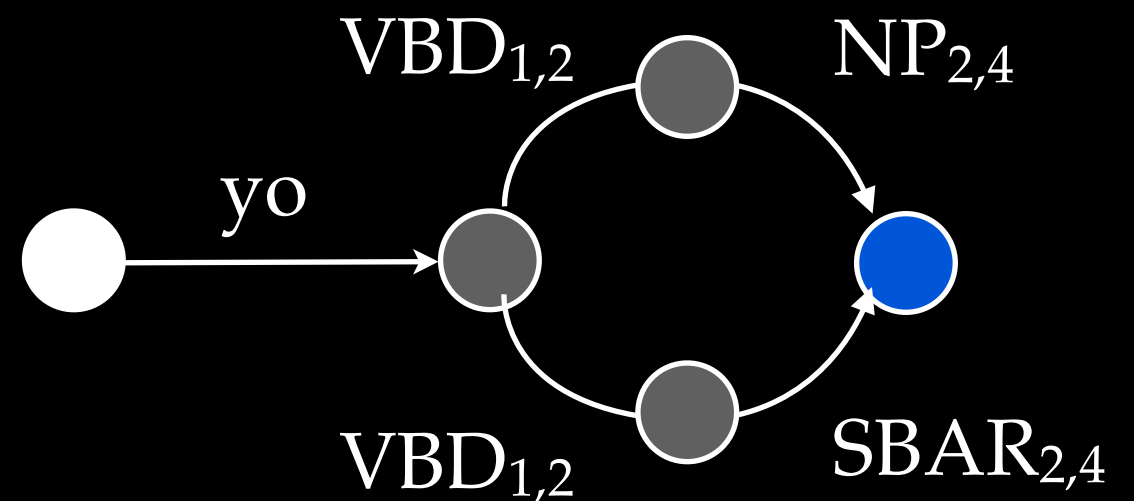
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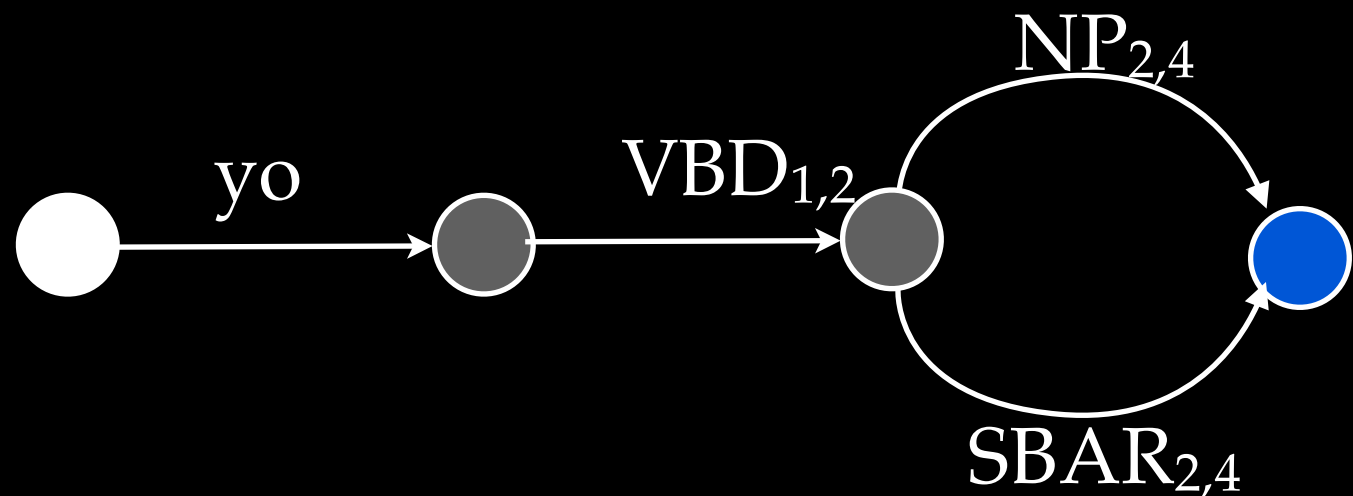
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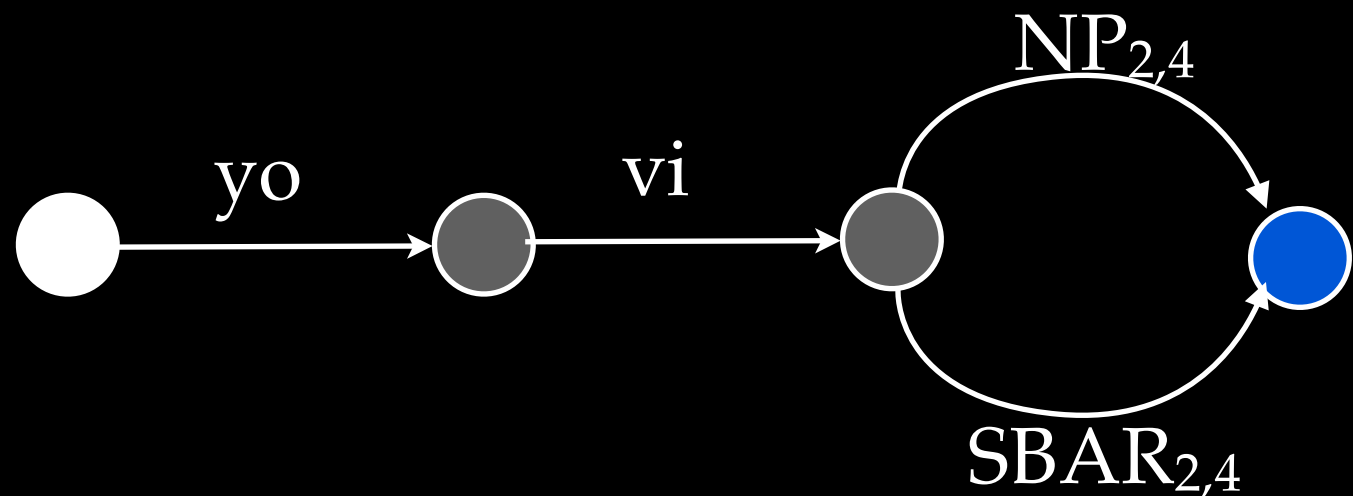
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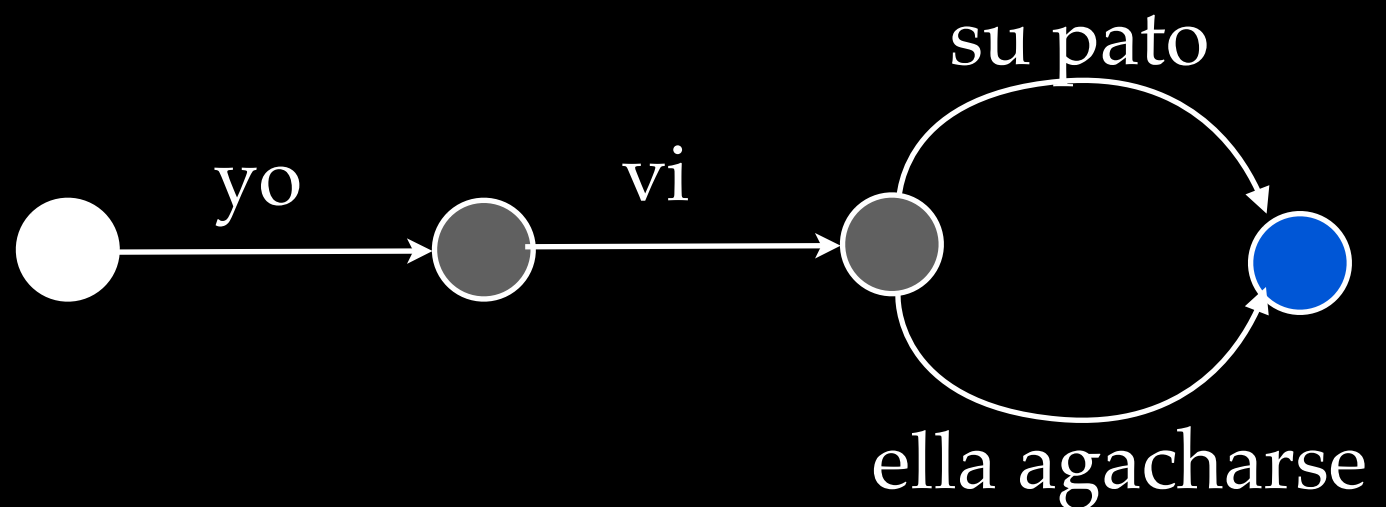
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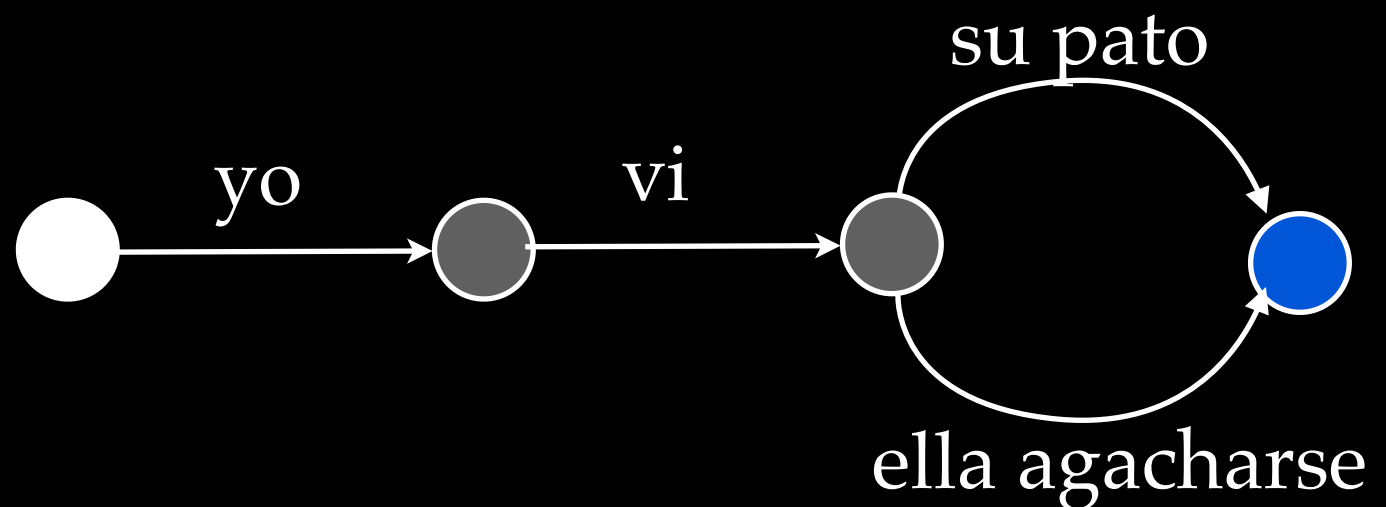
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Better: lazy algorithm

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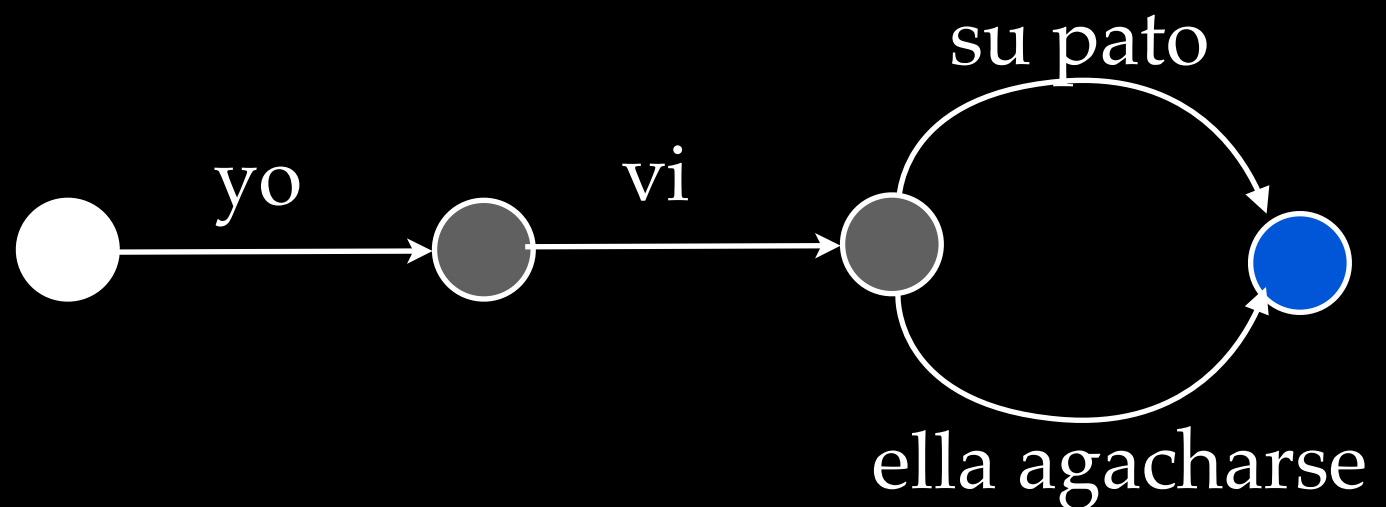
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Even better: convert to PDA

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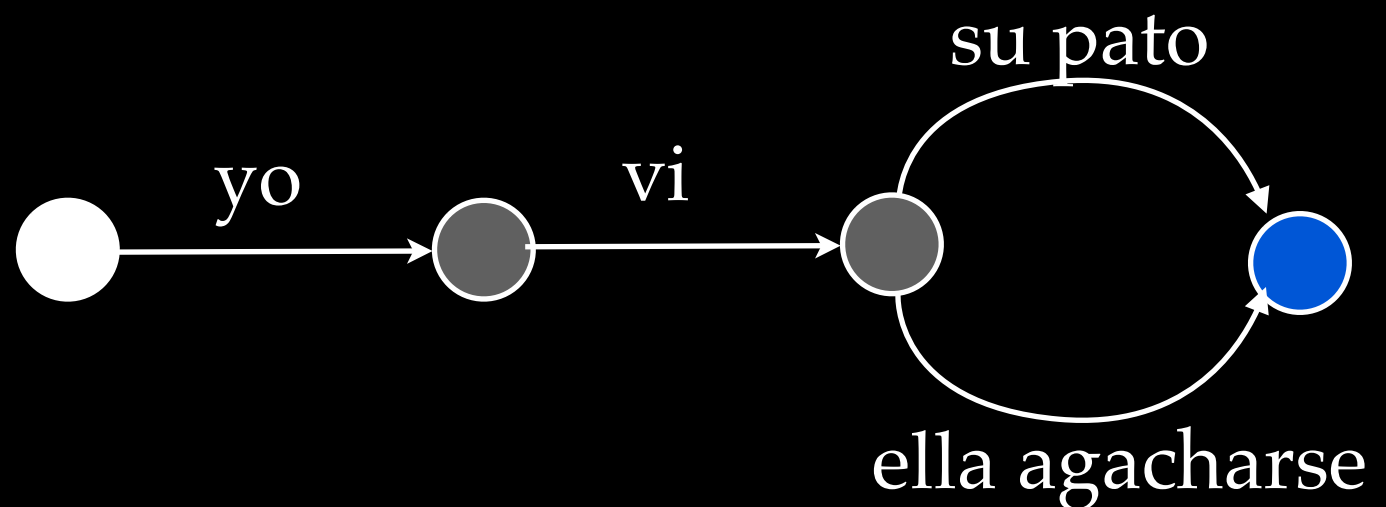
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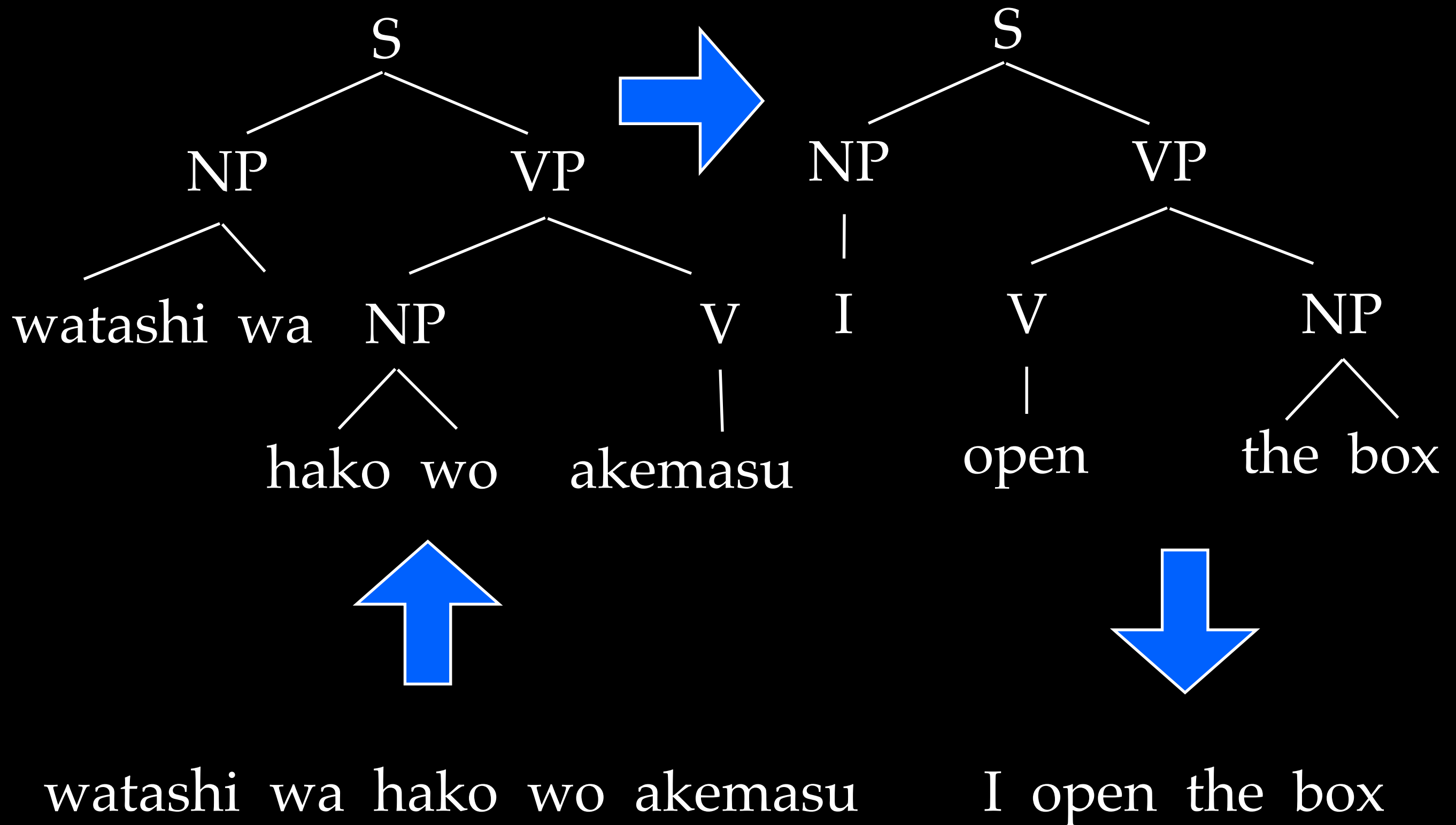


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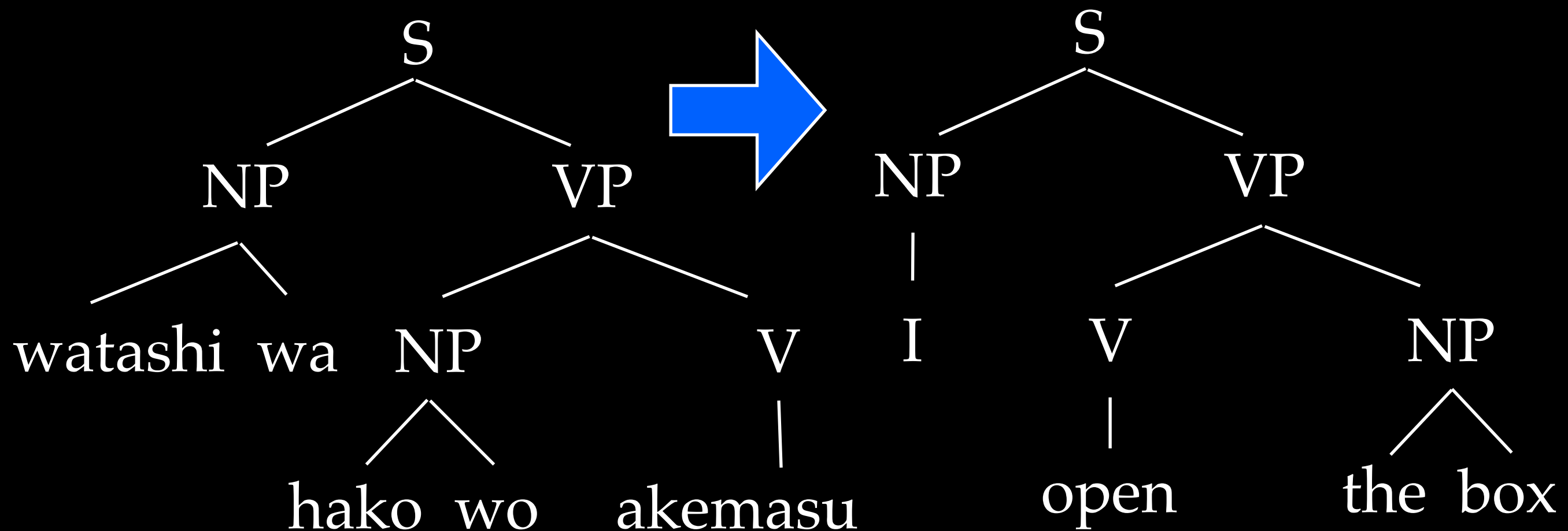
Even better: convert to PDA

Cambridge: best NIST 2009 Arabic system

Parting Thoughts



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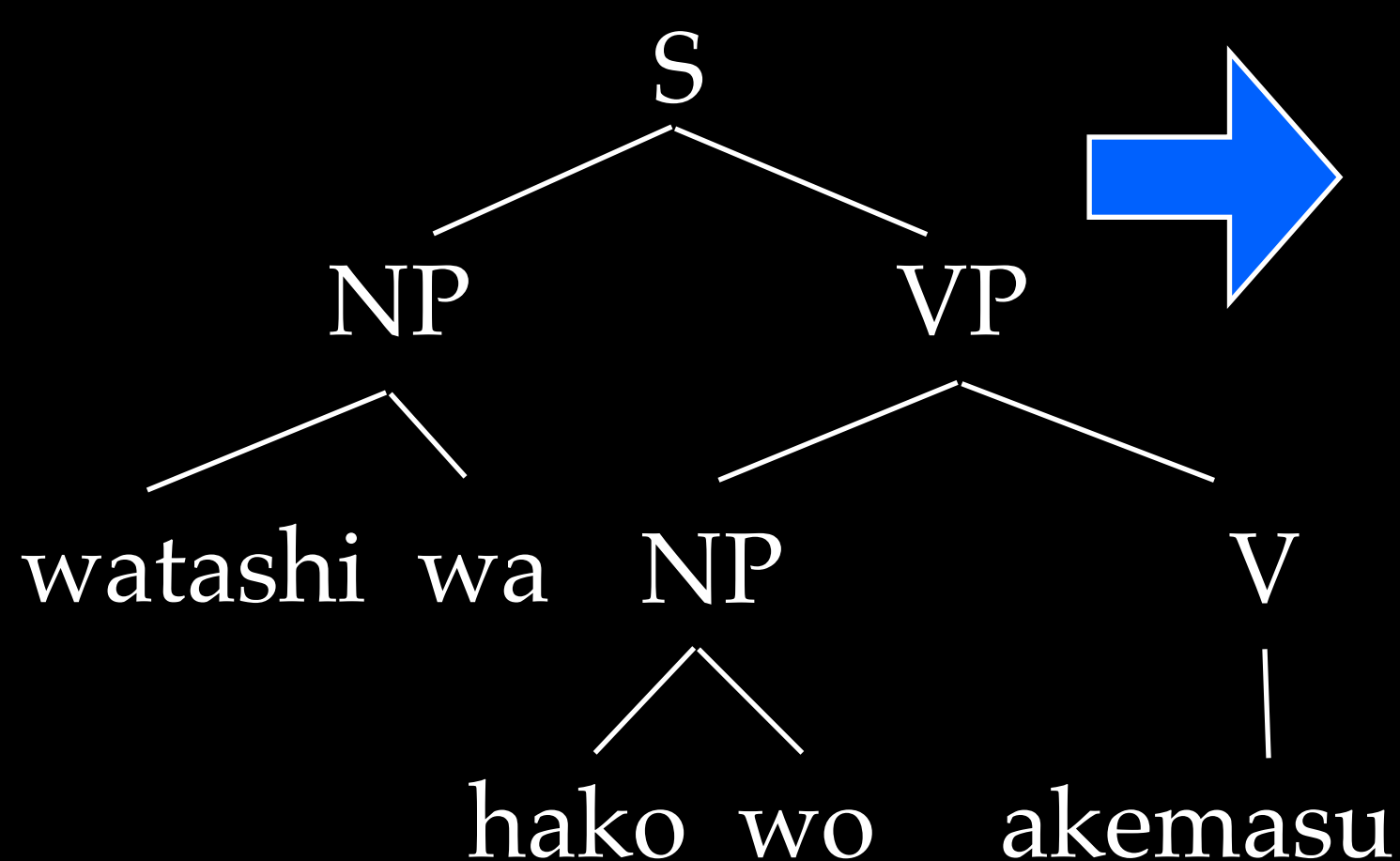


Intersection of weighted
CFL and RL

watashi wa hako wo akemasu

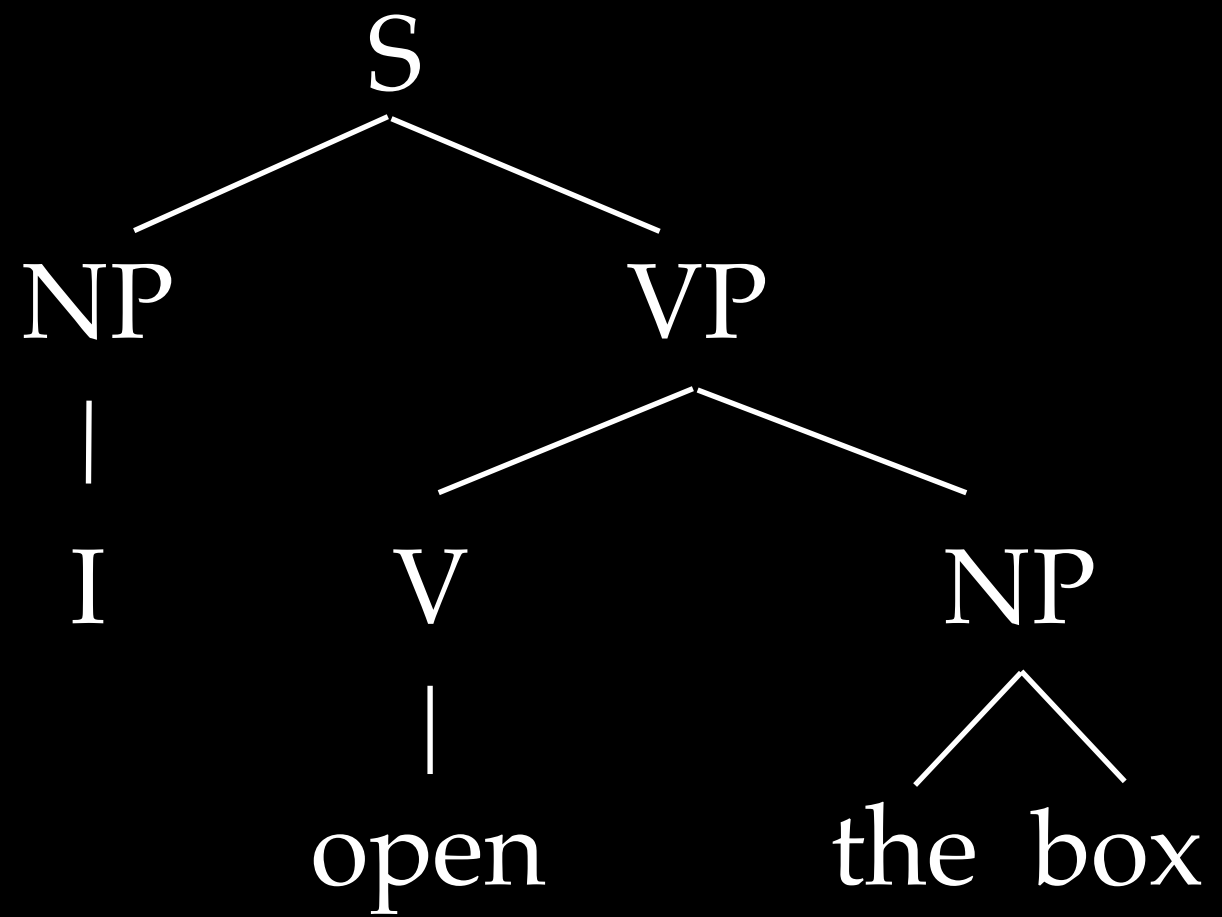
I open the box

Parting Thoughts



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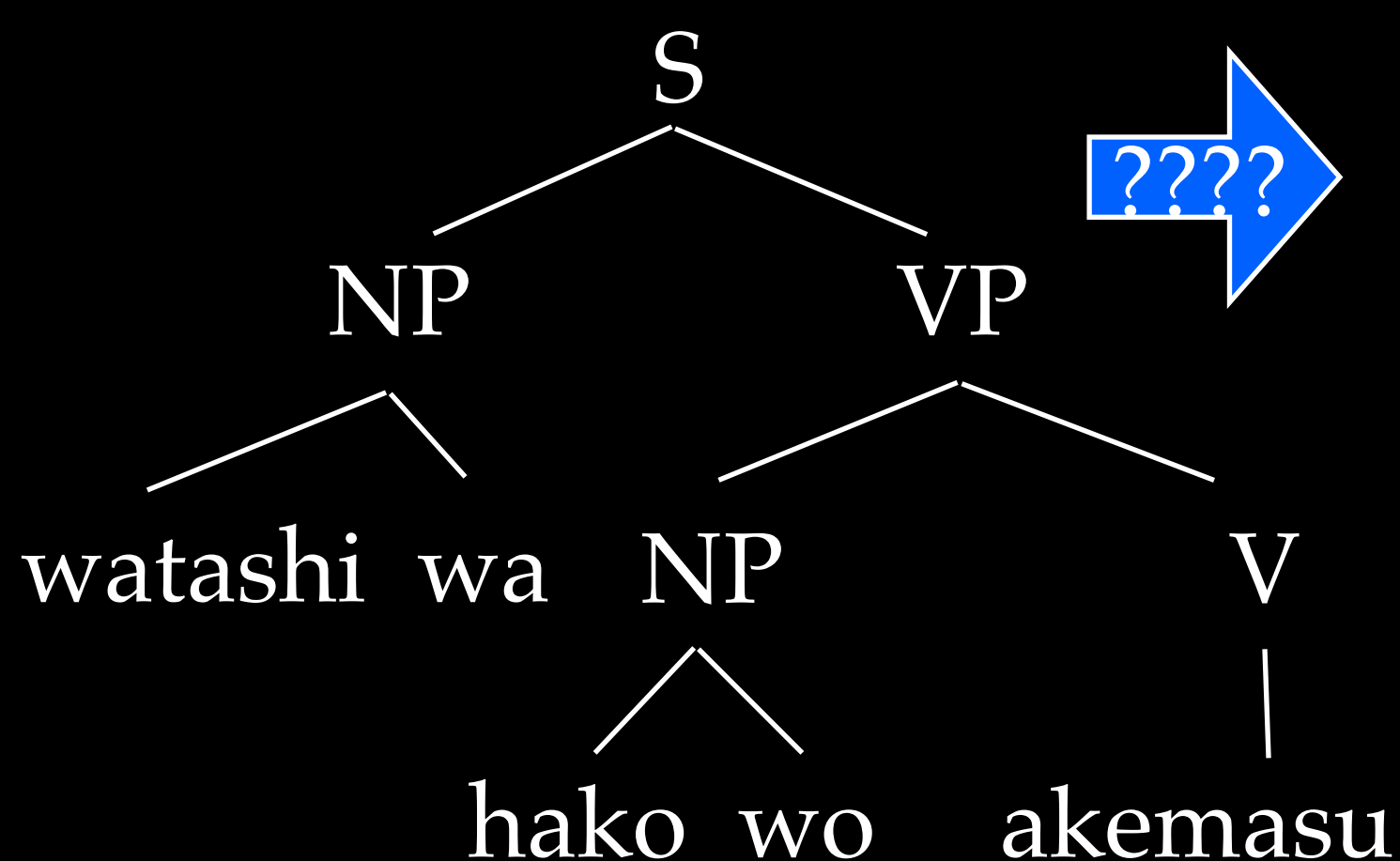
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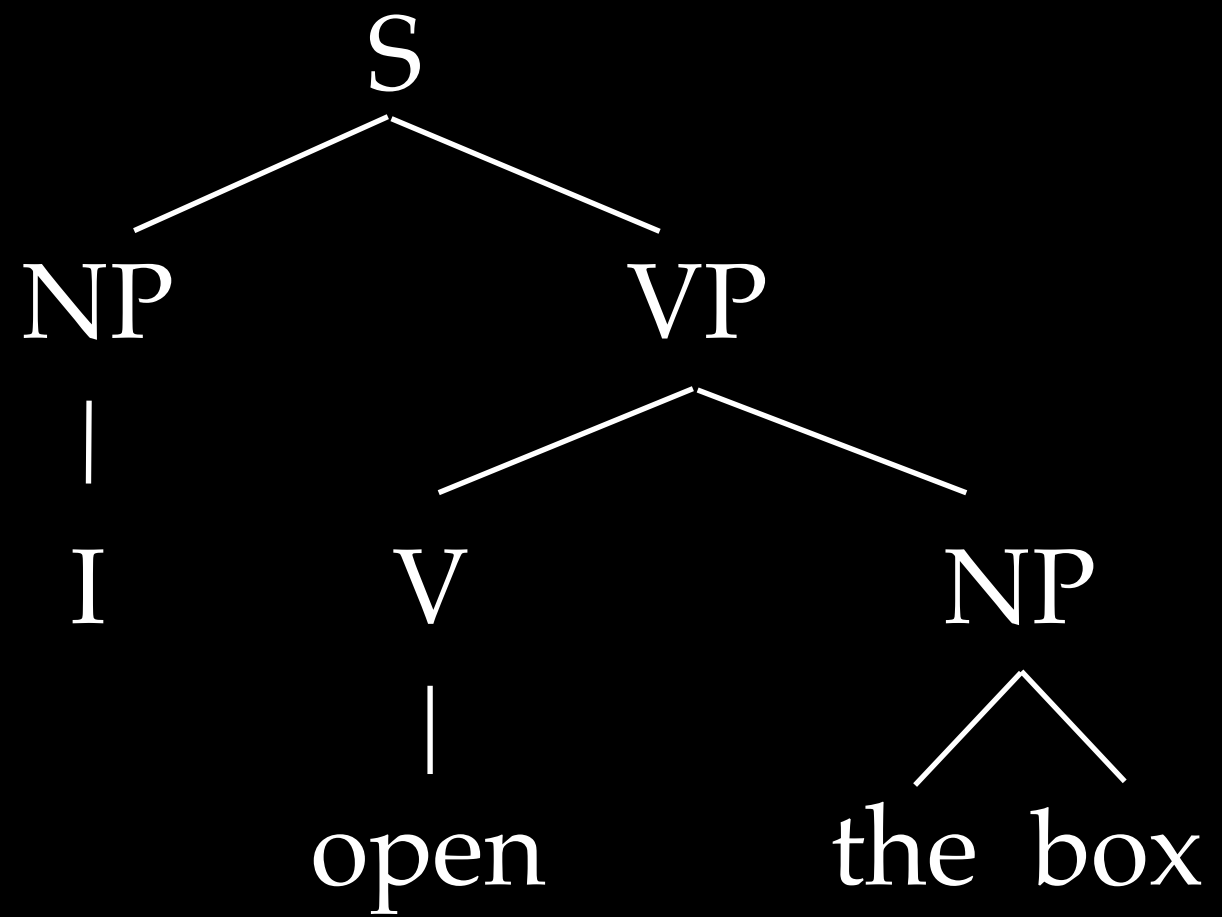
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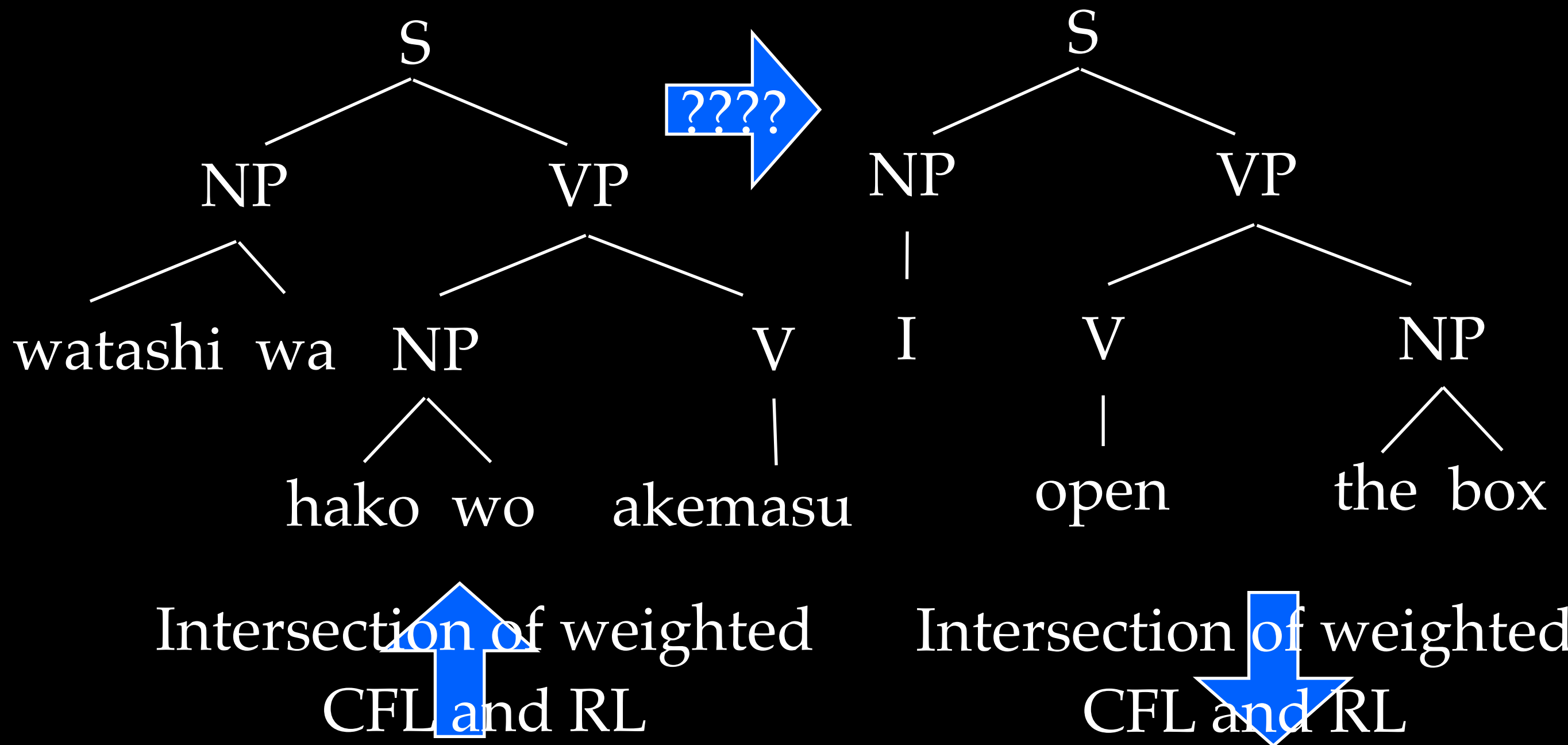
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Intersection of weighted
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I open the box

Parting Thoughts



watashi wa hako wo akemasu I open the box

Weighted *tree* languages, automata, and transducers.

Parting Thoughts

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Not all languages are context-free!

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$$\mathcal{L} = \{abc, aabbcc, aaabbbccc, \dots\} = \forall_n \in [1, \infty) a^n b^n c^n$$

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superset of CFL, subset of CSL, polynomial-time

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superset of CFL, subset of CSL, polynomial-time
Tree-adjoining grammar, Combinatory categorial
grammar, many others.