

Advanced Databases - Exercise Sheet No. 1

Third Year of the "Computer Engineering" Program

Exercise I

Consider the following set of functional dependencies for a relation R ($U = \{A, B, C, D, E, G, H\}$):

$F = \{AB \rightarrow C, B \rightarrow D, CD \rightarrow E, CE \rightarrow GH, G \rightarrow A\}$.

Show that

- 1) $BG \rightarrow DH \in F^+$
- 2) $CD \rightarrow B \notin F^+$
- 3) $ABC \rightarrow DEG \in F^+$

Exercise II

Consider the following set of functional dependencies for a relation R ($U = \{A, B, C, D, E, G, H\}$):

$F = \{BC \rightarrow D, DG \rightarrow A, DE \rightarrow G, C \rightarrow E, H \rightarrow B\}$.

Verify whether the following dependencies hold:

- 1) $CH \rightarrow AE$
- 2) $BC \rightarrow DEG$
- 3) $ADEG \rightarrow BC$

Exercise III

Consider the following set of functional dependencies for a relation R ($U := \{A, B, C, D, E, G, H\}$):

$F = \{AC \rightarrow B, C \rightarrow D, BD \rightarrow E, BE \rightarrow GH, G \rightarrow A\}$.

- 1) Demonstrate why attribute C must be part of every key of $R(U)$.
- 2) Determine, with proof, all the keys of $R(U)$ corresponding to F .

Exercise IV

Consider the following sets of functional dependencies:

$F = \{AB \rightarrow C, B \rightarrow A, AD \rightarrow E, BD \rightarrow I\}$,

$G = \{AB \rightarrow C, B \rightarrow A, AD \rightarrow EI\}$.

Verify whether the assertion $F^+ = G^+$ holds.

Exercise V

Consider the following relation:

COMMANDE (ProductNum, ProductName, ClientNum, ClientName, Date, UnitPrice, Number, VAT)

(The amount of VAT naturally depends on the product.)

- 1) Determine the functional dependencies in the relation "COMMANDE." What are the candidate keys?
- 2) In which normal form is the relation "COMMANDE"? Explain why it is not in a higher normal form.
- 3) Decompose the relation "COMMANDE" into relations of a higher normal form. Provide each resulting relation in the format `RELATION(Attribute1, ...)`, underlining the attributes of the primary key.

Exercise VI

Consider the following set of functional dependencies for a relation $R(U := \{A, B, C, D, E, F\})$:

$DF := \{ A \rightarrow BC, C \rightarrow AD, E \rightarrow ABC, F \rightarrow CD, CD \rightarrow BEF \}$.

- 1) List all the keys of R.
- 2) Explain why R is in Third Normal Form (3NF).