

1. Арифметическое кодирование *Arith*

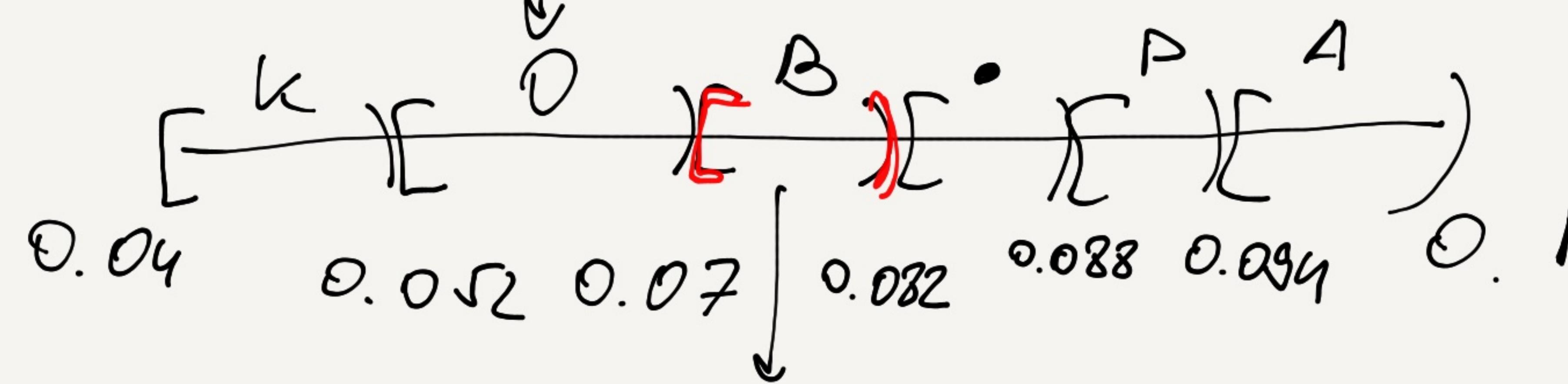
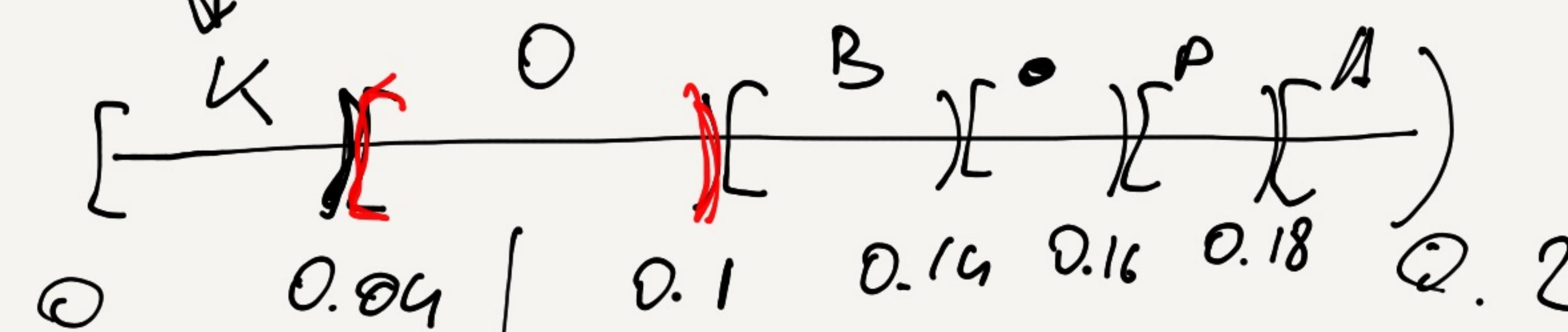
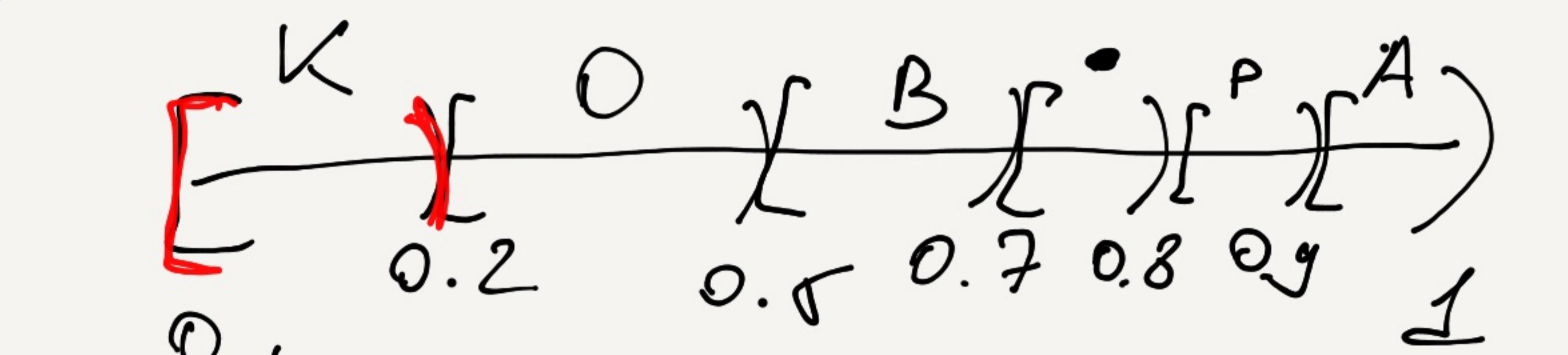
2. PPM *Moffat*

3. BWT / MTF / RLE *UTM*

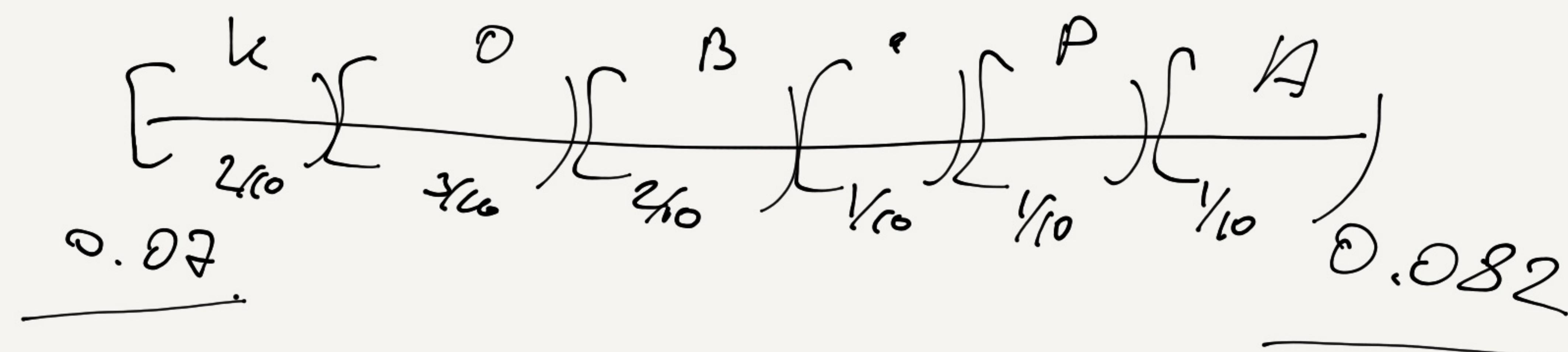
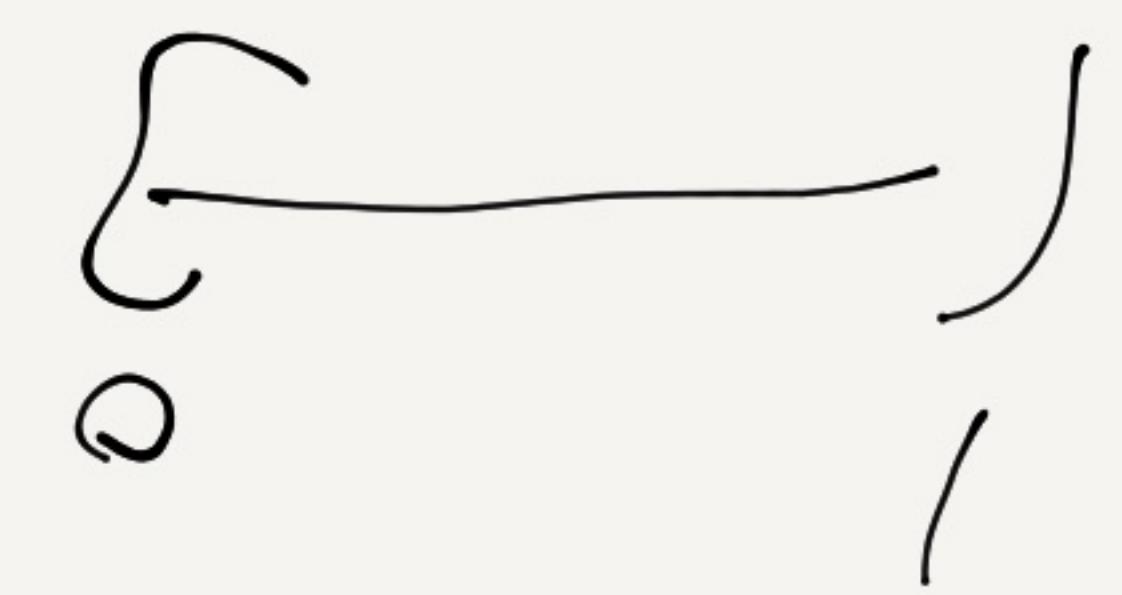
Moffat

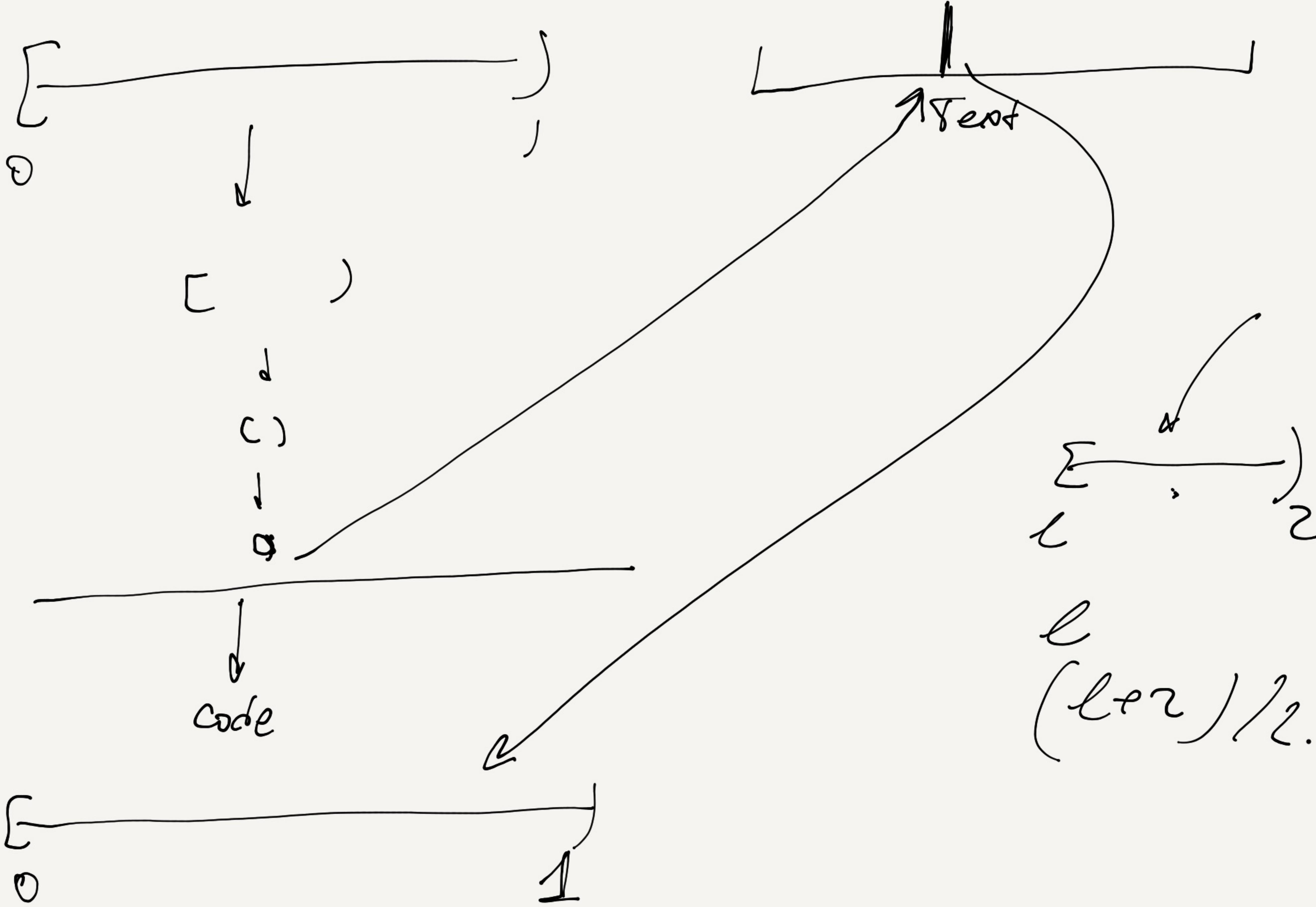
KOB, KOPABA,

K - 2 10
 O - 3 ←
 B - 2
 . - 1
 P - 1
 A - 1
 ↑



$$0.06 \frac{2}{10}$$

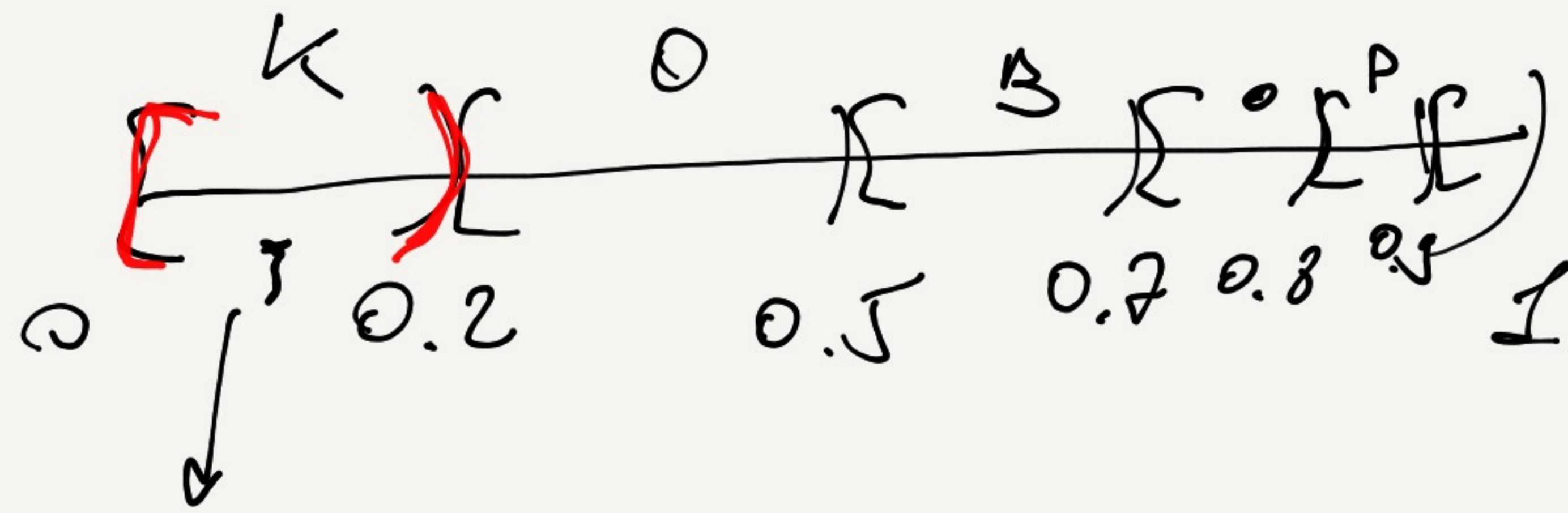




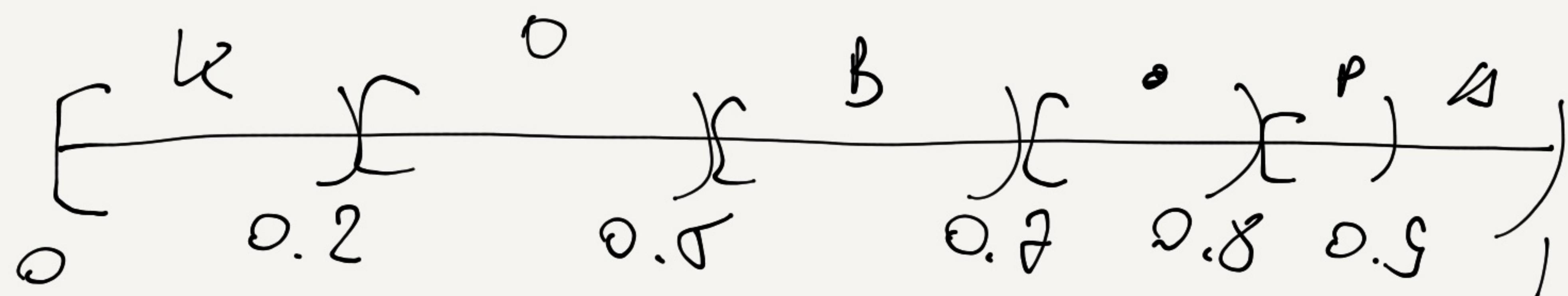
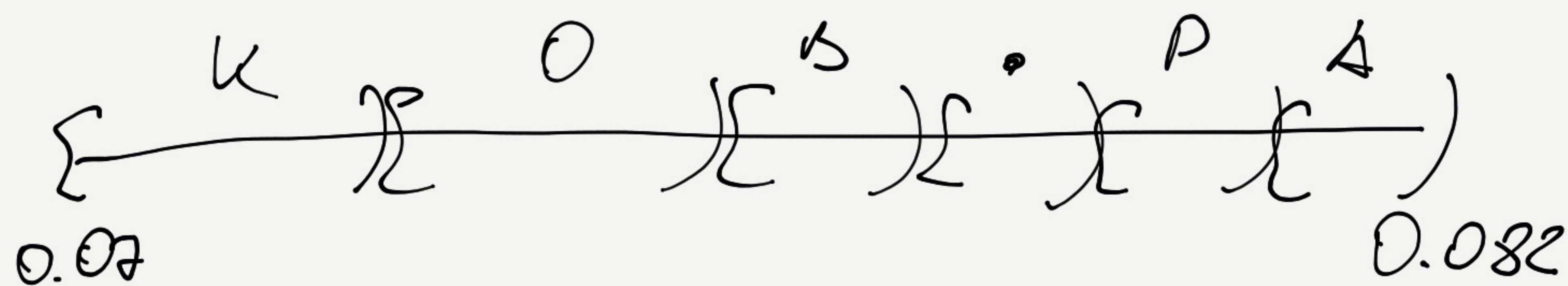
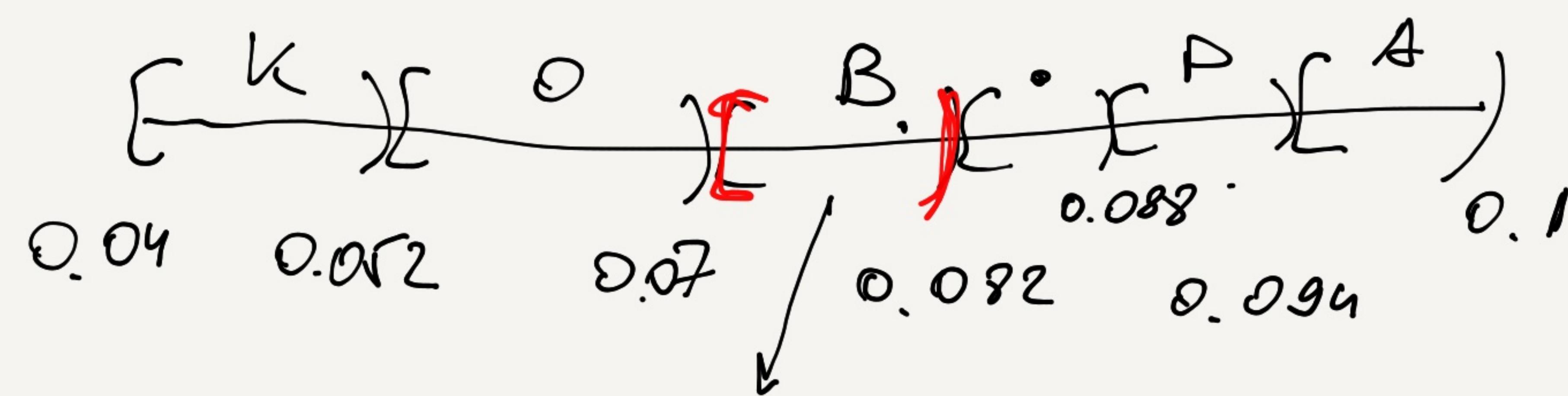
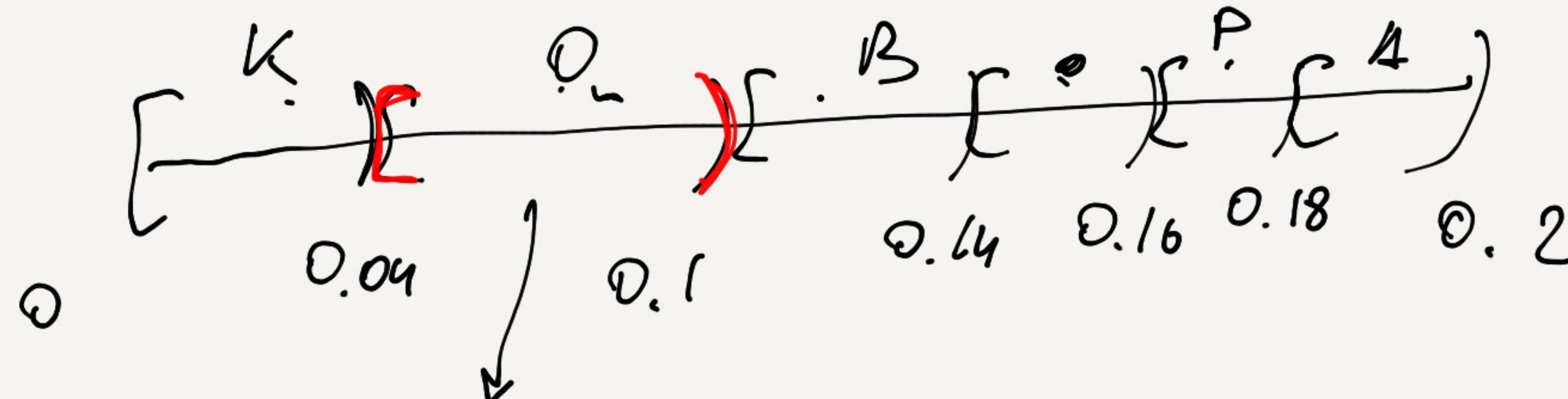
(3, 0.076)

K-2
O-3
B-2
•-1
P-1
A-1

q m



KOB



A : 0 - 0.03

B : 0.03 - 0.041

B : 0.041 - 0.056

- - - -

7. 0.995 - 0.9956

Cum

Freq: 7 6 5 .

Freq: 0 1 1 1 1 1 1

Freq: 7 6 5 .

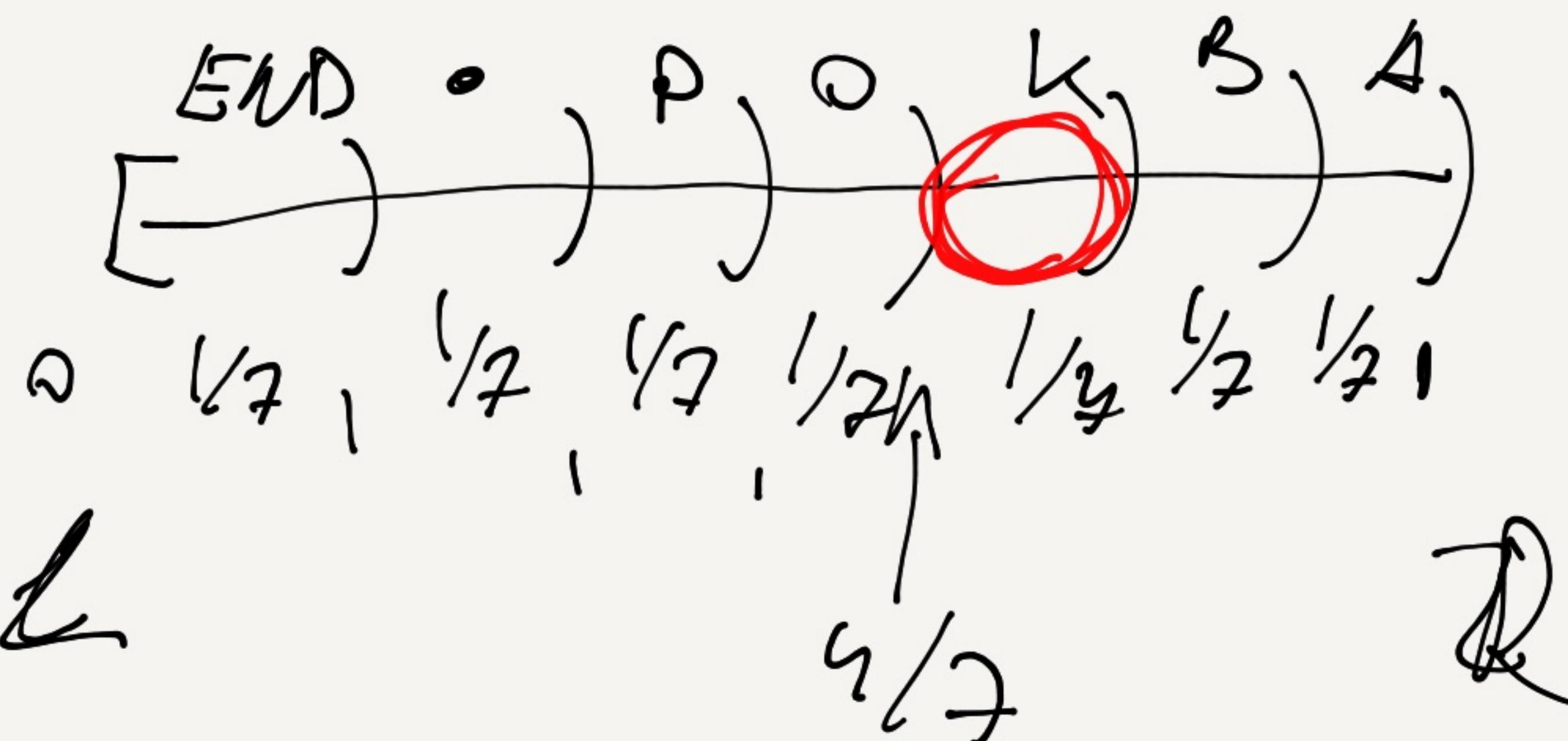
4 3 2 1 0

KOB. 100 DO BS

A B K O P.

↓

(ART)
END



$$\Sigma \frac{4}{7}; \frac{5}{2}$$

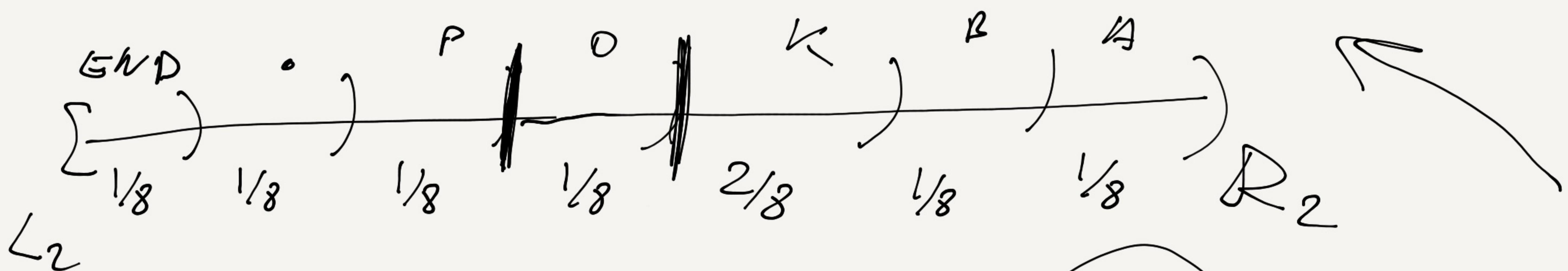
$$L + (R-L) \cdot \frac{4}{7} = L_2$$

$$L + (R-L) \cdot \frac{5}{2} = R_2$$

	A	B	<u>K</u>	O	P	.	END	
index	0	1	2	3	4	5	6	7

Freq: 0 1 1 2 ~~+2~~ 1 1 1

Cum-Freq: ~~8/9~~ ~~7/8~~ ~~6/2~~ ~~4/5~~ ~~3~~ 2 1 0



$$\left[L_2 + (R_2 - L_2) \cdot \frac{3}{8} = L_3 \right]$$

$$L_2 + (R_2 - L_2) \cdot \frac{4}{8} = R_3$$

$$L = 0 \quad | \longrightarrow \quad L = 0$$

$$R = 1$$

$$N = 8$$

$$R = 2^{n-1}$$

123456 1235678

E L R.

$$L = 00000000_2$$

$$R = 1111111_2$$

441000 999999

$$L = \boxed{00110011}0000_2$$

$$R = \boxed{00111111}111_2$$

000456 999555

$$L = 00110000$$

$$R = 1111111$$

Code \rightarrow Stream
0011 Output

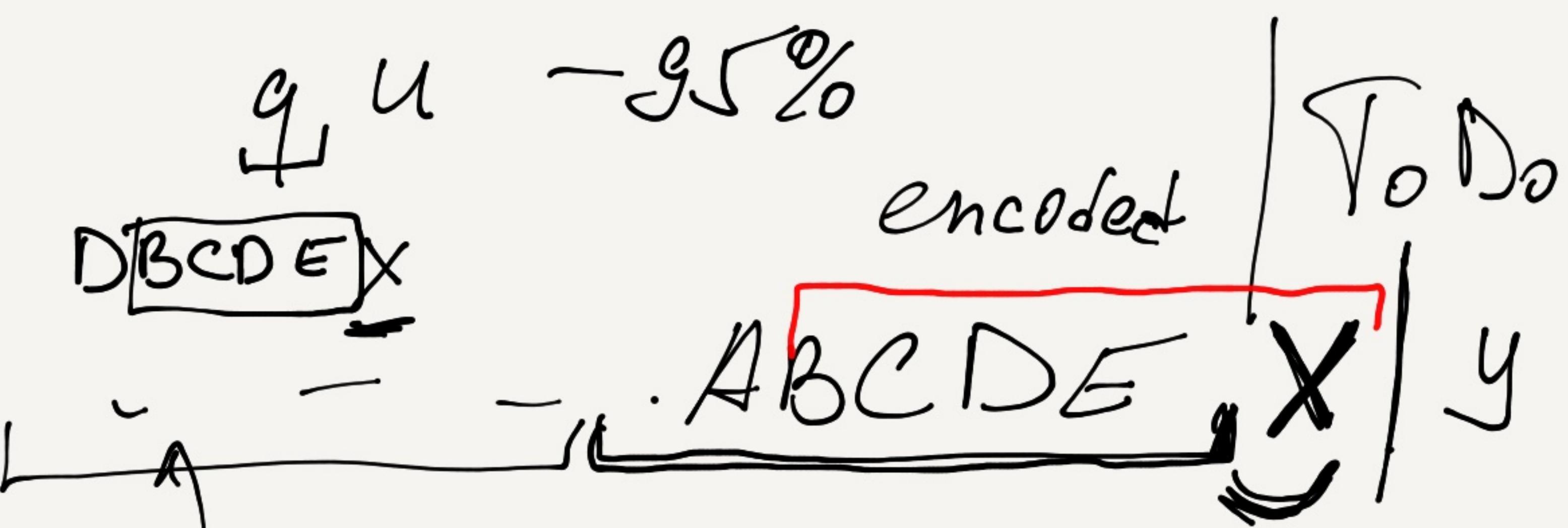
$R - L < \frac{\text{coded-Syms}}{\text{Cum-Freq Co}}$

Cum-Freq Co]

Prediction by Partial Matching

PPM.

$u = 2\%$



- Ие: $BCDPEYAAACG$
- $BCDPEYAAACG$, но без x

$\rightarrow BCDPEYAAACG$, с x .

$ABCDE: A - 5$

$B - 10$

$C - 20$

$X - 10$

$ART - 1$

$f_{req} = \frac{5}{44}$

$F = \frac{6}{44}$

$F = \frac{20}{44}$

$F = \frac{10}{44}$

$F = \frac{1}{44}$

$Code(X)$

$5 \rightarrow 4$

$ABCDE: X$
 $\underbrace{\quad\quad\quad}_{\leftarrow 1}$

$BCDE: x_{e_1}$

$ABCDE \rightarrow BCDE$

$CDE: x_{e_1}$

$DE: x_{e_1}$

$ABCDE: A - 5$

$E: x_{e_1}$

$B - 20$

x_{e_1}

$C - 30$

$ART - 1$.

$Code[ART] \rightarrow$

$ABCDE \rightarrow BCDE$

$$freq(ART) = \frac{1}{56}$$

$$freq(C) = \frac{30}{56}$$

$$freq(A) = \frac{5}{56}$$

$$freq(B) = \frac{20}{56}$$

Context + symbol : Frequency



A B CDE
↓
BCDE
↓
CDE
↓
DE
↓
E →

$$A = 20$$

$$B = 30$$

$$C = 40$$

~~X = 10~~ → code
⋮

~~Huffman~~ = 1. → [X]

$$X = 1$$

A B C A B D

Context = 3

↓ ↓
 code (A) ART code (B) ART code (C) A B
~~WTF-8~~ 1 ~~WTF-8~~ 11 ~~WTF-8~~ 00 1

Context = 0

cxt = 1

ART = 1.

A = 2

B = 2

C = 1

D = 1

→ cxt = 2 cxt = 1 cxt = 0
 ART ART ART
 0 0 000 code (D)
 0 0 WTF-8

Context = 1

A :

ART = 1
B = 2

B : ART = 1 .

C = 1 .
 D = 1 .

C : ART = 1
 A = 1

PPMA

ART = 1

PPMC : $\text{freq(ART)} = \frac{R}{R_{\text{avg}}}$

ART = $\frac{\text{freq(ART)}}{R_{\text{avg}}} = \frac{4}{28.28}$
 A - 5.
 B - 10.
 C - 10.

$\text{freq(B)} = \frac{10}{29}$

CAB : $\frac{\text{ART}}{D} = 1$

Context = 2 : CA :
 ART = 1
 B = 1

AB : $\frac{\text{ART}}{C} = 1$
 C = 1
 D = 1
 ART = 1
 BC : $\frac{\text{ART}}{A} = 1$
 A = 1

Context = 3 :

ABC : $\frac{\text{ART}}{B} = 1$
 A = 1
 BC : $\frac{\text{ART}}{A} = 1$
 B = 1

$$\begin{array}{l} \text{ABC : } AR\Gamma = 1 \\ \begin{array}{l} A = 10 \\ B = 20 \\ C = 30 \end{array} \end{array}$$

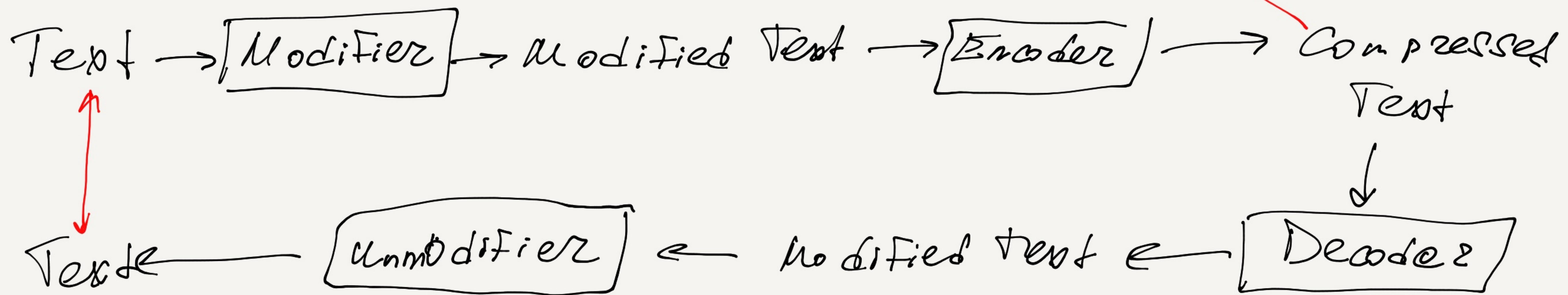
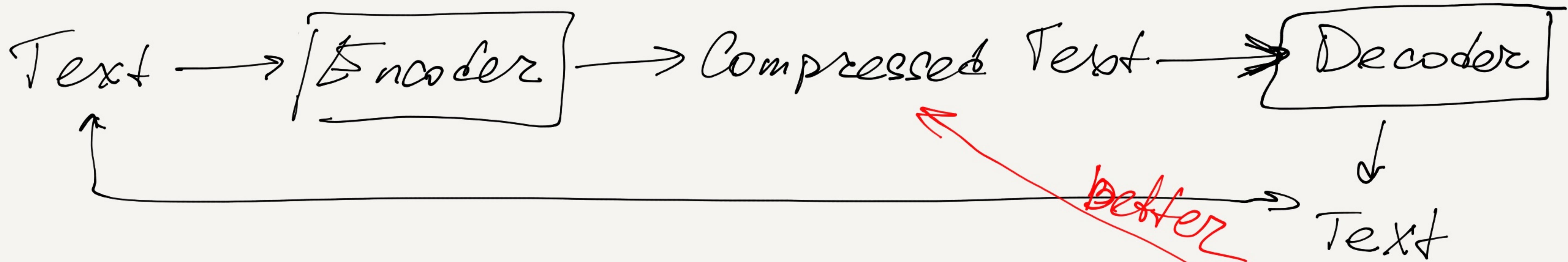
$$\begin{array}{l} BC : AR\Gamma = 1 \\ \begin{array}{l} \cancel{A} = 50 \\ \cancel{B} = 30 \\ \cancel{C} = 40 \\ D = 20 \\ \hline E = 60 \\ x = 10 \end{array} \end{array}$$

$A \setminus BC, X$

BCX

$$Cf_x = 3$$

$$f_{\text{req}}(x) = \frac{10}{71} \rightarrow f_{\text{req}}(x) = \underline{\underline{\frac{10}{71}}}$$



БАРРОУЗА - Чилет 4

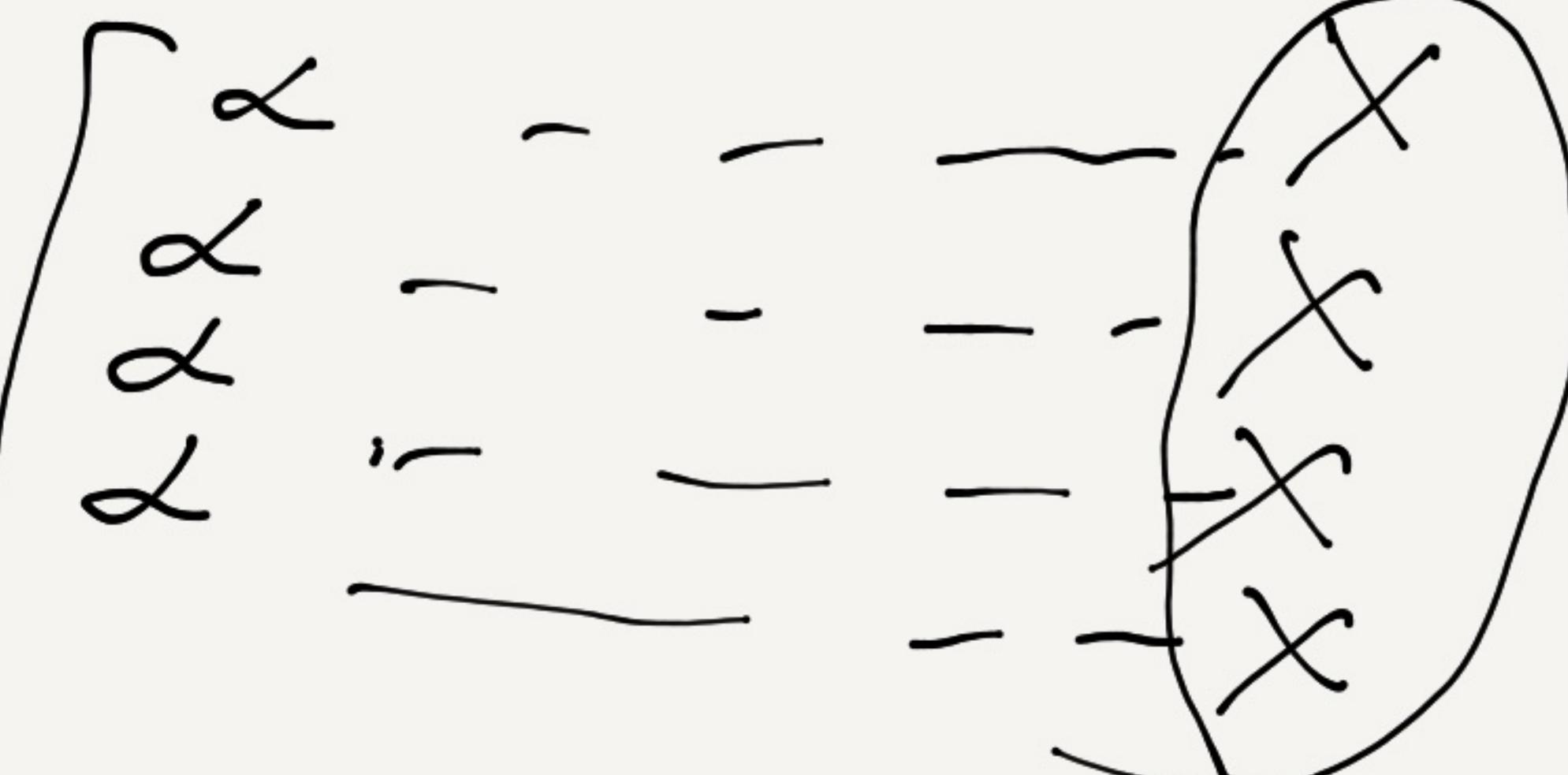
Barrooz - Wheeler Transform (B_{WT})

word = $X\alpha$

- АБРАКАДАБРА
- БРАКАДАБРА
- РАКАДАБРА АБ
- АКАДАБРА АБР
- КАДАБРА АБРА
- АДАБРА АБРАК
- ДАБРА АБРАКА
- АБРА АБРАКАД
- БРА АБРАКАДА
- РА АБРАКАДАБ
- А АБРАКАДАБР

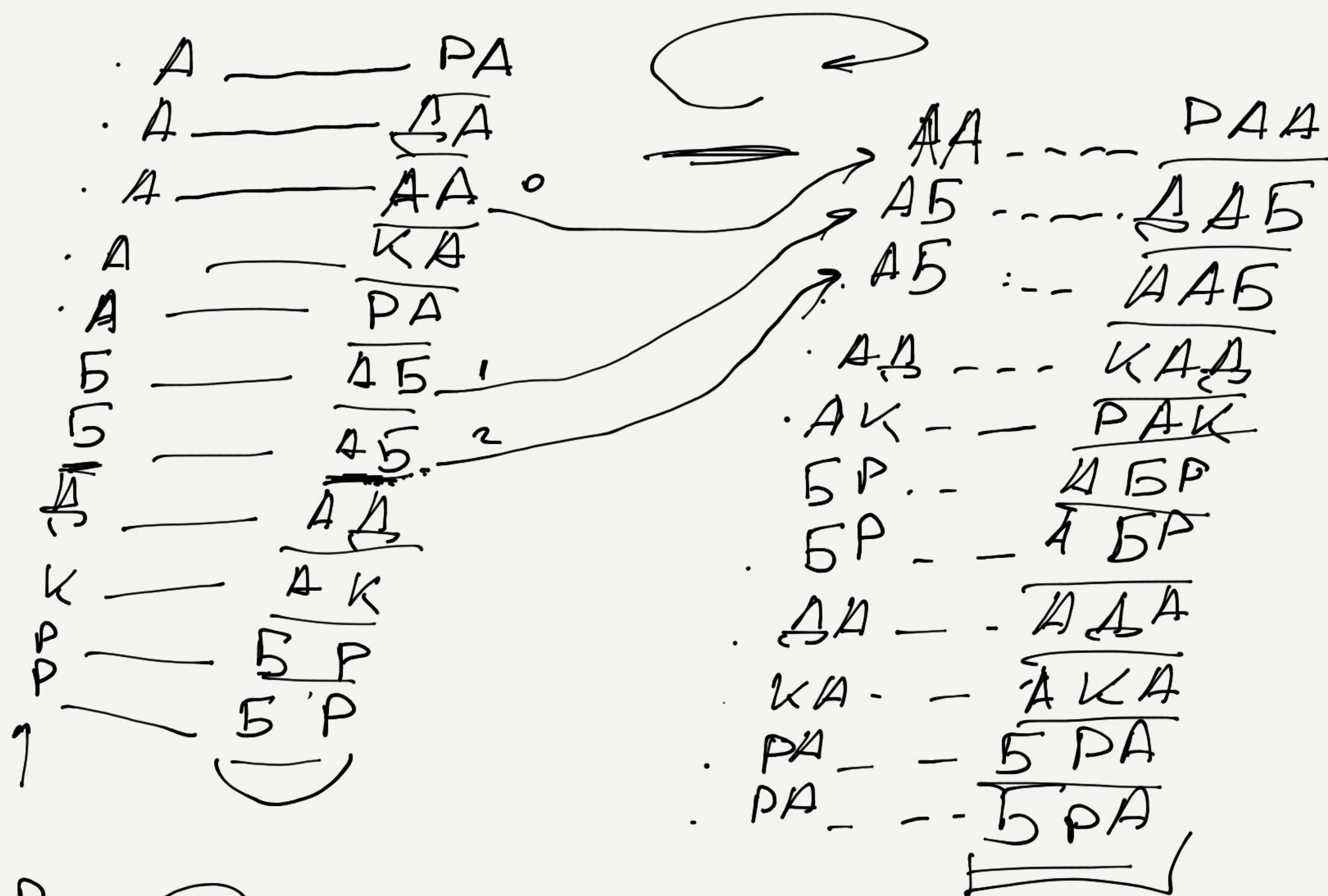
-
- 0. АДВРДКАДАБР
 - 1. АБРДАБРАКАД
 - 2. АБРАКАДАБРА
 - 3. АД АБРА АБРАК
 - 4. АКАДАБРА АЕР
 - 5. БРД АБРА КАДА
 - 6. БРАКАДАБРАД
 - 7. ДАБРА АБРАКА
 - 8. КАДАБРА АБРА
 - 9. РА АБРАКАДАБ
 - 10. РАСКАДАБРА АБ

$X\alpha$
 $XX\alpha$
 $X\alpha$
 $X\alpha$



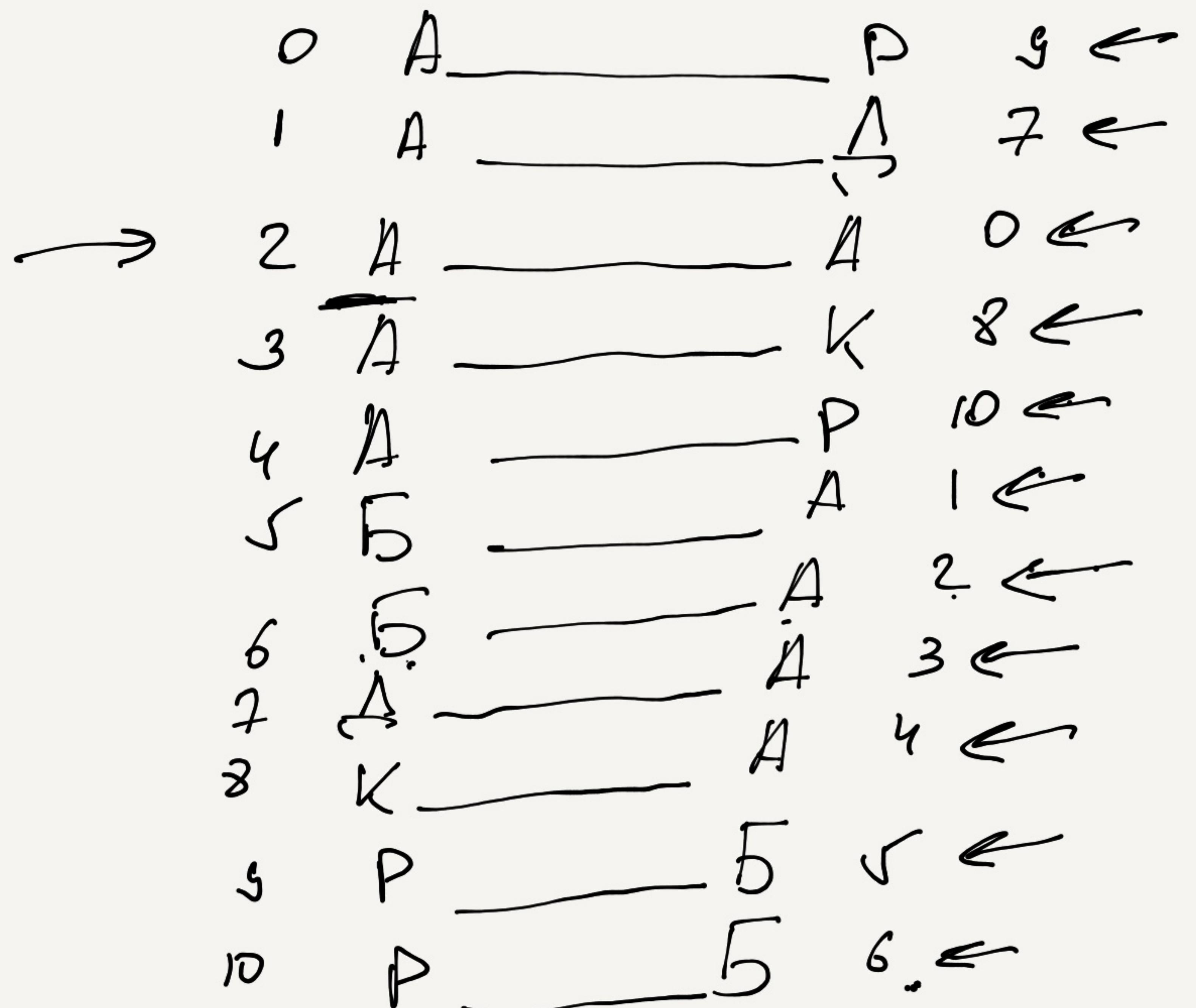
ABRAKADABRA

< РДАКРААААББ >



- ДДБ - - - P
- ДБР - - A
- ДБР - - - A
- ДДА - - - K
- ДКА - - - P
- БРА - - B
- БРА - - - A
- ДДБ - - - B
- .. КАД - - - . A
- PAА - G
- PAK. E

$$O(n^3 \log n)$$



→ РДАКРАААББ, 2.

АБРАКАДАБРА

O(A)

АБРАКАДАБРА → РДАКРАААББ

Move To Front (MTF)

РАДАКРАДАББ
 ↑↑↑↑↑↑↑↑↑↑↑↑

43243200040

АБРАКАДАБРА → 23

↓ modifier = ВИГРМФ

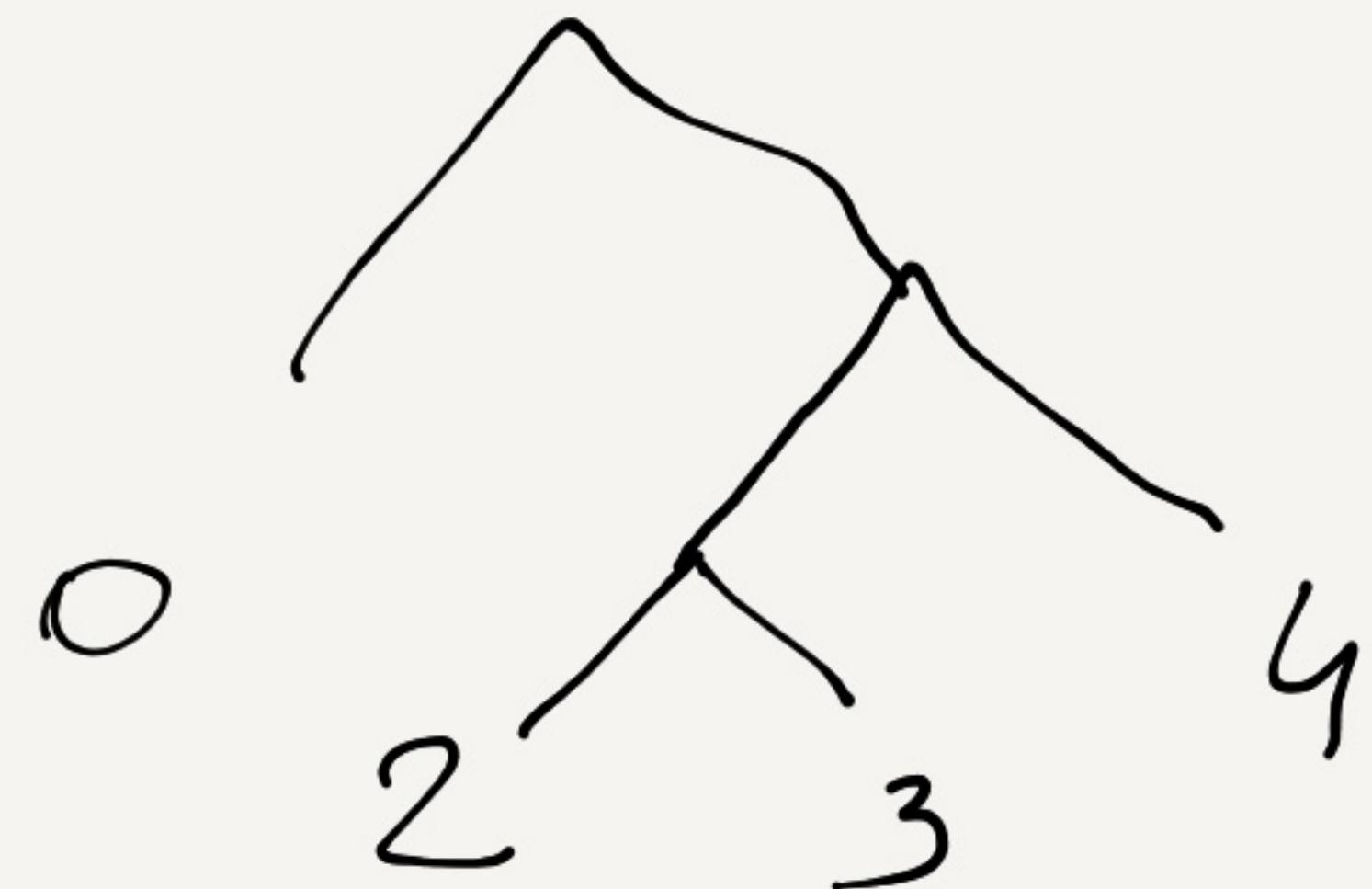
43243200040

0 - 4

2 - 2 } 4

3 - 2 } 4

4 - 3



word bits

0 - 1

4 - 2

2 - 3

3 - 3

А Б А К Р

0 1 2 3 4

РАБАК

ДРАБК

АДРБК

КАДРБ

РКАДБ

АРКДБ

БАРКД

2 — X
 2 — X
 X — X
 . .
 2 — X

XXX...Xg...Xg...Xg...

00...010...0

$$4+6+6+6=22$$

432 432 000 40
 ↓ ↓ ↓ ↓ ↓ ↓ ↓
 Р А К Р А А А Б Б

X - - - - X
 ↓ .
 k O. - - - 0

А Б Д К Р
 0 1 2 3 4
 Р А Б Д К
 Д Р А Б К
 А Д Р Б К
 К А Д Р Б
 Р К А Д Б
 А Р К Д Б
 Б А Р К Д

АБРАКАДАБРА
 11111111
 01424141442

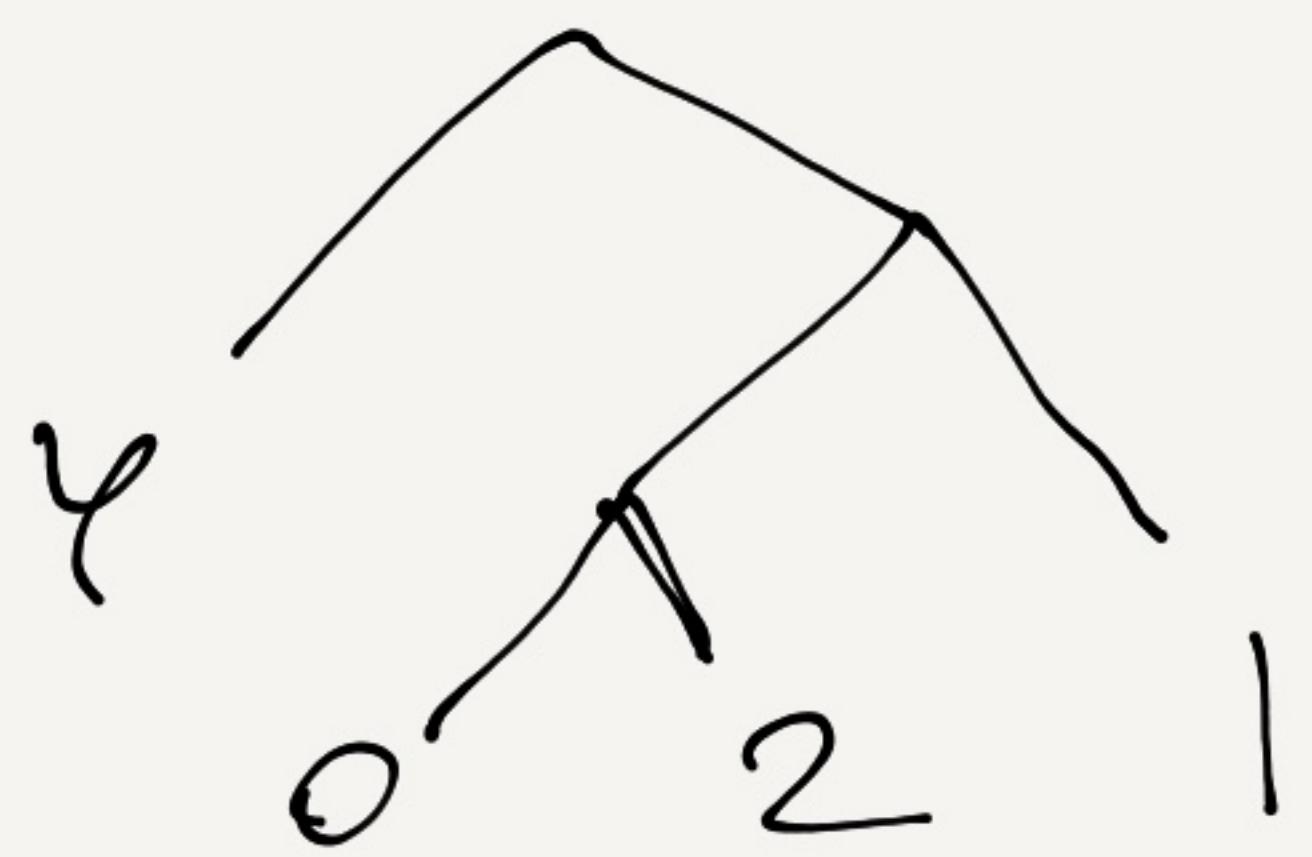
word bits

0 - 1

1 - 3

2 - 2

4 - 4



А Б Д К Р
 0 1 2 3 4
 Б А Д К Р
 Р Б А Д К
 А Р Б Д К
 К А Р Б Д
 А К Р Б Д
 Б А К Р Б
 А Д К Р Б

Б А Д К Р
 Р Б А Д К
 А Р Б Д К.

4 + 6 * 6 + 3 = 19.

Run Length Encoding

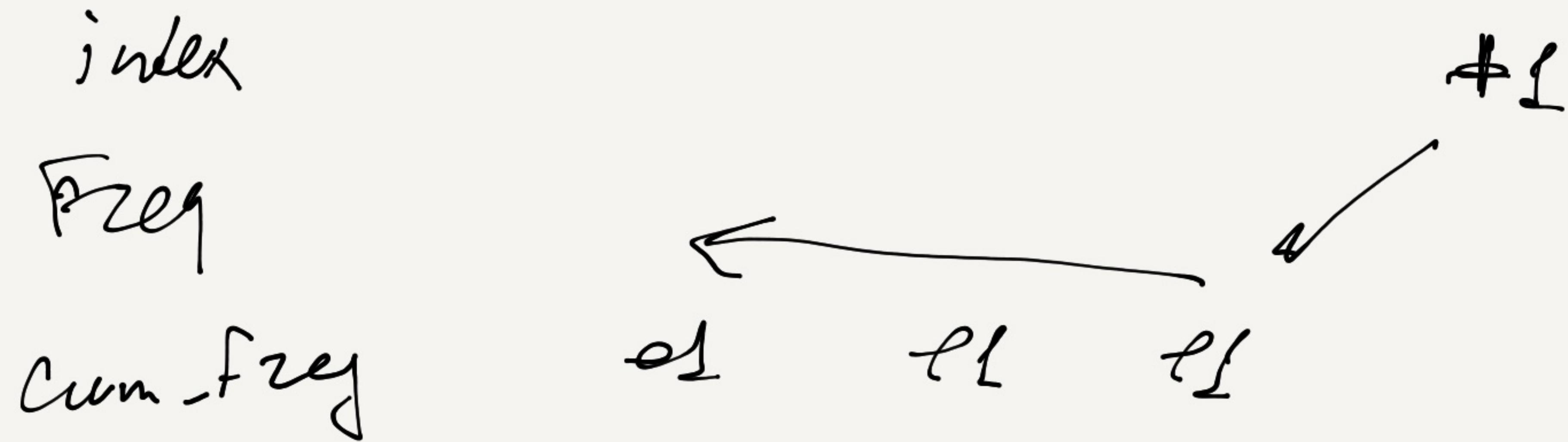
RLE

PDAKPA~~AAB~~
↓↓↓↓
PDAKPA~~AAB~~2

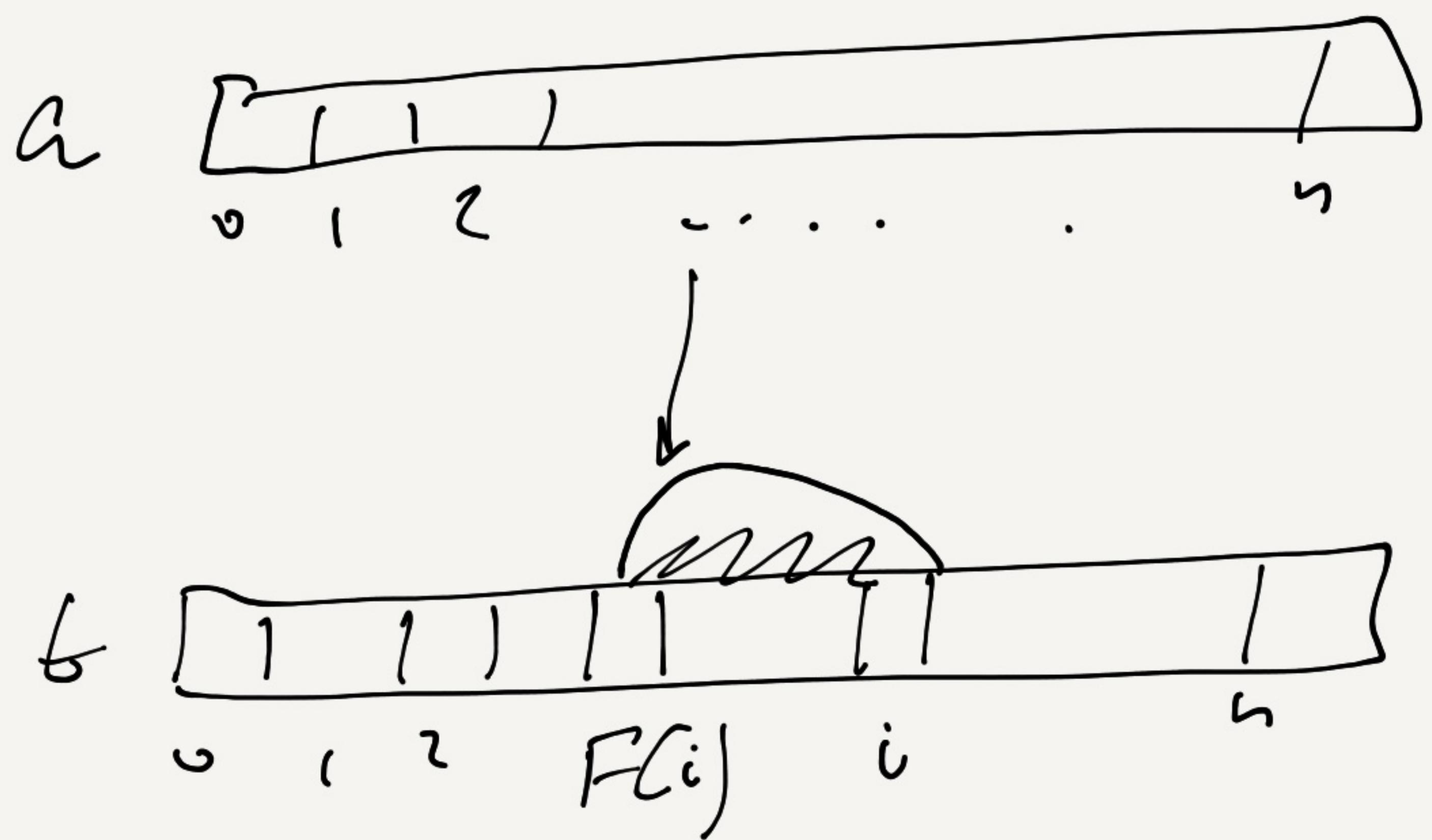
101
 $x \dots x$
 \downarrow $(x_i + 1) \forall i$
 x_{10} $L = 3 \in \mathbb{Z}$
 \downarrow

↓↓↓↓↓ . . . ↓↓
PDAKPA~~AAB~~
↑↑↑↑↑↑↑↑↑↑

A B K O P . EN



Дерево Реквика



$$F(i) = i \& (i+1)$$

00011010011001111
0000

$$t_i = \sum_{j=F(i)}^i a_j$$

$$t_7 = \sum_{v=0}^2 a_v$$

$$t_9 = \sum_{v=8}^9 a_v$$

110 & 1000 =

= 0.

1001 & 1010 = 1000

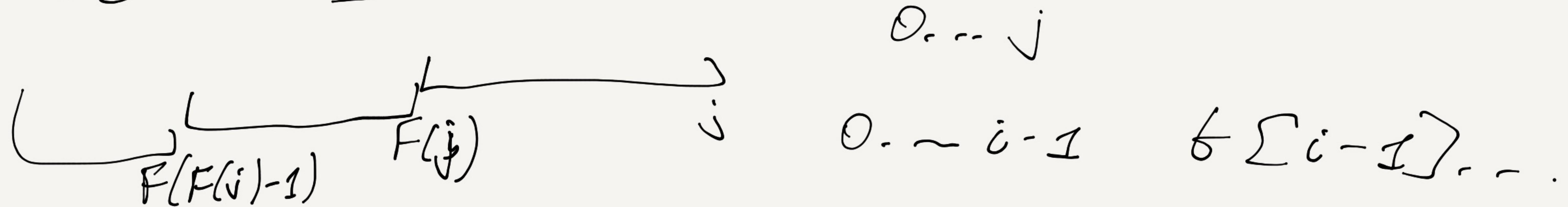
$O \dots j$

$$a[i] + a[\{i+1\}] + \dots + a[j]$$

$O(n)$

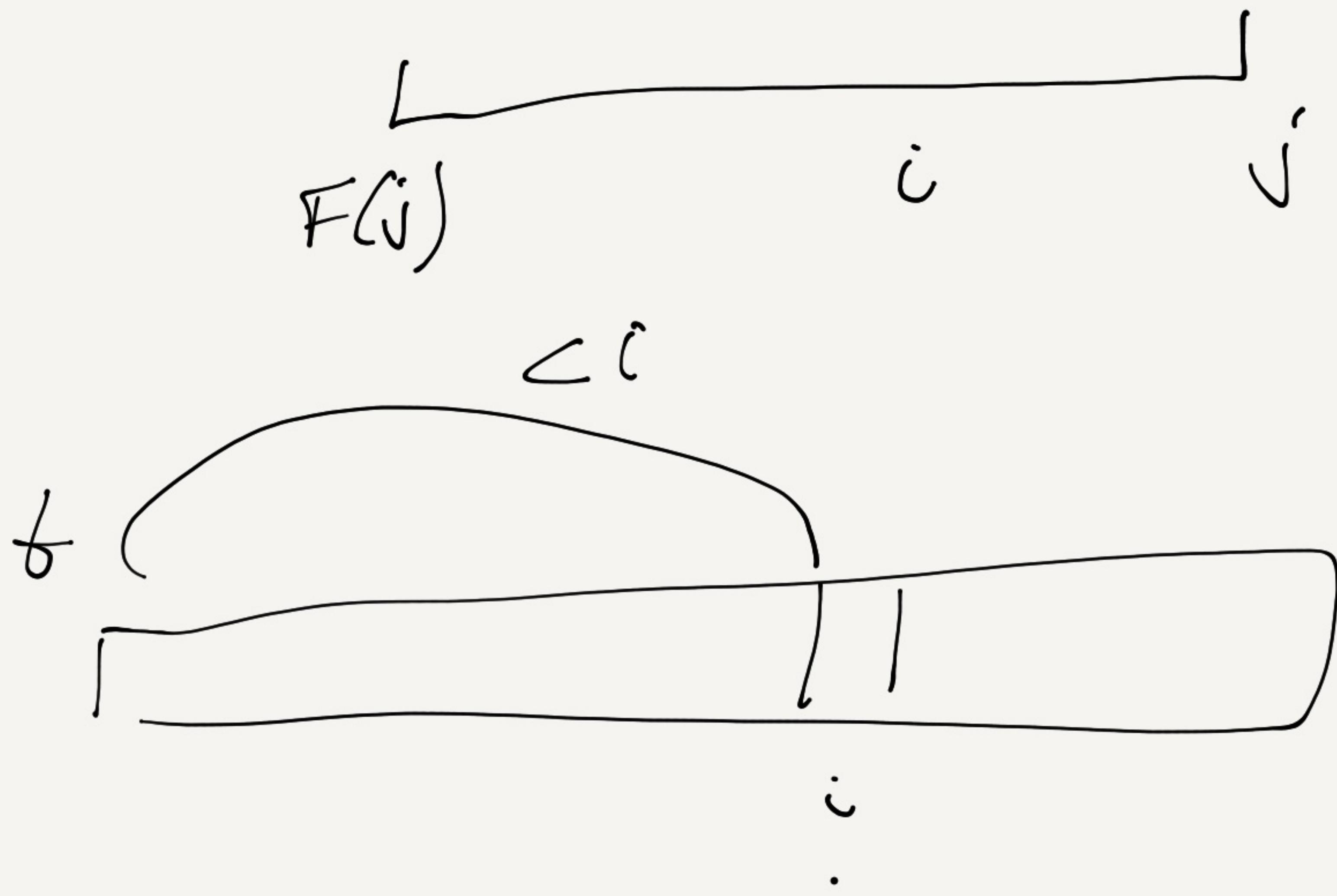
$$t[j] = a[F(j)] + \dots + a[j] \quad O(\log n)$$

$t[F(j)-1]$



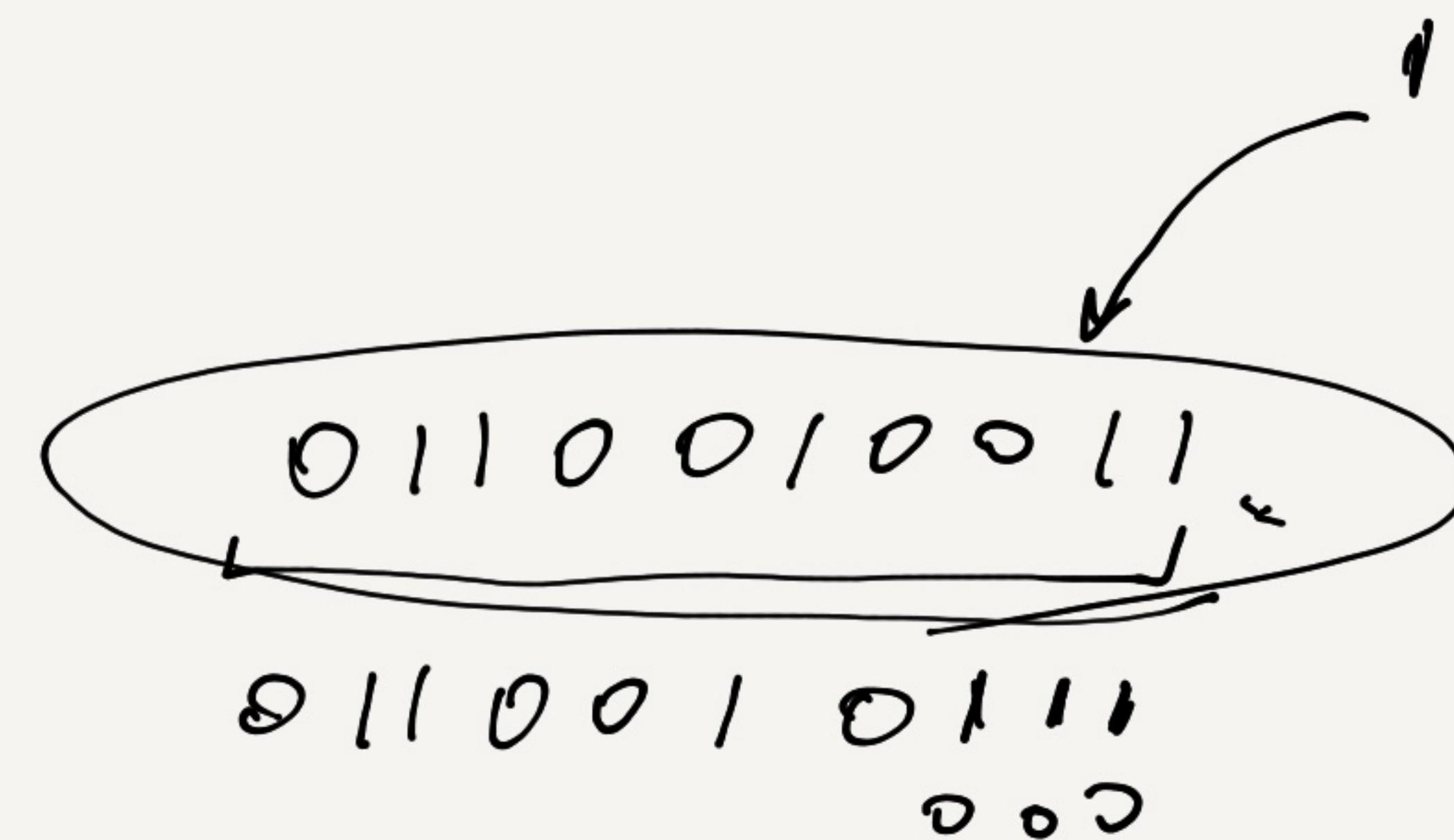
$t[F(F(j)-1)-1]$

$a[i] \neq 3$



$t[i:j]$

$F(i) \leq i \leq j$



$$F(i) = i \& (i+1) \quad 0110010000$$

$$0110010111$$

$t[i:i]$ $\neq 3$

$$c_{new} = i / (i+1)$$

$t[i_{new}] \neq 3$

$t[i_{new}] \neq 3$

$$\epsilon_{new_2} = c_{new} / (c_{new} + 1)$$