

The Hidden Flaw

Why Your Computer Can't Do Simple Math
(And Why It Matters)

```
>>> 0.1 + 0.2  
0.30000000000000004
```



This isn't a bug. This is by design. Let's uncover why.

Our World: The Language of Ten

$$123.45 = 1 \times 10^2 + 2 \times 10^1 + 3 \times 10^0 + 4 \times 10^{-1} + 5 \times 10^{-2}$$

Everything is built from powers of 10.
Simple and intuitive for us.

The Computer's World: The Language of Two

$$101.01_2 = 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 + 0 \times 2^{-1} + 1 \times 2^{-2}$$

Everything is built from powers of 2.
All 0s and 1s.

The Flaw in Translation

In Base-10

$$1/3 = 0.\textcolor{blue}{3}333333333\dots$$

In Base-2

$$1/10 = 0.000\textcolor{blue}{1}100110011\dots$$

Just as we can't write $1/3$ perfectly,
a computer can't write 0.1 perfectly.

A Float is a Necessary Approximation



A **float** stores an approximation. It cuts the repeating binary number after a fixed number of bits. So, **0.1** is actually stored as something incredibly close, but not exact: **0.100000000000000055...**

The Fundamental Rule of Precision

In Base-10

A fraction is finite only if its denominator's prime factors are **2s** and **5s**.

Finite: $1/2, 1/5, 1/8 (2^3), 1/10 (2 \times 5)$

Infinite: $1/3$ (Fails because of **3**).

In Base-2

A fraction is finite only if its denominator's prime factors are **2s**.

Finite: $1/2, 1/4 (2^2)$

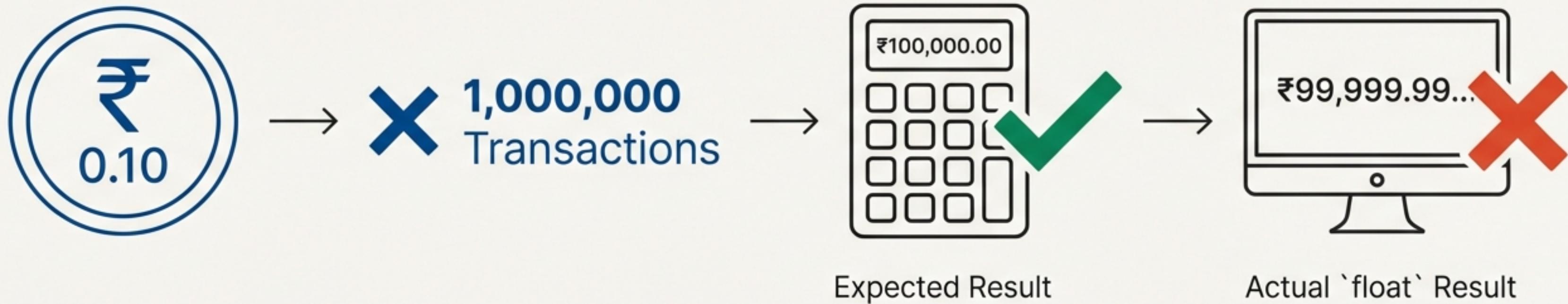
Infinite: $1/10$ (which is $1/(2 \times 5)$).
It is infinite because of the **5**.

The Crime Scene Revisited

$$\begin{array}{r} 0.10000000000000000555\dots \\ + 0.20000000000000001110\dots \\ \hline = 0.30000000000000004 \end{array}$$

You are not adding `0.1 + 0.2`. You are adding two slightly inaccurate approximations. Their tiny 'rounding error' tails combine.

Why This is Unacceptable for Money



Small errors accumulate. Banks don't tolerate 'slightly off'.

The Right Tool: Thinking in Base-10 with Decimal

The `Decimal` type performs math the way *we* do—in base-10. It avoids binary translation entirely.

```
from decimal import Decimal
```

- ✓ Numbers are stored and computed in base-10.
- ✓ Decimal fractions stay exact.
- ✓ No infinite binary representation.
- ✓ No truncation. No hidden error.

The Exact Answer

Standard `float`

```
print(0.1 + 0.2)
```

```
0.30000000000000004
```



Python `Decimal`

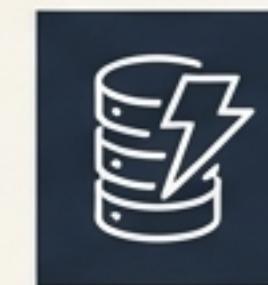
```
from decimal import Decimal
```

```
print(Decimal("0.1") + Decimal("0.2"))
```

```
Decimal('0.3')
```



Why Professional Systems Insist on Precision



AWS
DynamoDB

“ DynamoDB stores numbers as exact decimals. Accepting floats would corrupt data. AWS refuses to guess how to round. So they force you to be explicit.

This isn't just a best practice; it's a requirement for data integrity at scale.

Your Simple, Safe Mental Model

‘float’

 Fast

 Approximate

Unsafe for money & data integrity

‘Decimal’

 Slower

 Exact

Safe for money & data integrity

Binary cannot represent most decimals exactly. Decimal arithmetic can.

Make It Real

Run this once and never forget it.

```
# The float comparison fails
print(0.1 + 0.2 == 0.3) False
```

```
# The Decimal comparison succeeds
from decimal import Decimal
print(Decimal("0.1") + Decimal("0.2") == Decimal("0.3")) True
```

This is not trivia. This is foundational.