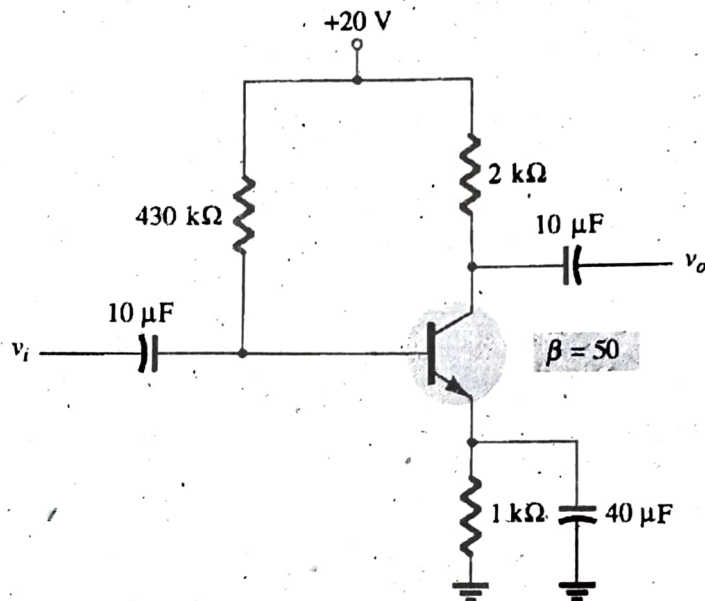


**EXAMPLE 4.4** For the emitter-bias network of Fig. 4.23, determine:

- $I_B$
- $I_C$
- $V_{CE}$
- $V_C$
- $V_E$
- $V_B$
- $V_{BC}$



**FIG. 4.23**

*Emitter-stabilized bias circuit for Example 4.4.*

**Solution:**

$$\begin{aligned} \text{a. Eq. (4.17): } I_B &= \frac{V_{CC} - V_{BE}}{R_B + (\beta + 1)R_E} = \frac{20 \text{ V} - 0.7 \text{ V}}{430 \text{ k}\Omega + (51)(1 \text{ k}\Omega)} \\ &= \frac{19.3 \text{ V}}{481 \text{ k}\Omega} = 40.1 \mu\text{A} \end{aligned}$$

$$\begin{aligned} \text{b. } I_C &= \beta I_B \\ &= (50)(40.1 \mu\text{A}) \\ &\approx 2.01 \text{ mA} \end{aligned}$$

c. Eq. (4.19):  $V_{CE} = V_{CC} - I_C(R_C + R_E)$   
 $= 20 \text{ V} - (2.01 \text{ mA})(2 \text{ k}\Omega + 1 \text{ k}\Omega) = 20 \text{ V} - 6.03 \text{ V}$   
 $= \mathbf{13.97 \text{ V}}$

d.  $V_C = V_{CC} - I_C R_C$   
 $= 20 \text{ V} - (2.01 \text{ mA})(2 \text{ k}\Omega) = 20 \text{ V} - 4.02 \text{ V}$   
 $= \mathbf{15.98 \text{ V}}$

e.  $V_E = V_C - V_{CE}$   
 $= 15.98 \text{ V} - 13.97 \text{ V}$   
 $= \mathbf{2.01 \text{ V}}$

or  $V_E = I_E R_E \cong I_C R_E$   
 $= (2.01 \text{ mA})(1 \text{ k}\Omega)$   
 $= \mathbf{2.01 \text{ V}}$

f.  $V_B = V_{BE} + V_E$   
 $= 0.7 \text{ V} + 2.01 \text{ V}$   
 $= \mathbf{2.71 \text{ V}}$

g.  $V_{BC} = V_B - V_C$   
 $= 2.71 \text{ V} - 15.98 \text{ V}$   
 $= \mathbf{-13.27 \text{ V}}$  (reverse-biased as required)

**EXAMPLE 4.8** Determine the dc bias voltage  $V_{CE}$  and the current  $I_C$  for the voltage-divider configuration of Fig. 4.35.

**Solution:** Eq. (4.28):  $R_{Th} = R_1 \parallel R_2$

$$= \frac{(39 \text{ k}\Omega)(3.9 \text{ k}\Omega)}{39 \text{ k}\Omega + 3.9 \text{ k}\Omega} = 3.55 \text{ k}\Omega$$

Eq. (4.29):  $E_{Th} = \frac{R_2 V_{CC}}{R_1 + R_2}$

$$= \frac{(3.9 \text{ k}\Omega)(22 \text{ V})}{39 \text{ k}\Omega + 3.9 \text{ k}\Omega} = 2 \text{ V}$$

Eq. (4.30):  $I_B = \frac{E_{Th} - V_{BE}}{R_{Th} + (\beta + 1)R_E}$

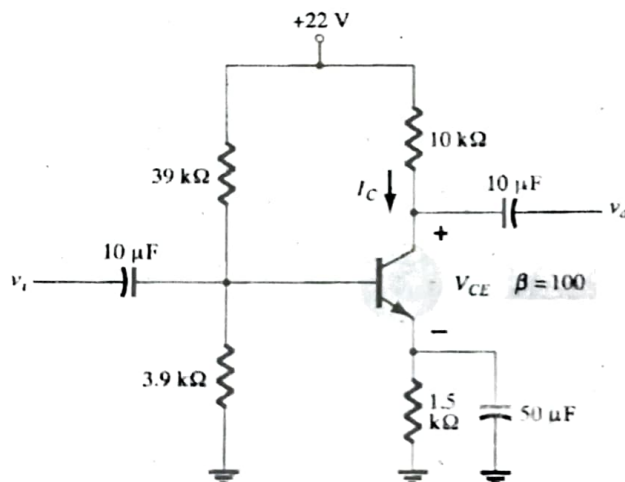
$$= \frac{2 \text{ V} - 0.7 \text{ V}}{3.55 \text{ k}\Omega + (101)(1.5 \text{ k}\Omega)} = \frac{1.3 \text{ V}}{3.55 \text{ k}\Omega + 151.5 \text{ k}\Omega}$$

$$= 8.38 \text{ }\mu\text{A}$$

$$I_C = \beta I_B$$

$$= (100)(8.38 \text{ }\mu\text{A})$$

$$= 0.84 \text{ mA}$$



**FIG. 4.35**

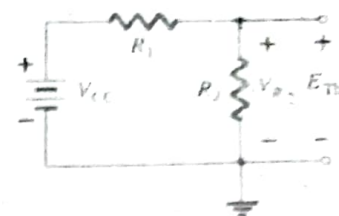
Beta-stabilized circuit for Example 4.8.

Eq. (4.31):  $V_{CE} = V_{CC} - I_C(R_C + R_E)$

$$= 22 \text{ V} - (0.84 \text{ mA})(10 \text{ k}\Omega + 1.5 \text{ k}\Omega)$$

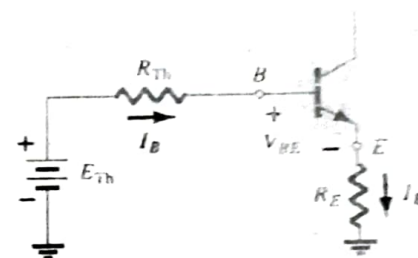
$$= 22 \text{ V} - 9.66 \text{ V}$$

$$= 12.34 \text{ V}$$



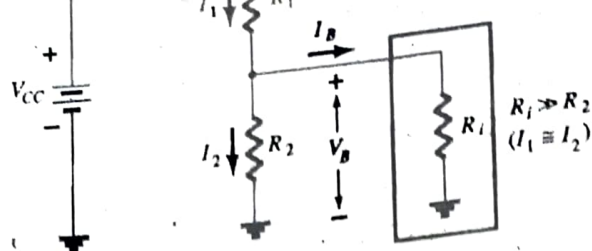
**FIG. 4.33**

Determining  $E_{Th}$ .



**FIG. 4.34**

Inserting the Thévenin equivalent circuit.



**FIG. 4.36**

Partial-bias circuit for calculating the approximate base voltage  $V_B$ .

determined using the voltage-divider rule (hence the name for the configuration). That is,

$$V_B = \frac{R_2 V_{CC}}{R_1 + R_2} \quad (4.32)$$

Because  $R_i = (\beta + 1)R_E \cong \beta R_E$  the condition that will define whether the approximate approach can be applied is

$$\beta R_E \geq 10R_2 \quad (4.33)$$

In other words, if  $\beta$  times the value of  $R_E$  is at least 10 times the value of  $R_2$ , the approximate approach can be applied with a high degree of accuracy.

Once  $V_B$  is determined, the level of  $V_E$  can be calculated from

$$V_E = V_B - V_{BE} \quad (4.34)$$

and the emitter current can be determined from

$$I_E = \frac{V_E}{R_E} \quad (4.35)$$

and

$$I_{CQ} \cong I_E \quad (4.36)$$

The collector-to-emitter voltage is determined by

$$V_{CE} = V_{CC} - I_C R_C - I_E R_E \quad \checkmark$$

but because  $I_E \cong I_C$ ,

$$V_{CEQ} = V_{CC} - I_C (R_C + R_E) \quad \checkmark \quad (4.37)$$

Note in the sequence of calculations from Eq. (4.33) through Eq. (4.37) that  $\beta$  does not appear and  $I_B$  was not calculated. The  $Q$ -point (as determined by  $I_{CQ}$  and  $V_{CEQ}$ ) is therefore independent of the value of  $\beta$ .

**EXAMPLE 4.9** Repeat the analysis of Fig. 4.35 using the approximate technique, and compare solutions for  $I_{CQ}$  and  $V_{CEQ}$ .

**Solution:** Testing:

$$\begin{aligned} \beta R_E &\geq 10R_2 \\ (100)(1.5 \text{ k}\Omega) &\geq 10(3.9 \text{ k}\Omega) \\ 150 \text{ k}\Omega &\geq 39 \text{ k}\Omega \text{ (satisfied)} \end{aligned}$$

$$\begin{aligned}\text{Eq. (4.32): } V_B &= \frac{R_2 V_{CC}}{R_1 + R_2} \\ &= \frac{(3.9 \text{ k}\Omega)(22 \text{ V})}{39 \text{ k}\Omega + 3.9 \text{ k}\Omega} \\ &= 2 \text{ V}\end{aligned}$$

Note that the level of  $V_B$  is the same as  $E_{Th}$  determined in Example 4.7. Essentially, therefore, the primary difference between the exact and approximate techniques is the effect of  $R_{Th}$  in the exact analysis that separates  $E_{Th}$  and  $V_B$ .

$$\begin{aligned}\text{Eq. (4.34): } V_E &= V_B - V_{BE} \\ &= 2 \text{ V} - 0.7 \text{ V} \\ &= 1.3 \text{ V}\end{aligned}$$

$$I_{CQ} \cong I_E = \frac{V_E}{R_E} = \frac{1.3 \text{ V}}{1.5 \text{ k}\Omega} = 0.867 \text{ mA}$$

compared to 0.84 mA with the exact analysis. Finally,

$$\begin{aligned}V_{CEQ} &= V_{CC} - I_C(R_C + R_E) \\ &= 22 \text{ V} - (0.867 \text{ mA})(10 \text{ k}\Omega + 1.5 \text{ k}\Omega) \\ &= 22 \text{ V} - 9.97 \text{ V} \\ &= 12.03 \text{ V}\end{aligned}$$

versus 12.34 V obtained in Example 4.8.

The results for  $I_{CQ}$  and  $V_{CEQ}$  are certainly close, and considering the actual variation in parameter values, one can certainly be considered as accurate as the other. The larger the level of  $R_1$  compared to  $R_2$ , the closer is the approximate to the exact solution. Example 4.11 will compare solutions at a level well below the condition established by Eq. (4.33).

**EXAMPLE 4.10** Repeat the exact analysis of Example 4.8 if  $\beta$  is reduced to 50, and compare solutions for  $I_{CQ}$  and  $V_{CEQ}$ .

**Solution:** This example is not a comparison of exact versus approximate methods, but a testing of how much the  $Q$ -point will move if the level of  $\beta$  is cut in half.  $R_{Th}$  and  $E_{Th}$  are the same:

$$R_{Th} = 3.55 \text{ k}\Omega, \quad E_{Th} = 2 \text{ V}$$

$$\begin{aligned}I_B &= \frac{E_{Th} - V_{BE}}{R_{Th} + (\beta + 1)R_E} \\ &= \frac{2 \text{ V} - 0.7 \text{ V}}{3.55 \text{ k}\Omega + (51)(1.5 \text{ k}\Omega)} = \frac{1.3 \text{ V}}{3.55 \text{ k}\Omega + 76.5 \text{ k}\Omega} \\ &= 16.24 \mu\text{A}\end{aligned}$$

$$\begin{aligned}I_{CQ} &= \beta I_B \\ &= (50)(16.24 \mu\text{A}) \\ &= 0.81 \text{ mA}\end{aligned}$$

$$\begin{aligned}V_{CEQ} &= V_{CC} - I_C(R_C + R_E) \\ &= 22 \text{ V} - (0.81 \text{ mA})(10 \text{ k}\Omega + 1.5 \text{ k}\Omega) \\ &= 12.69 \text{ V}\end{aligned}$$

Tabulating the results, we have:

*Effect of  $\beta$  variation on the response of the voltage-divider configuration of Fig. 4.35.*

$\beta$	$I_{CQ} \text{ (mA)}$	$V_{CEQ} \text{ (V)}$
100	0.84 mA	12.34 V
50	0.81 mA	12.69 V

The results clearly show the relative insensitivity of the circuit to the change in  $\beta$ . Even though  $\beta$  is drastically cut in half, from 100 to 50, the levels of  $I_{CQ}$  and  $V_{CEQ}$  are essentially the same.

Because  $I_C' \cong I_C$  and  $I_E \cong I_C$ , we have

$$I_C(R_C + R_E) + V_{CE} - V_{CC} = 0$$

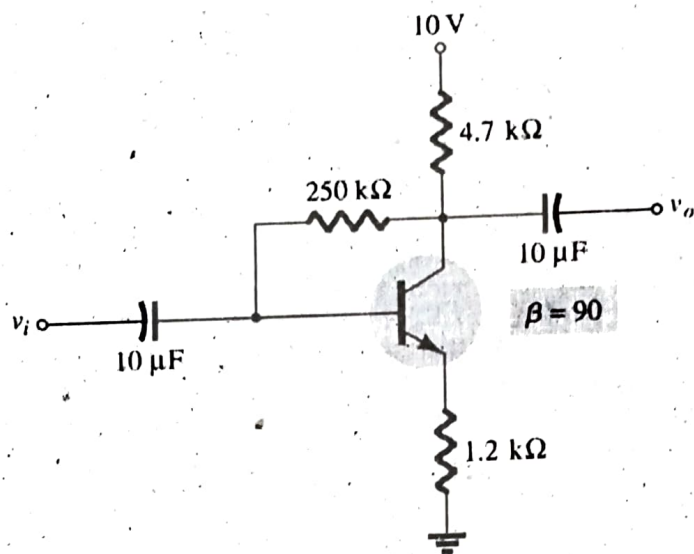
$$V_{CE} = V_{CC} - I_C(R_C + R_E)$$

(4.42)

and

which is exactly as obtained for the emitter-bias and voltage-divider bias configurations.

**EXAMPLE 4.12** Determine the quiescent levels of  $I_{CQ}$  and  $V_{CEQ}$  for the network of Fig. 4.41.



**FIG. 4.41**

Network for Example 4.12.

**Solution:** Eq. (4.41): 
$$I_B = \frac{V_{CC} - V_{BE}}{R_F + \beta(R_C + R_E)}$$

$$= \frac{10 \text{ V} - 0.7 \text{ V}}{250 \text{ k}\Omega + (90)(4.7 \text{ k}\Omega + 1.2 \text{ k}\Omega)}$$

$$= \frac{9.3 \text{ V}}{250 \text{ k}\Omega + 531 \text{ k}\Omega} = \frac{9.3 \text{ V}}{781 \text{ k}\Omega}$$

$$= 11.91 \mu\text{A}$$

$$I_{CQ} = \beta I_B = (90)(11.91 \mu\text{A})$$

$$= 1.07 \text{ mA}$$

$$V_{CEQ} = V_{CC} - I_C(R_C + R_E)$$

$$= 10 \text{ V} - (1.07 \text{ mA})(4.7 \text{ k}\Omega + 1.2 \text{ k}\Omega)$$

$$= 10 \text{ V} - 6.31 \text{ V}$$

$$= 3.69 \text{ V}$$



### 4.5 Voltage-Divider Bias Configuration

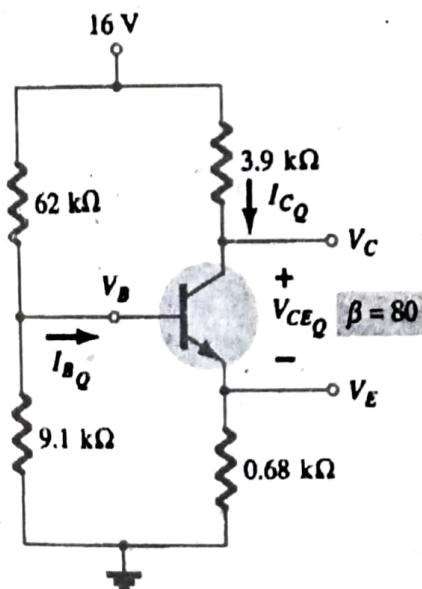
15. For the voltage-divider bias configuration of Fig. 4.125, determine:

- $I_{BQ}$
- $I_{CQ}$
- $V_{CEQ}$
- $V_C$
- $V_E$
- $V_B$

16. a. Repeat problem 15 for  $\beta = 140$  using the general approach (not the approximate).  
b. What levels are affected the most? Why?

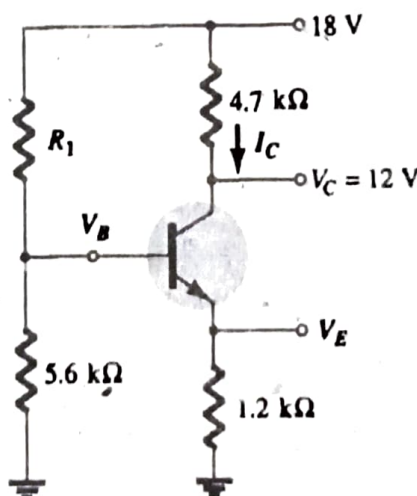
17. Given the information provided in Fig. 4.126, determine:

- $I_C$
- $V_E$
- $V_B$
- $R_1$



**FIG. 4.125**

Problems 15, 16, 20, 23, 25, 67,  
69, 70, 73, and 77.



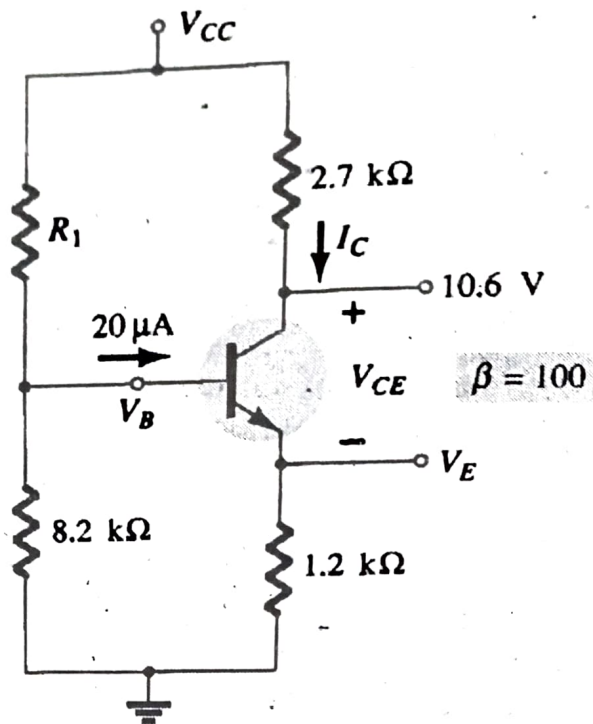
**FIG. 4.126**

Problems 17 and 19.

18. Given the information appearing in Fig. 4.127, determine:

- $I_C$
- $V_E$
- $V_{CC}$
- $V_{CE}$
- $V_B$
- $R_1$

BJTs



**FIG. 4.127**

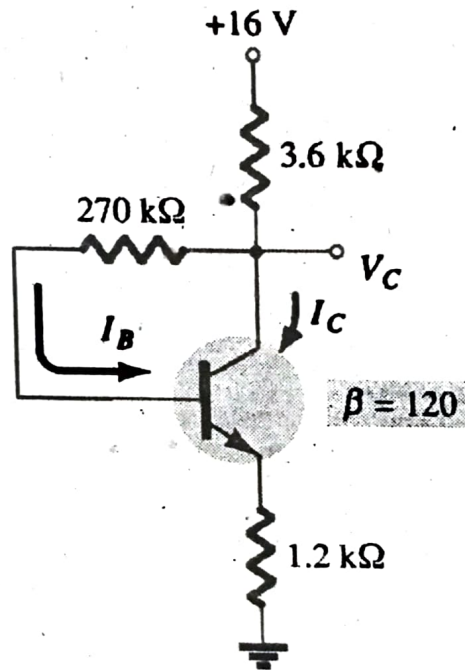
*Problem 18.*



#### 4.6 Collector-Feedback Configuration

27. For the collector-feedback configuration of Fig. 4.129, determine:

- a.  $I_B$ .
- b.  $I_C$ .
- c.  $V_C$ .



**FIG. 4.129**

Problems 27, 28, 74, and 78.