# Bayesian Analysis of Player Performance over Time

Nathaniel Brown

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# Objective

► Investigate Bayesian modelling techniques on shooting data, and to learn more about time-dependency in the data.

## **Previous Studies**

- ► Gilovich, Vallone, & Tversky (1985)
- ▶ Wetzels (2016)
- ▶ Bar-Eli, Avugos, & Raab (2006)

Data

## Description of Dataset

- Player-tracking data provided by the Duke Men's Basketball team.
- Recorded using SportVU, a player-tracking system from STATS, LLC.
- ▶ Final Sequence Play-by-Play Optical: contains information of players' basketball actions (e.g., shot makes and attempts, dribbles, passes, fouls) and their time stamps for every game.
- ▶ Final Sequence Optical: contains precise locations for all 10 players and the ball at a rate of 25 times per second for every game.

## Missing Data

- ► The ability to record this data depends on specialized tracking cameras, and not every arena has the technology installed.
- ► Has data for 94 out of the 147 games played between the 2013-2014 and 2016-2017 seasons (82 at Home and 12 Away).

## Data Cleaning

- Translate the locations to a half-court setting.
- Convert the x-y coordinates (feet) to polar coordinates (feet and radians).
- Add an indicator for home games.
- Only use the shots that Duke players attempt (no opposing players appear in more than 5 games).

# Data Cleaning (cont.)

Table 1: Summary of Dataset

| Name   | Туре  | Values   | Extra Details  |
|--|---|--|--|
| season<br>gameid<br>time<br>globalplayerid<br>r<br>theta<br>home<br>result | categorical<br>categorical<br>continuous<br>categorical<br>continuous<br>continuous<br>categorical<br>categorical | $ \begin{cases} 2014,  \dots,  2017 \rbrace \\ \text{NA} \\ \text{NA} \\ \text{NA} \\ [0,  \infty) \\ [-\pi,  \pi] \\ \{0,1\} \\ \{0,1\} \end{cases} $ | 94 unique values 13-digit timestamp in milliseconds 31 unique values Distance of shot from hoop (feet) Angle of shot (radians) 1 if shot occured during a home game 1 if shot was made(response) |

Table 2: Sample of Dataset

| season | gameid       | time          | globalplayerid | r       | theta   | home | result |
|--------|--------------|---------------|----------------|---------|---------|------|--------|
| 2014   | 201401070173 | 1389141733839 | 603106         | 4.2076  | 1.0746  | 1    | 1      |
| 2014   | 201401070173 | 1389141844712 | 601140         | 16.6537 | 1.2973  | 1    | 0      |
| 2014   | 201401070173 | 1389143172185 | 696289         | 18.7901 | -0.0581 | 1    | 1      |
| 2014   | 201401070173 | 1389143196303 | 601140         | 23.4629 | 0.9539  | 1    | 1      |
| 2014   | 201401070173 | 1389143220261 | 756880         | 6.5365  | 0.0696  | 1    | 0      |

# Data Cleaning (cont.)

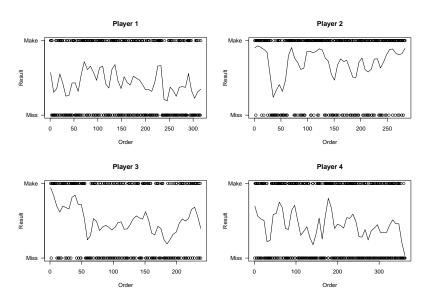
Distribution of Shot Locations  $\theta = 0$ Result

Figure 1: Locations and Results of All Shots

## Exploratory Data Analysis

- Visualize changes in success rate over time in individuals and in population.
- ▶ Moving average only accounts for shot order and outcome.

# Exploratory Data Analysis (cont.)



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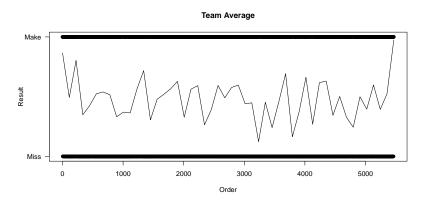


Figure 2: Moving Average of Shot Success Rate



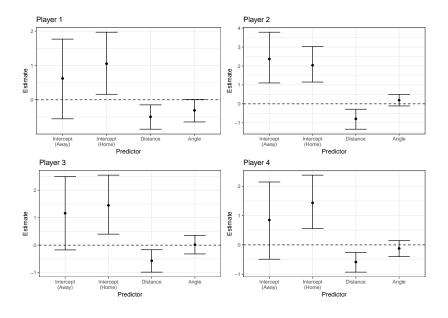
## Model-Building

- ► Types of Models
- Generalized Linear Model
- Hierarchical Generalized Linear Model
- Discounted Likelihood Hierarchical Model
- ► All models based off a logistic regression model
- ▶ Built using JAGS library in R (R2jags)

## Generalized Linear Model: Notation

$$logit(p_i) = \beta_{int} + x_{r,i}\beta_r + x_{\theta,i}\beta_\theta + x_{H,i}\beta_H$$

#### Generalized Linear Model: Results



# Generalized Linear Model: Results (cont.)

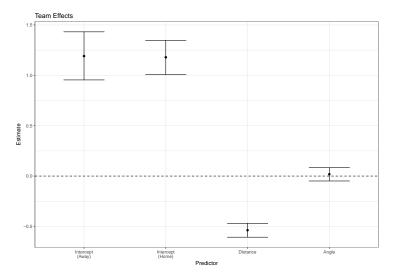


Figure 3: GLM Posterior Distributions for Four Players

## Hierarchical Model: Notation

$$\begin{split} \mathsf{logit}(\textit{p}_{\mathsf{j}\mathsf{i}}) &= \beta_{\mathsf{int, j}} + x_{\mathsf{r, j}\mathsf{i}}\beta_{\mathsf{r, j}} + x_{\theta, \mathsf{j}\mathsf{i}}\beta_{\theta, \mathsf{j}} + x_{\mathsf{H, j}\mathsf{i}}\beta_{\mathsf{H, j}}, \\ \beta_{\mathsf{int, j}} &\sim \textit{N}(\beta_{\mathsf{int}}, \tau_{\mathsf{int}}^2), \\ \beta_{\mathsf{r, j}} &\sim \textit{N}(\beta_{\mathsf{r}}, \tau_{\mathsf{r}}^2), \\ \beta_{\theta, \mathsf{j}} &\sim \textit{N}(\beta_{\theta}, \tau_{\theta}^2), \\ \beta_{\mathsf{H, j}} &\sim \textit{N}(\beta_{\mathsf{H}}, \tau_{\mathsf{H}}^2). \end{split}$$

#### Hierarchical Model: Results

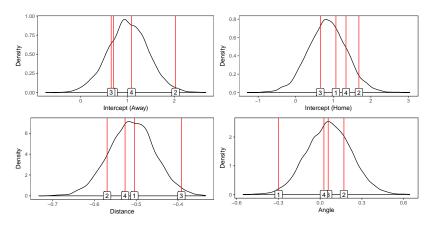
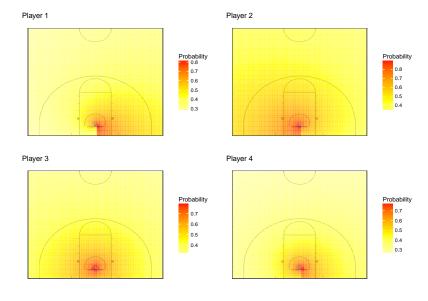


Figure 4: Population Distribution with Four Player Effects

#### Hierarchical Model: Contour Plots



## Hierarchical Model: Contour Plots (cont.)

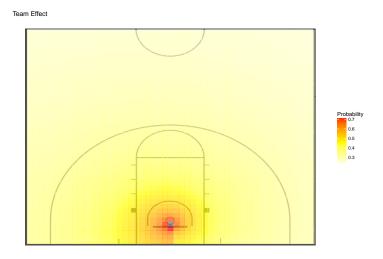


Figure 5: Contour Plots for Four Players and Population of Players

## Discounted Model: Notation

Hierarchical model equation:

$$logit(p_{ji}) = \beta_{int, j} + x_{r,ji}\beta_{r, j} + x_{\theta,ji}\beta_{\theta,j} + x_{H, ji}\beta_{H, j}.$$

Binomial likelihood term without discounting:

$$L_{\mathrm{gj}}(\Theta) = \prod_{i=1}^{\mathsf{n}_{\mathrm{gj}}} p(\mathsf{y}_{\mathrm{gji}}|\Theta) \propto \prod_{i=1}^{\mathsf{n}_{\mathrm{gj}}} p_{\mathrm{gji}}^{\mathsf{y}_{\mathrm{gji}}} (1 - p_{\mathrm{gji}})^{1 - \mathsf{y}_{\mathrm{gji}}}.$$

Exponential discounting to the outcomes for  $0 < \delta < 1$ :

$$\pi_{\mathsf{gji}} = \left( p_{\mathsf{gji}}^{\mathsf{y}_{\mathsf{gji}}} (1 - p_{\mathsf{gji}})^{1 - \mathsf{y}_{\mathsf{gji}}} 
ight)^{\delta^{|\mathcal{g} - \mathcal{g}_0|}},$$

Discounted Likelihood:

$$\Lambda_{gj}(\Theta) = \prod_{i=1}^{n_{gj}} \pi_{gji},$$

#### Discounted Model: Ones Trick

```
for(i in 1:N){
  # delta = discount rate
 wt[i] <- delta^abs(games[i]-g0)
  # model equation with random effects by player
 logit(prob[i]) <-
    beta_int[player[i]]*int[i] +
    beta_home[player[i]]*home[i] +
    beta_r[player[i]]*logr[i] +
    beta_theta[player[i]]*theta[i]
  # likelihood function
 p1[i] <- prob[i]^result[i]
 p2[i] <- (1-prob[i])^(1-result[i])
  # discounted likelihood function
 pi[i] <- (p1[i] * p2[i])^wt[i]
  # defines correct discounted likelihood function
 y[i] ~ dbern(pi[i])
```

# Discounted Model: Weighting

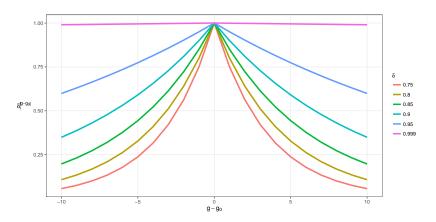


Figure 6: Illustration of Discounted Weighting

#### Discounted Model: Results

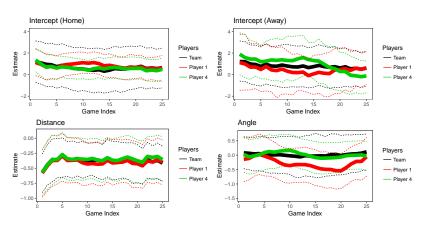


Figure 7: Parameters for Two Players and Population over Time,  $\delta=0.750$ 

## Discounted Model: Results (cont.)

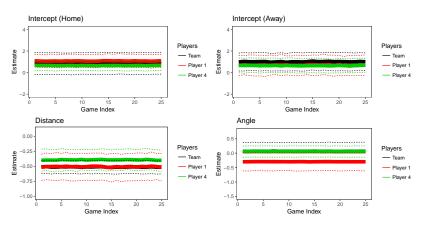
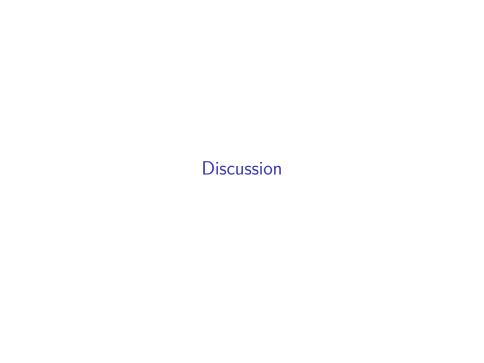


Figure 8: Parameters for Two Players and Population over Time,  $\delta=0.999$ 



#### **Evaluation of Models**

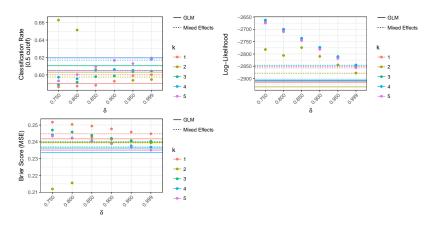


Figure 9: Model Evaluation

## Calibration Plots

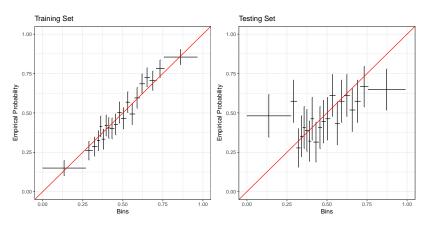


Figure 10: Calibration Plots for Discounted Likelihood Model,  $\delta=0.850$ 

#### Results from Model with $\delta = 0.850$

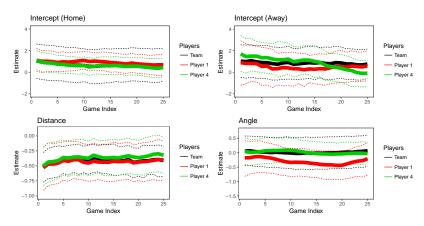


Figure 11: Parameters for Two Players and Population over Time,  $\delta=0.850$ 

#### Conclusion

- ► Some weak evidence for time-dependency in shooting success rate.
- Angle only matters for certain players.
- ▶ Effects of Home-court advantage are not strong in this dataset.

#### **Future Goals**

- ▶ Incorporate more advanced predictors.
- ▶ Add random effects on discount factor.

## Acknowledgments

- Mike West, for advising me through this project.
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