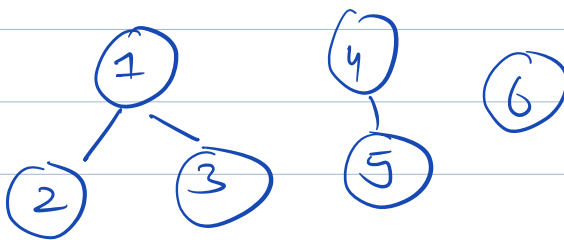


1, 2, 5, 6, 3, 4.

1, 2, 6, 5, 3, 4

1, 2, 6, 5, 4, 3

DFS



= 1 2 3 4 5 6

```

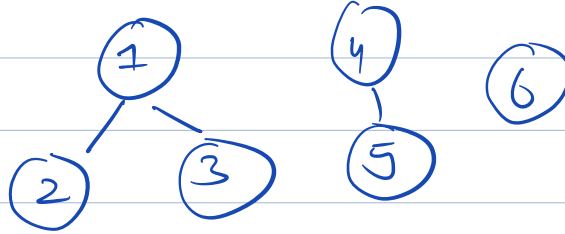
for (int i = 1 ; i <= 6 ; i++) {
    if (!visited[i])
        dfs(i);
}
  
```

}

1	2	3	4	5	6
1	1	1	1	1	1

Q Count the number of connected components.

C_1 C_2 C_3



cnt = 0;

```
for (int i = 1 ; i <= 6 ; i++) {
```

```
    if (!visited[i]) {
```

```
        dfs(i);
```

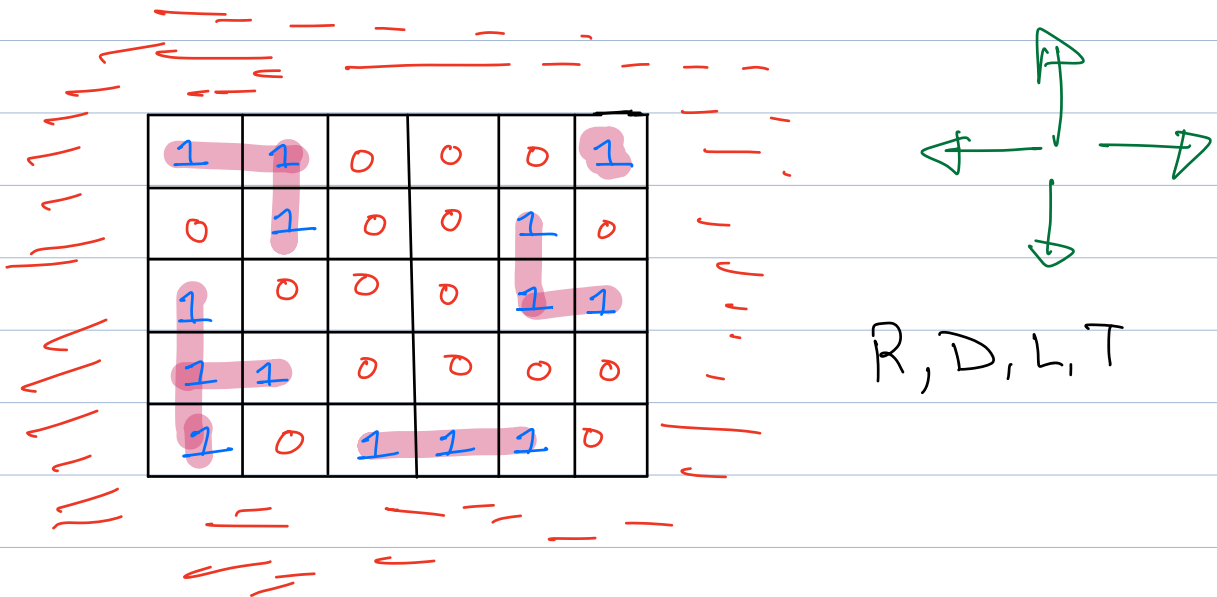
```
        cnt++;
```

```
    }
```

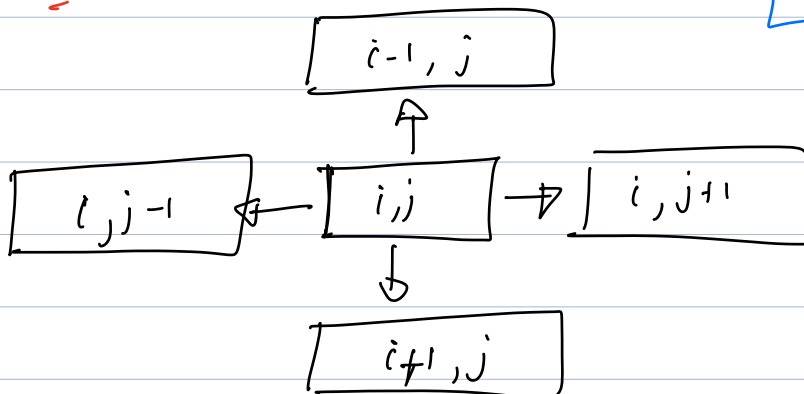
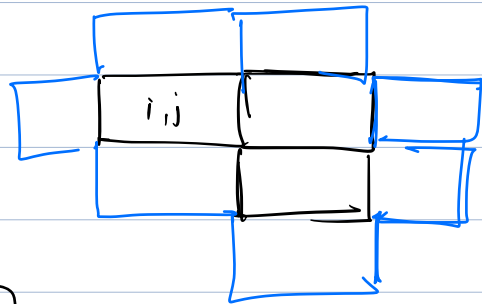
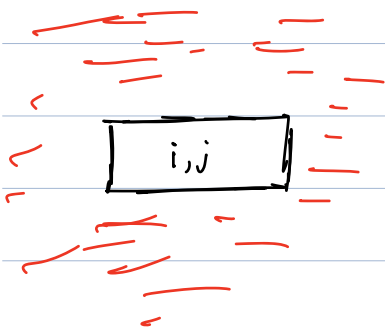
```
}
```

```
return cnt
```

Number of Islands



no of islands = 5



We will use the input 2D matrix to track visited nodes

mat[i][j] → 1 : land, unvisited
→ 0 : water
→ 2 : land, visited

```
for (int i = 0; i < n; i++) {
```

```
    for (int j = 0; j < m; j++) {
```

```
        if (mat[i][j] == 1) {  
            dfs(i, j);  
            cnt++;  
        }
```

```
    }
```

```
}
```

```
return cnt;
```

```
bool checkIsValid (int i, int j, int n, int m) {
```

```
    if (i < 0 || i >= n || j < 0 || j >= m)  
        return false;
```

```
    return true;
```

```
}
```

```
void dfs (int i, int j) {
```

```
    mat[i][j] = 2;
```

```
    int x[4] = {1, -1, 0, 0};
```

```
    int y[4] = {0, 0, 1, -1};
```

```
    for (int k=0; k<4; k++) {
```

```
        int x-n => i + x[k];
```

```
        int y-n => j + y[k]
```

```
        if (checkIfValid (x-n, y-n) &&
```

```
            mat[x-n][y-n] == 1)
```

```
            dfs (x-n, y-n);
```

```
    }
```

```
}
```

$T_C: O(V+E)$

$V = mn$

$E = 4mn$

$T_C: O(mn)$

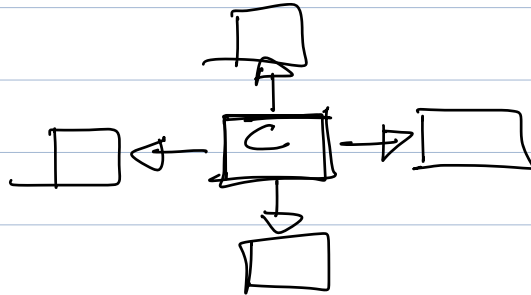
$SC: O(mn)$

Rotten Oranges.

In how
many days.
every living
area is
rotten affected

C	1	1	0	1	0
1	1	0	1	1	0
0	0	1	C	0	1
C	1	1	0	1	1
1	1	0	0	1	C

C \Rightarrow affected
by covid.
1 \Rightarrow not affected
area
0 \Rightarrow no life
present.



DAY 1

C	1	1	0	1	0
1	1	0	1	1	0
0	0	1	C	0	1
C	1	1	0	1	1
1	1	0	0	1	C

0, 1, 2, 3, 4

DAY 2

C	1	1	0	1	0
1	1	0	1	1	0
0	0	1	C	0	1
C	1	1	0	1	1
1	1	0	0	1	C

DAY 3

C	1	1	0	1	0
1	1	0	1	1	0
0	0	1	C	0	1
C	1	1	0	1	1
1	1	0	0	1	C

Ans \Rightarrow 3 days

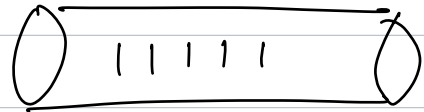
C	1	1	0	1	0
1	1	0	1	1	0
0	0	1	C	0	1
C	1	1	0	1	1
1	1	0	0	1	C

1) Traverse the matrix and insert
valid cells in the Queue.

2) Perform BFS and maintain level.

Whenever from (i, j) you
visit a neighbor (x, y)
 $level[x][y] = level[i][j]$
 $+ 1$

C	1	1	0	1	0
1	1	0	1	1	0
0	0	1	C	0	1
C	1	1	0	1	1
1	1	0	0	1	C



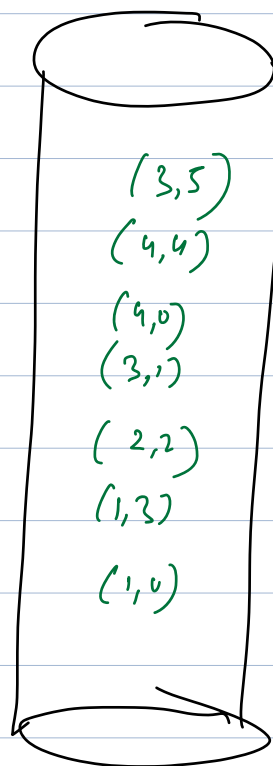
Size = 8

max-level = 2

10:32 pm

	0	1	2	3	4	5
0	C	1	1	0	1	0
1	1	1	0	1	1	0
2	0	0	1	C	0	1
3	C	1	1	0	1	1
4	1	1	0	0	1	C

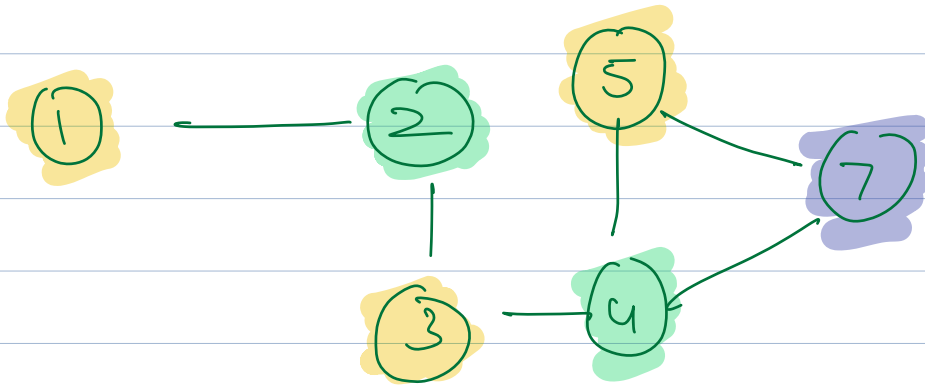
	0	1	2	3	4	5
0	0	1	2		3	
1	1	2		1	2	
2			1	0		2
3	0	1	2		2	1
4	1	2			1	0



$(0,1)$

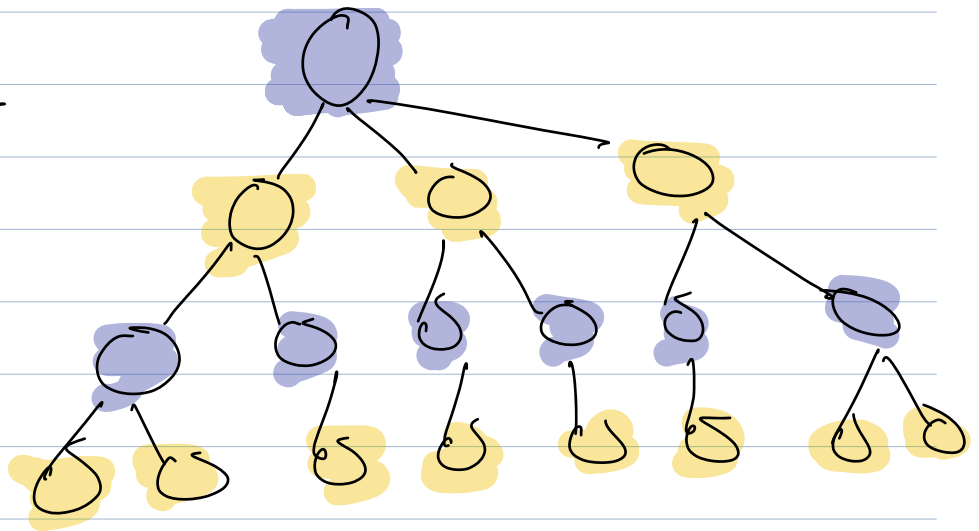
Chromatic numbers \Rightarrow np hard = [no polynomial time solution]

Min number of colors required to color the graph such that no 2 adjacent nodes have the same color.

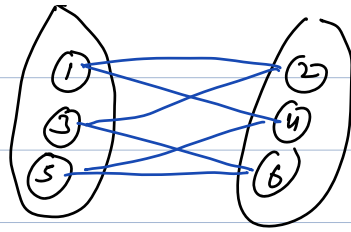
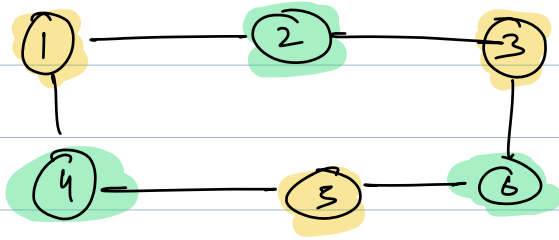


Chromatic number = 3

Tree

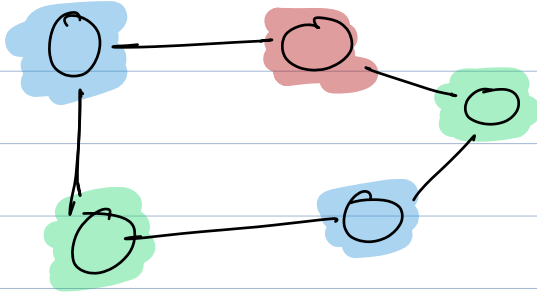


Chromatic number for a tree = 2



Even Cycles

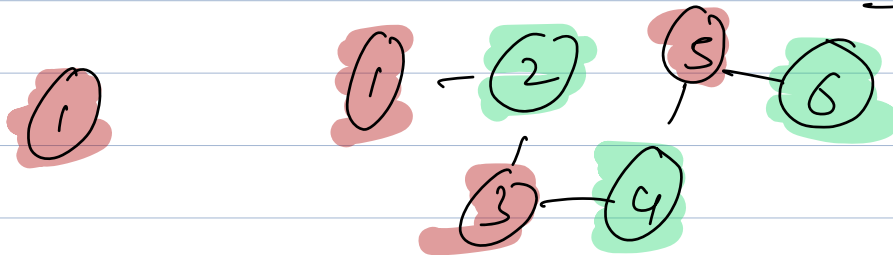
chromatic number $= 2$



Odd Cycles

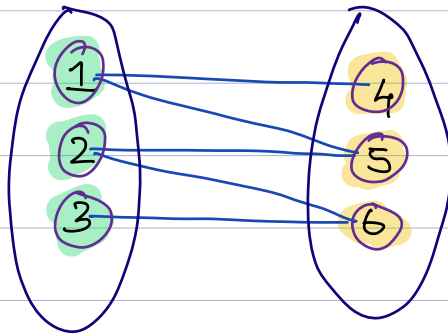
chromatic number $= 3$

For any acyclic graphs the chromatic number ≤ 2

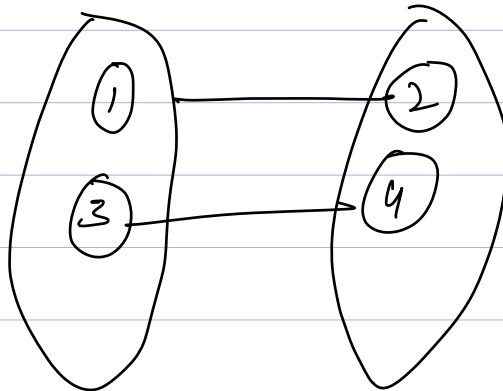
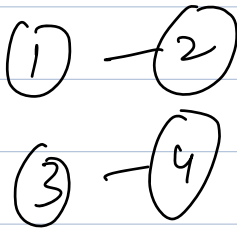


Bipartite graphs

A graph which can be broken down into two distinct sets U & V such that no two nodes in U & V have an edge b/w them.



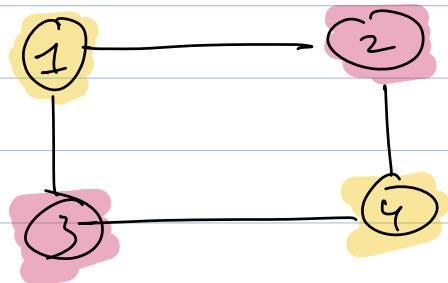
Chromatic
number of a
bipartite graph
is 2.





Even length cycles are bipartite.

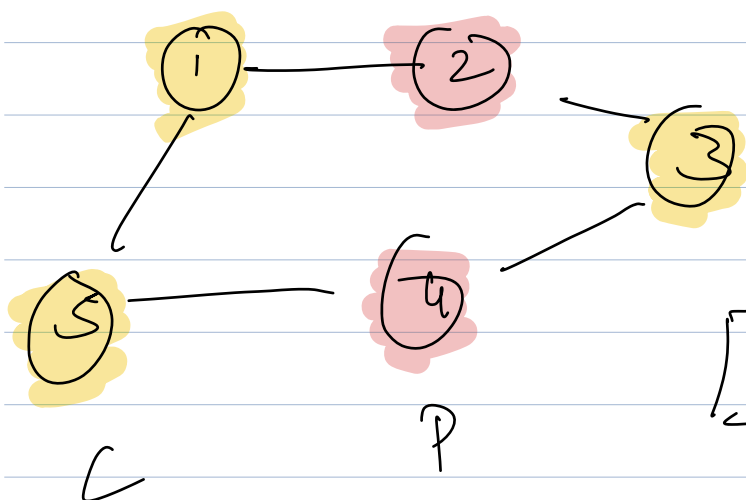
Trees are bipartite.

Acyclic graphs are bipartite.



 = 1
 = 0

1	0	0	1
1	2	3	4



1	0	1	0	1
1	2	3	4	5

Pseudo Code :

$(1, 0)$

Color $\rightarrow 0$
 $\rightarrow 1$

int visited[n]; int color[n], isBipartite = true;

void dfs (int node, int c) {

visited [node] = 1;

color [node] = c;

for (int i = 0; i < adj [node].size(); i++) {

int child = adj [node][i];

if (visited [child]) {

if (color [child] == color [node])
isBipartite = false;

0 \rightarrow 1

1 \rightarrow 0

1-c

1^c

} else {

dfs (child, 1-c)

}

}

}

T.C: $O(V+E)$

S.C: $O(V+E)$

