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1 % Abhilash Gudgunti
2 % 11th November, 2024
3 % ECE 202 Project 1: Phase 5
4 % Power series expansion of function of form Acos(wt)
5
6 clear % clear registers
7 clf % clear figures
8 format shortG
9
10 % Setting up Givens
11 A = 12; % Amplitude of the wave
12 w = 40; % Frequency of the wave
13
14 % Asking User for Inputs
15 % No. of non-zero terms in the truncated series
16 N = input("Enter the no. of non-zero terms for the truncated series: ");
17
18 ti = input("Enter the intial time (in ms): "); % Initial time (in ms)
19 tf = input("Enter the final time (in ms)" + ...
20     "(should be greater than intitial time): "); % Final time (in ms)
21 % No. of Intervals between each time value
22 int = input("Enter the number of intervals between the time" + ...
23     "(recommneded >400): ");
24
25 % Defining arrays
26 n = (0:2:2*(N-1))'; % values of n for the first N non-zero terms. (up by 2)
27 an = A*(-1).^(n./2) .* w.^n ./ factorial(n); % Array of values of a_n
28
29 % Outputting a table of n and a_n
30 T = table(n, an, 'VariableNames',{'n','Coefficients (a_n)'});
31
32 % Setting up array of time
33 tms = linspace(ti, tf, int+1); % time between 0 - 200 ms
34 t = tms/1000; % time in seconds to compute in functions
35
36 % Initialize the function array f as zeros
37 f = zeros(size(t)); % initialize f as an array of zeros
38 p = zeros(size(n)); % initialize p as an array for plot objects
39
40 %FOR Loop to define funciton efficiently
41 hold on
42 for k = 1:N
43     f = f + an(k)*t.^n(k); % adding each term to the series
44
45     % Plotting each function
46     if k == N
47         % thicker line for the last function
48         p(k) = plot(tms, f, 'LineWidth', 3);
49     else
50         p(k) = plot(tms, f, 'LineWidth', 1.5);
51     end
52 end
53
```

```
54 % Computing average Deviation
55 Avg_dev = sum(abs(A*cos(w*t) - f))/int+1
56
57 % ====PLOTING====
58
59 plot([ti,tf], [0,0], 'k', 'LineWidth', 1) % x-axis (not shown in legend)
60
61 % Setting legends for the figure
62 legend(p, "n = " + n, 'Location', 'bestoutside');
63
64 % Figure components
65 ax = gca; ax.FontSize = 16;
66 title(sprintf(['ECE 202 Project 1 Phase 5:\nApproximation of ' ...
67     'f(x) = %gcos(%gt) \nfor %g non-zero terms\n ' ...
68     'with an average deviation of %.2f from the function'], ...
69     A, w , N, Avg_dev), "FontSize", 19);
70 xlabel('Time t (in ms)', 'FontSize', 17);
71 ylabel('f(t)', 'FontSize', 17);
72 ylim([-1.2*A , 1.2*A]);
73 xlim([ti, tf]);
74 ax.GridAlpha = 0.4; % making the grid darker
75 grid on
76 hold off
77
78 % ====CHECK====
79
80 % Check difference between new and old approach for the final function
81 if N == 6
82     %Inefficiently represented function
83     f1 = an(1) * t.^n(1); % The first non zero term
84     f2 = f1 + an(2) * t.^n(2); % The second non zero term
85     f3 = f2 + an(3) * t.^n(3); % The third non zero term
86     f4 = f3 + an(4) * t.^n(4); % The fourth non zero term
87     f5 = f4 + an(5) * t.^n(5); % The fifth non-zero term
88     f6 = f5 + an(6) * t.^n(6); % The sixth non zero term
89     check = max(abs(f - f6)) % should be zero for the final function
90 end
91
92 %Yes, The graph continues to look the same visually from phase 2 and
93 %nothing has been changed (from Phase 3)
94
95 %(Phase 5) While computing the average deviation, It is seen that with an
96 %increase in the number of non-zero terms for the truncated series, the
97 %average deviation approaches 0. This is correct because, as we increase.
98 %the number of non-zero terms, we are increasing a better approximation for
99 %our function.
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```
1 >> ECE202_P1_Phase5
2 Enter the no. of non-zero terms for the truncated series: 10
3 Enter the intial time (in ms): 0
4 Enter the final time (in ms)(should be greater than intitial time): 200
5 Enter the number of intervals between the time(recommended >400): 1000
6
7 T =
8
9 10x2 table
10
11      n      Coefficients (a_n)
12      —      —
13
14      0          12
15      2         -9600
16      4        1.28e+06
17      6       -6.8267e+07
18      8        1.9505e+09
19     10       -3.4675e+10
20     12        4.203e+11
21     14       -3.695e+12
22     16        2.4633e+13
23     18       -1.288e+14
24
25
26 Avg_dev =
27
28      1.2424
29
30 >>
```

ECE 202 Project 1 Phase 5:
Approximation of $f(x) = 12\cos(40t)$
for 10 non-zero terms
with an average deviation of 1.24 from the function

