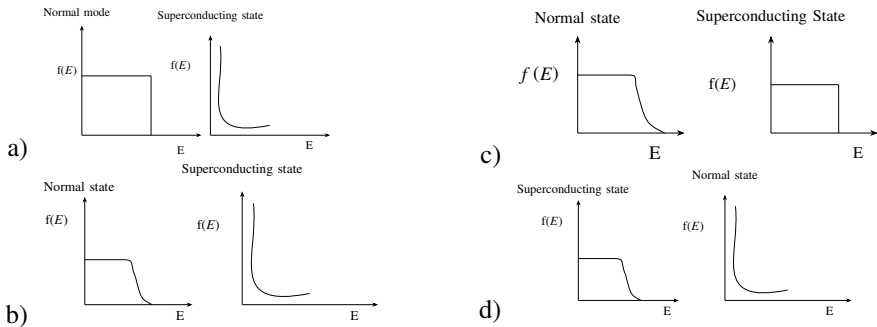
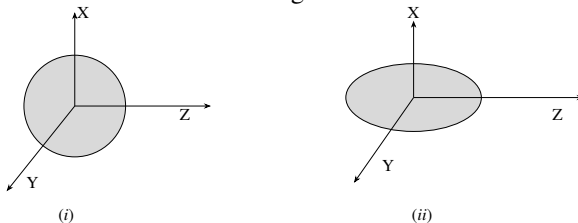


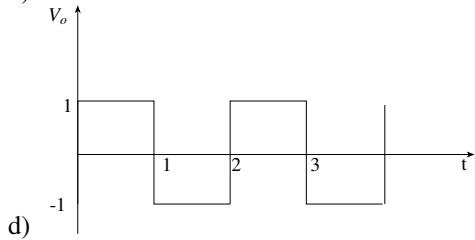
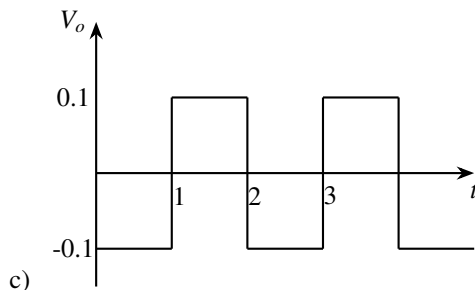
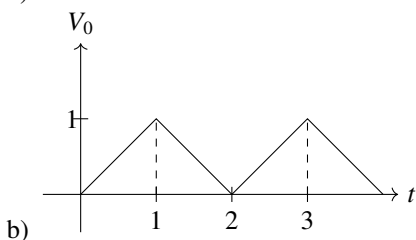
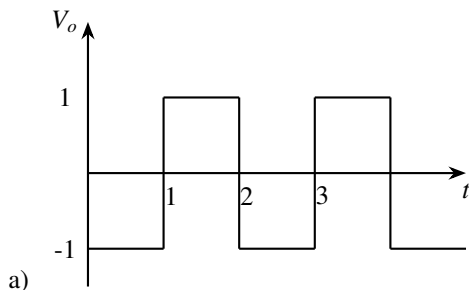
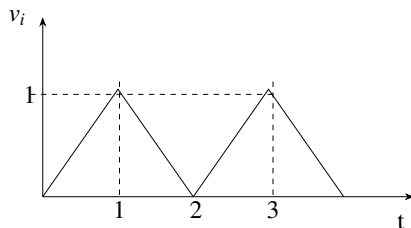
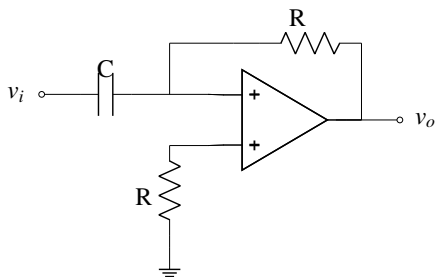
- 40) The band gap of an intrinsic semiconductor is  $E_g = 0.72\text{eV}$  and  $m_h^* = 6m_e^*$ . At  $300\text{K}$ , the Fermi level with respect to the valence band (in  $\text{eV}$ ) is at \_\_\_\_\_ (upto three decimal places)  $k_B = 1.38 \times 10^{-23} \text{JK}^{-1}$  [GATE 2015]
- 41) The number of permitted transitions from  $^2P_{3/2} \rightarrow ^2S_{1/2}$  in the presence of a weak magnetic field is \_\_\_\_\_ [GATE 2015]
- 42) Which one of the following represents the electron occupancy for a superconductor in its normal and superconducting states? [GATE 2015]



- 43) A charge  $-q$  is distributed uniformly over a sphere, with a positive charge  $q$  at its center in (i). Also in (ii), a charge  $-q$  is distributed uniformly over an ellipsoid with a positive charge  $q$  at its center. With respect to the origin of the coordinate system, which one of the following statements is correct? [GATE 2015]



- a) The dipole moment is zero in both (i) and (ii)
- b) The dipole moment is non-zero in (i) but zero in (ii)
- c) The dipole moment is zero in (i) but non-zero in (ii)
- d) The dipole moment is non-zero in both (i) and (ii)
- 44) Consider the circuit shown in the figure, where  $RC = 1$ . For an input signal  $V_1$  shown below, choose the correct  $V_o$  from the options: [GATE 2015]



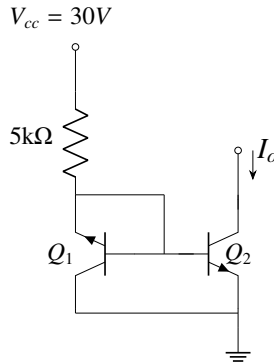
45) A long solenoid is embedded in a conducting medium and is insulated from the medium. If the current through the solenoid is increased at a constant rate, the induced current in the medium as a function of the radial distance  $r$  from the axis of the solenoid is proportional to [GATE 2015]

- a)  $r^2$  inside the solenoid and  $\frac{1}{r}$  outside      c)  $r^2$  inside the solenoid and  $\frac{1}{r^2}$  outside  
b)  $r$  inside the solenoid and  $\frac{1}{r^2}$  outside      d)  $r$  inside the solenoid and  $\frac{1}{r}$  outside

46) In the simple current source in the figure,  $Q_1$  and  $Q_2$  are identical transistors with current gain  $\beta = 100$  and  $V_{BE} = 0.7V$  [GATE 2015]

47) Match the phrases in Group I and Group II and identify the correct option.

- a) (P-i), (Q-ii), (R-iii), (S-iv)      c) (P-iii), (Q-iv), (R-i), (S-ii)  
b) (P-ii), (Q-i), (R-iv), (S-iii)      d) (P-iii), (Q-i), (R-iv), (S-ii)



The current  $I_o$  (in mA) is \_\_\_\_\_ (upto two decimal places) [GATE 2015]

### Group I

- (P) Electron spin resonance (ESR)
- (Q) Nuclear magnetic resonance (NMR)
- (R) Transition between vibrational states of a molecule
- (S) Electronic transition

### Group II

- (i) radio frequency
- (ii) visible range frequency
- (iii) microwave frequency
- (iv) far-infrared range  $\hat{A}$

48) Consider the motion of the Sun with respect to the rotation of the Earth about its axis. If  $\vec{F}_c$  and  $\vec{F}_{Co}$  denote the centrifugal and the Coriolis forces, respectively, acting on the Sun, then [GATE 2015]

- a)  $\vec{F}_c$  is radially outward and  $\vec{F}_{Co} = \vec{F}_c$
- b)  $\vec{F}_c$  is radially inward and  $\vec{F}_{Co} = -2\vec{F}_c$
- c)  $\vec{F}_c$  is radially outward and  $\vec{F}_{Co} = -2\vec{F}_c$
- d)  $\vec{F}_c$  is radially outward and  $\vec{F}_{Co} = 2\vec{F}_c$

49) In a rigid-rotator of mass  $M$ , if the energy of the first excited state is  $1meV$ , then the fourth excited state energy (in  $meV$ ) is \_\_\_\_\_

50) A plane wave  $(\hat{x} + i\hat{y})\mathbf{E}_0 \exp[i(kz - \omega t)]$  after passing through an optical element emerges as  $(\hat{x} - i\hat{y})\mathbf{E}_0 \exp[i(kz - \omega t)]$ , where  $k$  and  $\omega$  are the wavevector and the angular frequency, respectively. The optical element is a [GATE 2015]

- a) quarter wave plate
- b) half wave plate
- c) polarizer
- d) Faraday rotator

51) The Lagrangian for a particle of mass  $m$  at a position  $\vec{r}$  moving with a velocity  $\vec{v}$  is given by  $L = \frac{m}{2}\vec{v}^2 + C\vec{r} \cdot \vec{v} - V(\mathbf{r})$ , where  $V(r)$  is a potential and  $C$  is a constant. If  $\vec{p}_c$  is the canonical momentum, then its Hamiltonian is given by [GATE 2015]

- a)  $\frac{1}{2m}(\vec{p}_c + C\vec{r})^2 + V(r)$
- b)  $\frac{1}{2m}(\vec{p}_c - C\vec{r})^2 + V(r)$
- c)  $\frac{p_c^2}{2m} + V(r)$
- d)  $\frac{1}{2m}p_c^2 + C^2r^2 + V(r)$

- 52) The Hamiltonian for a system of two particles of masses  $m_1$  and  $m_2$  at  $\vec{r}_1$  and  $\vec{r}_2$  having velocities  $\vec{v}_1$  and  $\vec{v}_2$  is given by  $H = \frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2 + \frac{C}{(\vec{r}_1 - \vec{r}_2)^2} \hat{z} \cdot (\vec{r}_1 \times \vec{r}_2)$ , where  $C$  is a constant. Which one of the following statements is correct? [GATE 2015]
- The total energy and total momentum are conserved
  - Only the total energy is conserved
  - Only the total energy and the  $z$ -component of the total angular momentum are conserved
  - The total energy and total angular momentum are conserved