

3 no question Ans:

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12)

Given,

$$P \wedge (P \rightarrow Q) \rightarrow Q$$

12)

$$\equiv P \wedge (\neg P \vee Q) \rightarrow Q \quad (\text{other useful})$$

$$\equiv P \wedge \neg (\neg P \vee Q) \vee Q \quad (\text{same other useful})$$

$$\equiv P \wedge \neg (\neg P) \vee (\neg Q) \vee Q \quad (\text{De Morgan's})$$

$$\equiv P \wedge P \vee \neg Q \vee Q \quad (\text{commutative and other})$$

$$\equiv P \vee T$$

$$\equiv T$$

So, it's a tautology.

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Q9 no question Ans:

The order of nested quantifiers matters if quantifiers are of different type

$\forall x \exists y L(x, y)$ is not the same as $\exists y \forall x L(x, y)$

Example:

* Assume $L(x, y)$ denotes "x loves y"

* Then $\forall x \exists y L(x, y)$

* Translates to: Every body loves somebody

* And: $\exists y \forall x L(x, y)$

* Translates to: There is some one who is loved by everyone.

2 no question Ans:

Assume: The domain of x is all people

(1) All your friends are perfect.

Translation: $\forall x \text{ perfect}(x) \rightarrow \forall x P(x)$

(2) At least one of your friends is perfect.

Translation: $\forall x A(x, \text{perfect}) \rightarrow \text{perfect}(x)$

or $\forall x \exists y P(x, y)$

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